

# Apunte ICPC

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# Notas previas

## 0.1. Abreviaciones utilizadas

```
1 typedef long long ll;
2 //en ciertos casos es necesario cambiar int por ll
3 typedef vector<int> vi;
4 typedef vector<vector<int> > vvi;
5 typedef pair<int,int> ii;
6 typedef vector<vector<ii> > vvii; //util para grafos
7 typedef pair<pair<int,int>,int> iii;
8 #define mp(x,y) make_pair(x,y)
9 #define pb(x) push_back(x)
```

# Capítulo 1

## Estructuras de datos

### 1.1. Fenwick Tree

**Nota:** Ambas implementaciones tienen rangos entre 1 a n.

#### 1.1.1. Actualizaciones por rango, consultas puntales

```
1 struct FenwickTree{
2     vi FT;
3     FenwickTree(int N){
4         FT.resize(N+1,0);
5     }
6
7     int query(int i){
8         int ans = 0;
9         for(;;i-=i&(-i)) ans += FT[i];
10        return ans;
11    }
12
13    int query(int i, int j){
14        return query(j)-query(i-1);
15    }
16
17    void update(int i, int v){
18        for(;;i<FT.size();i+=i&(-i)) FT[i] += v;
19    }
20
21    void update(int i, int j, int v){
22        update(i,v); update(j+1,-v);
23    }
24 };
```

### 1.1.2. Actualizaciones puntuales, consultas por rango

La consulta  $query(a, b)$  corresponde a la sumatoria de los elementos entre los índices  $a$  y  $b$ .

```

1 struct FenwickTree {
2     vi ft;
3     FenwickTree(){}
4     FenwickTree(int n){
5         ft.assign(n + 1, 0);
6     }
7
8     int query(int b) {
9         int sum = 0;
10        for (; b; b -= b&(-b)) sum += ft[b];
11        return sum;
12    }
13
14    int query(int a, int b) { \\RSQ
15        return query(b) - (a == 1 ? 0 : query(a - 1));
16    }
17
18    void update(int k, int v) {                                // note: n = ft.
19        size() - 1                                             size() - 1
20        for (; k < (int)ft.size(); k += k&(-k)) ft[k] += v;
21    };

```

## 1.2. Union-Find

Utilizada para trabajar conjuntos disjuntos. Sirve para encontrar componentes conexas en grafos no dirigidos.

```

1 class UnionFind {
2 private:
3     vi p, rank, setSize;
4     int numSets;
5 public:
6     UnionFind(int N) {
7         setSize.assign(N, 1); numSets = N; rank.assign(N, 0);
8         p.assign(N, 0); for (int i = 0; i < N; i++) p[i] = i; }
9     int findSet(int i) { return (p[i] == i) ? i : (p[i] = findSet(p[i]
10        )); }
11    bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }
12    void unionSet(int i, int j) {
13        if (!isSameSet(i, j)) { numSets--;
14        int x = findSet(i), y = findSet(j);
15        // rank is used to keep the tree short
16        if (rank[x] > rank[y]) { p[y] = x; setSize[x] += setSize[y]; }
17        else { p[x] = y; setSize[y] += setSize[x];
18            if (rank[x] == rank[y]) rank[y]++; } }
19
20    int numDisjointSets() { return numSets; }
21    int sizeOfSet(int i) { return setSize[findSet(i)]; }

```

## 1.3. Segment Tree

### 1.3.1. Iterativo

```

1  struct prodsign {
2      int sgn;
3      prodsign() {sgn = 1;}
4      prodsign(int x) {
5          sgn = (x > 0) - (x < 0);
6      }
7      prodsign(const prodsign &a,
8              const prodsign &b) {
9          sgn = a.sgn*b.sgn;
10     }
11 };
12
13 // Maximum Sum (SPOJ)
14 struct maxsum {
15     int first, second;
16     maxsum() {first = second = -1;}
17     maxsum(int x) {
18         first = x; second = -1;
19     }
20     maxsum(const maxsum &a,
21           const maxsum &b) {
22         if (a.first > b.first) {
23             first = a.first;
24             second = max(a.second,
25                         b.first);
26         } else {
27             first = b.first;
28             second = max(a.first,
29                         b.second);
30         }
31     }
32     int answer() {
33         return first + second;
34     }
35 };
36
37 // Range Minimum Query
38 struct rminq {
39     int value;
40     rminq() {value = INT_MAX;}
41     rminq(int x) {value = x;}
42     rminq(const rminq &a,
43           const rminq &b) {
44         value = min(a.value,
45                     b.value);
46     }
47 };
48
49
50 template<class node> class ST {
51     vector<node> t;
52     int n;
53

```

```

54 public:
55     ST(vector<node> &arr) {
56         n = arr.size();
57         t.resize(n*2);
58         copy(arr.begin(), arr.end(), t.begin() + n);
59         for (int i = n-1; i > 0; --i)
60             t[i] = node(t[i<<1], t[i<<1|1]);
61     }
62
63     // 0-indexed
64     void set_point(int p, const node &value) {
65         for (t[p += n] = value; p > 1; p >>= 1)
66             t[p>>1] = node(t[p], t[p^1]);
67     }
68
69     // inclusive exclusive, 0-indexed
70     node query(int l, int r) {
71         node ans1, ansr;
72         for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
73             if (l&1) ans1 = node(ans1, t[l++]);
74             if (r&1) ansr = node(t[--r], ansr);
75         }
76         return node(ans1, ansr);
77     }
78 };

```

### 1.3.2. Lazy

```

1  struct RSQ {
2      static intt const neutro = 0;
3      static intt op(intt x, intt y) {
4          return x + y;
5      }
6      static intt
7          lazy_op(int i, int j, intt x) {
8          return (j - i + 1)*x;
9      }
10 };
11
12 struct RMinQ {
13     static intt const neutro = 1e18;
14     static intt op(intt x, intt y) {
15         return min(x, y);
16     }
17     static intt
18         lazy_op(int i, int j, intt x) {
19         return x;
20     }
21 };
22
23
24 template<class t> class SegTreeLazy {
25     vector<intt> arr, st, lazy; int n;
26
27     void build(int u, int i, int j) {
28         if (i == j) {
29             st[u] = arr[i];

```



```

30         return;
31     }
32     int m = (i+j)/2, l = u*2+1, r = u*2+2;
33     build(l, i, m);
34     build(r, m+1, j);
35     st[u] = t::op(st[l], st[r]);
36 }
37
38 void propagate(int u, int i, int j, intt x) {
39     st[u] += t::lazy_op(i, j, x);
40     if (i != j) {
41         lazy[u*2+1] += x;
42         lazy[u*2+2] += x;
43     }
44     lazy[u] = 0;
45 }
46
47 intt query(int a, int b, int u, int i, int j) {
48     if (j < a or b < i)
49         return t::neutro;
50     int m = (i+j)/2, l = u*2+1, r = u*2+2;
51     if (lazy[u])
52         propagate(u, i, j, lazy[u]);
53     if (a <= i and j <= b)
54         return st[u];
55     intt x = query(a, b, l, i, m);
56     intt y = query(a, b, r, m+1, j);
57     return t::op(x, y);
58 }
59
60 void update(int a, int b, intt value,
61 int u, int i, int j) {
62     int m = (i+j)/2, l = u*2+1, r = u*2+2;
63     if (lazy[u])
64         propagate(u, i, j, lazy[u]);
65     if (a <= i and j <= b)
66         propagate(u, i, j, value);
67     else if (j < a or b < i) return; else {
68         update(a, b, value, l, i, m);
69         update(a, b, value, r, m+1, j);
70         st[u] = t::op(st[l], st[r]);
71     }
72 }
73
74 public:
75     SegTreeLazy(vector<intt>& v) {
76         arr = v;
77         n = v.size();
78         st.resize(n*4+5);
79         lazy.assign(n*4+5, 0);
80         build(0, 0, n-1);
81     }
82
83     intt query(int a, int b) {
84         return query(a, b, 0, 0, n-1);
85     }
86

```

```

87     void update(int a, int b, intt value) {
88         update(a, b, value, 0, 0, n-1);
89     }
90 };

```

### 1.3.3. Pair

```

1  #include <bits/stdc++.h>
2  #define inf 0x7fffffff
3  #define optimizar_io ios_base::sync_with_stdio(0);cin.tie(0);
4
5  using namespace std;
6
7  typedef long long int ll;
8  typedef pair <int,int> par;
9  typedef vector< par > vi;
10 class SegmentTree {
11 public:
12     SegmentTree(const vi&_A){
13         arr = _A; n = (int)arr.size();
14         tree.resize(4*n);
15         lazy.resize(4*n);
16         for(int i = 0; i < 4*n; i++){
17             lazy[i] = 0;
18             tree[i] = make_pair(0,i);
19         }
20         build_tree(1,0,n-1);
21     }
22     par rmq(ll i,ll j) {return query_tree(1,0,n-1,i,j);}
23     void update(ll i,ll j, ll val){update_tree(1,0,n-1,i,j,val);}
24 private:
25     vi arr, tree;
26     vector <long long int > lazy;
27     ll n;
28     void build_tree(ll node, ll a, ll b) {
29         if(a > b) return;
30         if(a == b) {
31             tree[node] = arr[a];
32             return;
33         }
34         build_tree(node*2, a, (a+b)/2);
35         build_tree(node*2+1, 1+(a+b)/2, b);
36         tree[node] = (tree[node*2].first < tree[node*2 +1].first) ?
37             tree[node*2] : tree[node*2+1];
38     }
39     void update_tree(ll node, ll a, ll b, ll i, ll j, ll value) {
40         if(lazy[node] != 0) {
41             tree[node].first += lazy[node]; //+=
42             if(a != b) {
43                 lazy[node*2] += lazy[node]; //+=
44                 lazy[node*2+1] += lazy[node]; //+=
45             }
46             lazy[node] = 0;
47         }
48         if(a > b || a > j || b < i) return;

