Recent Advances in Dependency Parsing

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Overview of the Tutorial

- ► Introduction to Dependency Parsing (Joakim)
- ► Graph-based parsing post-2008 (Ryan)
- ► Transition-based parsing post-2008 (Joakim)
- Summary and final thoughts (Ryan)

Transition-Based Dependency Parsing

```
Configuration:
                  (S, B, A)
                   ([], [0, 1, \ldots, n], \{])
Initial:
Terminal:
                   (S, [], A)
Shift:
                   (S, i|B, A)
                                \Rightarrow (S|i, B, A)
Reduce:
                   (S|i, B, A) \Rightarrow (S, B, A)
                                                                              adi
                   (S|i,j|B,A) \Rightarrow (S|i|j,B,A \cup \{(i,j,k)\})
                                                                                             verb
                                                                                                    adi
                                                                                                           noun
                                                                                                                           adi
                                                                                                                                     noun
Right-Arc(k):
Left-Arc(k):
                   (S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\})
```

Overview

- ► Improved learning and inference
 - Beam search and structured prediction
 - Dynamic programming
 - Easy-first parsing
 - Dynamic oracles
- Non-projective parsing
 - ▶ Online reordering
 - Multiplanar parsing
- Joint morphological and syntactic analysis

The Basic Idea

- ▶ Define a transition system for dependency parsing
- ▶ Learn a model for scoring possible transitions
- ▶ Parse by searching for the optimal transition sequence

Arc-Eager Transition System [Nivre 2003]

Configuration: (S, B, A) [S = Stack, B = Buffer, A = Arcs]

Initial: $([], [0, 1, ..., n], \{])$

Terminal: (S, [], A)

Shift: $(S, i|B, A) \Rightarrow (S|i, B, A)$

Reduce: $(S|i,B,A) \Rightarrow (S,B,A)$ h(i,A)

Right-Arc(k**):** $(S|i,j|B,A) \Rightarrow (S|i|j,B,A \cup \{(i,j,k)\})$

Left-Arc(k): $(S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\}) \neg h(i,A) \land i \neq 0$

Notation: S|i = stack with top i and remainder S j|B = buffer with head j and remainder Bh(i,A) = i has a head in A

```
[ROOT]<sub>S</sub> [Economic, news, had, little, effect, on, financial, markets, .]<sub>B</sub>
```

```
ROOT Economic news had little effect on financial markets .

adj noun verb adj noun prep adj noun .
```

```
[ROOT, Economic] [news, had, little, effect, on, financial, markets, .] [B
```

```
ROOT Economic news had little effect on financial markets adj noun verb adj noun prep adj noun
```

```
[ROOT]<sub>S</sub> [news, had, little, effect, on, financial, markets, .]<sub>B</sub>
```

```
ROOT Economic news had little effect on financial markets . adj noun verb adj noun prep adj noun .
```

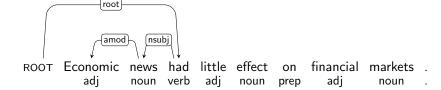
```
ROOT, news s [had, little, effect, on, financial, markets, .] B
```

```
ROOT Economic news had little effect on financial markets . adj noun verb adj noun prep adj noun .
```

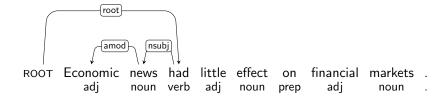
[ROOT]_S [had, little, effect, on, financial, markets, .]_B

```
ROOT Economic news had little effect on financial markets adj noun verb adj noun prep adj noun
```

[ROOT, had]_S [little, effect, on, financial, markets, .]_B



[ROOT, had, little]_S [effect, on, financial, markets, .]_B



noun

adj

Example Transition Sequence

[ROOT, had]s [effect, on, financial, markets, .]B

root

amod

ROOT Economic news had little effect on financial markets .

adj

noun

prep

verb

noun

adj

noun

Example Transition Sequence

noun

[ROOT, had, effect]_S [on, financial, markets, .]_B root dobj nsubj amod Economic little effect financial markets news had on adj verb adj adj

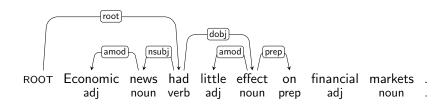
noun

prep

[ROOT, had, effect, on]_S [financial, markets, .]_B

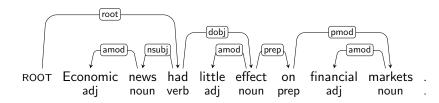
```
root
                            dobj
                nsubj
                             amod
                                      prep
Economic
                          little
                                 effect
                                              financial
                                                         markets
            news
                    had
                                         on
    adj
                    verb
                           adj
                                                 adj
             noun
                                 noun
                                         prep
                                                           noun
```

[ROOT, had, effect, on, financial]_S [markets, $.]_B$

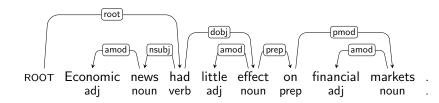


ROOT, had, effect, on S [markets, .] Broot dobj nsubj amod prep amod Economic little effect financial markets news had on adj verb adj adj noun noun prep noun

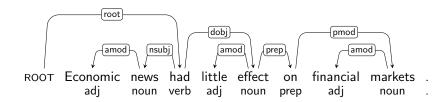
ROOT, had, effect, on, markets S $[.]_B$



[ROOT, had, effect, on]_S $[.]_B$



[ROOT, had, effect]_S [.]_B



[ROOT, had]_S $[.]_B$ root dobj pmod nsubj amod amod prep amod ROOT Economic little effect financial news had on markets adj verb adj adj noun noun prep noun

[ROOT, had, $.]_S$ []_B root dobj pmod nsubj amod amod prep amod little effect ROOT Economic financial news had on markets adj verb adj adj noun noun prep noun

Arc-Standard Transition System [Nivre 2004]

```
Configuration: (S, B, A) [S = Stack, B = Buffer, A = Arcs]
```

Initial: $([], [0, 1, ..., n], \{])$

Terminal: ([0], [], A)

Shift: $(S, i|B, A) \Rightarrow (S|i, B, A)$

Right-Arc(k**):** $(S|i|j,B,A) \Rightarrow (S|i,B,A \cup \{(i,j,k)\})$

Left-Arc(k**):** $(S|i|j,B,A) \Rightarrow (S|j,B,A \cup \{(j,i,k)\}) \quad i \neq 0$

