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Introduction to Deep Learning for Engineers

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Amir Barati Farimani
Associate Professor of Mechanical Engineering and Bio-Engineering
Carnegie Mellon University

Story so far on CNN:

1. Concept of Representation + Learning

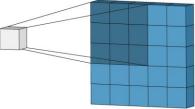
We need a UNIVERSAL REPRESENTATION LEARNER to ease the learning

2. How to learn robust representation?

We need a representation learner that can automatically learn the features needed for the task

3. How to learn spatial, high level features (Swan example)
Since high level features are spatial (not pixels) we need a scanner to scan patches of data instead of single pixels



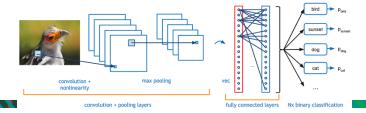


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Story so far on CNN:

- 4. How to build a scanner for feature learning? what should be the properties of this scanner?
- 1. It should be numbers (a matrix) because it should be machine readable
- 2. It should be learnable
- 3. It should be flexible in size and dimension
- 4. Should be pluggable to Neural Networks
- 5. Can we design the scanners based on the learning tasks?

Yes, and we should. Because the mode of data might be different (sound, image, video) and features are needed based on the task to make a good model, the scanner should ONLY learn the relevant features connecting them to the output





Story so far on CNN:

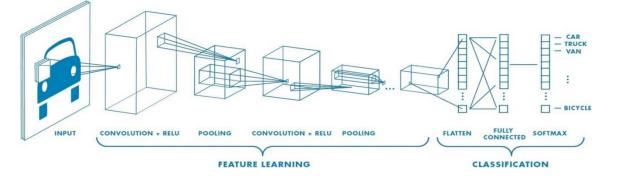
6. How can the scanners learn?

Inspired by iterative optimization and backpropagation in neural networks, we can iteratively learn the initialized weights of scanners (remember these are numbers)

7. How can we plug in the scanners into Neural networks?

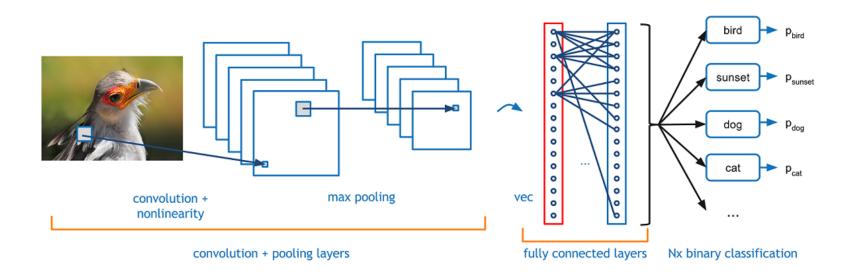
By flattening the output of the last convolved map and passing it to the FC layer, we can forward propagate, and we can backpropagate to learn the parameters of a filter

(scanner)





Recap: CNN Overall Architecture





CNNs are Automatic Feature Detectors

Sharing Weights

Feature Detection

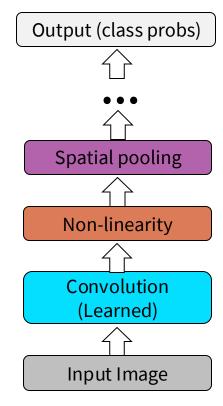
Spatial Local Features

Translation In-variant



Convolutional Neural Networks (CNN)

- FEED-FORWARD FEATURE EXTRACTION:
 - 1. Convolve input with learned filters
 - 2. Apply non-linearity
 - 3. Spatial pooling (downsample)
- SUPERVISED TRAINING OF CONVOLUTIONAL FILTERS BY BACK-PROPAGATING CLASSIFICATION ERROR



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Convolution

- APPLY LEARNED FILTER WEIGHTS
- ONE FEATURE MAP PER FILTER
- STRIDE CAN BE GREATER THAN 1 (FASTER, LESS MEMORY)







Feature Map

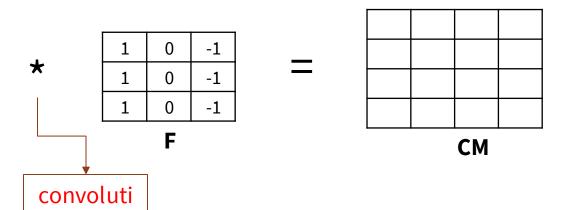


Assume a 6x6 matrix **M** as input. The 2D convolution of **M** with *filter* (*or kernel*) **F** and *stride* 1 is a 4x4 matrix **CM** (sometimes called *feature map*) computed as follows:

on

operator

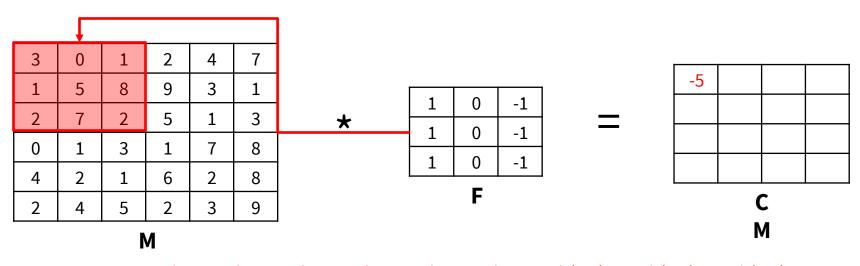
3	3 0 1 2 4 7												
1	5	8	9	3	1								
2 7 2 5 1 3													
0	1	3	1	7	8								
4	2	1	6	2	8								
2 4 5 2 3 9													
			M										



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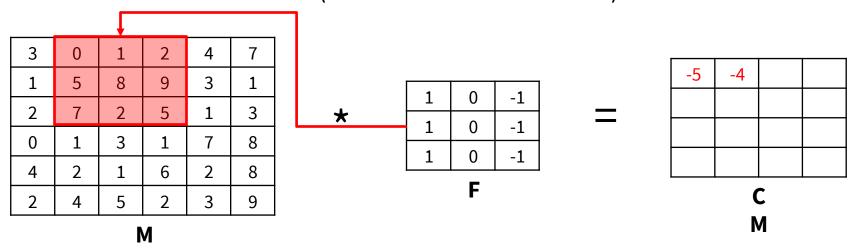
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$$3*1 + 1*1 + 2*1 + 0*0 + 5*0 + 7*0 + 1*(-1) + 8*(-1) + 2*(-1)$$



Assume a 6x6 matrix **M** as input. The 2D convolution of **M** with *filter* (*or kernel*) **F** and *stride* 1 is a 4x4 matrix **CM** (sometimes called *feature map*) computed as follows:



0*1 + 5*1 + 7*1 + 1*0 + 8*0 + 2*0 + 2*(-1) + 9*(-1) + 5*(-1)



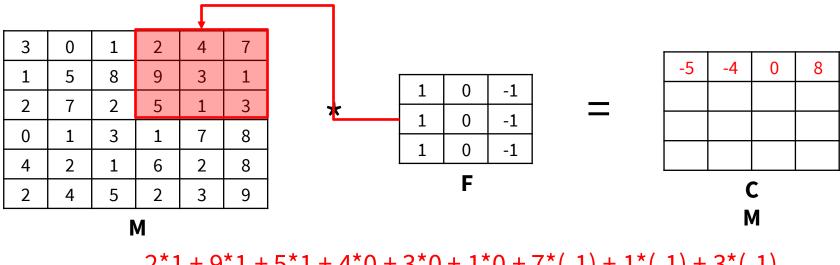
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0	1	3	1	7	8			1	0	-1					
4	2	1	6	2	8			1	0	-1					
2	4	5	2	3	9				F				(
		ı	M			•							N	1	

$$1*1 + 8*1 + 2*1 + 2*0 + 9*0 + 5*0 + 4*(-1) + 3*(-1) + 1*(-1)$$



Assume a 6x6 matrix **M** as input. The 2D convolution of **M** with *filter (or kernel)* **F** and *stride* 1 is a 4x4 matrix **CM** (sometimes called *feature map*) computed as follows:



$$2*1 + 9*1 + 5*1 + 4*0 + 3*0 + 1*0 + 7*(-1) + 1*(-1) + 3*(-1)$$



ASSUME A 6x6 MATRIX **M** AS INPUT. THE 2D CONVOLUTION OF **M** WITH *FILTER* (*OR KERNEL*) **F** AND *STRIDE* **1** IS A 4x4 MATRIX **CM** (SOMETIMES CALLED *FEATURE MAP*) COMPUTED AS FOLLOWS:

3	6	1	2	4	7									
1	5	8	9	3	1					•	-5	-4	0	8
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		ľ	M			•						N	4	

$$1*1 + 2*1 + 0*1 + 5*0 + 7*0 + 1*0 + 8*(-1) + 2*(-1) + 3*(-1)$$



Assume a 6x6 matrix **M** as input. The 2D convolution of **M** with *filter (or kernel)* **F** and *stride* 1 is a 4x4 matrix **CM** (sometimes called *feature map*) computed as follows:

