

**DIFFERENTIAL EQUATIONS
(Common to CE, ME, CSE, IT Branches)****Time: 3 Hours****Max Marks: 60**

Answer ONE Question from each Unit

All Questions Carry Equal Marks

All parts of the Question must be answered at one place

UNIT-I

1. a) Solve $(4x^3y + 4\cos(2x)y^{-2})dx + (3x^4 - 5y^{-2})dy = 0$ **6M**
- b) Show that the family $y^2 = 4a(x+a)$, where 'a' is a parameter, is self-orthogonal **6M**
- (OR)
2. Find the orthogonal trajectories of the family $r^2 = a \cos 2\theta$, where 'a' is a parameter. **12M**

UNIT-II

3. a) Solve: $y''' - 2y'' + 4y' - 8y = 8\sin 2t$ **6M**
- b) Solve: $y'' - 2y' - 3y = -3te^{-t}$ **6M**
- (OR)
4. a) Solve: $y''' - 3y'' + 3y' - y = e^x$ **6M**
- b) Solve: $y'' - 6y' + 9y = \frac{e^{3t}}{t^2}$ **6M**

UNIT-III

5. Show that $\int_{-1}^1 x^n P_n(x) dx = \frac{2^{n+1} (n!)^2}{(2n+1)!}$, $n \in \mathbb{N}$. **12M**
6. a) Find $P_n(0)$, $n \in \mathbb{N}$ **6M**
- b) Show that $J_n'(x) = \frac{n}{x} J_n(x) - J_{n+1}(x)$ **6M**

UNIT-IV

7. a) Form the partial differential equation by eliminating the arbitrary functions f, g from $z = yf(x) + xg(y)$. **6M**
- b) Solve $(x^2 - yz)p + (y^2 - xz)q = (z^2 - yx)$ **6M**
- (OR)
8. a) Form the partial differential equation by eliminating the arbitrary functions f, g from $z = f(x)g(y)$ **6M**
- b) Solve $p(1+q) = qz$ **6M**

UNIT-V

9. Solve $\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial x \partial y} - 6 \frac{\partial^2 z}{\partial y^2} = y \cos x$ **12M**
- (OR)
10. Solve $\frac{\partial^3 z}{\partial x^3} - 2 \frac{\partial^3 z}{\partial x^2 \partial y} = 2e^{2x} + 3x^2 y$. **12M**

Time: 3 Hours**Max Marks: 60**

Answer ONE Question from each Unit

All Questions Carry Equal Marks

All parts of the Question must be answered at one place

UNIT-I

1. a) Solve $(D^2 - 4D + 3)y = 3e^x + 100$ 7M

b) Solve $(x^2y - 2xy^2) dx - (x^3 - 3x^2y) dy = 0$ 5M

(OR)

2. Solve $\frac{d^2y}{dx^2} - y = \frac{2}{1+e^x}$ by method of variation of parameters 12M

UNIT-II

3. Given that $f(x) = x$ for $0 < x < 2\pi$ find the Fourier expression of $f(x)$. 12M

(OR)

4. a) Find the Fourier series expansion of the periodic function of period 2π 7M

$$f(x) = \begin{cases} -\pi & -\pi < x < 0 \\ x & 0 < x < \pi \end{cases}$$

b) Represent the following function by a Fourier sine series $f(x) = e^{ax}$ for $0 < x < \pi$ 5M

UNIT-III

5. a) Using Fourier cosine integral representation of an appropriate function, show 6M

that $\int_0^\infty \frac{\cos wx}{k^2 + w^2} dw = \frac{\pi e^{-kx}}{2k}$, $x > 0$, $k > 0$

b) Find the Fourier sine transform of $f(x) = \frac{e^{-ax}}{x}$ for $0 < x < \pi$ 6M

(OR)

6. Prove that Fourier transform of $f(x) = e^{\frac{-x^2}{2}}$ is self reciprocal 12M

UNIT-IV

7. Obtain the Laplace transform of the following 12M

1) $t^2 e^t \sin 4t$

2) $e^{-4t} \frac{\sin 3t}{t}$

3) $\int_0^\infty \frac{e^{-t} - e^{-4t}}{t} dt$

(OR)

8. Using Laplace transform technique solve the following initial value 12M

problem $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + 2y = 5 \sin x$, where $y(0) = y'(0) = 0$

UNIT-V

9. a) State and Prove initial and final value theorems of Z-transforms 7M

b) Find the z-transform of $f(k) = \sin ak$, $a \geq 0$ 5M

(OR)

10. Solve $Z^{-1} \left[\frac{z^2 - 20z}{(z-2)^2(z-4)} \right]$ 12M

AR16

CODE: 16BS1002

SET-2

**ADITYA INSTITUTE OF TECHNOLOGY AND MANAGEMENT, TEKKALI
(AUTONOMOUS)**

I B.Tech II Semester Supplementary Examinations, February-2022

**ENGINEERING MATHEMATICS – II
(Common to all Branches)**

Time: 3 Hours

Max Marks: 70

Answer ONE Question from each Unit

All Questions Carry Equal Marks

All parts of the Question must be answered at one place

UNIT-I

1. Find a positive root of $x^3 - x - 1 = 0$ correct upto two decimal places by using Bisection method. 14M

(OR)

