

$$Li_2(z, N) = -dz \sum_{n=0}^{N-1} \frac{\log(1-z')}{z'} \bigg|_{z'=(n+\frac{1}{2})dz}$$