1 5 8 9 3 1 2 7 2 5 1 3 0 1 3 1 7 8 4 2 1 6 2 8 2 4 5 2 3 9			ľ	М										N	1	
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3 0 1 2 4 7	3	0	ſ	2	4	7		1								

$$5*1 + 7*1 + 1*1 + 8*0 + 2*0 + 3*0 + 9*(-1) + 5*(-1) + 1*(-1)$$



The Convolution operation¹

Assume a 6x6 matrix **M** as input. The 2D convolution of **M** with *filter (or kernel)* **F** and *stride* 1 is a 4x4 matrix **CM** (sometimes called *feature map*) computed as follows:

		N	M											
2	4	5	2	3	9			F					CM	
4	2	1	6	2	8				-1		-3	-2	-3	-16
0	1	3	1	7	8		1	0	- <u>l</u>		0	-2	-4	-7
2	7	2	5		3	ж	1	0	- <u>l</u>	=	-10	-2	2	3
1	5	8	9	3	1		1	0	1		-5	-4	0	8
3	0	1	2	4	7							_		

1*1 + 6*1 + 2*1 + 7*0 + 2*0 + 3*0 + 8*(-1) + 8*(-1) + 9*(-1)

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ASSUME A M, A 7x7 MATRIX. THE 2D CONVOLUTION OF M WITH *FILTER* F AND *STRIDE* 2 IS A 3x3 MATRIX **CM** COMPUTED AS FOLLOWS:

	Ţ					7	_							
2	3	7	4	6	2	9								
6	6	9	8	7	4	3								
3	4	8	3	8	9	7		3	4	4		91		
7	8	3	6	6	3	4_	*	1	0	2	=			
4	2	1	8	3	4	6		-1	0	3				
3	2	4	1	9	8	3			F		I		CN	V
0	1	3	9	2	1	4			-				0.	-

M

$$2*3 + 6*1 + 3*(-1) + 3*4 + 6*0 + 4*0 + 7*4 + 9*2 + 8*3$$



ASSUME A M, A 7x7 MATRIX. THE 2D CONVOLUTION OF M WITH FILTER F AND STRIDE 2 IS A

					3x	(3 MA	TRIX CM COI	MPUT	ED AS	FOLI	_OWS:		
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7	8	3	6	6	3	4	*	1	0	2	=		
4	2	1	8	3	4	6		-1	0	3			
3	2	4	1	9	8	3			F		1		<u> </u>
0	1	3	9	2	1	4			-				M
			M	-	•								

7*3 + 9*1 + 8*(-1) + 4*4 + 8*0 + 3*0 + 6*4 + 7*2 + 8*3



Assume a M, a 7x7 matrix. The 2D convolution of M with *filter* F and *stride* 2 is a 3x3 matrix **CM** computed as follows:

					lue									
2	3	7	4	6	2	9								
6	6	9	8	7	4	3								
3	4	8	3	8	9	7		3	4	4		91	100	88
7	8	3	6	6	3	4	*	1	0	2	=			
4	2	1	8	3	4	6		-1	0	3				
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0	1	3	9	2	1	4			-				M	
	-		M	•										

$$6*3 + 7*1 + 8*(-1) + 2*4 + 4*0 + 9*0 + 9*4 + 3*2 + 7*3$$



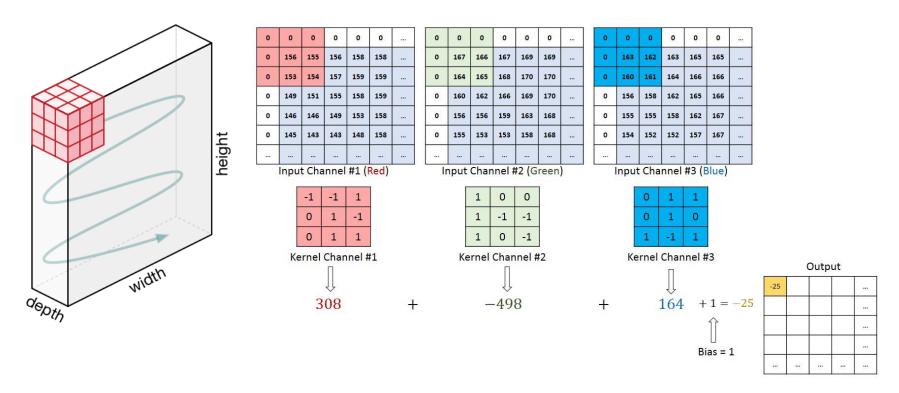
Assume a M, a 7x7 matrix. The 2D convolution of M with *filter* F and *stride* 2 is a 3x3 matrix **CM** computed as follows:

L	U	+	ا ک	ا ع		+	+							M	
Γ	0	1	3	9	2	1	4			•					
	3	2	4	1	9	8	3			F		I		C	
	4	2	1	8	3	4	6		-1	0	3				
	7	8	3	6	6	3	4_	*	1	0	2	=	57		
B	3	4	8	3	8	9	7	_	3	4	4		91	100	88
	6	6	9	8	7	4	3								
	2	3	7	4	6	2	9								

$$3*3 + 7*1 + 4*(-1) + 4*4 + 8*0 + 2*0 + 8*4 + 3*2 + 1*3$$



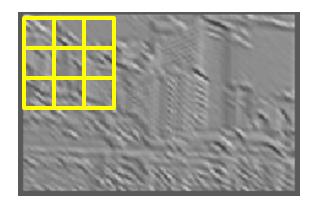
Recap: How it works for Images?



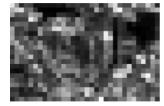


Spatial Pooling

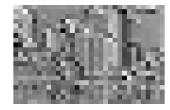
- SUM OR MAX OVER NON-OVERLAPPING / OVERLAPPING REGIONS
- ROLE OF POOLING:
 - Invariance to small transformations
 - Larger receptive fields (neurons see more of input)



Max



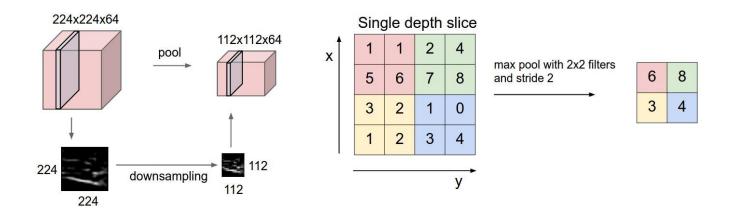
Sum



Adapted from Rob Fergus

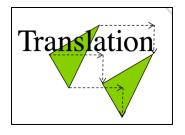
Spatial Pooling

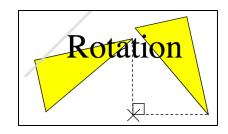
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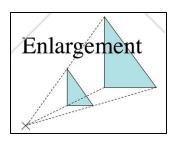


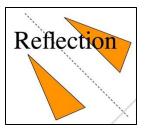


Some Types of Linear Transformations











Types of Pooling functions

- A pooling function replaces the output of the net at a certain location with a summary statistic of the nearby inputs
- Popular pooling functions:
 - max pooling operation reports the maximum output within a rectangular neighborhood
 - 2. Average of a rectangular neighborhood
 - 3. L² norm of a rectangular neighborhood
 - 4. Weighted average based on the distance from the central pixel



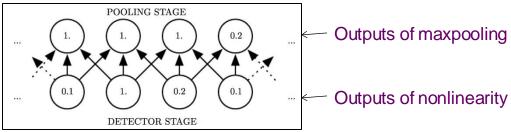
Pooling Causes Translation Invariance

- In all cases, pooling helps make the representation become approximately *invariant* to small translations of the input
 - If we translate the input by a small amount values of most of the outputs does not change (example next slide)
 - Pooling can be viewed as adding a strong prior that the function the layer learns must be invariant to small translations

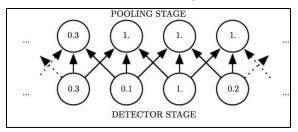


Max Pooling Introduces Invariance to Translation

View of middle of output of a convolutional layer



Same network after the input has been shifted by one pixel



 Every input value has changed, but only half the values of output have changed because maxpooling units are only sensitive to maximum value in neighborhood not exact value



Importance of Translation Invariance

- Invariance to translation is important if we care about whether a feature is present rather than exactly where it is
 - Ex: for detecting a face just need to know that an eye is present in a region, not its exact location
- In other context it is more important to preserve location of a feature
 - Ex: to determine a corner we need to know whether two edges are present and test whether they meet