2. a Determine the missing values in the following table 7M

x	0	5	10	15	20	25
y	6	10	-	17	-	31

- b Determine the polynomial using Newton's forward difference formula, from the following data 7M

x	0	1	2	3
f(x)	1	2	1	10

UNIT-II

3. a Evaluate $\int_0^1 \frac{1}{1+x} dx$ by using Trapezoidal rule 7M

- b Evaluate $\int_0^1 \frac{1}{1+x} dx$ by using Simpson's $\frac{1}{3}$ rule. 7M

(OR)

4. Using Runge-Kutta method of fourth order, solve $\frac{dy}{dx} = 1 + y^2$ with $y(0) = 0$ at $x = 0.2, 0.4$ 14M

UNIT-III

5. a Find the Laplace transform of $(\sin t - \cos t)^2$ 7M

- b Find the Laplace transforms of the function $f(t) = \frac{e^{-at} - e^{-bt}}{t}$ 7M

(OR)

6. Using Laplace transform solve the differential equation $(D^2 + 2D - 3)y = \sin t, y(0) = y'(0) = 0$ 14M

UNIT-IV

7. a Determine the Fourier series for $f(x) = 1 - x^2$ in $(-1,1)$ 7M
- b Obtain the half range sine series $f(x) = x^2$ in $(0,4)$ 7M
- (OR)**
8. Determine the Fourier series for $f(x) = x$ in $(0, 2\pi)$ 14 M

UNIT-V

9. Form a partial differential equation from $z = x f(ax + by) + g(ax + by)$, where f and g are arbitrary functions and a is a constant 14M
- (OR)**
10. Solve the one dimensional wave equation $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$ subject to $y(0,t) = 0$, $y(\pi,t) = 0$, $y(x,0) = \sin 2x$ and $\frac{\partial y}{\partial t}(x,0) = 0$, where $0 \leq x \leq \pi$ and $t \geq 0$ 14M

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AR13

CODE: 13BS1003

SET-1

ADITYA INSTITUTE OF TECHNOLOGY AND MANAGEMENT, TEKKALI
(AUTONOMOUS)

I B.Tech II Semester Supplementary Examinations, February-2022

ENGINEERING MATHEMATICS -III (Common to all Branches)

Time: 3 Hours

Max Marks: 70

PART-A

ANSWER ALL QUESTIONS

[1 x 10 = 10 M]

1. a) Define the rank of Matrix
- b) Define eigen values and eigen vectors
- c) Define Fourier Sine and Cosine integral formulas
- d) Write the Fourier series formula in the interval $(-l, l)$
- e) State Cayley – Hamilton theorem
- f) Find the rank of the matrix $\begin{bmatrix} -1 & 0 & 6 \\ 3 & 6 & 1 \\ -5 & 1 & 3 \end{bmatrix}$
- g) Write the Dirichlet conditions of Fourier series
- h) Define Beta function
- i) Write Gamma function
- j) Write the value of $\zeta(a^n)$

PART-B

Answer one question from each unit

[5x12=60M]

UNIT-I

2. Define rank of the matrix ? Find the rank of the matrix by reducing it to normal form 12M

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3 \\ 3 & 0 & 5 & -10 \end{bmatrix}$$

(OR)

3. Analyse for what values of a, b the equations $x + y + z = 3$, $x + 2y + 2z = 6$, $x + ay + 3z = b$ have
i) no solution ii) a unique solution iii) an infinite number of solutions? 12M

UNIT-II

4. Find the Eigen values of the matrix $A = \begin{bmatrix} 3 & -2 & -5 \\ 4 & -1 & -5 \\ -2 & -1 & -3 \end{bmatrix}$ and the corresponding Eigen vectors. 12M

(OR)

5. Find the nature, index and signature of the quadratic form $10x^2 + 2y^2 + 5z^2 - 4xy - 10zx + 6yz$ 12M

UNIT-III

6. Obtain the half-range Fourier cosine and sine series for the function $f(x) = x$ in the interval $0 < x < 2\pi$. 12M

(OR)

7. a) Find the Fourier transform of $f(x) = e^{-x/2}$, $-\infty < x < \infty$ 6M
b) Find the Fourier sin transform of $2e^{-5x} + 5e^{-2x}$ 6M

UNIT-IV

8. Solve $Z^{-1} \left[\frac{z^3 - 20z}{(z-2)^3(z-4)} \right]$ 12M

(OR)

9. Solve the difference equation, using Z-transform:
 $u_{n+2} - 3u_{n+1} + 2u_n = 0$, $u_0 = 0$, $u_1 = 1$ 12M

UNIT-V

10. Show that $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$. 12M

(OR)

11. a) Evaluate $\int_0^2 (8 - x^3)^{1/3} dx$ using β and γ functions 6M

- b) Prove that $\int_0^\infty e^{-y^{1/m}} dy = m\Gamma(m)$ 6M