```

```

50     if(a >= i && b <= j) {
51         tree[node].first += value; //+=
52         if(a != b) {
53             lazy[node*2] += value; //+=
54             lazy[node*2+1] += value; //+=
55         }
56         return;
57     }
58     update_tree(node*2, a, (a+b)/2, i, j, value);
59     update_tree(1+node*2, 1+(a+b)/2, b, i, j, value);
60     tree[node] = (tree[node*2].first < tree[node*2+1].first) ? tree[
        node*2] : tree[node*2+1];
61 }
62
63 par query_tree(ll node, ll a, ll b, ll i, ll j) {
64     //Cuidado con -inf que est como entero en caso de usar long
        long
65     if(a > b || a > j || b < i) return make_pair ((ll)inf,-1); //(-
        inf,max) (inf,min)
66     if(lazy[node] != 0){
67         tree[node].first += lazy[node]; //+=
68         if(a != b) {
69             lazy[node*2] += lazy[node]; //+=
70             lazy[node*2+1] += lazy[node]; //+=
71         }
72         lazy[node] = 0;
73     }
74
75     if(a >= i && b <= j) return tree[node];
76     par q1 = query_tree(node*2, a, (a+b)/2, i, j);
77     par q2 = query_tree(1+node*2, 1+(a+b)/2, b, i, j);
78     par res = (q1.first < q2.first) ? q1 : q2;
79     return res;
80 }
81 };
82
83 int main() {
84     //optimizar_io
85     int a,b,c,d,aux,aux2;
86     scanf("%d_%d_%d_%d",&a,&b,&c,&d);
87     vi conexo,disconexo;
88     conexo.resize(a);
89     disconexo.resize(a);
90     vector <vector <int> > adj;
91     adj.resize(a);
92     for(int i=0;i<b;i++){
93         cin>>aux >> aux2;
94         adj[aux-1].push_back(aux2-1);
95         adj[aux2-1].push_back(aux-1);
96     }
97     for(int i = 0; i < a; i++){
98         conexo[i] = make_pair(adj[i].size(),i);
99         disconexo[i] = make_pair(a-1-adj[i].size(),i);
100 }
101 SegmentTree amigo(conexo);
102 SegmentTree enemigo(disconexo);
103 vector <bool> respuesta;

```

```

104     respuesta.resize(a,true);
105     par temp;
106     while(1){
107         temp = amigo.rm(0,a-1);
108         if(temp.first >= c || c == 0){
109             temp = enemigo.rm(0,a-1);
110             if(temp.first >= d || d == 0)break;
111         }
112         respuesta[temp.second] = false;
113         for(int i = 0; i < adj[temp.second].size() ; i++){
114             amigo.update(adj[temp.second][i],adj[temp.second][i],-1);
115             enemigo.update(adj[temp.second][i],adj[temp.second][i],+1);
116         }
117         enemigo.update(0,a-1,-1);
118         amigo.update(temp.second,temp.second,50000000);
119         enemigo.update(temp.second,temp.second,50000000);
120     }
121     ll imprimir = 0;
122     for(int i = 0; i < a; i++)if(respuesta[i])imprimir++;
123     printf("%lld\n",imprimir);
124     return 0;
125 }

```

## 1.4. Wavelet Tree

```

1  typedef vector<int>::iterator iter;
2
3  class WaveTree {
4      vector<vector<int>> r0; int n, s;
5      vector<int> arrCopy;
6
7      void build(iter b, iter e, int l, int r, int u) {
8          if (l == r)
9              return;
10         int m = (l+r)/2;
11         r0[u].reserve(e-b+1); r0[u].push_back(0);
12         for (iter it = b; it != e; ++it)
13             r0[u].push_back(r0[u].back() + (*it<=m));
14         iter p = stable_partition(b, e, [=](int i){
15             return i<=m;});
16         build(b, p, l, m, u*2);
17         build(p, e, m+1, r, u*2+1);
18     }
19
20     int q, w;
21     int range(int a, int b, int l, int r, int u) {
22         if (r < q or w < l)
23             return 0;
24         if (q <= l and r <= w)
25             return b-a;
26         int m = (l+r)/2, za = r0[u][a], zb = r0[u][b];
27         return range(za, zb, l, m, u*2) +
28             range(a-za, b-zb, m+1, r, u*2+1);
29     }
30
31 public:
32     //arr[i] in [0,sigma)

```

```

33 WaveTree(vector<int> arr, int sigma) {
34     n = arr.size(); s = sigma;
35     r0.resize(s*2); arrCopy = arr;
36     build(arr.begin(), arr.end(), 0, s-1, 1);
37 }
38
39 //k in [1,n], [a,b) is 0-indexed, -1 if error
40 int quantile(int k, int a, int b) {
41     //extra conditions disabled
42     if (/*a < 0 or b > n or*/ k < 1 or k > b-a)
43         return -1;
44     int l = 0, r = s-1, u = 1, m, za, zb;
45     while (l != r) {
46         m = (l+r)/2;
47         za = r0[u][a]; zb = r0[u][b]; u*=2;
48         if (k <= zb-za)
49             a = za, b = zb, r = m;
50         else
51             k -= zb-za, a -= za, b -= zb,
52             l = m+1, ++u;
53     }
54     return r;
55 }
56
57 //counts numbers in [x,y] in positions [a,b)
58 int range(int x, int y, int a, int b) {
59     if (y < x or b <= a)
60         return 0;
61     q = x; w = y;
62     return range(a, b, 0, s-1, 1);
63 }
64
65 //count occurrences of x in positions [0,k)
66 int rank(int x, int k) {
67     int l = 0, r = s-1, u = 1, m, z;
68     while (l != r) {
69         m = (l+r)/2;
70         z = r0[u][k]; u*=2;
71         if (x <= m)
72             k = z, r = m;
73         else
74             k -= z, l = m+1, ++u;
75     }
76     return k;
77 }
78
79 //x in [0,sigma)
80 void push_back(int x) {
81     int l = 0, r = s-1, u = 1, m, p; ++n;
82     while (l != r) {
83         m = (l+r)/2;
84         p = (x<=m);
85         r0[u].push_back(r0[u].back() + p);
86         u*=2; if (p) r = m; else l = m+1, ++u;
87     }
88 }
89

```

```

90      //doesn't check if empty
91      void pop_back() {
92          int l = 0, r = s-1, u = 1, m, p, k; --n;
93          while (l != r) {
94              m = (l+r)/2; k = r0[u].size();
95              p = r0[u][k-1] - r0[u][k-2];
96              r0[u].pop_back();
97              u*=2; if (p) r = m; else l = m+1, ++u;
98          }
99      }
100
101      //swap arr[i] with arr[i+1], i in [0,n-1)
102      void swap_adj(int i) {
103          int &x = arrCopy[i], &y = arrCopy[i+1];
104          int l = 0, r = s-1, u = 1;
105          while (l != r) {
106              int m = (l+r)/2, p = (x<=m), q = (y<=m);
107              if (p != q) {
108                  r0[u][i+1] ^= r0[u][i] ^ r0[u][i+2];
109                  break;
110              }
111              u*=2; if (p) r = m; else l = m+1, ++u;
112          }
113          swap(x, y);
114      }
115  };

```

## Capítulo 2

# Grafos

### 2.1. DFS

```
1 void graphCheck(int u) {                                // DFS for checking graph
    edge properties
2     dfs_num[u] = DFS_GRAY;    // color this as DFS_GRAY (temp) instead
    of DFS_BLACK
3     for (int j = 0; j < (int)AdjList[u].size(); j++) {
4         ii v = AdjList[u][j];                            // weighted graph
5         if (dfs_num[v.first] == DFS_WHITE) {              // Tree Edge, DFS_GRAY
            to DFS_WHITE
6             dfs_parent[v.first] = u;                      // parent of this
            children is me
7             graphCheck(v.first);
8         }
9         else if (dfs_num[v.first] == DFS_GRAY) {          //
            DFS_GRAY to DFS_GRAY
10            if (v.first == dfs_parent[u])                  // to differentiate
                these two cases
11                printf("Bidirectional (%d, %d) - (%d, %d)\n", u, v.first,
                    v.first, u);
12            else // the most frequent application: check if the given
                graph is cyclic
13                printf("Back Edge (%d, %d) (Cycle)\n", u, v.first);
14        }
15        else if (dfs_num[v.first] == DFS_BLACK)            // DFS_GRAY
            to DFS_BLACK
16            printf("Forward/Cross Edge (%d, %d)\n", u, v.first);
17    }
18    dfs_num[u] = DFS_BLACK;    // after recursion, color this as
    DFS_BLACK (DONE)
19    topoSort.push_back(u);
20 }
```

### 2.2. Brexit

```
1 int main(){
2     int c,p,x,l;
```

```

3  cin>>c>>p>>x>>l;
4  int u,v;
5  vector<vector<int> > g(c,vector<int>());
6  for(int i=0;i<p;i++){
7      cin>>u>>v;
8      g[u-1].push_back(v-1);
9      g[v-1].push_back(u-1);
10 }
11 vector<int> d(c,0);
12 vector<int> ori(c,0);
13 for(int i=0;i<c;i++){
14     d[i]=ori[i]=g[i].size();
15 }
16 x--;
17 l--;
18 vector<bool> vivo(c,true);
19 vivo[l]=false;
20 queue<int> q;
21 q.push(l);
22 while(!q.empty()){
23     int nodo=q.front();
24     q.pop();
25     vivo[nodo]=false;
26     for(int i=0;i<g[nodo].size();i++){
27         int next=g[nodo][i];
28         if(vivo[next]){
29             d[next]--;
30             if(d[next]==ori[next]/2){
31                 q.push(next);
32             }
33         }
34     }
35 }
36 if(vivo[x]){
37     puts("stay");
38 }else{
39     puts("leave");
40 }
41 return 0;
42 }

```

## 2.3. Kruskal

```

1  vector< pair<int, ii> > EdgeList;    // (weight, two vertices) of
    the edge
2  for (int i = 0; i < E; i++) {
3      scanf("%d_%d_%d", &u, &v, &w);    // read the triple: (u,
        v, w)
4      EdgeList.push_back(make_pair(w, ii(u, v)));    // (w,
        u, v)
5      AdjList[u].push_back(ii(v, w));
6      AdjList[v].push_back(ii(u, w));
7  }
8  sort(EdgeList.begin(), EdgeList.end()); // sort by edge weight O(E
    log E)
9
    // note: pair object has built-in comparison
    function

```



```

10
11 int mst_cost = 0;
12 UnionFind UF(V);                                // all V are disjoint sets
    initially
13 for (int i = 0; i < E; i++) {                    // for each edge
    , O(E)
14     pair<int, int> front = EdgeList[i];
15     if (!UF.isSameSet(front.second.first, front.second.second)) { //
        check
16         mst_cost += front.first;                  // add the weight of e
            to MST
17         UF.unionSet(front.second.first, front.second.second); //
            link them
18     } }                                           // note: the runtime cost of UFDS is very
        light
19
20 // note: the number of disjoint sets must eventually be 1 for a
    valid MST
21 printf("MST cost = %d\n", mst_cost);