Greedy Inference

▶ Given an oracle o that correctly predicts the next transition o(c), parsing is deterministic:

```
Parse(w_1, ..., w_n)

1 c \leftarrow ([]_S, [0, 1, ..., n]_B, \{ \})

2 while B_c \neq []

3 t \leftarrow o(c)

4 c \leftarrow t(c)

5 return G = (\{0, 1, ..., n\}, A_c)
```

- Complexity given by upper bound on number of transitions
- ightharpoonup Parsing in O(n) time for the arc-eager transition system

From Oracles to Classifiers

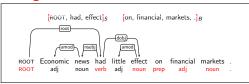
► An oracle can be approximated by a (linear) classifier:

$$o(c) = \operatorname*{argmax}_{t} \mathbf{w} \cdot \mathbf{f}(c, t)$$

- ▶ History-based feature representation $\mathbf{f}(c,t)$
- ► Weight vector w learned from treebank data

► Features over input tokens relative to S and B

Configuration



Features

```
pos(S_2) = ROOT

pos(S_1) = verb

pos(S_0) = noun

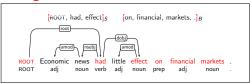
pos(B_0) = prep

pos(B_1) = adj

pos(B_2) = noun
```

► Features over input tokens relative to S and B

Configuration



Features

```
\operatorname{word}(S_2) = \operatorname{ROOT}

\operatorname{word}(S_1) = \operatorname{had}

\operatorname{word}(S_0) = \operatorname{effect}

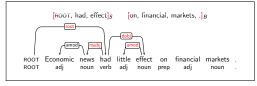
\operatorname{word}(B_0) = \operatorname{on}

\operatorname{word}(B_1) = \operatorname{financial}

\operatorname{word}(B_2) = \operatorname{markets}
```

- ► Features over input tokens relative to S and B
- ► Features over the (partial) dependency graph defined by A

Configuration

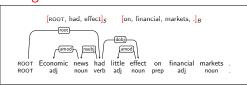


Features

```
\begin{array}{lll} \mathsf{dep}(S_1) & = & \mathsf{root} \\ \mathsf{dep}(\mathsf{lc}(S_1)) & = & \mathsf{nsubj} \\ \mathsf{dep}(\mathsf{rc}(S_1)) & = & \mathsf{dobj} \\ \mathsf{dep}(S_0) & = & \mathsf{dobj} \\ \mathsf{dep}(\mathsf{lc}(S_0)) & = & \mathsf{amod} \\ \mathsf{dep}(\mathsf{rc}(S_0)) & = & \mathsf{NIL} \end{array}
```

- ▶ Features over input tokens relative to *S* and *B*
- ► Features over the (partial) dependency graph defined by A
- ► Features over the (partial) transition sequence

Configuration



Features

 $t_{i-1} = \text{Right-Arc(dobj)}$ $t_{i-2} = \text{Left-Arc(amod)}$

 $t_{i-3} = Shift$

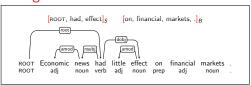
 $t_{i-4} = \text{Right-Arc(root)}$

 $t_{i-5} = \text{Left-Arc(nsubj)}$

 $t_{i-6} = Shift$

- ► Features over input tokens relative to S and B
- ► Features over the (partial) dependency graph defined by A
- ► Features over the (partial) transition sequence

Configuration



Features

 $t_{i-2} = \text{Left-Arc(amod)}$ $t_{i-3} = \text{Shift}$ $t_{i-4} = \text{Right-Arc(root)}$ $t_{i-5} = \text{Left-Arc(nsubj)}$ $t_{i-6} = \text{Shift}$

 $t_{i-1} = Right-Arc(dobj)$

► Feature representation unconstrained by parsing algorithm

Local Learning

- ► Given a treebank:
 - ▶ Reconstruct oracle transition sequence for each sentence
 - ▶ Construct training data set $D = \{(c, t) | o(c) = t\}$
 - ▶ Maximize accuracy of local predictions o(c) = t
- Any (unstructured) classifier will do (SVMs are popular)
- ► Training is local and restricted to oracle configurations

Greedy, Local, Transition-Based Parsing

- Advantages:
 - Highly efficient parsing linear time complexity with constant time oracles and transitions
 - Rich history-based feature representations no rigid constraints from inference algorithm
- Drawback:
 - Sensitive to search errors and error propagation due to greedy inference and local learning
- ► The major question in transition-based parsing has been how to improve learning and inference, while maintaining high efficiency and rich feature models

Beam Search

▶ Maintain the *k* best hypotheses [Johansson and Nugues 2006]:

```
Parse(w_1, ..., w_n)

1 Beam \leftarrow \{([]_S, [0, 1, ..., n]_B, \{ \})\}

2 while \exists c \in \text{Beam} [B_c \neq []]

3 foreach c \in \text{Beam}

4 foreach t

5 Add(t(c), \text{NewBeam})

6 Beam \leftarrow \text{Top}(k, \text{NewBeam})

7 return G = (\{0, 1, ..., n\}, A_{\text{Top}(1, \text{Beam})})
```

Note:

- $\blacktriangleright \mathsf{Score}(c_0,\ldots,c_m) = \sum_{i=1}^m \mathbf{w} \cdot \mathbf{f}(c_{i-1},t_i)$
- ► Simple combination of locally normalized classifier scores
- Marginal gains in accuracy

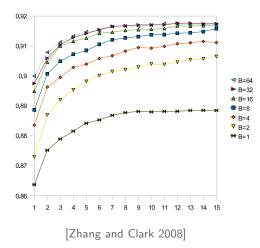
Structured Prediction

- Parsing as structured prediction [Zhang and Clark 2008]:
 - Minimize loss over entire transition sequence
 - Use beam search to find highest-scoring sequence
- ► Factored feature representations:

$$\mathbf{f}(c_0,\ldots,c_m)=\sum_{i=1}^m\mathbf{f}(c_{i-1},t_i)$$

- Online learning from oracle transition sequences:
 - ► Structured perceptron [Collins 2002]
 - ► Early update [Collins and Roark 2004]
 - ► Max-violation update [Huang et al. 2012]

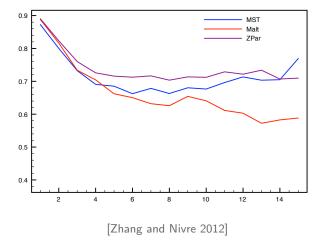
Beam Size and Training Iterations



The Best of Two Worlds?

