$$Li_{2}(z,N) = -dz \sum_{n=0}^{N-1} \frac{\log(1-z')}{z'} \Big|_{z'=(n+\frac{1}{2})dz}$$

$$dz = \frac{z}{N}$$