```

## 2.4. Single source shortest path

## 2.5. Edmond Blonsson

```

1  /*
2  GETS:
3  V->number of vertices
4  E->number of edges
5  pair of vertices as edges (vertices are 1..V)
6
7  GIVES:
8  output of edmonds() is the maximum matching
9  match[i] is matched pair of i (-1 if there isn't a matched pair)
10 */
11
12 // RECORDAR SETEAR LA VARIABLE GLOBAL V Y EL VECTOR DE VISITADOS
    ED O SINO NO FUNCIONA!!
13 #include <bits/stdc++.h>
14 using namespace std;
15 const int M=500;
16 struct struct_edge{int v;struct_edge* n;};
17 typedef struct_edge* edge;
18 struct_edge pool[M*M*2];
19 edge top=pool,adj[M];
20 int V,E,match[M],qh,qt,q[M],father[M],base[M];
21 bool inq[M],inb[M],ed[M][M];
22 void add_edge(int u,int v){
23     top->v=v,top->n=adj[u],adj[u]=top++;
24     top->v=u,top->n=adj[v],adj[v]=top++;
25 }
26 int LCA(int root,int u,int v){
27     static bool inp[M];
28     memset(inp,0,sizeof(inp));
29     while(1)
30     {
31         inp[u=base[u]]=true;

```

```

32         if (u==root) break;
33         u=father[match[u]];
34     }
35     while(1)
36     {
37         if (inp[v=base[v]]) return v;
38         else v=father[match[v]];
39     }
40 }
41 void mark_blossom(int lca,int u){
42     while (base[u]!=lca)
43     {
44         int v=match[u];
45         inb[base[u]]=inb[base[v]]=true;
46         u=father[v];
47         if (base[u]!=lca) father[u]=v;
48     }
49 }
50 void blossom_contraction(int s,int u,int v){
51     int lca=LCA(s,u,v);
52     memset(inb,0,sizeof(inb));
53     mark_blossom(lca,u);
54     mark_blossom(lca,v);
55     if (base[u]!=lca)
56         father[u]=v;
57     if (base[v]!=lca)
58         father[v]=u;
59     for (int u=0;u<V;u++)
60         if (inb[base[u]])
61         {
62             base[u]=lca;
63             if (!inq[u])
64                 inq[q[++qt]=u]=true;
65         }
66 }
67 int find_augmenting_path(int s){
68     memset(inq,0,sizeof(inq));
69     memset(father,-1,sizeof(father));
70     for (int i=0;i<V;i++) base[i]=i;
71     inq[q[qh=qt=0]=s]=true;
72     while (qh<=qt)
73     {
74         int u=q[qh++];
75         for (edge e=adj[u];e=e->n)
76         {
77             int v=e->v;
78             if (base[u]!=base[v]&&match[u]!=v)
79                 if ((v==s)|| (match[v]!=-1 && father[match[v]]!=-1))
80                     blossom_contraction(s,u,v);
81             else if (father[v]==-1)
82             {
83                 father[v]=u;
84                 if (match[v]==-1)
85                     return v;
86             }
87             else if (!inq[match[v]])
88                 inq[q[++qt]=match[v]]=true;
89         }
90     }

```

```

89     }
90 }
91 return -1;
92 }
93 int augment_path(int s,int t){
94     int u=t,v,w;
95     while (u!=-1)
96     {
97         v=father[u];
98         w=match[v];
99         match[v]=u;
100        match[u]=v;
101        u=w;
102    }
103    return t!=-1;
104 }
105 int edmonds(){
106     int matchc=0;
107     memset(match,-1,sizeof(match));
108     for (int u=0;u<V;u++){
109         if (match[u]==-1)
110             matchc+=augment_path(u,find_augmenting_path(u));
111     }
112     return matchc;
113 }
114 int main(){
115     int n,m;
116     scanf("%d %d",&n,&m);
117     string s;
118     vector < vector <string> > jueces(n);
119     vector < pair <int,int> > parejas;
120     int distintos = 0;
121     map <string,int> M;
122     int contador = 0;
123     for(int i = 0; i < n; i++){
124         for(int j = 0; j < m; j++){
125             cin >> s;
126             if(M.count(s) == 0){
127                 distintos++;
128                 // cout << s << endl;
129                 M[s] = contador;
130                 contador++;
131             }
132             jueces[i].push_back(s);
133         }
134     }
135     //printf("distintos = %d\n",distintos);
136     vector <vector <bool> > adj(distintos,vector <bool>(distintos,
137         true));
138     for(int i = 0; i < n; i++){
139         for(int j = 0; j < m; j++){
140             for(int k = j+1; k < m; k++){
141                 adj[M[jueces[i][j]]][M[jueces[i][k]]] = false;
142                 adj[M[jueces[i][k]]][M[jueces[i][j]]] = false;
143             }
144         }
145     }
146     V = distintos;

```

```

145     for(int i = 0; i < adj.size();i++){
146         for(int j = i+1; j < adj[i].size();j++){
147             if(adj[i][j] && !ed[i][j]){
148                 add_edge(i,j);
149                 ed[i][j]=ed[j][i]=true;
150             }
151         }
152     }
153     int final =edmonds();
154     if(final >= abs(m-distintos))puts("S");
155     else puts("N");
156     return 0;
157 }

```

## 2.6. Flood Fill

```

1  #include <bits/stdc++.h>
2
3  using namespace std;
4
5  int n,m;
6  int mapa[2020][2020];
7  int total;
8  int w;
9  int sumar=507;
10 int xx[]={0,0,1,-1};
11 int yy[]={1,-1,0,0};
12 #define fix(x) (x)=2*((x)+sumar)
13 typedef pair<int,int> ii;
14 inline bool check(int x,int y){
15     return x>=0 && x<2020 && y>=0 && y<2020;
16 }
17
18 void fill(int x,int y){
19     total--;
20     queue<ii> q;
21     q.push(ii(x,y));
22     mapa[x][y]=-1;
23     while(!q.empty()){
24         x=q.front().first;
25         y=q.front().second;
26
27         q.pop();
28         for(int i=0;i<4;i++){
29             //printf("ini: %d %d\n",x+xx[i],y+yy[i]);
30             if(check(x+xx[i],y+yy[i]) && mapa[x+xx[i]][y+yy[i]]<w){
31                 //printf("a: %d %d\n",x+xx[i],y+yy[i]);
32                 //printf("%d\n",mapa[x+2*xx[i]][y+2*yy[i]]);
33                 if(check(x+2*xx[i],y+2*yy[i])&&mapa[x+2*xx[i]][y+2*yy[i]]
34                     ]!=-1){
35                     //printf("b: %d %d\n",x+2*xx[i],y+2*yy[i]);
36                     mapa[x+2*xx[i]][y+2*yy[i]]=-1;
37                     //puts("a");
38                     total++;
39                     q.push(ii(x+2*xx[i],y+2*yy[i]));
40                     //printf("%d %d\n",q.front().first,q.front().second);

```

```

41
42     }
43
44     }
45 }
46 //puts("fin");
47 }
48
49 int main(){
50     int x1,y1,x2,y2,h,minX,maxX,minY,maxY;
51     while(scanf("%d",&n)){
52         total=0;
53
54         if(n==0){
55             break;
56         }
57         for(int i=0;i<2020;i++){
58             for(int j=0;j<2020;j++){
59                 mapa[i][j]=0;
60             }
61         }
62         minX=minY=10000;
63         while(n--){
64             scanf("%d%d%d%d%d",&x1,&y1,&x2,&y2,&h);
65             fix(x1);
66             fix(y1);
67             fix(x2);
68             fix(y2);
69             if(x1==x2){
70                 for(int i=min(y1,y2);i<=max(y1,y2);i++){
71                     mapa[x1][i]=h;
72                 }
73             }else{
74                 for(int i=min(x1,x2);i<=max(x1,x2);i++){
75                     mapa[i][y1]=h;
76                 }
77             }
78         }
79     }
80
81     scanf("%d",&w);
82     fill(1,1);
83
84     printf("%d\n",1010*1010-total-2);
85
86 }
87 return 0;
88 }

```

## 2.7. Dijkstra

Utilizamos la representacion vvii con pares (vecino,peso)

```
1 asd
```

## Capítulo 3

# Matemática

### 3.1. Formulas útiles

#### 3.1.1. Sumatorias

$$\begin{aligned}\sum_{i=1}^n i &= \frac{n(n+1)}{2} \\ \sum_{i=1}^n i^2 &= \frac{n(n+1)(2n+1)}{6} \\ \sum_{i=1}^n i^3 &= \frac{n^2(n+1)^2}{4}\end{aligned}$$

### 3.2. Teorema chino del resto

Para el sistema de congruencias:

$$x \equiv a_1 \pmod{n_1}$$

$$x \equiv a_2 \pmod{n_2}$$

$$\vdots$$

$$x \equiv a_k \pmod{n_k}$$

Si  $\forall i, j, i \neq j : n_i$  y  $n_j$  son coprimos, entonces el sistema tiene solución única módulo  $M = n_1 n_2 \dots n_k$

### 3.3. Pascal

```
1 for(int i=1;i<150;i++){
2     for(int j=1;j<i+3;j++){
3         pascal[i][j]=pascal[i-1][j-1]+pascal[i-1][j];
4     }
5 }
6 cin>>n;
7 for(ll i=0;i<n+1;i++){
8     printf("%lld_",pascal[n-1][i]);
9 }
```

### 3.4. Criba

```
1 vector<bool> isprime;
2 vector<int> primes;
3 void sieve(int n) {
4     isprime.assign(n + 1,true);
5
6     isprime[1] = false; isprime[2] = true;
7     for (int i = 2; i <= n; i++) {
8         if (isprime[i]) {
9             for (int j = i*i; j < n; j+=i) {
10                 isprime[j] = false;
11             }
12         }
13     }
14     for (int i = 2; i < n; i++) {
15         if (isprime[i]) {
16             primes.push_back(i);
17         }
18     }
19     return;
20 }
```