- ► Like graph-based dependency parsing (MSTParser):
 - ▶ Global learning minimize loss over entire sentence
 - ▶ Non-greedy search accuracy increases with beam size
- ► Like (old school) transition-based parsing (MaltParser):
 - ► Highly efficient complexity still linear for fixed beam size
 - ▶ Rich features no constraints from parsing algorithm

Precision by Dependency Length



Even Richer Feature Models

	ZPar	Malt
Baseline	92.18	89.37
+distance	+0.07	-0.14
+valency	+0.24	0.00
+unigrams	+0.40	-0.29
$+ {\sf third} ext{-}{\sf order}$	+0.18	0.00
+label set	+0.07	+0.06
Extended	93.14	89.00

[Zhang and Nivre 2011, Zhang and Nivre 2012]

► Adding graph-based features may require special techniques [Zhang and Clark 2008, Bohnet and Kuhn 2012]

Dynamic Programming

- ▶ If beam search reduces search errors, why not exact inference?
- Dynamic programming for transition-based parsers:
 - Using a graph-structured stack [Huang and Sagae 2010]
 - Using push-computations [Kuhlmann et al. 2011]
- Adds constraints on feature representations

Deduction System for Arc-Eager Parsing

Items:
$$[i^b, j] \Leftrightarrow (S, i|B, A) \Rightarrow^* (S|i, j|B', A')$$

$$b = \begin{cases} 1 & \text{if } \llbracket h(i) \in A' \rrbracket \\ 0 & \text{otherwise} \end{cases}$$

Goal: $[0^0, n+1]$

Axiom: $[0^0, 1]$

Rules: Shift: $[i^b, j] \Rightarrow [j^0, j+1]$

Reduce: $[i^b, m] \wedge [m^1, j] \Rightarrow [i^b, j]$

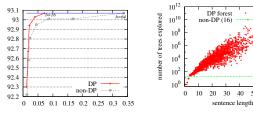
Right-Arc: $[i^b, j] \Rightarrow [j^1, j+1]$

Left-Arc: $[i^b, m] \wedge [m^0, j] \Rightarrow [i^b, j]$

[Kuhlmann et al. 2011]

Theory and Practice

- Theoretical results:
 - ▶ Arc-eager parsing in $O(n^3)$ time (cf. Eisner)
 - ▶ Arc-standard parsing in $O(n^5)$ time (cf. CKY)
- ► In practice:
 - Results hold only for very simplistic feature models
 - Practical implementations use beam search
 - Benefits from ambiguity packing



[Huang and Sagae 2010]

The Need for Speed

- Beam search helps but slows down the parser
- Dynamic programming in addition constrains feature model
- What can we do to maintain the highest speed?
 - ► Easy-first parsing give up left-to-right incremental search
 - Dynamic oracles learn how to recover from errors
- These two ideas can be combined

Easy-First Non-Directional Parsing

► Process dependencies from easy to hard (not left to right) and from local to global (bottom up) [Goldberg and Elhadad 2010]

```
Configuration: (L, A)  [L = \text{List}, A = \text{Arcs}]
Initial: ([0, 1, ..., n], \{ \})

Terminal: ([0], A)

Attach-Right(i, k): ([v_1, ..., v_m], A) \Rightarrow ([v_1, ..., v_{i-1}, v_{i+1}, ..., v_m], A \cup \{(v_{i+1}, v_i, k)\})

Attach-Left(i, k): ([v_1, ..., v_m], A) \Rightarrow ([v_1, ..., v_i, v_{i+2}, ..., v_m], A \cup \{(v_i, v_{i+1}, k)\})
```

Parsing Algorithm

▶ Given an oracle o that selects the highest-confidence transition o(c), parsing is deterministic:

```
Parse(w_1, ..., w_n)

1 c \leftarrow ([0, 1, ..., n], \{ \})

2 while length(L_c) > 1

3 t \leftarrow o(c)

4 c \leftarrow t(c)

5 return G = (\{0, 1, ..., n\}, A_c)
```

- Number of possible transitions grows with sentence length
- ▶ Parsing in $O(n \log n)$ time with priority heap

Parsing Example



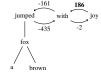
(2) AttachRight(1)

$$a \underbrace{\overbrace{\begin{array}{c} -52 \\ 314 \\ \end{array}}^{-159} fox}_{brown} \underbrace{\overbrace{\begin{array}{c} -176 \\ 0 \\ \end{array}}^{-176} with}_{-146} \underbrace{\begin{array}{c} 246 \\ \text{with} \\ 12 \\ \end{array}}_{joy}$$

(3) ATTACHRIGHT(1)



(4) AttachLeft(2)



(5) ATTACHLEFT(1)



(6)



[Goldberg and Elhadad 2010]

Oracles Revisited

- How do we train the easy-first parser?
- Recall our training procedure for greedy parsers:
 - Reconstruct oracle transition sequence for each sentence
 - ▶ Construct training data set $D = \{(c, t) | o(c) = t\}$
 - ▶ Maximize accuracy of local predictions o(c) = t
- Presupposes a unique optimal transition for each configuration
 - Does not make sense for the easy-first parser
 - ► Turns out to be a bad idea in general

Online Learning with a Conventional Oracle

```
Learn(\{T_1,\ldots,T_N\})
      \mathbf{w} \leftarrow 0.0
        for i in 1..K
                for j in 1..N
                       c \leftarrow ([\ ], [0, 1, \ldots, n_i], \{\ \})
                       while B_c \neq []
 6
                               t^* \leftarrow \operatorname{argmax}_t \mathbf{w} \cdot \mathbf{f}(c, t)
                               t_o \leftarrow o(c, T_i)
 8
                              if t^* \neq t_0
                                     \mathbf{w} \leftarrow \mathbf{w} + \mathbf{f}(c, t_o) - \mathbf{f}(c, t^*)
10
                               c \leftarrow t_o(c)
11
         return w
```