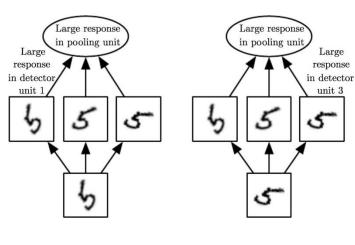
Learning other Invariances

- Pooling over spatial regions produces invariance to translation
- But if we pool over the results of separately parameterized convolutions, the features can learn which transformations to become invariant to



Learning Invariance to Rotation

 A pooling unit that pools over multiple features that are learned with separate parameters can learn to be invariant to transformations of the input



Input tilted left gets large response from unit tuned to left-tilted images Tilted Right



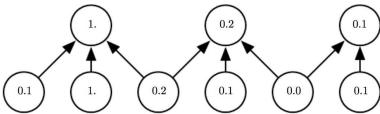
Using Fewer Pooling Units than Detector Units

- Because pooling summarizes the responses over a whole neighborhood, it is possible to use fewer pooling units than detector units
 - This is due to the effect of reporting summary statistics for pooling regions spaced k
 pixels apart rather than one pixel apart
 - This improves computational efficiency because the next layer has k times fewer inputs to process
- An example is given next



Pooling with Downsampling

 Max-pooling with a pool width of three and a stride between pools of two

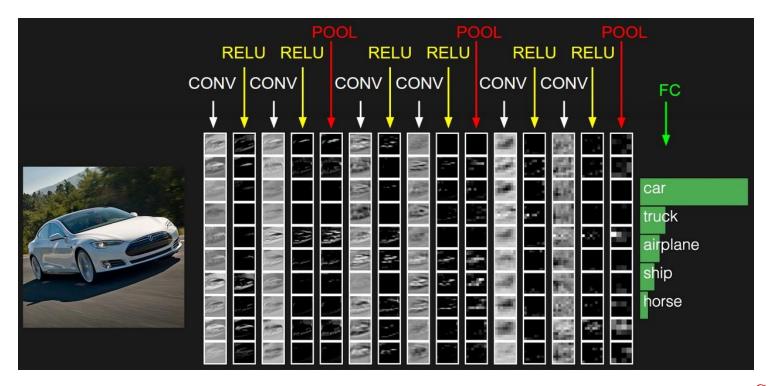


- This reduces representation size by a factor of two
 - Which reduces computational burden of next layer
 - Rightmost pooling region has a smaller size but must be included if we don't want to ignore some of the detector units

Downsampling makes a digital audio signal smaller by lowering its sampling rate or sample size (bits per sample). It decreases the bit rate when transmitting over a limited bandwidth or to convert to a more limited audio format

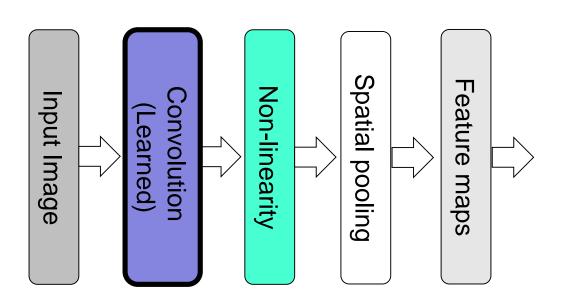


Feature Map (Convolution Layer)



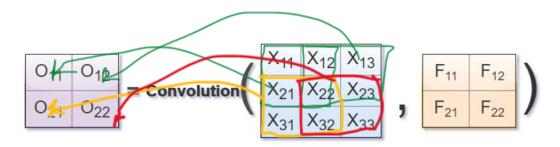


CNN Components





Backprop in Convolution



$$O_{11} = F_{11}X_{11} + F_{12}X_{12} + F_{21}X_{21} + F_{22}X_{22}$$

$$O_{12} = F_{11}X_{12} + F_{12}X_{13} + F_{21}X_{22} + F_{22}X_{23}$$

$$O_{21} = F_{11}X_{21} + F_{12}X_{22} + F_{21}X_{31} + F_{22}X_{32}$$

$$O_{22} = F_{11}X_{22} + F_{12}X_{23} + F_{21}X_{32} + F_{22}X_{33}$$



Backprop in Convolution

$$O_{11} = F_{11}X_{11} + F_{12}X_{12} + F_{21}X_{21} + F_{22}X_{22}$$
 $O_{12} = F_{11}X_{12} + F_{12}X_{13} + F_{21}X_{22} + F_{22}X_{23}$
 $O_{21} = F_{11}X_{21} + F_{12}X_{22} + F_{21}X_{31} + F_{22}X_{32}$
 $O_{22} = F_{11}X_{22} + F_{12}X_{23} + F_{21}X_{32} + F_{22}X_{33}$

$$\frac{\partial E}{\partial F_{12}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{12}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{12}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{12}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{12}}
\frac{\partial E}{\partial F_{21}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{21}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{21}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{21}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{21}}
\frac{\partial E}{\partial F_{22}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{22}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{22}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{22}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{22}}
\frac{\partial E}{\partial F_{22}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{22}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{22}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{22}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{22}}$$

 $\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{11}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{11}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{11}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{11}}$

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Backprop in Convolution

Which evaluates to-

$$O_{11} = F_{11}X_{11} + F_{12}X_{12} + F_{21}X_{21} + F_{22}X_{22}$$

$$O_{12} = F_{11}X_{12} + F_{12}X_{13} + F_{21}X_{22} + F_{22}X_{23}$$

$$O_{21} = F_{11}X_{21} + F_{12}X_{22} + F_{21}X_{31} + F_{22}X_{32}$$

$$O_{22} = F_{11}X_{22} + F_{12}X_{23} + F_{21}X_{32} + F_{22}X_{33}$$

$$\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}} X_{11} + \frac{\partial E}{\partial O_{12}} X_{12} + \frac{\partial E}{\partial O_{21}} X_{21} + \frac{\partial E}{\partial O_{22}} X_{22}$$

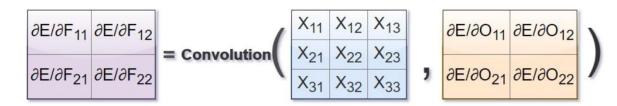
$$\frac{\partial E}{\partial F_{12}} = \frac{\partial E}{\partial O_{11}} X_{12} + \frac{\partial E}{\partial O_{12}} X_{13} + \frac{\partial E}{\partial O_{21}} X_{22} + \frac{\partial E}{\partial O_{22}} X_{23}$$

$$\frac{\partial E}{\partial F_{21}} = \frac{\partial E}{\partial O_{11}} X_{21} + \frac{\partial E}{\partial O_{12}} X_{22} + \frac{\partial E}{\partial O_{21}} X_{31} + \frac{\partial E}{\partial O_{22}} X_{32}$$

$$\frac{\partial E}{\partial F_{22}} = \frac{\partial E}{\partial O_{11}} X_{22} + \frac{\partial E}{\partial O_{12}} X_{23} + \frac{\partial E}{\partial O_{21}} X_{32} + \frac{\partial E}{\partial O_{22}} X_{33}$$

Backprop in Convolution

If we look closely the previous equation can be written in form of our convolution operation.



$$\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}} X_{11} + \frac{\partial E}{\partial O_{12}} X_{12} + \frac{\partial E}{\partial O_{21}} X_{21} + \frac{\partial E}{\partial O_{22}} X_{22}$$

$$\frac{\partial E}{\partial F_{12}} = \frac{\partial E}{\partial O_{11}} X_{12} + \frac{\partial E}{\partial O_{12}} X_{13} + \frac{\partial E}{\partial O_{21}} X_{22} + \frac{\partial E}{\partial O_{22}} X_{23}$$

$$\frac{\partial E}{\partial F_{21}} = \frac{\partial E}{\partial O_{11}} X_{21} + \frac{\partial E}{\partial O_{12}} X_{22} + \frac{\partial E}{\partial O_{21}} X_{31} + \frac{\partial E}{\partial O_{22}} X_{32}$$

$$\frac{\partial E}{\partial F_{22}} = \frac{\partial E}{\partial O_{11}} X_{22} + \frac{\partial E}{\partial O_{12}} X_{23} + \frac{\partial E}{\partial O_{21}} X_{32} + \frac{\partial E}{\partial O_{22}} X_{33}$$



Backprop in Convolution

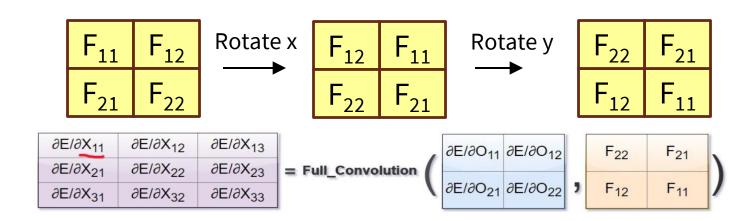
Similarly we can find the gradients of the error 'E' with respect to the input matrix 'X'.