# Capítulo 4

## Geometria

### 4.1. Intersection

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 template< class T > bool inside(T a, T b, T c) { return a<=b && b<=
    c; }
4 typedef vector<int> vi;
5
6 class UnionFind{
7 private:
8     vi p, rank;
9 public:
10     UnionFind(int N){
11         rank.assign(N,0);
12         p.assign(N,0);
13         for(int i=0;i<N;i++){
14             p[i]=i;
15         }
16     }
17     int findSet(int i){
18         return (p[i]==i) ? i : (p[i] = findSet(p[i]));
19     }
20     bool isSameSet(int i, int j){
21         return findSet(i) == findSet(j);
22     }
23     void unionSet(int i,int j){
24         if(!isSameSet(i,j)){
25             int x = findSet(i), y = findSet(j);
26             if(rank[x]>rank[i]) p[y]=x;
27             else{
28                 p[x]=y;
29                 if(rank[x]==rank[y]) rank[y]++;
30             }
31         }
32     }
33     void imprimir(){
34         for(int i=0;i<p.size();i++) printf("%d_",p[i]);
35         puts("");
```



```

36     }
37 };
38
39 const int MAX = 1024;
40
41 struct Point { int x, y; };
42 struct Segment { Point a, b; };
43
44 Segment seg[MAX];
45 inline int direction(Point &pi, Point &pj, Point &pk) {
46     return (pk.x-pi.x)*(pj.y-pi.y)-(pj.x-pi.x)*(pk.y-pi.y);
47 }
48
49 inline bool onsegment(Point &pi, Point &pj, Point &pk) {
50     return (inside(min(pi.x,pj.x),pk.x,max(pi.x,pj.x)) && inside(min(
        pi.y,pj.y),pk.y,max(pi.y,pj.y)));
51 }
52
53 inline bool intersect(Point &p1, Point &p2, Point &p3, Point &p4) {
54     int d1, d2, d3, d4;
55     d1 = direction(p3, p4, p1);
56     d2 = direction(p3, p4, p2);
57     d3 = direction(p1, p2, p3);
58     d4 = direction(p1, p2, p4);
59     if(((d1>0 && d2<0)||(d1<0 && d2>0)) && ((d3>0 && d4<0)||(d3<0 &&
        d4>0))) return true;
60     if(!d1 && onsegment(p3, p4, p1)) return true;
61     if(!d2 && onsegment(p3, p4, p2)) return true;
62     if(!d3 && onsegment(p1, p2, p3)) return true;
63     if(!d4 && onsegment(p1, p2, p4)) return true;
64     return false;
65 }
66
67
68 int main(){
69     int t;
70     cin>>t;
71     int n,m;
72     while(t--){
73         Point p[n];
74         Point q[n];
75         cin>>n>>m;
76         for(int i=0;i<n;i++){
77             int a,b,c,d;
78             cin>>a>>b>>c>>d;
79             seg[i].a.x = a;
80             seg[i].a.y = b;
81             seg[i].b.x = c;
82             seg[i].b.y = d;
83         }
84         UnionFind uf(n);
85         for(int i=0;i<n;i++){
86             for(int j=i+1;j<n;j++){
87                 if( intersect(seg[i].a, seg[i].b, seg[j].a, seg[j].b)){
88                     uf.unionSet(i,j);
89                 }
90             }

```

```

91     }
92     // uf.imprimir();
93     for(int i=0;i<m;i++){
94         int a,b;
95         cin>>a>>b;
96         if(uf.isSameSet(a-1,b-1)) puts("YES");
97         else puts("NO");
98     }
99 }
100 return 0;
101 }

```

## 4.2. Rectangle union

```

1  #include <cstdio>
2  #include <algorithm>
3  using namespace std;
4  struct event {
5      int ind; // Index of rectangle in rects
6      bool type; // Type of event: 0 = Lower-left ; 1 = Upper-right
7      event() {} ;
8      event(int ind, int type) : ind(ind), type(type) {} ;
9  };
10 struct point {
11     int x, y;
12 };
13 int n, e; // n = number of rectangles; e = number of edges
14 point rects [1000][2]; // Each rectangle consists of 2 points: [0]
    = lower-left ; [1] = upper-right
15 event events_v [2000]; // Events of horizontal sweep line
16 event events_h [2000]; // Events of vertical sweep line
17 bool compare_x(event a, event b) { return rects[a.ind][a.type].x<
    rects[b.ind][b.type].x; }
18 bool compare_y(event a, event b) { return rects[a.ind][a.type].y<
    rects[b.ind][b.type].y; }
19 bool in_set [10000]; // Boolean array in place of balanced binary
    tree (set)
20 long long area; // The output: Area of the union
21 int main() { /// x -> v; y -> h
22     scanf("%d", &n);
23     for (int i=0;i<n;++i) {
24         scanf("%d_%d_%d_%d", &rects[i][0].x, &rects[i][0].y, // Lower-
            left coordinate
25             &rects[i][1].x, &rects[i][1].y); // Upper-right coordinate
26         events_v[e] = event(i, 0);
27         events_h[e++] = event(i, 0);
28         events_v[e] = event(i, 1);
29         events_h[e++] = event(i, 1);
30     }
31     sort(events_v, events_v+e, compare_x);
32     sort(events_h, events_h+e, compare_y); // Pre-sort set of
        horizontal edges
33     in_set[events_v[0].ind] = 1;
34     for (int i=1;i<e;++i) { // Vertical sweep line
35         event c = events_v[i];
36         int cnt = 0; // Counter to indicate how many rectangles are
            currently overlapping

```

```

37     // Delta_x: Distance between current sweep line and previous
        sweep line
38     int delta_x = rects[c.ind][c.type].x - rects[events_v[i-1].ind
        ][events_v[i-1].type].x;
39     int begin_y;
40     if (delta_x==0) continue;
41     for (int j=0;j<e;++j) if (in_set[events_h[j].ind]==1) { //
        Horizontal sweep line
42         if (events_h[j].type==0) {
43             if (cnt==0) begin_y = rects[events_h[j].ind][0].y; // Block
                starts
44             ++cnt;
45         } else {
46             --cnt;
47             if (cnt==0) { // Block ends
48                 int delta_y = (rects[events_h[j].ind][1].y-begin_y);
49                 area+=delta_x * delta_y;
50             }
51         }
52     }
53     in_set[c.ind] = (c.type==0);
54 }
55 printf("%lld\n", area);
56 return 0;
57 }

```

### 4.3. Closest pair

```

1  #define px second
2  #define py first
3  typedef pair<ll,ll> pairll;
4  int n;
5  pairll pnts[100000];
6  set<pairll> box;
7  double best;
8  int compx(pairll a,pairll b){
9      return a.px<b.px;
10 }
11 int main(){
12     scanf("%d",&n);
13     for(int i=0;i<n;i++){
14         scanf("%lld_%lld",&pnts[i].px,&pnts[i].py);
15     }
16     sort(pnts,pnts+n,compx);
17     best=1000000000000;
18     box.insert(pnts[0]);
19     int left=0;
20     for(int i=1;i<n;i++){
21         while(left<i && pnts[i].px-pnts[left].px > best) box.erase(pnts
            [left++]);
22         for(typeof(box.begin()) it=box.lower_bound(make_pair(pnts[i].py
            -best, pnts[i].px-best));
23             it!=box.end() && pnts[i].py+best>=it->py; it++){
24             best = min(best, sqrt(pow(pnts[i].py - it->py, 2.0)+pow(
                pnts[i].px - it->px, 2.0)));
25         }
26         box.insert(pnts[i]);

```

```

27     printf("%.2f\n",best);
28 }
29 }

```

#### 4.4. Radial sweep example

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  const double eps = 1e-10, PI = acos(-1.0);
5
6  inline int sgn(double x) {
7      if (fabs(x) <= eps) return 0;
8      else if (x > eps) return 1;
9      else return -1;
10 }
11
12 struct Point {
13     double x, y, ang;
14     Point() : x(0), y(0) {}
15     Point(double a, double b) : x(a), y(b) {
16         ang = atan2(y, x);
17     }
18     Point operator + (const Point &rhs) const {
19         return Point(x + rhs.x, y + rhs.y);
20     }
21     Point operator - (const Point &rhs) const {
22         return Point(x - rhs.x, y - rhs.y);
23     }
24     Point operator * (double k) const {
25         return Point(x * k, y * k);
26     }
27     Point operator / (double k) const {
28         return Point(x / k, y / k);
29     }
30     double dot(const Point &rhs) const {
31         return x * rhs.x + y * rhs.y;
32     }
33     double det(const Point &rhs) const {
34         return x * rhs.y - y * rhs.x;
35     }
36     double abs() const {
37         return hypot(x, y);
38     }
39     void read() {
40         scanf("%lf%lf", &x, &y);
41     }
42 } 0;
43
44 double nowAng;
45
46 Point inter(Point A, Point B, Point C, Point D) {
47     return A + (B - A) * ((D - C).det(C - A) / (D - C).det(B - A));
48 }
49
50 struct Line {
51     Point A, B;

```

```

52     Line() {}
53     Line(Point a, Point b) : A(a), B(b) {}
54     double dis() const {
55         if (sgn((O - A).det(O - B)) == 0) return min((O - A).abs(),
56             (O - B).abs());
57         return (O - inter(A, B, O, Point(cos(nowAng), sin(nowAng))))
58             .abs();
59     }
60     bool operator < (const Line &rhs) const {
61         return sgn(dis() - rhs.dis()) < 0;
62     };
63     struct Event {
64         double ang;
65         int id, type;
66         Event() : ang(0), id(0), type(0) {}
67         Event(double a, int b, int c) : ang(a), id(b), type(c) {}
68         bool operator < (const Event &rhs) const {
69             if (sgn(ang - rhs.ang) != 0) return sgn(ang - rhs.ang) < 0;
70             return type < rhs.type;
71         }
72     };
73
74     const int MAXN = 30000 + 10;
75
76     Point P[MAXN];
77     Line L[MAXN];
78     int S, N, M;
79
80     vector<Event> E;
81     set<Line> Seg;
82     set<Line>::iterator its[MAXN];
83
84     double fix(double x) {
85         if (x < 0) x += PI * 2;
86         if (x >= PI * 2) x -= PI * 2;
87         return x;
88     }
89
90     int gao(int id) {
91         int ret = 0;
92         E.clear();
93         for (int i = 0; i < N; ++ i) {
94             if (i == id) continue;
95             Point tmp = P[i] - P[id];
96             E.push_back(Event(tmp.ang, i, 1));
97         }
98         for (int i = 0; i < M; ++ i) {
99             Point A = L[i].A - P[id];
100             Point B = L[i].B - P[id];
101             double delta = fix(B.ang - A.ang);
102             if (sgn(delta - PI) > 0) swap(A, B);
103             if (sgn(A.ang - B.ang) > 0) {
104                 E.push_back(Event(A.ang, i, 0));
105                 E.push_back(Event(PI, i, 2));
106                 E.push_back(Event(-PI, i, 0));