Online Learning with a Conventional Oracle

```
Learn(\{T_1,\ldots,T_N\})
      \mathbf{w} \leftarrow 0.0
       for i in 1..K
                for j in 1..N
                       c \leftarrow ([\ ], [0, 1, \ldots, n_i], \{\ \})
                       while B_c \neq []
 6
                              t^* \leftarrow \operatorname{argmax}_t \mathbf{w} \cdot \mathbf{f}(c, t)
                              t_o \leftarrow o(c, T_i)
 8
                              if t^* \neq t_0
                                     \mathbf{w} \leftarrow \mathbf{w} + \mathbf{f}(c, t_0) - \mathbf{f}(c, t^*)
                              c \leftarrow t_0(c)
10
11
         return w
```

▶ Oracle $o(c, T_i)$ returns the optimal transition for c and T_i

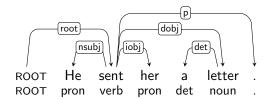
Conventional Oracle for Arc-Eager Parsing

$$o(c,T) = \begin{cases} \text{Left-Arc} & \text{if } \mathsf{top}(S_c) \leftarrow \mathsf{first}(B_c) \text{ in } T \\ \mathsf{Right-Arc} & \text{if } \mathsf{top}(S_c) \rightarrow \mathsf{first}(B_c) \text{ in } T \\ \mathsf{Reduce} & \text{if } \exists v < \mathsf{top}(S_c) : v \leftrightarrow \mathsf{first}(B_c) \text{ in } T \\ \mathsf{Shift} & \text{otherwise} \end{cases}$$

- Correct:
 - ▶ Derives T in a configuration sequence $C_{o,T} = c_0, \ldots, c_m$
- Problems:
 - Deterministic: Ignores other derivations of T
 - ▶ Incomplete: Valid only for configurations in $C_{o,T}$

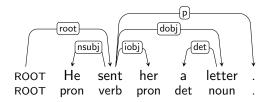
Transitions:

Stack Buffer Arcs [] [ROOT, He, sent, her, a, letter, .]



Transitions: SH

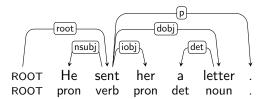
Stack Buffer
[ROOT] [He, sent, her, a, letter, .]



Transitions: SH-RA

Stack Buffer

[ROOT, He] [sent, her, a, letter, .]

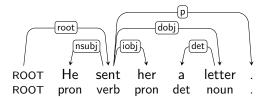


Arcs

 $ROOT \xrightarrow{root} sent$

Transitions: SH-RA-LA





Arcs

$$\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \end{array}$$

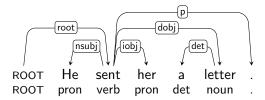
Transitions: SH-RA-LA-SH

Stack

Buffer

ROOT, sent

[her, a, letter, .]

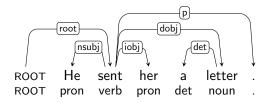


Arcs

$$ROOT \xrightarrow{root} sent$$

Transitions: SH-RA-LA-SH-RA

Stack Buffer [ROOT, sent, her] [a, letter, .]



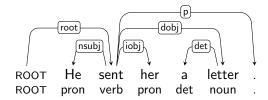
Arcs

 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \overset{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH

Stack Buffer

[ROOT, sent, her, a] [letter, .]

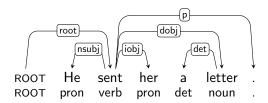


Arcs

$$\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \overset{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \end{array}$$

Transitions: SH-RA-LA-SH-RA-SH-LA

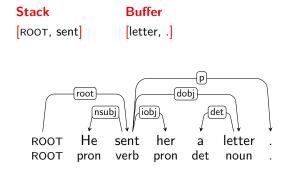
Stack Buffer [ROOT, sent, her] [letter, .]



Arcs

 $\begin{array}{c} \text{ROOT} \overset{\text{root}}{\longrightarrow} \text{ sent} \\ \text{He} \overset{\text{sbj}}{\longleftarrow} \text{ sent} \\ \text{sent} \overset{\text{iobj}}{\longrightarrow} \text{ her} \\ \text{a} \overset{\text{det}}{\longleftarrow} \text{ letter} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE



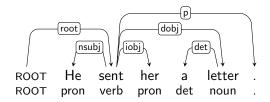
Arcs

 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \overset{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \\ \mathsf{a} \overset{\mathsf{det}}{\longleftarrow} \mathsf{letter} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA

Stack Buffer

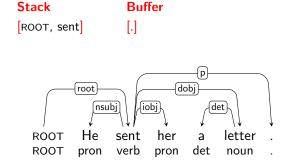
[ROOT, sent, letter] [.]



Arcs

 $\begin{array}{c} \text{ROOT} \xrightarrow{\text{root}} \text{ sent} \\ \text{He} \xleftarrow{\text{sbj}} \text{ sent} \\ \text{sent} \xrightarrow{\text{iobj}} \text{ her} \\ \text{a} \xleftarrow{\text{det}} \text{ letter} \\ \text{sent} \xrightarrow{\text{dobj}} \text{ letter} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA-RE

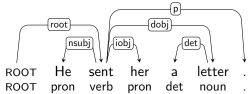


Arcs

 $\begin{array}{c} \text{ROOT} \xrightarrow{\text{root}} \text{ sent} \\ \text{He} \xleftarrow{\text{sbj}} \text{ sent} \\ \text{sent} \xrightarrow{\text{iobj}} \text{ her} \\ \text{a} \xleftarrow{\text{det}} \text{ letter} \\ \text{sent} \xrightarrow{\text{dobj}} \text{ lettel} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA





Arcs

 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{sent} \xrightarrow{\mathsf{iobj}} \mathsf{her} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{dobj}} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{p}} . \end{array}$

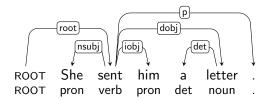
SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions:

SH-RA-LA-SH-RA

Stack Buffer

[ROOT, sent, her] [a, letter, .]

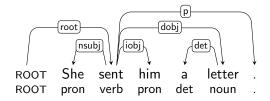


Arcs

 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \overset{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA-SH-RA-RE

Stack Buffer
[ROOT, sent] [a, letter, .]

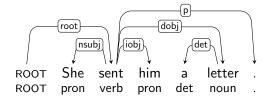


Arcs

 $\begin{array}{c} \mathsf{ROOT} \stackrel{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \stackrel{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \stackrel{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA-SH-RA-RE-SH

Stack Buffer [ROOT, sent, a] [letter, .]

