



Parallel Code Optimization:

·Algorithm

-Need to have efficient algorithms (Also optimize the serial performance)

Communication

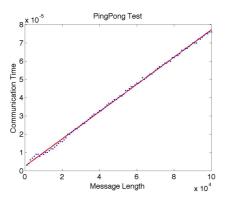
-Need to minimize communication time

Load balance

-Need to have equal work load



Communication overhead



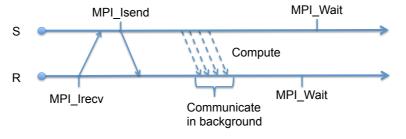
 T_{Comm} (n)=t_s+n t_w, t_s=2.5 μs, β=10.7 GB/s, (t_w=1/β) \Rightarrow T_{Comm}(1)=2500 ns + 0.7ns, latency>>transfer time Compare: 37GFlop/s => 92500 operations/latency

⇒ Need to minimize and/or hide the latency (and keep the total communication volume down) !



Communication optimization:

1. Non-blocking/buffered communicationOverlap computations and communication



⇒ Avoid synchronization and hide latency (and data transfer time).



2. Derived datatypes

Send non-contiguous data in one call

- MPI Type vector(...) -- Regular distribution
- MPI_Type_indexed(...) -- Irregular distribution
- MPI_Type_struct(...) -- Different datatypes
- => Reduce number of communication calls (latency)

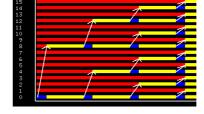
```
MPI_Type_vector(4,3,5,MPI_DOUBLE,&strided);
MPI_Type_commit(&strided);
MPI_Send(A,1,strided,to,tag,comm);
```



3. Collective communication calls

Uses efficient algorithms to communicate with many processors in one call:

- MPI_Bcast(...)
- MPI_Scatter(...)
- MPI_Gather(...)
- MPI_Allgather(...)
- MPI Alltoall(...)
- MPI_Reduce(...)



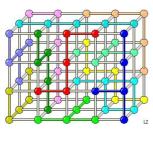
⇒ Parallelize the communication (reduce latency)

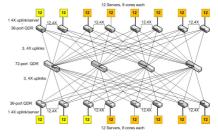


4. Virtual topologies

Communicator with structure. Makes a mapping to physical topology optimizing (localizing) the communication. Helps in algorithm construction reflecting the communication pattern.

- MPI Cart create(...)
- MPI_Graph_create(...)





Virtual topology

Physical topology



5. Persistent communication

Initiate communication once and activate repeatedly ⇒ Reduces initialization overhead (latency), useful when we have many calls and complicated patterns.

```
MPI_Send_init(...);
MPI_Recv_init(...):
etc (many calls)

for (i=0; i<n; i++)
{
    MPI_Startall(...);
    Compute
    MPI_Waitall(...)
    Use data
}</pre>
```



6. Message probing

Reduce synchronization OH by not ordering messages, use first-come first-serve.
Avoid sending length in a separate call.

```
while (i<nproc)
{
    MPI_Probe(MPI_ANY_SOURCE,..., &stat);
    MPI_Get_count(&stat,type,&len);
    MPI_Recv(data,len,type,stat.MPI_SOURCE,...);
    i++;
}</pre>
```



Example: Numerical PDE Solver

Consider the Hyperbolic PDE:

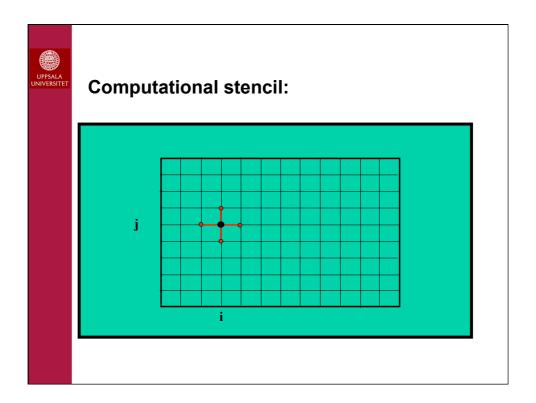
$$u_t + u_x + u_y = F(t, x, y) \quad 0 \le x \le 1, 0 \le y \le 1$$

$$\begin{cases} u(t, 0, y) = h_1(t, y) & 0 \le y \le 1 \\ u(t, x, 0) = h_2(t, x) & 0 \le x \le 1 \end{cases}$$
Boundary Conditions
$$u(0, x, y) = g(x, y) \quad Initial \ Conditions$$

Solve with explicit finite difference method, for example Leap-Frog

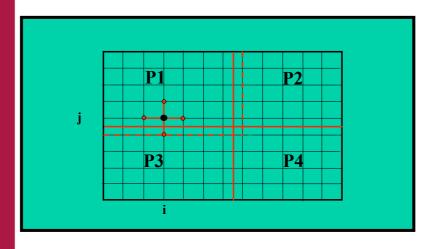


Core of the computations:





Parallelization, partition grid:





Message Passing Version:



```
! Send and receive left-right
if ('not at left boundary')
   call mpi_send(left, ...)
end if

if ('not at right boundary')
   call mpi_recv(right, ...)
   call mpi_send(right, ...)
end if

if ('not at left boundary')
   call mpi_recv(left, ...)
end if

! Send and receive up-down
...
```



Note:

- Structured domain decomposition
 Use cartesian processor topology (simplifies communication)
- The communication is repeated
 Use persistent communication objects
 (mpi_send_init, mpi_startall, mpi_waitall)
- Inner domain independent of neighbors
 Overlap communication with computations (asynchronous communication)



```
! Create virtual topology
mpi_cart_create( ... )
mpi_cart_shift(dim1,left,right, ... )
...
! Initiate communication
mpi_send_init(left, ... )
mpi_recv_init(left, ... )
mpi_send_init(right, ... )
...
! Timestepping
do k=2,Nt
    mpi_startall( ... )
    update inner points
    mpi_waitall( ... )
    update partition boundary
end do
```



PDE Solver (lab MPI):

Program files:

- wave.c
 -- Main program
- <u>initcomm.c</u> -- Persistent communication
- <u>diffop.c</u> -- Computational core

(+ some additional files)

Task: Study implementation details and measure the parallel performance for different problem sizes. Compare performance running within one server and using several servers (out of node communication).



Real example: Combustion simulation

HPC User: Michael Liberman, Physics dept UU

Problem:

Navier-Stokes 2D, chemical reaction terms
Modeling of deflagration-to-detonation transition
(i.e. knocking which must be avoided in engines)
=> Efficient burning and good fuel economy

Needs:

Requires a very accurate numerical resolution of the flame front => Efficiently parallelized code for a large number of processors



Results:

Orginal code parallelized with MPI, standard MPI_Send/MPI_Recv, and 1D partitioning

- Changed standard calls to non-blocking persistent communication objects
- Extended to 2D partitioning, virtual topology
- Extended to multi-block partitioning, (allows for AMR and two-level parallelization)
- Efficient load balancing for multi-block grids
- => Very high parallel efficiency (Super linear on SunFire 15K)