```

```

107         E.push_back(Event(B.ang, i, 2));
108     }
109     else {
110         E.push_back(Event(A.ang, i, 0));
111         E.push_back(Event(B.ang, i, 2));
112     }
113 }
114 sort(E.begin(), E.end());
115 Seg.clear();
116 for (int i = 0; i < (int)E.size(); ++ i) {
117     int nowID = E[i].id;
118     nowAng = E[i].ang;
119     if (E[i].type == 0) {
120         its[nowID] = Seg.insert(Line(L[nowID].A - P[id], L[
            nowID].B - P[id])).first;
121     }
122     else if (E[i].type == 1) {
123         ret += (Seg.empty() || sgn(Seg.begin()->dis() - (P[id]
            - P[nowID]).abs()) > 0);
124     }
125     else if (E[i].type == 2) {
126         Seg.erase(its[nowID]);
127     }
128 }
129 return ret;
130 }
131
132 int main() {
133     0 = Point(0, 0);
134     while (scanf("%d%d%d", &S, &N, &M) == 3) {
135         for (int i = 0; i < N; ++ i) P[i].read();
136         for (int i = 0; i < M; ++ i) {
137             L[i].A.read();
138             L[i].B.read();
139         }
140         for (int i = 0; i < S; ++ i) {
141             printf("%d\n", gao(i));
142         }
143     }
144     return 0;
145 }

```

## 4.5. Line sweep example

```

1 struct point{
2     int x,y,valor;
3 };
4
5 bool comp1(const point &lhs,const point &rhs){
6     return lhs.y<rhs.y;
7 }
8
9 bool comp2(const point &lhs,const point &rhs){
10     return (lhs.x==rhs.x?lhs.y<rhs.y:lhs.x<rhs.x);
11 }
12
13 point poly[200010];

```

```

14
15 int main(){
16     int p,v;
17     while(scanf("%d %d",&p,&v)!=EOF){
18         for(int i=0;i<p;i++){
19             scanf("%d %d",&poly[i].x,&poly[i].y);
20             poly[i].valor=i+1;
21         }
22         for(int i=p;i<p+v;i++){
23             scanf("%d %d",&poly[i].x,&poly[i].y);
24             poly[i].valor=-1;
25         }
26
27         sort(poly,poly+p+v,comp1);           //orden por y;
28
29         int original=poly[0].y;                //compresion de puntos por y
30         int comprimido=1;
31         poly[0].y=comprimido;
32         for(int i=1;i<p+v;i++){
33             if(poly[i].y==original){
34                 poly[i].y=comprimido;
35             }else{
36                 original=poly[i].y;
37                 comprimido++;
38                 poly[i].y=comprimido;
39             }
40         }
41         FenwickTree FT(800010);
42         sort(poly,poly+p+v,comp2);           //orden por x
43         int perdido=0;
44         for(int i=0;i<p+v;i++){
45             if(poly[i].valor==-1){
46                 FT.update(poly[i].y,poly[i+1].y-1,1); //los vertices
47                 //siempre van de a pares
48                 i++;
49             }else{
50                 if(FT.query(poly[i].y)%2==0){
51                     perdido+=poly[i].valor;
52                 }
53             }
54             printf("%lld\n",perdido);
55         }
56         return 0;
57     }

```

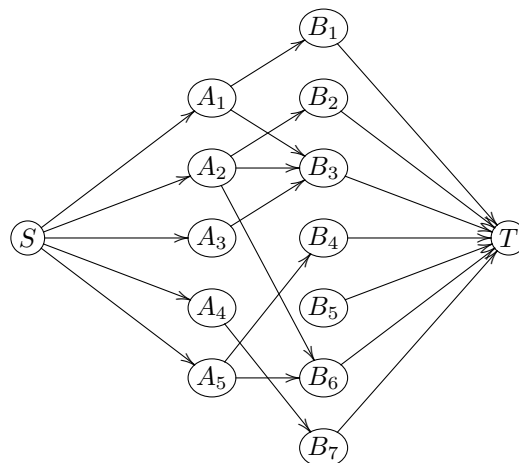
## Capítulo 5

# Flujo

### 5.1. Problemas de asignación

#### 5.1.1. Bipartite matching

Tenemos dos conjuntos  $A$  y  $B$ , donde cada elemento de  $A$  es compatible con ciertos elementos de  $B$ . Además, tenemos la condición de que podemos asociar cada elemento de  $A$  con a lo más un solo elemento de  $B$ . Bipartite matching nos permite saber la cantidad máxima de asociaciones posibles.



Modelamiento utilizado. Todas las aristas llevan 1 de flujo.



## 5.2. Dinic

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  typedef long long intt;
5  typedef pair<int, int> par;
6  typedef vector<vector<int> > graph;
7  typedef vector<vector<par> > wgraph;
8  #define pb push_back
9  #define ppb pop_back
10 vector <int> origen, destino, capacidad, costos, dia, orden, inicial;
11 class Dinic {
12     struct edge {
13         int to, rev;
14         intt f, cap;
15     };
16     vector<vector<edge>> g;
17     vector<intt> dist;
18     vector<int> q, work;
19     int n, sink;
20     bool bfs(int start, int finish) {
21         dist.assign(n, -1);
22         dist[start] = 0;
23         int head = 0, tail = 0;
24         q[tail++] = start;
25         while (head < tail) {
26             int u = q[head++];
27             for (const edge &e : g[u]) {
28                 int v = e.to;
29                 if (dist[v] == -1 and e.f < e.cap) {
30                     dist[v] = dist[u] + 1;
31                     q[tail++] = v;
32                 }
33             }
34         }
35         return dist[finish] != -1;
36     }
37     intt dfs(int u, intt f) {
38         if (u == sink) return f;
39         for (int &i = work[u]; i < (int)g[u].size(); ++i) {
40             edge &e = g[u][i];
41             int v = e.to;
42             if (e.cap <= e.f or dist[v] != dist[u] + 1)
43                 continue;
44             intt df = dfs(v, min(f, e.cap - e.f));
45             if (df > 0) {
46                 e.f += df;
47                 g[v][e.rev].f -= df;
48                 return df;
49             }
50         }
51         return 0;
52     }
53 public:
54     Dinic(int n) {
55         this->n = n;

```

```

56     g.resize(n);
57     dist.resize(n);
58     q.resize(n);
59 }
60 Dinic(){
61
62 }
63 // aristas bidireccionales si cap de edge b = cap, si es 0 no son
    bidireccionales!!
64 void add_edge(int u, int v, intt cap) {
65     edge a = {v, (int)g[v].size(), 0, cap};
66     edge b = {u, (int)g[u].size(), 0, 0};
67     g[u].pb(a);
68     g[v].pb(b);
69 }
70 intt max_flow(int source, int dest) {
71     sink = dest;
72     intt ans = 0;
73     while (bfs(source, dest)) {
74         work.assign(n, 0);
75         while (intt delta = dfs(source, 1000)) ans += delta;
76     }
77     return ans;
78 }
79 };
80
81 //contruyo el dinic
82
83 Dinic construir(int maximo,int tam,int g,int d){
84     Dinic D(tam+1);
85     for(int i = 0;i < inicial.size();i++){
86         D.add_edge(0,(i)*(d+1) +1,inicial[i]);
87     }
88     for(int i = 0; i < inicial.size();i++){
89         for(int j = 0; j < d; j++){
90             D.add_edge(i*(d+1) + 1 + j,i*(d+1)+2+j,g);
91         }
92     }
93     for(int i = 0;i < origen.size();i++)if(costos[i] <= maximo){
94         D.add_edge(origen[i],destino[i],capacidad[i]);
95     }
96     return D;
97 }
98
99 // busqueda binaria cuando quiero minimizar un valor X asociado al
    flujo
100
101 int BS(int lo,int hi, int tam,int tope,int d){
102     int mi;
103     while(lo<hi){
104         mi = (lo+hi)/2;
105         Dinic D = construir(orden[mi],tam,tope,d);
106         int flujo = D.max_flow(0,tam);
107         if(flujo==tope) hi = mi;
108         else lo = mi+1;
109     }
110     return lo;

```

```

111 }
112 int main(){
113     int t,aux;
114     scanf("%d",&t);
115     int caso = 1;
116     while(t--){
117         int n,d,m,u,v,c,p,e;
118         scanf("%d_%d_%d",&n,&d,&m);
119         origen.clear();destino.clear();capacidad.clear();
120         costos.clear(),orden.clear(),inicial.clear();
121         set <int> ordenNR;
122         for(int i = 0; i < m; i++){
123             scanf("%d_%d_%d_%d_%d",&u,&v,&c,&p,&e);
124             origen.push_back( (u-1)*(d+1) + e +1);
125             destino.push_back( (v-1)*(d+1) + e+2);
126             capacidad.push_back(c);
127             costos.push_back(p);
128             ordenNR.insert(p);
129         }
130         int total = 0;
131         for(int i = 0; i < n; i++){
132             scanf("%d",&aux);
133             inicial.pb(aux);
134             total += aux;
135         }
136         for(auto it = ordenNR.begin();it != ordenNR.end();it++){
137             orden.push_back(*it);
138         }
139         int tama = n*(d+1);
140         sort(orden.begin(),orden.end());
141         int sol = BS(0,orden.size()-1,tama,total,d);
142         printf("Case_%d:",caso);
143         Dinic D = construir(orden[sol],tama,total,d);
144         int flujo = D.max_flow(0,tama);
145         if(flujo>=total)printf("_%d\n",orden[sol]);
146         else puts("_Impossible");
147         caso++;
148     }
149     return 0;
150 }

```

## Capítulo 6

# Programación dinámica

### 6.1. 0/1 Knapsack

```
1  int f[1000]={0};
2  int n=0, m=0;
3  int main(void)
4  {
5      cin >> n >> m;
6      for (int i=1;i<=n;i++)
7      {
8          int price=0, value=0;
9          cin >> price >> value;
10         for (int j=m;j>=price;j--)
11             if (f[j-price]+value>f[j])
12                 f[j]=f[j-price]+value;
13     }
14     cout << f[m] << endl;
15     return 0;
16 }
```

### 6.2. Bitonic Sequence