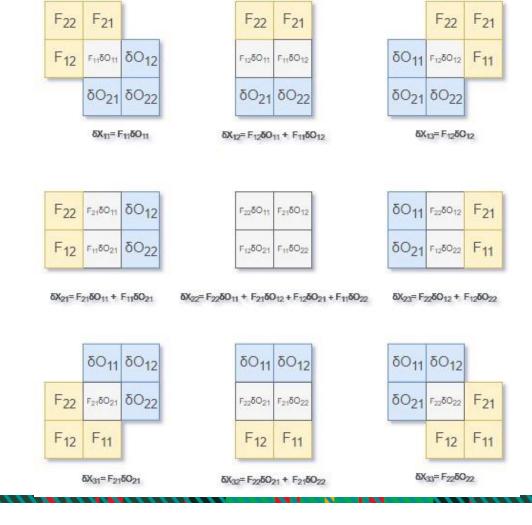
$$\begin{split} \frac{\partial E}{\partial X_{11}} &= \frac{\partial E}{\partial O_{11}} F_{11} + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{12}} &= \frac{\partial E}{\partial O_{11}} F_{12} + \frac{\partial E}{\partial O_{12}} F_{11} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{13}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} F_{12} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{21}} &= \frac{\partial E}{\partial O_{11}} F_{21} + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{11} + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{22}} &= \frac{\partial E}{\partial O_{11}} F_{22} + \frac{\partial E}{\partial O_{12}} F_{21} + \frac{\partial E}{\partial O_{21}} f_{12} + \frac{\partial E}{\partial O_{22}} F_{11} \\ \frac{\partial E}{\partial X_{23}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} F_{22} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} F_{11} \\ \frac{\partial E}{\partial X_{31}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{21} + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{32}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{22} + \frac{\partial E}{\partial O_{22}} F_{21} \\ \frac{\partial E}{\partial X_{33}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} F_{22} \end{split}$$



The previous computation can be obtained by a different type of convolution operation known as full convolution.

In order to obtain the gradients of the input matrix we need to rotate the filter by 180 degree and calculate the full convolution of the rotated filter by the gradients of the output with respect to error.







Backpropagation of max pooling

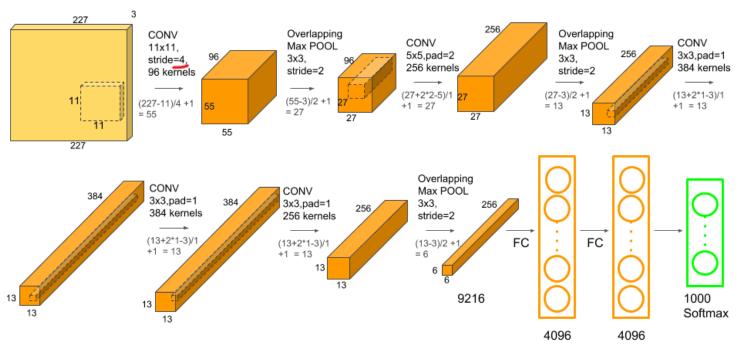
Suppose you have a matrix M of four elements:

a	b	
С	d	

and maxpool(M) returns d.

Then, the maxpool function really only depends on d. So, the derivative of maxpool relative to d is 1, and its derivative relative to a,b,c is zero. So you backpropagate 1 to the unit corresponding to d, and you backpropagate zero for the other units.



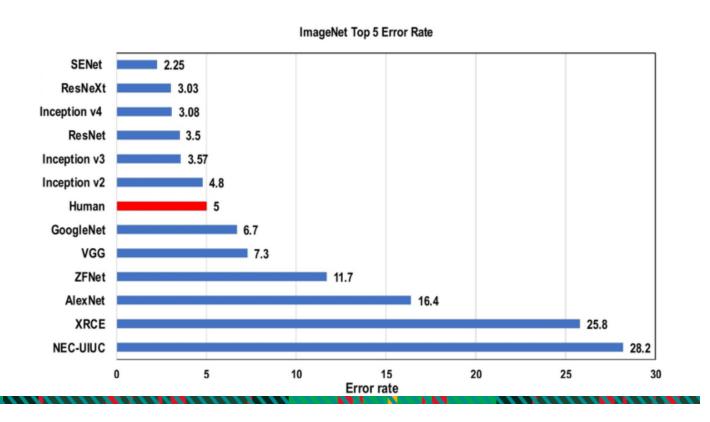




Carnegie Mellon University

Different CNN Architectures

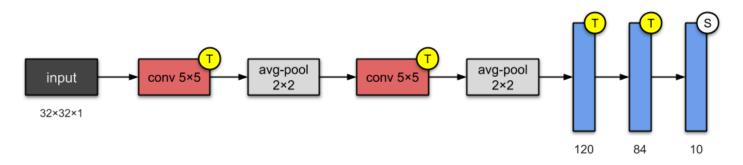
Notable CNN models¹⁹





Notable CNN models

LENET (1998)8



(2) ENDING THE NETWORK WITH ONE OR MORE FULLY-CONNECTED LAYERS



LeNet-5

Gradient Based Learning Applied To Document Recognition
- Y. Lecun, L. Bottou, Y. Bengio, P. Haffner; 1998
Helped establish how we use CNNs today
Replaced manual feature

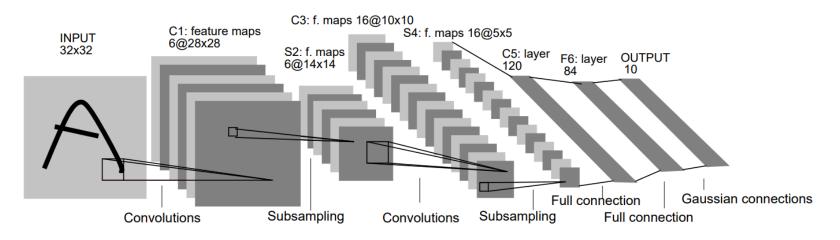


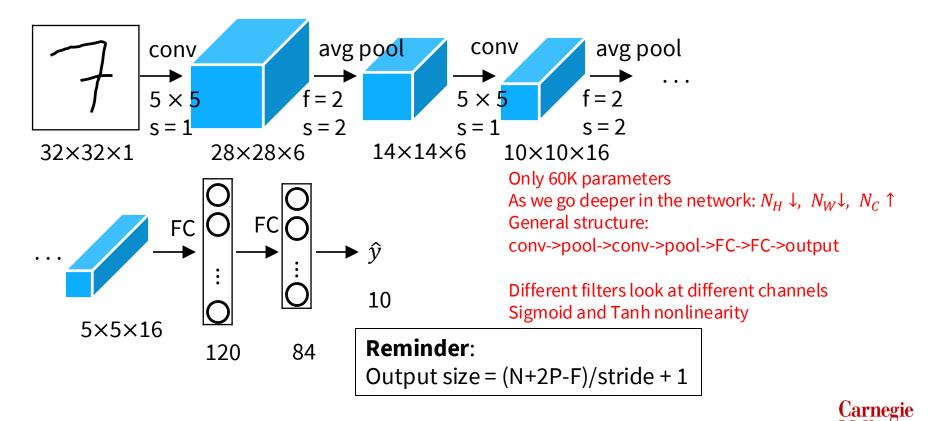
Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

United in the set of units whose weights are constrained to be identical.

Wellon

University

LeNet-5



Mellon University
[LeCun et al., 1998]

ImageNet Classification with Deep Convolutional Neural Networks

- Alex Krizhevsky, Ilya Sutskever, Geoffrey E. Hinton; 2012

Facilitated by GPUs, highly optimized convolution implementation and large datasets (ImageNet)

One of the largest CNNs to date

Has 60 Million parameter compared to 60k parameter of LeNet-5

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners

The annual "Olympics" of computer vision.

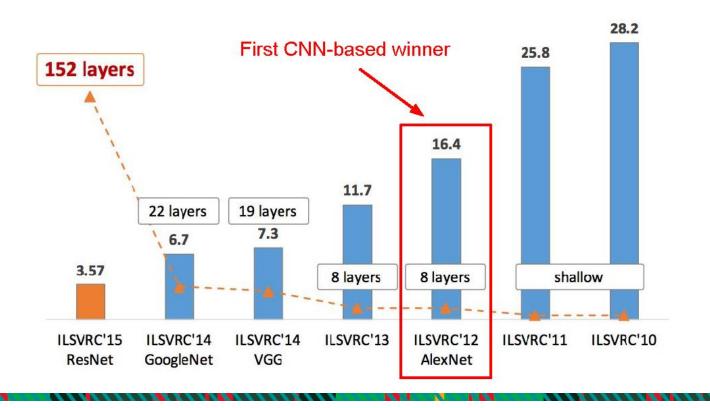
Teams from across the world compete to see who has the best computer vision model for tasks such as classification, localization, detection, and more.