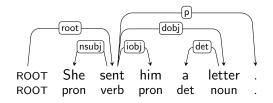


Arcs

 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{sent} \overset{\mathsf{iobj}}{\longrightarrow} \mathsf{her} \end{array}$

Transitions: SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA-SH-RA-RE-SH-LA

Stack Buffer [ROOT, sent] [letter, .]



Arcs

 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{sent} \xrightarrow{\mathsf{iobj}} \mathsf{her} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \end{array}$

Transitions:

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA-SH-RA-LA-SH-RA-RE-SH-LA-RA

Stack Buffer [ROOT, sent, letter] [.]

p dobi root nsubi (iobj det She ROOT sent him letter ROOT pron verb pron det noun

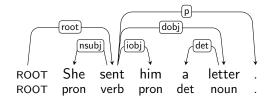
Arcs

 $\begin{array}{c} \text{ROOT} \xrightarrow{\text{root}} \text{sent} \\ \text{He} \xleftarrow{\text{sbj}} \text{sent} \\ \text{sent} \xrightarrow{\text{iobj}} \text{her} \\ \text{a} \xleftarrow{\text{det}} \text{letter} \\ \text{sent} \xrightarrow{\text{dobj}} \text{letter} \end{array}$

Transitions:

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-SH-RA-RA-RE

Stack Buffer [ROOT, sent] [.]



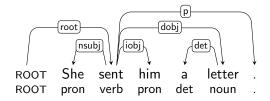
Arcs

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Transitions:

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA
SH-RA-LA-SH-RA-RE-SH-LA-RA-RE-RA

Stack Buffer [ROOT, sent, .]



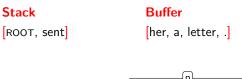
Arcs

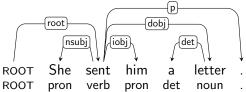
 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{sent} \xrightarrow{\mathsf{iobj}} \mathsf{her} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{dobj}} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{p}} . \end{array}$

Non-Optimality

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH





Arcs

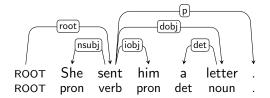
 $\mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent}$ He $\xleftarrow{\mathsf{sbj}} \mathsf{sent}$

Non-Optimality

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH





Arcs

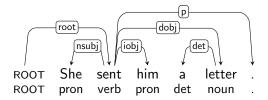
 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \end{array}$

Non-Optimality

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH

Stack Buffer [ROOT, sent, her, a] [letter, .]

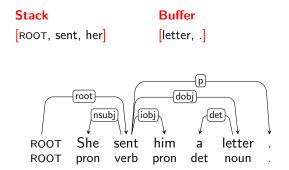


Arcs

 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA



Arcs

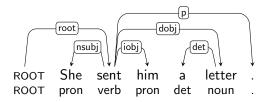
 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{a} \overset{\mathsf{det}}{\longleftarrow} \mathsf{letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH

Stack Buffer

[ROOT, sent, her, letter]



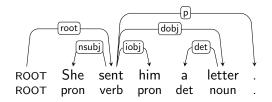
Arcs

 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

Stack Buffer [ROOT, sent, letter, .]



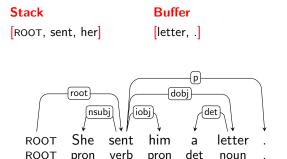
Arcs

 $\begin{array}{c} \mathsf{ROOT} \overset{\mathsf{root}}{\longrightarrow} \mathsf{sent} \\ \mathsf{He} \overset{\mathsf{sbj}}{\longleftarrow} \mathsf{sent} \\ \mathsf{a} \overset{\mathsf{det}}{\longleftarrow} \mathsf{letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

SH-RA-LA-SH-SH-SH-LA



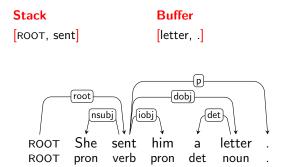
Arcs

 $\begin{array}{c} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

SH-RA-LA-SH-SH-SH-LA-LA



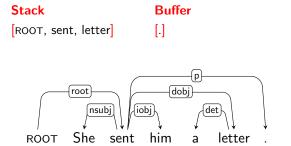
Arcs

 $\begin{array}{c} \text{ROOT} \xrightarrow{\text{root}} \text{ sent} \\ \text{He} \xleftarrow{\text{sbj}} \text{ sent} \\ \text{a} \xleftarrow{\text{det}} \text{ letter} \\ \text{her} \xleftarrow{?} \text{ letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

SH-RA-LA-SH-SH-SH-LA-LA-RA



pron

det

noun

verb

pron

Arcs

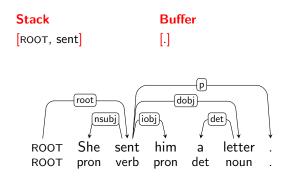
 $\begin{array}{l} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \\ \mathsf{her} \xleftarrow{?} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{dobj}} \mathsf{letter} \end{array}$

ROOT

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

SH-RA-LA-SH-SH-SH-LA-LA-RA-RE



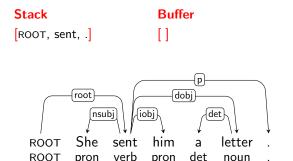
Arcs $ROOT \xrightarrow{root} sent$ He \xleftarrow{sbj} sent

 $\begin{array}{c} \text{det} & \text{det} \\ \text{a} \xleftarrow{\text{det}} & \text{letter} \\ \text{her} \xleftarrow{?} & \text{letter} \\ \text{sent} & \xrightarrow{\text{dobj}} & \text{letter} \end{array}$

SH-RA-LA-SH-RA-SH-LA-RE-RA-RE-RA

Transitions: SH-RA-LA-SH-SH-SH-LA-SH-SH [3/6]

SH-RA-LA-SH-SH-SH-LA-LA-RA-RE-RA [5/6]



Arcs

 $\begin{array}{l} \mathsf{ROOT} \xrightarrow{\mathsf{root}} \mathsf{sent} \\ \mathsf{He} \xleftarrow{\mathsf{sbj}} \mathsf{sent} \\ \mathsf{a} \xleftarrow{\mathsf{det}} \mathsf{letter} \\ \mathsf{her} \xleftarrow{?} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{\mathsf{dobj}} \mathsf{letter} \\ \mathsf{sent} \xrightarrow{p} . \end{array}$

Dynamic Oracles

- Optimality:
 - ▶ A transition is optimal if the best tree remains reachable
 - ▶ Best tree = $\operatorname{argmin}_{T'} \mathcal{L}(T, T')$
- Oracle:
 - ▶ Boolean function o(c, t, T) =true if t is optimal for c and T
 - ▶ Non-deterministic: More than one transition can be optimal
 - Complete: Correct for all configurations
- New problem:
 - ► How do we know which trees are reachable?