```
1  /*
2   DP para obtener la secuencia bitonic mas larga
3   BitonicSubsequence = secuencia que en primera instancia crece, y
4                       luego decrece.
5   Complejidad  $O(n^2)$ 
6   Espacio lineal
7   */
8  #include <bits/stdc++.h>
9
10 using namespace std;
11
12 int bitonicSequence(vector <int> &bitonic){
13     int lis[bitonic.size()],lds[bitonic.size()];
14     for(int i = 0; i < bitonic.size();i++){
```

```

15     lis[i] = 1;
16     lds[i] = 1;
17 }
18 for(int i = 1; i < bitonic.size();i++){
19     for(int j = 0; j < i; j++){
20         if(bitonic[i] > bitonic[j])lis[i] = max(lis[i],lis[j]+1);
21     }
22 }
23 for(int i = bitonic.size()-2; i >= 0 ;i--){
24     for(int j = bitonic.size()-1; j > i; j--){
25         if(bitonic[i] > bitonic[j])lds[i] = max(lds[i],lds[j]+1);
26     }
27 }
28 int max = 0;
29 for(int i = 0; i < bitonic.size();i++){
30     if(max < lis[i] + lds[i]-1)max = lis[i] + lds[i]-1;
31 }
32 return max;
33 }
34
35 int main(){
36     vector <int> bitonic;
37     int n,aux;
38     scanf("%d",&n);
39     for(int i = 0; i < n; i++){
40         scanf("%d",&aux);
41         bitonic.push_back(aux);
42     }
43     printf("%d\n",bitonicSequence(bitonic));
44     return 0;
45 }
46
47 /*
48 16
49 0 8 4 12 2 10 6 14 1 9 5 13 3 11 7 5
50 */

```

### 6.3. Box Stacking

```

1 package com.interview.dynamic;
2
3 import java.util.Arrays;
4
5 /**
6  * Date 05/09/2015
7  * @author tusroy
8  *
9  * Given different dimensions and unlimited supply of boxes for
10  * each dimension, stack boxes
11  * on top of each other such that it has maximum height but with
12  * caveat that length and width
13  * of box on top should be strictly less than length and width of
14  * box under it. You can
15  * rotate boxes as you like.
16  *
17  * 1) Create all rotations of boxes such that length is always
18  * greater or equal to width

```

```

15  * 2) Sort boxes by base area in non increasing order (length *
    width). This is because box
16  * with more area will never ever go on top of box with less area.
17  * 3) Take T[] and result[] array of same size as total boxes after
    all rotations are done
18  * 4) Apply longest increasing subsequence type of algorithm to get
    max height.
19  *
20  * If n number of dimensions are given total boxes after rotation
    will be 3n.
21  * So space complexity is O(n)
22  * Time complexity - O(nlogn) to sort boxes. O(n^2) to apply DP on
    it So really O(n^2)
23  *
24  * References
25  * http://www.geeksforgeeks.org/dynamic-programming-set-21-box-
    stacking-problem/
26  * http://people.cs.clemson.edu/~bcdean/dp\_practice/
27  */
28  public class BoxStacking {
29
30      public int maxHeight(Dimension[] input) {
31          //get all rotations of box dimension.
32          //e.g if dimension is 1,2,3 rotations will be 2,1,3 3,2,1
33          //3,1,2 . Here length is always greater
34          //or equal to width and we can do that without loss of
35          //generality.
36          Dimension[] allRotationInput = new Dimension[input.length *
37              3];
38          createAllRotation(input, allRotationInput);
39
40          //sort these boxes in non increasing order by their base
41          //area.(length X width)
42          Arrays.sort(allRotationInput);
43
44          //apply longest increasing subsequence kind of algorithm on
45          //these sorted boxes.
46          int T[] = new int[allRotationInput.length];
47          int result[] = new int[allRotationInput.length];
48
49          for (int i = 0; i < T.length; i++) {
50              T[i] = allRotationInput[i].height;
51              result[i] = i;
52          }
53
54          for (int i = 1; i < T.length; i++) {
55              for (int j = 0; j < i; j++) {
56                  if (allRotationInput[i].length < allRotationInput[j]
57                      .length
58                      && allRotationInput[i].width <
59                          allRotationInput[j].width) {
60                      if (T[j] + allRotationInput[i].height > T[i]){
61                          T[i] = T[j] + allRotationInput[i].height;
62                          result[i] = j;
63                      }
64                  }
65              }
66          }
67      }
68  }

```

```

59         }
60
61         //find max in T[] and that will be our max height.
62         //Result can also be found using result[] array.
63         int max = Integer.MIN_VALUE;
64         for(int i=0; i < T.length; i++){
65             if(T[i] > max){
66                 max = T[i];
67             }
68         }
69
70         return max;
71     }
72
73     //create all rotations of boxes, always keeping length greater
74     or equal to width
75     private void createAllRotation(Dimension[] input,
76         Dimension[] allRotationInput) {
77         int index = 0;
78         for (int i = 0; i < input.length; i++) {
79             allRotationInput[index++] = Dimension.createDimension(
80                 input[i].height, input[i].length, input[i].
81                 width);
82             allRotationInput[index++] = Dimension.createDimension(
83                 input[i].length, input[i].height, input[i].
84                 width);
85             allRotationInput[index++] = Dimension.createDimension(
86                 input[i].width, input[i].length, input[i].
87                 height);
88         }
89     }
90
91     public static void main(String args[]) {
92         BoxStacking bs = new BoxStacking();
93         Dimension input[] = { new Dimension(3, 2, 5), new Dimension
94             (1, 2, 4) };
95         int maxHeight = bs.maxHeight(input);
96         System.out.println("Max height is " + maxHeight);
97         assert 11 == maxHeight;
98     }
99 }
100
101 /**
102  * Utility class to hold dimensions
103  * @author tusroy
104  */
105
106 class Dimension implements Comparable<Dimension> {
107     int height;
108     int length;
109     int width;
110
111     Dimension(int height, int length, int width) {
112         this.height = height;
113         this.length = length;
114         this.width = width;
115     }
116
117     public int compareTo(Dimension d) {
118         return this.height - d.height;
119     }
120 }

```

```

111     }
112
113     Dimension() {
114     }
115
116     static Dimension createDimension(int height, int side1, int
117         side2) {
118         Dimension d = new Dimension();
119         d.height = height;
120         if (side1 >= side2) {
121             d.length = side1;
122             d.width = side2;
123         } else {
124             d.length = side2;
125             d.width = side1;
126         }
127         return d;
128     }
129
130     /**
131      * Sorts by base area(length X width)
132      */
133     @Override
134     public int compareTo(Dimension d) {
135         if (this.length * this.width >= d.length * d.width) {
136             return -1;
137         } else {
138             return 1;
139         }
140     }
141
142     @Override
143     public String toString() {
144         return "Dimension[" + height + ", length=" + length
145             + ", width=" + width + "]";
146     }

```

#### 6.4. Break multiple words with no space into space

```

1 package com.interview.dynamic;
2
3 import java.util.*;
4
5 /**
6  * Date 08/01/2014
7  * @author tusroy
8  *
9  * Given a string and a dictionary, split this string into multiple
10     words such that
11     * each word belongs in dictionary.
12     *
13     * e.g peanutbutter -> pea nut butter
14     * e.g Iliketoplay -> I like to play
15     *

```





```

67     }
68
69     //fill up the matrix in bottom up manner
70     for(int l = 1; l <= word.length(); l++){
71         for(int i=0; i < word.length() -l + 1 ; i++){
72             int j = i + l-1;
73             String str = word.substring(i,j+1);
74             //if string between i to j is in dictionary T[i][j]
              is true
75             if(dict.contains(str)){
76                 T[i][j] = i;
77                 continue;
78             }
79             //find a k between i+1 to j such that T[i][k-1] &&
              T[k][j] are both true
80             for(int k=i+1; k <= j; k++){
81                 if(T[i][k-1] != -1 && T[k][j] != -1){
82                     T[i][j] = k;
83                     break;
84                 }
85             }
86         }
87     }
88     if(T[0][word.length()-1] == -1){
89         return null;
90     }
91
92     //create space separate word from string is possible
93     StringBuffer buffer = new StringBuffer();
94     int i = 0; int j = word.length() -1;
95     while(i < j){
96         int k = T[i][j];
97         if(i == k){
98             buffer.append(word.substring(i, j+1));
99             break;
100         }
101         buffer.append(word.substring(i,k) + " ");
102         i = k;
103     }
104
105     return buffer.toString();
106 }
107
108 /**
109  * Prints all the words possible instead of just one
    combination.
110  * Reference
111  * https://leetcode.com/problems/word-break-ii/
112  */
113 public List<String> wordBreakTopDown(String s, Set<String>
    wordDict) {
114     Map<Integer, List<String>> dp = new HashMap<>();
115     int max = 0;
116     for (String s1 : wordDict) {
117         max = Math.max(max, s1.length());
118     }
119     return wordBreakUtil(s, wordDict, dp, 0, max);

```

```

120     }
121
122     private List<String> wordBreakUtil(String s, Set<String> dict,
123         Map<Integer, List<String>> dp, int start, int max) {
124         if (start == s.length()) {
125             return Collections.singletonList("");
126         }
127         if (dp.containsKey(start)) {
128             return dp.get(start);
129         }
130
131         List<String> words = new ArrayList<>();
132         for (int i = start; i < start + max && i < s.length(); i++)
133         {
134             String newWord = s.substring(start, i + 1);
135             if (!dict.contains(newWord)) {
136                 continue;
137             }
138             List<String> result = wordBreakUtil(s, dict, dp, i + 1,
139                 max);
140             for (String word : result) {
141                 String extraSpace = word.length() == 0 ? "" : " ";
142                 words.add(newWord + extraSpace + word);
143             }
144         }
145         dp.put(start, words);
146         return words;
147     }
148
149     /**
150      * Check if any one solution exists.
151      * https://leetcode.com/problems/word-break/
152      */
153     public boolean wordBreakTopDownOneSolution(String s, Set<String>
154         wordDict) {
155         Map<Integer, Boolean> dp = new HashMap<>();
156         int max = 0;
157         for (String s1 : wordDict) {
158             max = Math.max(max, s1.length());
159         }
160         return wordBreakTopDownOneSolutionUtil(s, wordDict, 0, max,
161             dp);
162     }
163
164     private boolean wordBreakTopDownOneSolutionUtil(String s, Set<
165         String> dict, int start, int max, Map<Integer, Boolean> dp)
166     {
167         if (start == s.length()) {
168             return true;
169         }
170         if (dp.containsKey(start)) {
171             return dp.get(start);
172         }

```