2012 marked the first year where a CNN was used to achieve a top 5 test error rate of 15.3%.

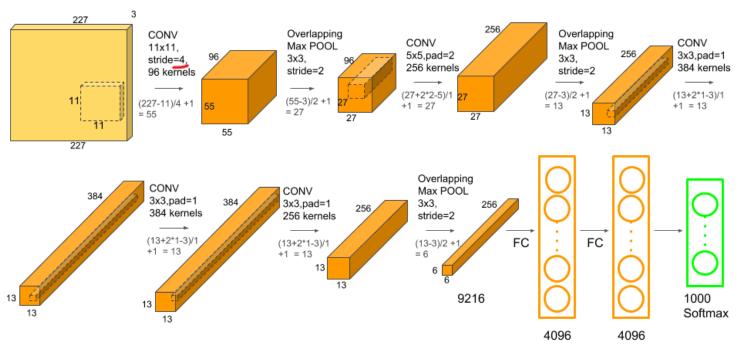
The next best entry achieved an error of 26.2%.



ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners









Architectur

eCONV1

MAX POOL1

NORM1

CONV2

MAX POOL2

NORM2

CONV3

CONV4

CONV5

Max POOL3

FC6

FC7

FC8

INPUT: 227X227X3 IMAGES (224X224

BEFORE PADDING)

FIRST LAYER: 96 11x11 FILTERS APPLIED AT

STRIDE 4

OUTPUT VOLUME SIZE?

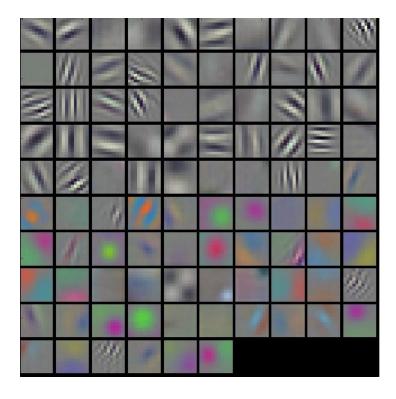
$$(N-F)/s+1 = (227-11)/4+1 = 55 ->$$

[55x55x96]

NUMBER OF PARAMETERS IN THIS LAYER?

$$(11*11*3)*96 = 35K$$

AlexNet filters



Carnegie Mellon University
[Krizhevsky et al., 2012]

Architecture

CONV1

MAX POOL1

NORM1

CONV2

MAX POOL2

NORM2

CONV3

CONV4

CONV5

Max POOL3

FC6

FC7

FC8

INPUT: 227X227X3 IMAGES (224X224 BEFORE PADDING)

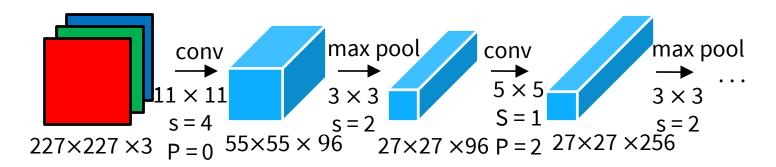
AFTER CONV1: 55x55x96

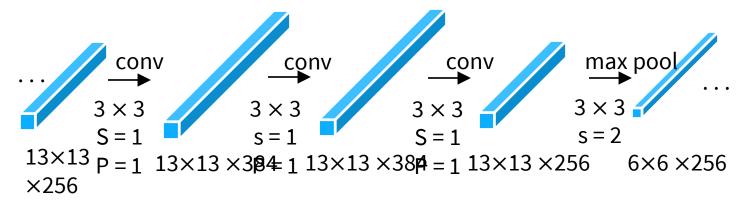
SECOND LAYER: 3x3 FILTERS APPLIED AT

STRIDE 2

OUTPUT VOLUME SIZE? (N-F)/s+1 = (55-3)/2+1 = 27 -> [27x27x96]

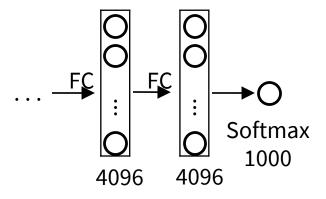
Number of parameters in this Layer?
0!





Carnegie Mellon University

[Krizhevsky et al., 2012]



DETAILS/RETROSPECTIVES:

FIRST USE OF RELU

USED NORM LAYERS (NOT COMMON ANYMORE)

HEAVY DATA AUGMENTATION

DROPOUT 0.5

BATCH SIZE 128

7 CNN ENSEMBLE



TRAINED ON GTX 580 GPU WITH ONLY 3 GB OF MEMORY.

NETWORK SPREAD ACROSS 2 GPUs, HALF THE NEURONS (FEATURE MAPS) ON EACH GPU.

CONV1, CONV2, CONV4, CONV5:

CONNECTIONS ONLY WITH FEATURE MAPS ON SAME GPU.

CONV3, FC6, FC7, FC8:

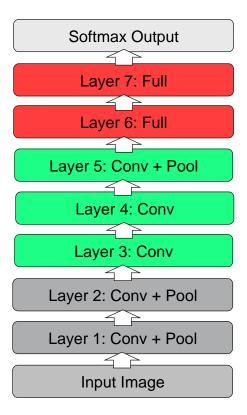
CONNECTIONS WITH ALL FEATURE MAPS IN PRECEDING LAYER, COMMUNICATION ACROSS GPUS.

AI EXNET WAS THE COMING OUT PARTY FOR CNNs in the computer vision community. THIS WAS THE FIRST TIME A MODEL PERFORMED SO WELL ON A HISTORICALLY DIFFICULT **IMAGENET DATASET.** THIS PAPER ILLUSTRATED THE BENEFITS OF CNNS AND BACKED THEM UP WITH RECORD BREAKING PERFORMANCE IN THE COMPETITION.

Model	Top-1	Top-5
Sparse coding [2]	47.1%	28.2%
SIFT + FVs [24]	45.7%	25.7%
CNN	37.5%	17.0 %



- " 8 layers total!
- " Trained on Imagenet dataset [Deng et al. CVPR'09]!
- " 18.2% top-5 error!

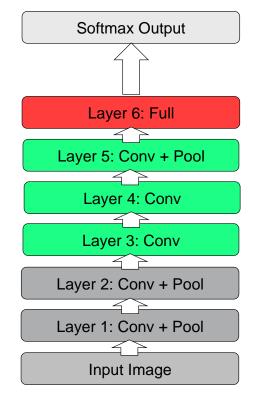


[From Rob Fergus' CIFAR 2016 tutorial] Krizhevsky et al., NIPS 2012



AlexNet

- "Remove top fully connected layer 7!
- " Drop ~16 million parameters!
- " Only 1.1% drop in performance!!



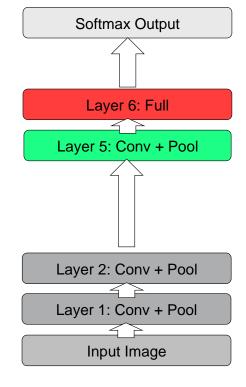
[From Rob Fergus' CIFAR 2016 tutorial] Krizhevsky et al., NIPS 2012



AlexNet

- " Remove layers 3 4,6 and 7!
- " Drop ~50 million parameters!
- " 33.5% drop in performance!!

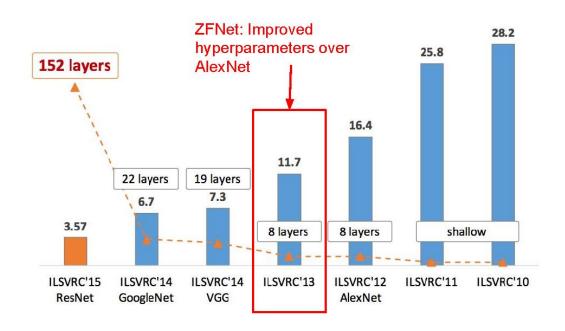
" Depth of the network is the key!