Reachability for Arcs and Trees

- Arc reachability:
 - ▶ An arc $w_i \rightarrow w_j$ is reachable in c iff $w_i \rightarrow w_j \in A_c$, or $w_i \in S_c \cup B_c$ and $w_i \in B_c$ (same for $w_i \leftarrow w_i$)
- Tree reachability:
 - ► A (projective) tree T is reachable in c iff every arc in T is reachable in c
- ► Arc-decomposable systems [Goldberg and Nivre 2013]:
 - Tree reachability reduces to arc reachability
 - Holds for some transition systems but not all
 - Arc-eager and easy-first are arc-decomposable
 - Arc-standard is not decomposable

Oracles for Arc-Decomposable Systems

$$o(c, t, T) = \left\{ egin{array}{ll} \mbox{true} & \mbox{if } [\mathcal{R}(c) - \mathcal{R}(t(c))] \cap T = \emptyset \\ \mbox{false} & \mbox{otherwise} \end{array}
ight.$$
 where $\mathcal{R}(c) \equiv \left\{ a \left| a
ight.$ is an arc reachable in $c
ight.$

Arc-Eager

$$o(c,\mathsf{LA},T) = \begin{cases} \mathsf{false} & \mathsf{if} \ \exists w \in B_c : s \leftrightarrow w \in T \ (\mathsf{except} \ s \leftarrow b) \\ \mathsf{true} & \mathsf{otherwise} \end{cases}$$

$$o(c,\mathsf{RA},T) = \begin{cases} \mathsf{false} & \mathsf{if} \ \exists w \in S_c : w \leftrightarrow b \in T \ (\mathsf{except} \ s \rightarrow b) \\ \mathsf{true} & \mathsf{otherwise} \end{cases}$$

$$o(c,\mathsf{RE},T) = \begin{cases} \mathsf{false} & \mathsf{if} \ \exists w \in B_c : s \rightarrow w \in T \\ \mathsf{true} & \mathsf{otherwise} \end{cases}$$

$$o(c,\mathsf{SH},T) = \begin{cases} \mathsf{false} & \mathsf{if} \ \exists w \in S_c : w \leftrightarrow b \in T \\ \mathsf{true} & \mathsf{otherwise} \end{cases}$$

Notation: s = node on top of the stack Sb = first node in the buffer B

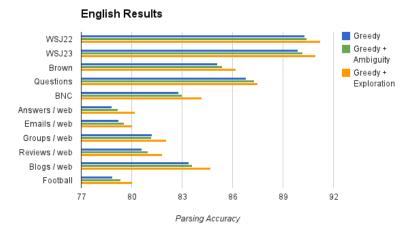
Online Learning with a Dynamic Oracle

```
Learn(\{T_1, \ldots, T_N\})
       \mathbf{w} \leftarrow 0.0
        for i in 1..K
                 for i in 1..N
                          c \leftarrow ([\ ]_S, [w_1, \dots, w_{n_i}]_B, \{\ \})
                          while B_c \neq []
  6
                                  t^* \leftarrow \operatorname{argmax}_t \mathbf{w} \cdot \mathbf{f}(c, t)
                                 t_o \leftarrow \operatorname{argmax}_{t \in \{t \mid o(c,t,T_i)\}} \mathbf{w} \cdot \mathbf{f}(c,t)
  8
                                 if t^* \neq t_o
  9
                                         \mathbf{w} \leftarrow \mathbf{w} + \mathbf{f}(c, t_0) - \mathbf{f}(c, t^*)
10
                                  c \leftarrow \text{choice}(t_o(c), t^*(c))
11
          return w
```

Online Learning with a Dynamic Oracle

```
Learn(\{T_1,\ldots,T_N\})
       \mathbf{w} \leftarrow 0.0
        for i in 1..K
                 for j in 1..N
                         c \leftarrow ([\ ]_S, [w_1, \dots, w_{n_i}]_B, \{\ \})
  5
                         while B_c \neq []
  6
                                 t^* \leftarrow \operatorname{argmax}_t \mathbf{w} \cdot \mathbf{f}(c, t)
                                 t_o \leftarrow \operatorname{argmax}_{t \in \{t \mid o(c,t,T_i)\}} \mathbf{w} \cdot \mathbf{f}(c,t)
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  9
10
                                 c \leftarrow \text{choice}(t_o(c), t^*(c))
11
          return w
```

- ► Ambiguity: use model score to break ties
- Exploration: follow model prediction even if not optimal



[Goldberg and Nivre 2012]

Ambiguity and Exploration

- Lessons from dynamic oracles:
 - Do not hide spurious ambiguity from the parser exploit it
 - Let the parser explore the consequences of its own mistakes
- Related work:
 - Bootstrapping [Choi and Palmer 2011]
 - Selectional branching [Choi and McCallum 2013]
 - Non-monotonic parsing [Honnibal et al. 2013]
 - Dynamic parsing strategy [Sartorio et al. 2013]

Summary: Learning and Inference

- ▶ Beam search and structured prediction:
 - Explores a larger search space at training and parsing time
 - Can be combined with dynamic programming
- Dynamic oracles:
 - Explores a larger search space only at training time
 - Can be combined with selectional branching and with flexible transition systems (easy-first, dynamic, non-monotonic)

Non-Projective Parsing

- ► So far only projective parsing models
- ► Non-projective parsing harder even with greedy inference
 - Non-projective: n(n-1) arcs to consider $-O(n^2)$
 - ▶ Projective: at most 2(n-1) arcs to consider -O(n)
- ► Also harder to construct dynamic oracles
 - Conjecture: arc-decomposability presupposes projectivity