```

170         for (int i = start; i < start + max && i < s.length(); i++)
171             {
172                 String newWord = s.substring(start, i + 1);
173                 if (!dict.contains(newWord)) {
174                     continue;
175                 }
176                 if (wordBreakTopDownOneSolutionUtil(s, dict, i + 1, max
177                     , dp)) {
178                     dp.put(start, true);
179                     return true;
180                 }
181             }
182         dp.put(start, false);
183         return false;
184     }
185
186     public boolean wordBreakBottomUp(String s, List<String>
187         wordList) {
188         boolean[] T = new boolean[s.length() + 1];
189         Set<String> set = new HashSet<>();
190         for (String word : wordList) {
191             set.add(word);
192         }
193         T[0] = true;
194         for (int i = 1; i <= s.length(); i++) {
195             for (int j = 0; j < i; j++) {
196                 if (T[j] && set.contains(s.substring(j, i))) {
197                     T[i] = true;
198                     break;
199                 }
200             }
201         }
202         return T[s.length()];
203     }
204
205     public static void main(String args[]){
206         Set<String> dictionary = new HashSet<String>();
207         dictionary.add("I");
208         dictionary.add("like");
209         dictionary.add("had");
210         dictionary.add("play");
211         dictionary.add("to");
212         String str = "Ihadliketoplay";
213         BreakMultipleWordsWithNoSpaceIntoSpace bmw = new
214             BreakMultipleWordsWithNoSpaceIntoSpace();
215         String result1 = bmw.breakWordDP(str, dictionary);
216
217         System.out.print(result1);
218     }
219 }

```

## 6.5. Burst Balloon

```

1 package com.interview.dynamic;
2
3 /**
4  * Date 03/02/2016

```

```

5  * @author Tushar Roy
6  *
7  * Given n balloons, indexed from 0 to n-1. Each balloon is painted
   with a number on it represented
8  * by array nums. You are asked to burst all the balloons. If the
   you burst balloon i you will
9  * get nums[left] * nums[i] * nums[right] coins. Here left and
   right are adjacent indices of i. After the burst,
10 * the left and right then becomes adjacent.
11 * Find the maximum coins you can collect by bursting the balloons
   wisely.
12 *
13 * Time complexity  $O(n^3)$ 
14 * Space complexity  $O(n^2)$ 
15 *
16 * Reference
17 * https://leetcode.com/problems/burst-balloons/
18 */
19 public class BurstBalloons {
20
21     /**
22      * Dynamic programming solution.
23      */
24     public int maxCoinsBottomUpDp(int[] nums) {
25
26         int T[][] = new int[nums.length][nums.length];
27
28         for (int len = 1; len <= nums.length; len++) {
29             for (int i = 0; i <= nums.length - len; i++) {
30                 int j = i + len - 1;
31                 for (int k = i; k <= j; k++) {
32                     //leftValue/rightValue is initially 1. If there
                       is element on
33                     // left/right of k then left/right value will
                       take that value.
34                     int leftValue = 1;
35                     int rightValue = 1;
36                     if (i != 0) {
37                         leftValue = nums[i-1];
38                     }
39                     if (j != nums.length - 1) {
40                         rightValue = nums[j+1];
41                     }
42
43                     //before is initially 0. If k is i then before
                       will
44                     //stay 0 otherwise it gets value T[i][k-1]
45                     //after is similarly 0 initially. if k is j
                       then after will
46                     //stay 0 other will get value T[k+1][j]
47                     int before = 0;
48                     int after = 0;
49                     if (i != k) {
50                         before = T[i][k-1];
51                     }
52                     if (j != k) {
53                         after = T[k+1][j];

```

```

54         }
55         T[i][j] = Math.max(leftValue * nums[k] *
56                             rightValue + before + after,
57                             T[i][j]);
58     }
59 }
60 return T[0][nums.length - 1];
61 }
62
63 /**
64  * Recursive solution.
65  */
66 public int maxCoinsRec(int nums[]) {
67     int[] nums1 = new int[nums.length + 2];
68     nums1[0] = 1;
69     nums1[nums1.length - 1] = 1;
70     for (int i = 0; i < nums.length; i++) {
71         nums1[i+1] = nums[i];
72     }
73     return maxCoinsRecUtil(nums1);
74 }
75
76 private int maxCoinsRecUtil(int[] nums) {
77     if (nums.length == 2) {
78         return 0;
79     }
80
81     int max = 0;
82     for (int i = 1; i < nums.length - 1; i++) {
83         int val = nums[i - 1]*nums[i]*nums[i+1] +
84                 maxCoinsRecUtil(formNewArray(nums, i));
85         if (val > max) {
86             max = val;
87         }
88     }
89     return max;
90 }
91
92 private int[] formNewArray(int[] input, int doNotIncludeIndex)
93 {
94     int[] newArray = new int[input.length - 1];
95     int index = 0;
96     for (int i = 0; i < input.length; i++) {
97         if (i == doNotIncludeIndex) {
98             continue;
99         }
100         newArray[index++] = input[i];
101     }
102     return newArray;
103 }
104
105 public static void main(String args[]) {
106     BurstBalloons bb = new BurstBalloons();
107     int input[] = {2, 4, 3, 5};

```

```

108         System.out.print(bb.maxCoinsBottomUpDp(input));
109     }
110 }

```

## 6.6. Catalan

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  /*
4  1) Count the number of expressions containing n pairs of
      parentheses which are correctly matched. For n = 3,
5  possible expressions are ((())), ()(()), ()()(), (())(), (()()).
6  2) Count the number of possible Binary Search Trees with n keys (
      See this)
7  3) Count the number of full binary trees (A rooted binary tree is
      full if every vertex has either two children or no children)
      with n+1 leaves.
8  */
9  // A recursive function to find nth catalan number
10 unsigned long int catalan(unsigned int n)
11 {
12     // Base case
13     if (n <= 1) return 1;
14
15     // catalan(n) is sum of catalan(i)*catalan(n-i-1)
16     unsigned long int res = 0;
17     for (int i=0; i<n; i++)
18         res += catalan(i)*catalan(n-i-1);
19
20     return res;
21 }
22
23 // Driver program to test above function
24 int main()
25 {
26     for (int i=0; i<10; i++)
27         cout << catalan(i) << " ";
28     return 0;
29 }

```

## 6.7. Coin changing

```

1  /*
2  DP sobre la cantidad de formas de pagar X dado un set de monedas(
      cantidad infinita)
3  Complejidad X*Monedas/
4  */
5
6  #include <bits/stdc++.h>
7
8  using namespace std;
9
10 int solution(int total, vector<int>&monedas){
11     vector <int> temp(total+1,0);
12     temp[0] = 1;

```

```

13     for(int i = 0; i < monedas.size();i++){
14         for(int j = 1; j <= total; j++)
15             if(j >= monedas[i])temp[j]+= temp[j-monedas[i]];
16     }
17     return temp[total];
18 }
19
20 int main(){
21     int total = 15;
22     vector <int> monedas;
23     monedas.push_back(3);
24     monedas.push_back(4);
25     monedas.push_back(6);
26     monedas.push_back(7);
27     monedas.push_back(9);
28     printf("%d\n",solution(total,monedas));
29     return 0;
30 }

```

## 6.8. Cutting sticks

```

1  //dada una vara, con cortes dados, el cortar cuesta el tamaño de
   la vara, se busca minimizar el costo total de realizar los
   cortes
2
3  #include <bits/stdc++.h>
4
5  int n, l, C[52], DP[52][52];
6  int min(int a, int b){ return (a < b)? a:b; }
7
8  int BottomUp(int ini, int fin)
9  {
10     int i, j, k, L;
11
12     /*Caso Base*/
13     for(i = 0; i < fin; i++)
14         DP[i][i+1] = 0;
15
16     for(L = 2; L <= fin; L++){
17         for(i = 0; i <= (fin - L); i++){
18             j = i + L;
19             DP[i][j] = INT_MAX;
20             for(k = i+1; k < j; k++){
21                 DP[i][j] = min(DP[i][j], DP[i][k] + DP[k][j] + (C[j]
22                                     ] - C[i]));
23             }
24         }
25
26         return DP[0][fin];
27     }
28
29     int main()
30     {
31         int i, sol;
32
33         while(1)

```



```

34     {
35         scanf("%d", &l);
36         if(l == 0) break;
37         scanf("%d", &n);
38         C[0] = 0;
39         for(i = 1; i <= n; i++)
40             scanf("%d", &C[i]);
41         C[n+1] = 1;
42         sol = BottomUp(0, n+1);
43         printf("The minimum cutting is %d.\n", sol);
44     }
45     return 0;
46 }

```

## 6.9. Distinct subsequence

```

1  package com.interview.dynamic;
2
3  /**
4   * Date 03/20/2016
5   * @author Tushar Roy
6   *
7   * Given a string S and a string T, count the number of distinct
8   * subsequences of T in S.
9   * Time complexity  $O(n^2)$ 
10  * Space complexity  $O(n^2)$ 
11  *
12  * https://leetcode.com/problems/distinct-subsequences/
13  */
14  public class DistinctSubsequence {
15      public int numDistinct(String s, String t) {
16          if (s.length() == 0 || t.length() == 0) {
17              return 0;
18          }
19          int[][] T = new int[t.length() + 1][s.length() + 1];
20          for (int i = 0; i < T[0].length; i++) {
21              T[0][i] = 1;
22          }
23          for (int i = 1; i < T.length; i++) {
24              for (int j = 1; j < T[0].length; j++) {
25                  if (s.charAt(j - 1) == t.charAt(i - 1)) {
26                      T[i][j] = T[i-1][j-1] + T[i][j-1];
27                  } else {
28                      T[i][j] = T[i][j-1];
29                  }
30              }
31          }
32          return T[t.length()][s.length()];
33      }
34
35      public static void main(String args[]) {
36          DistinctSubsequence ds = new DistinctSubsequence();
37          System.out.println(ds.numDistinct("abdacgblc", "abc"));
38      }
39  }