[From Rob Fergus' CIFAR 2016 tutorial] Krizhevsky et al., NIPS 2012

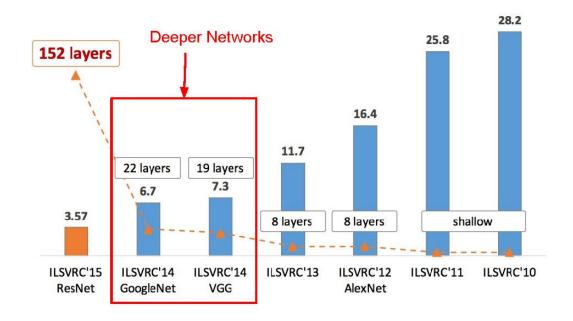


ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





VGGNet

VERY DEEP CONVOLUTIONAL NETWORKS FOR LARGE SCALE IMAGE RECOGNITION - KAREN SIMONYAN AND ANDREW ZISSERMAN; 2015

THE RUNNER-UP AT THE ILSVRC 2014 COMPETITION SIGNIFICANTLY DEEPER THAN ALEXNET

140 MILLION PARAMETERS

Input 3x3 conv, 64 3x3 conv, 64 Pool 1/2 3x3 conv, 128 3x3 conv, 128 Pool 1/2 3x3 conv, 256 3x3 conv, 256 Pool 1/2 3x3 conv, 512 3x3 conv, 512 3x3 conv, 512 Pool 1/2 3x3 conv, 512 3x3 conv, 512 3x3 conv, 512 Pool 1/2 FC 4096 FC 4096 FC 1000 Softmax

VGGNet

SMALLER FILTERS

ONLY 3X3 CONV FILTERS, STRIDE 1, PAD 1 AND 2X2 MAX POOL, STRIDE 2

DEEPER NETWORK

ALEXNET: 8 LAYERS

VGGNet: 16 - 19 Layers

ZFNet: 11.7% top 5 error in ILSVRC'13

VGGNET: 7.3% TOP 5 ERROR IN ILSVRC'14

VGGNet

WHY USE SMALLER FILTERS? (3x3 CONV)

STACK OF THREE 3x3 CONV (STRIDE 1) LAYERS HAS THE SAME EFFECTIVE RECEPTIVE FIELD AS ONE 7x7 CONV LAYER.

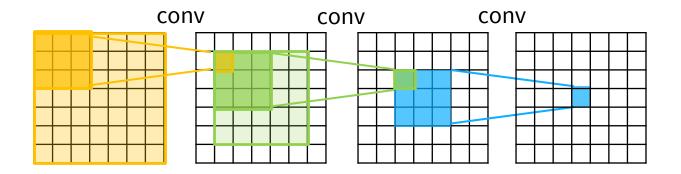
What is the effective receptive field of three 3x3 conv (stride 1) Layers?

7x**7**

But deeper, more non-linearities And fewer parameters: 3 * (3²C²) vs. 7²C² for C

CHANNELS PER LAYER

Reminder: Receptive Field





```
memory: 224*224*3=150K params: 0
Input
3x3 conv, 64 memory: 224*224*64=3.2M
                                              params: (3*3*3)*64 = 1,728
3x3 conv, 64 memory: 224*224*64=3.2M
                                              params: (3*3*64)*64 = 36,864
Pool
            memory: 112*112*64=800K
                                              params: 0
3x3 conv, 128memory: 112*112*128=1.6M
                                              params: (3*3*64)*128 = 73,728
                                              params: (3*3*128)*128 = 147,456
3x3 conv, 128memory: 112*112*128=1.6M
Pool
             memory: 56*56*128=400K params: 0
3x3 conv, 256memory: 56*56*256=800K params: (3*3*128)*256 = 294,912
3x3 conv, 256memory: 56*56*256=800K params: (3*3*256)*256 = 589,824
3x3 conv, 256memory: 56*56*256=800K params: (3*3*256)*256 = 589,824
             memory: 28*28*256=200K params: 0
Pool
3x3 \text{ conv}, 512 \text{ memory}: 28*28*512=400 \text{ K} params: (3*3*256)*512 = 1,179,648
3x3 conv. 512memory: 28*28*512=400K params: (3*3*512)*512 = 2,359,296
3x3 \text{ conv}, 512 \text{ memory}: 28*28*512=400 \text{ K} params: (3*3*512)*512 = 2,359,296
             memory: 14*14*512=100K params: 0
Pool
3x3 conv, 512memory: 14*14*512=100K params: (3*3*512)*512 = 2,359,296
3x3 \text{ conv}, 512 \text{ memory}: 14*14*512=100 \text{ K} params: (3*3*512)*512=2,359,296
3x3 \text{ conv}, 512 \text{ memory}: 14*14*512=100 \text{ K} params: (3*3*512)*512=2,359,296
Pool
            memory: 7*7*512=25K
                                        params: 0
FC 4096
                   memory: 4096
                                       params: 7*7*512*4096 = 102,760,448
                   memory: 4096
                                       params: 4096*4096 = 16,777,216
FC 4096
                   memory: 1000
FC 1000
                                       params: 4096*1000 = 4,096,000
```

VGGNet-

Input 3x3 conv, 64 3x3 conv, 64 Pool 3x3 conv, 128 3x3 conv, 128 Pool 3x3 conv, 256 3x3 conv, 256 3x3 conv, 256 Pool 3x3 conv, 512 3x3 conv, 512 3x3 conv, 512 Pool 3x3 conv, 512 3x3 conv, 512 3x3 conv, 512 Pool FC 4096 FC 4096 FC 1000 Softmax

VGG16:

TOTAL MEMORY: 24M * 4 BYTES ~= 96MB / IMAGE

TOTAL PARAMS: 138M PARAMETERS

```
memory: 224*224*3=150K params: 0
Input
3x3 conv, 64 memory: 224*224*64=3.2M
                                              params: (3*3*3)*64 = 1,728
3x3 conv, 64 memory: 224*224*64=3.2M
                                              params: (3*3*64)*64 = 36,864
Pool
            memory: 112*112*64=800K
                                              params: 0
3x3 conv, 128memory: 112*112*128=1.6M
                                             params: (3*3*64)*128 = 73,728
3x3 conv, 128memory: 112*112*128=1.6M
                                             params: (3*3*128)*128 = 147,456
Pool
            memory: 56*56*128=400K params: 0
3x3 conv, 256memory: 56*56*256=800K params: (3*3*128)*256 = 294,912
3x3 conv, 256memory: 56*56*256=800K params: (3*3*256)*256 = 589,824
3x3 conv, 256memory: 56*56*256=800K params: (3*3*256)*256 = 589,824
            memory: 28*28*256=200K params: 0
Pool
3x3 \text{ conv}, 512 \text{ memory}: 28*28*512=400 \text{ K} params: (3*3*256)*512 = 1,179,648
3x3 conv. 512memory: 28*28*512=400K params: (3*3*512)*512 = 2,359,296
3x3 \text{ conv}, 512 \text{ memory}: 28*28*512=400 \text{ K} params: (3*3*512)*512 = 2,359,296
            memory: 14*14*512=100K params: 0
Pool
3x3 conv, 512memory: 14*14*512=100K params: (3*3*512)*512 = 2,359,296
3x3 \text{ conv}, 512 \text{ memory}: 14*14*512=100 \text{ K} params: (3*3*512)*512=2,359,296
3x3 conv, 512memory: 14*14*512=100K params: (3*3*512)*512 = 2,359,296
Pool
            memory: 7*7*512=25K
                                       narams: 0
FC 4096
                   memory: 4096
                                      params: 7*7*512*4096 = 102.760.448
                   memory: 4096
FC 4096
                                       params: 4096*4096 = 16,777,216
FC 1000
                   memory: 1000
                                      params: 4096*1000 = 4,096,000
```

VGGNet

DETAILS/RETROSPECTIVES:

ILSVRC'14 2ND IN CLASSIFICATION, 1ST IN LOCALIZATION

SIMILAR TRAINING PROCEDURE AS ALEXNET

NO LOCAL RESPONSE NORMALISATION (LRN)

USE VGG16 OR VGG19 (VGG19 ONLY SLIGHTLY BETTER, MORE MEMORY)

USE ENSEMBLES FOR BEST RESULTS

FC7 FEATURES GENERALIZE WELL TO OTHER TASKS

TRAINED ON 4 NVIDIA TITAN BLACK GPUS FOR TWO TO THREE WEEKS.



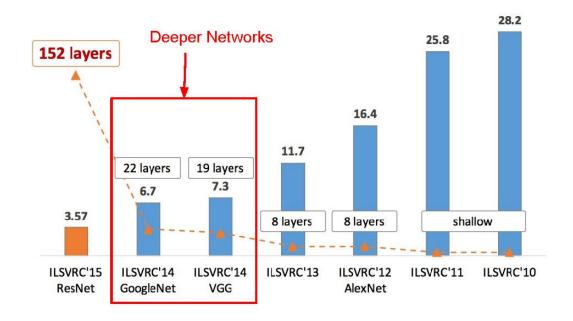


VGG NET REINFORCED THE NOTION
THAT CONVOLUTIONAL NEURAL NETWORKS HAVE TO HAVE
A DEEP NETWORK OF LAYERS IN ORDER FOR THIS
HIERARCHICAL REPRESENTATION OF VISUAL DATA TO
WORK.

KEEP IT DEEP.

KEEP IT SIMPLE.

