$$\mathrm{Li}_2(z) \approx -dz \sum_{n=0}^{N-1} \frac{\log(1-z')}{z'}\bigg|_{z'=(n+\frac{1}{2})dz}$$

$$dz = \frac{z}{N}$$

z