```

## 6.10. Divide and conquer

```

1  / tags: DP + divide and conquer optimization
2  #include <bits/stdc++.h>
3  using namespace std;
4  #define rep(i,a,b) for(int i=a; i<=b; i++)
5  typedef long long int ll;
6  #define MAXN 6000
7
8  int N;
9  ll B,C;
10 ll H[MAXN];
11 ll accH[MAXN];
12 ll accKH[MAXN];
13 ll dp[MAXN+1][MAXN];
14
15 ll deltaAccH(int i, int j) { return i > 0 ? accH[j] - accH[i-1] :
    accH[j]; }
16 ll deltaAccKH(int i, int j) { return i > 0 ? accKH[j] - accKH[i-1]
    : accKH[j]; }
17
18 // Compute total distance cost between i and j assuming that
19 // there is a station in both i and j
20 // (if i < 0, only in j)
21 // (if j >= N, only in i)
22 ll cost(int i, int j) {
23     // station only in j
24     if (i < 0) return j * accH[j] - accKH[j];
25
26     // station only in i
27     if (j >= N) return deltaAccKH(i, N-1) - i * deltaAccH(i, N-1);
28
29     // normal case: both stations
30     int ml = (i+j)/2;
31     int mr = ml+1;
32     ll left_cost = deltaAccKH(i, ml) - i * deltaAccH(i, ml);
33     ll right_cost = j * deltaAccH(mr, j) - deltaAccKH(mr, j);
34     return left_cost + right_cost;
35 }
36
37 // Solve DP[k][i] where i1 <= i <= i2 using divide and conquer
    optimization
38 // DP[k][i] = min { DP[k-1][j-1] + cost(j, i+1) for p1 <= j <= p2 }
39 void fill(int k, int i1, int i2, int j1, int j2) {
40     if (i1 > i2) return;
41     int im = (i1+i2)/2;
42     int jmin = max(j1, k-1);
43     int jmax = min(j2, im);
44     ll min_val = LLONG_MAX;
45     int best_j = -1;
46     rep(j,jmin,jmax) {
47         ll val = cost(j,im+1) + (j > 0 ? dp[k-1][j-1] : 0);
48         if (val < min_val) min_val = val, best_j = j;
49     }
50     dp[k][im] = min_val;
51     fill(k,i1,im-1,j1,best_j);
52     fill(k,im+1,i2,best_j,j2);

```

```

53 }
54
55 int main() {
56     while (scanf("%d%lld%lld", &N, &B, &C) == 3) {
57         rep(i,0,N-1) scanf("%lld", &H[i]);
58
59         // -- precompute acc sums --
60         accH[0] = H[0];
61         accKH[0] = 0;
62         rep(k, 1, N-1) {
63             accH[k] = accH[k-1] + H[k];
64             accKH[k] = accKH[k-1] + H[k] * k;
65         }
66
67         // -- DP --
68         // k = 0
69         rep(i,0,N-2) dp[0][i] = cost(-1, i+1);
70         // k >= 1
71         rep(k,1,N) fill(k,k-1,N-1,0,N-1);
72
73         // -- print output --
74         rep(k,1,N) {
75             if (k > 1) printf("\n");
76             ll total_cost = dp[k][N-1] * C + k * B;
77             printf("%lld", total_cost);
78         }
79         puts("");
80     }
81
82     return 0;
83 }

```

## 6.11. Edit Distance

```

1 package com.interview.dynamic;
2
3 import java.util.List;
4
5 /**
6  * Date 07/07/2014
7  * @author Tushar Roy
8  *
9  * Given two strings how many minimum edits(update, delete or add)
10    is needed to convert one string to another
11  *
12  * Time complexity is O(m*n)
13  * Space complexity is O(m*n)
14  *
15  * References:
16  * http://www.geeksforgeeks.org/dynamic-programming-set-5-edit-
17    distance/
18  * https://en.wikipedia.org/wiki/Edit\_distance
19  */
20 public class EditDistance {
21
22     /**
23      * Uses recursion to find minimum edits

```

```

22     */
23     public int recEditDistance(char[] str1, char str2[], int len1,
24                               int len2){
25         if(len1 == str1.length){
26             return str2.length - len2;
27         }
28         if(len2 == str2.length){
29             return str1.length - len1;
30         }
31         return min(recEditDistance(str1, str2, len1 + 1, len2 + 1)
32                   + str1[len1] == str2[len2] ? 0 : 1, recEditDistance(
33                     str1, str2, len1, len2 + 1) + 1, recEditDistance(str1,
34                     str2, len1 + 1, len2) + 1);
35     }
36
37     /**
38      * Uses bottom up DP to find the edit distance
39      */
40     public int dynamicEditDistance(char[] str1, char[] str2){
41         int temp[][] = new int[str1.length+1][str2.length+1];
42
43         for(int i=0; i < temp[0].length; i++){
44             temp[0][i] = i;
45         }
46
47         for(int i=0; i < temp.length; i++){
48             temp[i][0] = i;
49         }
50
51         for(int i=1; i <= str1.length; i++){
52             for(int j=1; j <= str2.length; j++){
53                 if(str1[i-1] == str2[j-1]){
54                     temp[i][j] = temp[i-1][j-1];
55                 }else{
56                     temp[i][j] = 1 + min(temp[i-1][j-1], temp[i-1][j], temp[i][j-1]);
57                 }
58             }
59         }
60
61         printActualEdits(temp, str1, str2);
62         return temp[str1.length][str2.length];
63     }
64
65     /**
66      * Prints the actual edits which needs to be done.
67      */
68     public void printActualEdits(int T[][], char[] str1, char[]
69                                   str2) {
70         int i = T.length - 1;
71         int j = T[0].length - 1;
72         while(true) {
73             if (i == 0 || j == 0) {
74                 break;
75             }
76             if (str1[i-1] == str2[j-1]) {

```

```

73         i = i-1;
74         j = j-1;
75     } else if (T[i][j] == T[i-1][j-1] + 1){
76         System.out.println("Edit_" + str2[j-1] + "_" + str1[i-1] + "in_" +
77             string2_to_string1);
78         i = i-1;
79         j = j-1;
80     } else if (T[i][j] == T[i-1][j] + 1) {
81         System.out.println("Delete_in_string1_" + str1[i-1]);
82         i = i-1;
83     } else if (T[i][j] == T[i][j-1] + 1){
84         System.out.println("Delete_in_string2_" + str2[j-1]);
85         j = j-1;
86     } else {
87         throw new IllegalArgumentException("Some_wrong_with_given_data");
88     }
89 }
90 }
91
92 private int min(int a,int b, int c){
93     int l = Math.min(a, b);
94     return Math.min(l, c);
95 }
96
97 public static void main(String args[]){
98     String str1 = "azced";
99     String str2 = "abcdef";
100     EditDistance editDistance = new EditDistance();
101     int result = editDistance.dynamicEditDistance(str1.toCharArray(), str2.toCharArray());
102     System.out.print(result);
103 }
104
105 }

```

## 6.12. Sum 2D Rectangle

```

1 package com.interview.dynamic;
2
3 /**
4  * Date 03/11/2016
5  * @author Tushar Roy
6  *
7  * Given a 2D array find the sum in given range defining a
8  * rectangle.
9  *
10 * Time complexity construction O(n*m)
11 * Time complexity of query O(1)
12 * Space complexity is O(n*m)
13 *
14 * Reference
15 * https://leetcode.com/problems/range-sum-query-2d-immutable/
16 */

```

```

16 public class Immutable2DSumRangeQuery {
17     private int[][] T;
18
19     public Immutable2DSumRangeQuery(int[][] matrix) {
20         int row = 0;
21         int col = 0;
22         if (matrix.length != 0) {
23             row = matrix.length;
24             col = matrix[0].length;
25         }
26         T = new int[row + 1][col + 1];
27         for (int i = 1; i < T.length; i++) {
28             for (int j = 1; j < T[0].length; j++) {
29                 T[i][j] = T[i - 1][j] + T[i][j - 1] + matrix[i -
30                     1][j - 1] - T[i - 1][j - 1];
31             }
32         }
33
34         public int sumQuery(int row1, int col1, int row2, int col2) {
35             row1++;
36             col1++;
37             row2++;
38             col2++;
39             return T[row2][col2] - T[row1 - 1][col2] - T[row2][col1 -
40                 1] + T[row1 - 1][col1 - 1];
41         }
42
43         public static void main(String args[]) {
44             int[][] input = {{3, 0, 1, 4, 2},
45                             {5, 6, 3, 2, 1},
46                             {1, 2, 0, 1, 5},
47                             {4, 1, 0, 1, 7},
48                             {1, 0, 3, 0, 5}};
49
50             int[][] input1 = {{2,0,-3,4}, {6, 3, 2, -1}, {5, 4, 7, 3},
51                             {2, -6, 8, 1}};
52             Immutable2DSumRangeQuery isr = new Immutable2DSumRangeQuery
53                 (input1);
54             System.out.println(isr.sumQuery(1, 1, 2, 2));
55         }
56     }
57 }

```

### 6.13. Sum Dice

```

1
2 package com.interview.dynamic;
3
4 /**
5  * @author Tushar Roy
6  * http://www.geeksforgeeks.org/dice-throw-problem/
7  * This solution assumes that 1,2,1 is different from 2,1,1 which
8  * is different from 1,1 2
9  * so total 3 ways are possible
10  * program to find number of ways to get sum 'x' with 'n'
11  */
12 public class DiceThrowWays {

```

```
12
13     public int numberOfWays(int n, int f, int k){
14
15         int T[][] = new int[n+1][k+1];
16         T[0][0] = 1;
17         /* for(int i=0; i < T.length; i++){
18             T[0][i] = 1;
19         }*/
20
21         for(int i=1; i <= n; i++){
22             for(int j=1; j <= i*f && j <= k ; j++){
23                 if(j == i){
24                     T[i][j] = 1;
25                     continue;
26                 }
27                 if(j < i){
28                     continue;
29                 }
30                 for(int l =1; l <=f ;l++){
31                     if(j >= l){
32                         T[i][j] += T[i-1][j-l];
33                     }
34                 }
35             }
36         }
37         return T[n][k];
38     }
39
40     public static void main(String args[]){
41         DiceThrowWays dtw = new DiceThrowWays();
42         System.out.println(dtw.numberOfWays(3, 3, 6));
43     }
44 }
```

## Capítulo 7

# Contenido adicional

### 7.1. Fast input

```
1
2 #define GETCHAR getchar_unlocked
3 #define PUTCHAR putchar_unlocked
4
5 inline void readInt(int &n){
6     n = 0;
7     bool flag=1;
8     char c;
9     int sign=1;
10    while (1){
11        c = GETCHAR();
12        if(c=='-') sign=-1;
13        else if(c>='0'&&c<='9') {n = n * 10 + c - '0';flag=0;}
14        else if(flag!=1) break;
15    }
16    n *= sign;
17 }
```

### 7.2. Usar en caso de emergencia





GOD BLESS OUR SAVIOUR

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