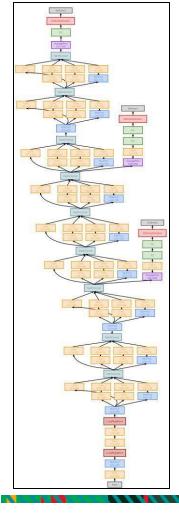
ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





Going Deeper with Convolutions - Christian Szegedy et al.; 2015 ILSVRC 2014 competition winner Also significantly deeper than AlexNet x12 less parameters than AlexNet

FOCUSED ON COMPUTATIONAL EFFICIENCY



22 LAYERS

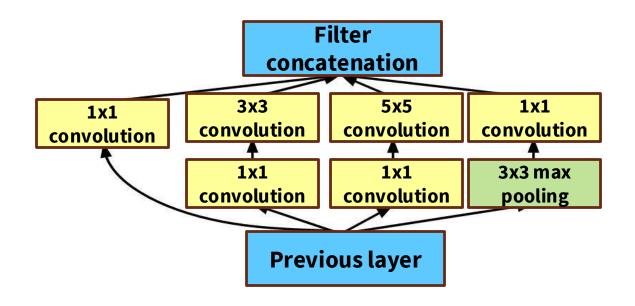
EFFICIENT "INCEPTION" MODULE - STRAYED FROM
THE GENERAL APPROACH OF SIMPLY STACKING
CONV AND POOLING LAYERS ON TOP OF EACH
OTHER IN A SEQUENTIAL STRUCTURE

No FC LAYERS

ONLY 5 MILLION PARAMETERS!

ILSVRC'14 CLASSIFICATION WINNER (6.7% TOP 5 ERROR)

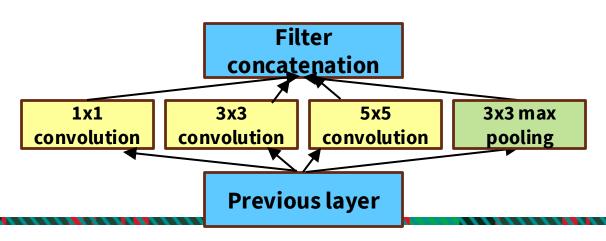
"INCEPTION MODULE": DESIGN A GOOD LOCAL NETWORK TOPOLOGY (NETWORK WITHIN A NETWORK) AND THEN STACK THESE MODULES ON TOP OF EACH OTHER



Carnegie Mellon University

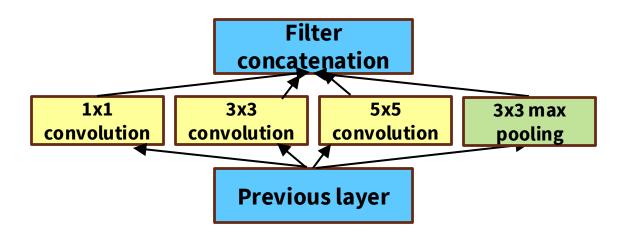
Naïve Inception Model

- Apply parallel filter operations on the input :
 - Multiple receptive field sizes for convolution (1x1, 3x3, 5x5)
 - > Pooling operation (3x3)
- Concatenate all filter outputs together depth-wise



Carnegie Mellon University

What's the problem with this?
 High computational complexity



Carnegie Mellon University

OUTPUT VOLUME SIZES:

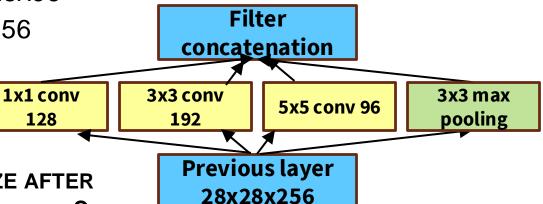
1x1 CONV, 128: 28x28x128

3x3 CONV, 192: 28x28x192

5x5 CONV, 96: 28x28x96

3x3 POOL: 28x28x256

Example:



WHAT IS OUTPUT SIZE AFTER FILTER CONCATENATION?

 $28 \times 28 \times (128 + 192 + 96 + 256) = 28 \times 28 \times 672$

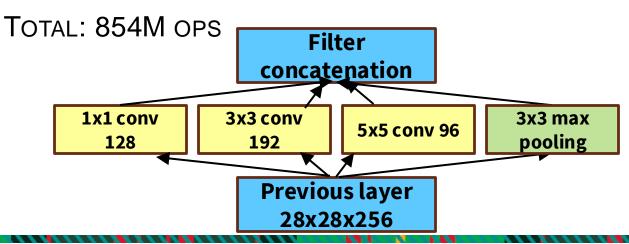
Carnegie Mellon University

NUMBER OF CONVOLUTION OPERATIONS:

1x1 CONV, 128: 28x28x128x1x1x256

3x3 CONV, 192: 28x28x192x3x3x256

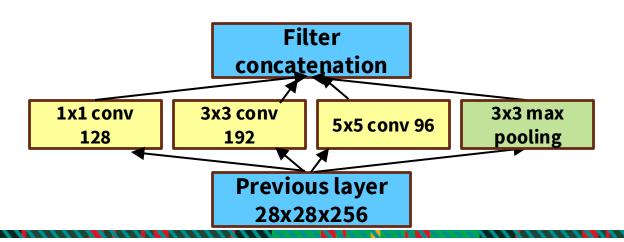
5x5 conv, 96: 28x28x96x5x5x256



Carnegie Mellon University

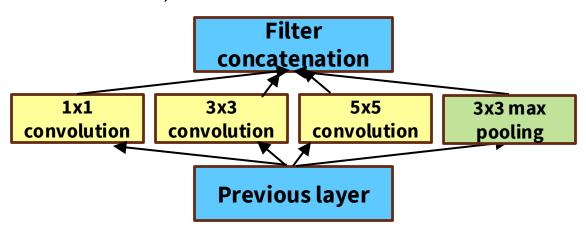
VERY EXPENSIVE COMPUTE!

POOLING LAYER ALSO PRESERVES FEATURE
DEPTH, WHICH MEANS TOTAL DEPTH AFTER
CONCATENATION CAN ONLY GROW AT EVERY LAYER.



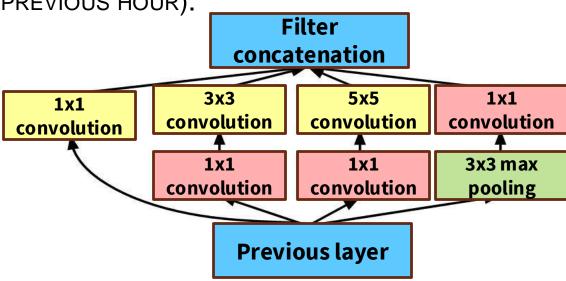
Carnegie Mellon University

SOLUTION: "BOTTLENECK" LAYERS THAT USE 1x1 CONVOLUTIONS TO REDUCE FEATURE DEPTH (FROM PREVIOUS HOUR).



Carnegie Mellon University

SOLUTION: "BOTTLENECK" LAYERS THAT USE 1X1 CONVOLUTIONS TO REDUCE FEATURE DEPTH (FROM PREVIOUS HOUR).



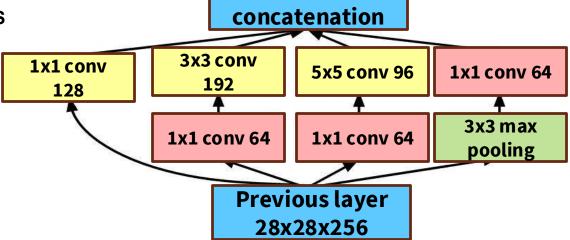
NUMBER OF CONVOLUTION OPERATIONS:

1x1 CONV, 64: 28x28x64x1x1x256 1x1 CONV, 64: 28x28x64x1x1x256

1x1 CONV, 128: 28x28x128x1x1x256 3x3 CONV, 192: 28x28x192x3x3x64 5x5 CONV, 96: 28x28x96x5x5x264

1x1 CONV, 64: 28x28x64x1x1x256

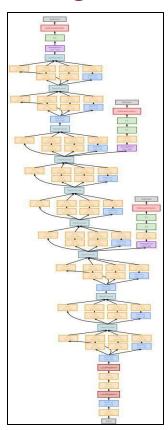
TOTAL: 353M OPS



Filter

COMPARED TO 854M OPS FOR NAIVE VERSION

Carnegie Mellon University



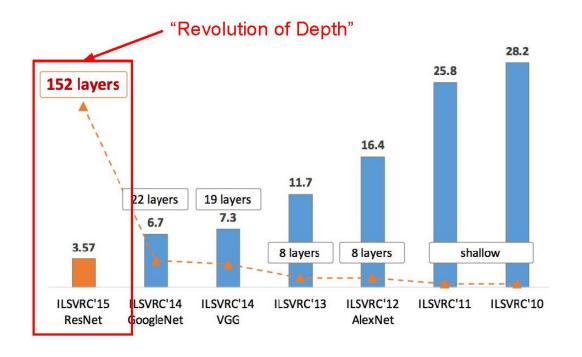
Details/Retrospectives:

- Deeper networks, with computational efficiency
- 22 layers
- Efficient "Inception" module
- No FC layers
- 12x less params than AlexNet
- ILSVRC'14 classification winner (6.7% top 5 error)



INTRODUCED THE IDEA THAT CNN LAYERS DIDN'T ALWAYS HAVE TO BE STACKED UP SEQUENTIALLY. COMING UP WITH THE INCEPTION MODULE, THE AUTHORS SHOWED THAT A CREATIVE STRUCTURING OF LAYERS CAN LEAD TO IMPROVED PERFORMANCE AND COMPUTATIONALLY EFFICIENCY.

