

Assignment 2: Python Code for BFGS and GA

AE413: Optimization techniques in engineering

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1 Overview

This report discusses the implementation and testing of two optimization algorithms: **BFGS (Broyden–Fletcher–Goldfarb–Shanno)** and **Genetic Algorithm (GA)** in python. Both algorithms serve different optimization needs, with BFGS being suitable for smooth, differentiable functions and GA being more flexible for complex, non-linear, and non-differentiable problems.

BFGS Algorithm

BFGS is a quasi-Newton method used to find local minima of smooth functions. It approximates the Hessian matrix to iteratively update the search direction, making it efficient for problems where derivatives are available and relatively inexpensive to compute. The BFGS method is particularly well-suited for smooth, unimodal functions and is widely used in various scientific and engineering applications due to its convergence properties and computational efficiency.

Genetic Algorithm (GA)

GA is an evolutionary algorithm inspired by the principles of natural selection and genetics. This implementation includes:

- **Elitism-based selection:** Ensures the fittest individuals are carried over to the next generation.
- **Simulated Binary Crossover (SBX):** Combines pairs of parents to produce offspring with a controlled level of diversity.
- **Normally Disturbed Mutation:** Introduces small variations in offspring to enhance exploration of the search space.

GA is particularly effective for global optimization, where the objective function may be non-linear, multi-modal, or non-differentiable.

2 Test Functions and Results

Two benchmark functions were used to evaluate the performance of BFGS and GA:

- **Bohachevsky Function:**

$$f(x, y) = x^2 + 2y^2 - 0.3 \cos(3\pi x) - 0.4 \cos(4\pi y) + 0.7$$

This unimodal function tests the algorithms' ability to converge to a global minimum in a smooth landscape.

- **Ackley Function:**

$$f(x, y) = -20 \exp \left(-0.2 \sqrt{0.5(x^2 + y^2)} \right) - \exp(0.5(\cos(2\pi x) + \cos(2\pi y))) + 20 + \exp(1)$$

Known for its numerous local minima, the Ackley function challenges the algorithms with a rugged, multimodal landscape.

3 Results from the Code

The following are sample outputs from running the BFGS and GA algorithms on the test functions:

```
Solution from BFGS: [-1.    1.5] and Solution from GA: [-0.99964371  1.65817322]
Solution from BFGS: [-0.    0.] and Solution from GA: [-0.06193411  0.02544361]
Solution from BFGS: [ 0. -0.] and Solution from GA: [0.01887624 0.95234389]
```

(Results may vary with different parameters)

4 Code Availability

The code for the BFGS and Genetic Algorithm implementations, including tests on the Bohachevsky and Ackley functions, is available on GitHub at: <https://github.com/airwarriorg91/Optimization-Techniques/tree/main/Assignment-2>

5 Conclusion

The BFGS algorithm is effective for smooth, unimodal functions like the Bohachevsky function, achieving convergence with relatively few iterations. The Genetic Algorithm, with elitism-based selection, SBX, and normally disturbed mutation, provides robust performance across both unimodal and multimodal functions, particularly with the challenging Ackley function. These results demonstrate the complementary strengths of BFGS and GA in solving diverse optimization problems.