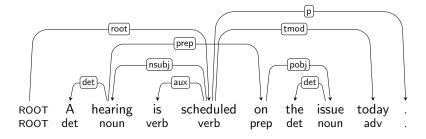
Previous Approaches

- Pseudo-projective parsing [Nivre and Nilsson 2005]
 - Preprocess training data, post-process parser output
 - Approximate encoding with incomplete coverage
 - Relatively high precision but low recall
- ► Extended arc transitions [Attardi 2006]
 - Transitions that add arcs between non-adjacent subtrees
 - ▶ Upper bound on arc degree (limited to local relations)
 - Exact dynamic programming algorithm [Cohen et al. 2011]
- ► List-based algorithms [Covington 2001, Nivre 2007]
 - Consider all word pairs instead of adjacent subtrees
 - Increases parsing complexity (and training time)
 - ► Improved accuracy and efficiency by adding "projective transitions" [Choi and Palmer 2011]

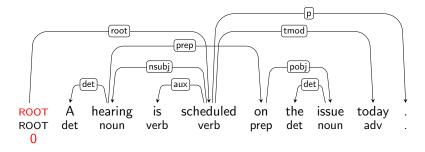
Novel Approaches

- ▶ Online reordering [Nivre 2009, Nivre et al. 2009]:
 - Reorder words during parsing to make tree projective
 - Add a special transition for swapping adjacent words
 - Quadratic time in the worst case but linear in the best case
- Multiplanar parsing [Gómez-Rodríguez and Nivre 2010]:
 - ► Factor dependency trees into *k* planes without crossing arcs
 - Use k stacks to parse each plane separately
 - ► Linear time parsing with constant *k*

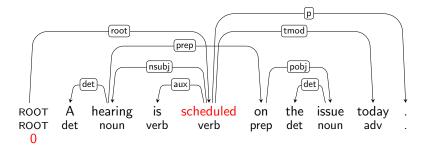
- Projectivity is a property of a dependency tree only in relation to a particular word order
 - Words can always be reordered to make the tree projective
 - Given a dependency tree T = (V, A, <), let the projective order $<_p$ be the order defined by an inorder traversal of T with respect to < [Veselá et al. 2004]



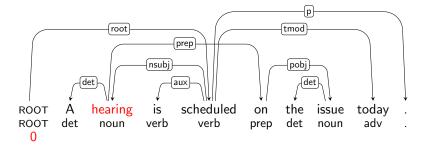
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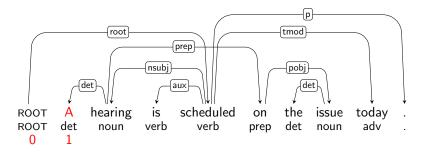
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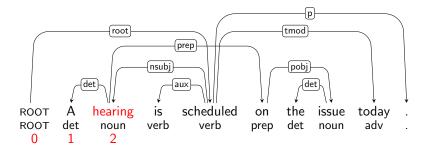
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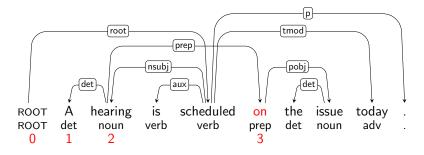
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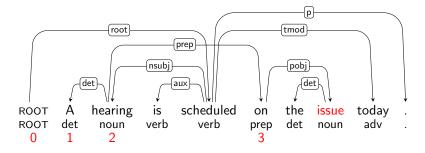
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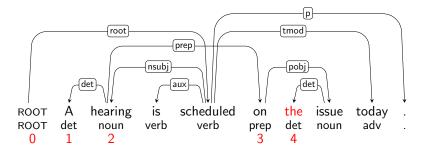
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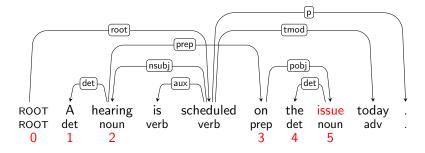
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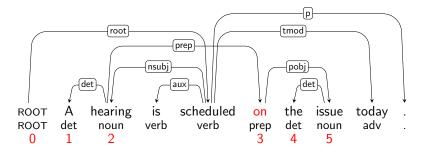
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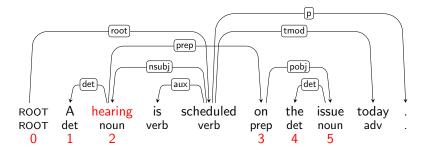
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 - Words can always be reordered to make the tree projective
 - ▶ Given a dependency tree T = (V, A, <), let the projective order $<_p$ be the order defined by an inorder traversal of T with respect to < [Veselá et al. 2004]



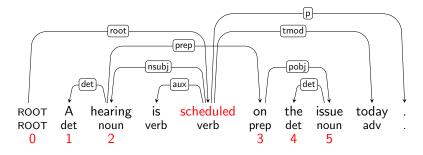
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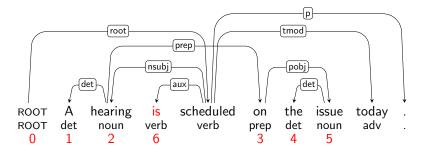
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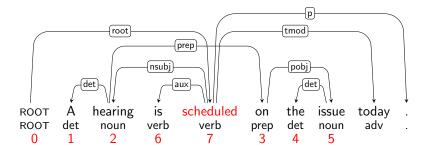
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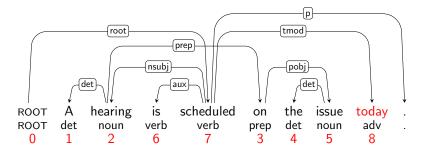
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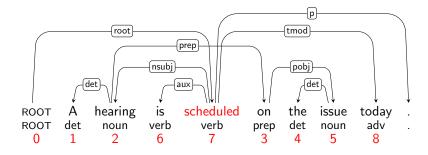
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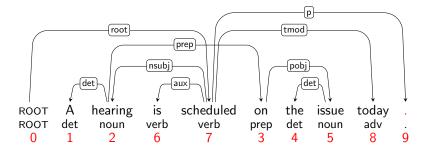


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 - ▶ Given a dependency tree T = (V, A, <), let the projective order $<_p$ be the order defined by an inorder traversal of T with respect to < [Veselá et al. 2004]



Projectivity and Word Order

- Projectivity is a property of a dependency tree only in relation to a particular word order
 - Words can always be reordered to make the tree projective
 - Given a dependency tree T = (V, A, <), let the projective order $<_p$ be the order defined by an inorder traversal of T with respect to < [Veselá et al. 2004]