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners





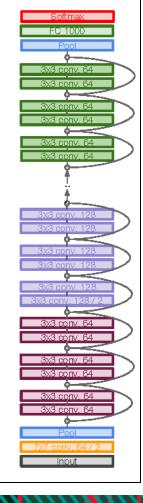
DEEP RESIDUAL LEARNING FOR IMAGE RECOGNITION
- KAIMING HE, XIANGYU ZHANG, SHAOQING REN,
JIAN SUN; 2015

EXTREMELY DEEP NETWORK – 152 LAYERS

DEEPER NEURAL NETWORKS ARE MORE DIFFICULT TO TRAIN.

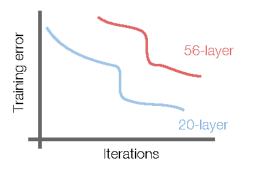
DEEP NETWORKS SUFFER FROM VANISHING AND EXPLODING GRADIENTS.

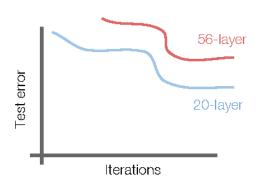
PRESENT A RESIDUAL LEARNING FRAMEWORK TO EASE THE TRAINING OF NETWORKS THAT ARE SUBSTANTIALLY DEEPER THAN THOSE USED PREVIOUSLY.



ILSVRC'15 classification winner (3.57% top 5 error, humans generally hover around a 5-10% error rate)
 Swept all classification and detection competitions in ILSVRC'15 and COCO'15!

 What happens when we continue stacking deeper layers on a convolutional neural network?





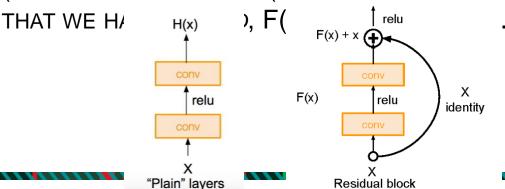
- 56-layer model performs worse on both training and test error
- -> The deeper model performs worse (not caused by overfitting)!

- **Hypothesis**: The problem is an optimization problem. Very deep networks are harder to optimize.
- Solution: Use network layers to fit residual mapping instead of directly trying to fit a desired underlying mapping.
- We will use skip connections allowing us to take the activation from one layer and feed it into another layer, much deeper into the network.
- Use layers to fit residual F(x) = H(x) x instead of H(x) directly



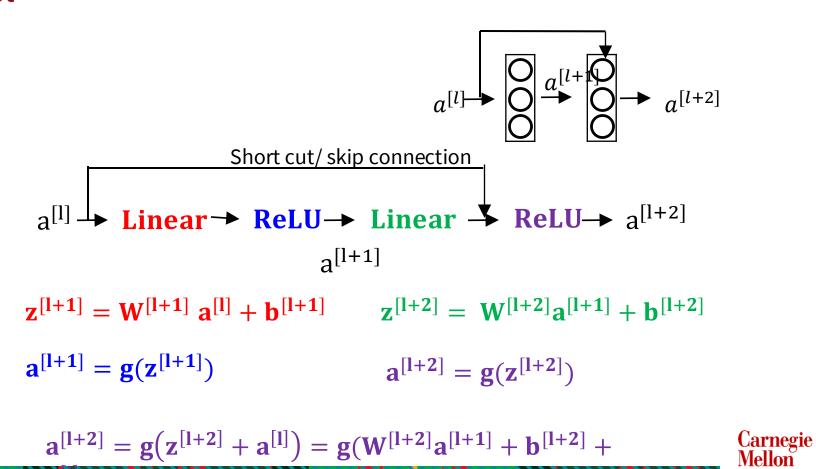
RESIDUAL BLOCK

Input x goes through conv-relu-conv series and gives us F(x). That result is then added to the original input x. Let's call that H(x) = F(x) + x. In traditional CNNs, H(x) would just be equal to F(x). So, instead of just computing that transformation (straight from x to F(x)). We're computing the term



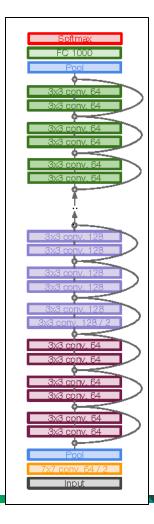
Carnegie Mellon University

[He et al., 2015]



[He et al., 2015]

University



FULL RESNET ARCHITECTURE:

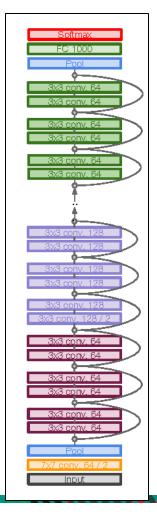
STACK RESIDUAL BLOCKS

EVERY RESIDUAL BLOCK HAS TWO 3x3 CONV LAYERS

PERIODICALLY, DOUBLE # OF FILTERS AND DOWNSAMPLE SPATIALLY USING STRIDE 2 (IN EACH DIMENSION)

ADDITIONAL CONV LAYER AT THE BEGINNING

NO FC LAYERS AT THE END (ONLY FC 1000 TO OUTPUT CLASSES)



TOTAL DEPTHS OF 34, 50, 101, OR 152 LAYERS FOR IMAGENET

FOR DEEPER NETWORKS (RESNET-50+), USE "BOTTLENECK" LAYER TO IMPROVE EFFICIENCY (SIMILAR TO GOOGLENET)

EXPERIMENTAL RESULTS:

ABLE TO TRAIN VERY DEEP NETWORKS WITHOUT DEGRADING
DEEPER NETWORKS NOW ACHIEVE LOWER TRAINING ERRORS
AS EXPECTED

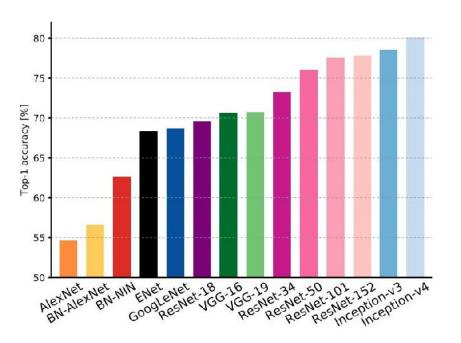
THE **BEST CNN** ARCHITECTURE THAT WE CURRENTLY HAVE AND IS A GREAT INNOVATION FOR THE IDEA OF RESIDUAL LEARNING.

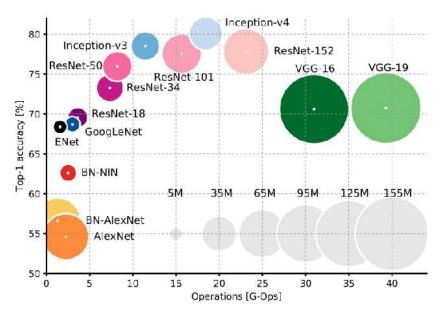
EVEN BETTER THAN HUMAN PERFORMANCE!



[He et al., 2015]

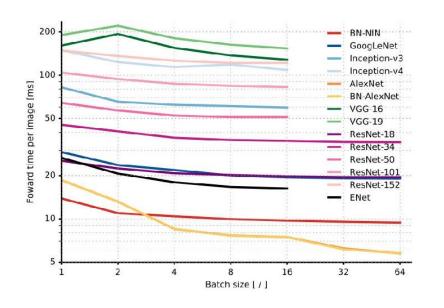
Accuracy comparison

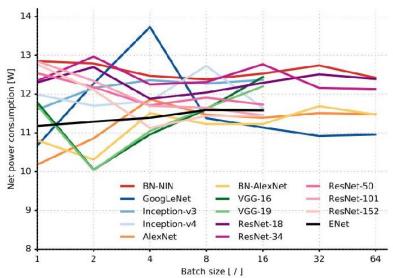






Forward pass time and power consumption







Summary

LENET-5

ALEXNET

VGG

GOOGLENET – INCEPTION MODULE

RESNET – RESIDUAL BLOCK



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