Transition System for Online Reordering

Configuration: (S, B, A) [S = Stack, B = Buffer, A = Arcs]

Initial: $([], [0, 1, ..., n], \{])$

Terminal: ([0], [], A)

Shift: $(S, i|B, A) \Rightarrow (S|i, B, A)$

Right-Arc(k**):** $(S|i|j,B,A) \Rightarrow (S|i,B,A \cup \{(i,j,k)\})$

Left-Arc(k): $(S|i|j, B, A) \Rightarrow (S|j, B, A \cup \{(j, i, k)\}) \quad i \neq 0$

Swap: $(S|i|j, B, A) \Rightarrow (S|j, i|B, A) \quad 0 < i < j$

0 < i < i

Transition System for Online Reordering

Configuration: (S, B, A) [S = Stack, B = Buffer, A = Arcs]Initial: $([], [0, 1, ..., n], \{ \})$ Terminal: ([0], [], A)Shift: $(S, i|B, A) \Rightarrow (S|i, B, A)$ Right-Arc(k): $(S|i|j, B, A) \Rightarrow (S|i, B, A \cup \{(i, j, k)\})$ Left-Arc(k): $(S|i|j, B, A) \Rightarrow (S|j, B, A \cup \{(j, i, k)\})$ $i \neq 0$

Transition-based parsing with two interleaved processes:

 $(S|i|i, B, A) \Rightarrow (S|i, i|B, A)$

- 1. Sort words into projective order $<_p$
- 2. Build tree T by connecting adjacent subtrees
- ightharpoonup T is projective with respect to $<_p$ but not (necessarily) <

Swap:

```
[]<sub>S</sub> [ROOT, A, hearing, is, scheduled, on, the, issue, today, .]<sub>B</sub>
```

```
hearing
                      is scheduled
       Α
                                            the
                                                 issue
                                                       today
ROOT
                                      on
                                                         adv
ROOT
       det
             noun
                     verb
                             verb
                                            det
                                      prep
                                                 noun
```

```
[ROOT]<sub>S</sub> [A, hearing, is, scheduled, on, the, issue, today, .]<sub>B</sub>
```

```
hearing
                      is scheduled
       Α
                                           the
                                                 issue
                                                       today
ROOT
                                      on
                                                        adv
ROOT
       det
             noun
                     verb
                             verb
                                            det
                                      prep
                                                 noun
```

```
[ROOT, A]<sub>S</sub> [hearing, is, scheduled, on, the, issue, today, .]<sub>B</sub>
```

```
hearing
                     is scheduled
       Α
                                           the
                                                 issue
                                                       today
ROOT
                                      on
                                                        adv
ROOT
       det
             noun
                    verb
                             verb
                                           det
                                      prep
                                                 noun
```

```
[ROOT, A, hearing]<sub>S</sub> [is, scheduled, on, the, issue, today, .]_B
```

```
hearing
                      is scheduled
       Α
                                           the
                                                 issue
                                                       today
ROOT
                                      on
                                                        adv
ROOT
       det
             noun
                     verb
                             verb
                                            det
                                      prep
                                                 noun
```

```
[ROOT, hearing]<sub>S</sub> [is, scheduled, on, the, issue, today, .]<sub>B</sub>
```

```
hearing
                      is
                           scheduled
                                                  issue
ROOT
                                             the
                                                         today
                                        on
ROOT
       det
                     verb
                              verb
                                             det
                                                          adv
             noun
                                       prep
                                                   noun
```

ROOT, hearing, is scheduled, on, the, issue, today, .] B



ROOT, hearing, is, scheduled S on, the, issue, today, B



[ROOT, hearing, scheduled] S [on, the, issue, today, R]



ROOT, hearing, scheduled, on S [the, issue, today, B]



ROOT, hearing, scheduled, on, the S [issue, today, R]



ROOT, hearing, scheduled, on, the, issue s today, .] B



ROOT, hearing, scheduled, on, issue S [today,]B



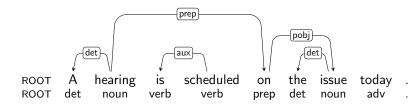
[ROOT, hearing, scheduled, on]_S [today, .]_B



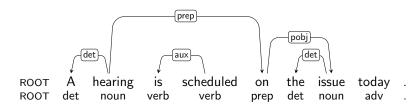
[ROOT, hearing, on]_S [scheduled, today, .]_B



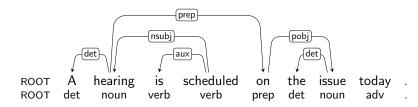
[ROOT, hearing]_S [scheduled, today, .]_B



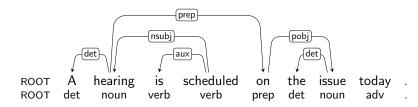
[ROOT, hearing, scheduled]_S [today, .]_B



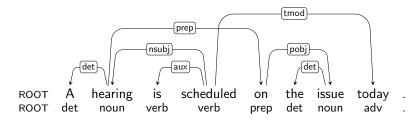
[ROOT, scheduled]_S [today, .]_B



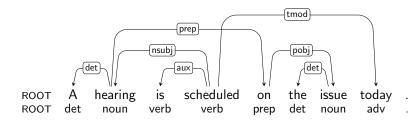
[ROOT, scheduled, today]_S $[.]_B$



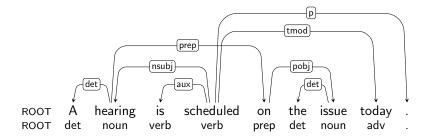
[ROOT, scheduled]_S [.]_B



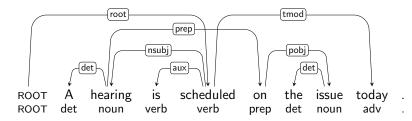
[ROOT, scheduled, .] $_{S}$ [] $_{B}$



[ROOT, scheduled]_S $[]_B$



 $[ROOT]_S$ $[]_B$



Analysis

- Correctness:
 - Sound and complete for the class of non-projective trees
- Complexity for greedy or beam search parsing:
 - Quadratic running time in the worst case
 - Linear running time in the average case
- Works well with beam search and structured prediction

	Czech		German	
	LAS	UAS	LAS	UAS
Projective	80.8	86.3	86.2	88.5
Reordering	83.9	89.1	88.7	90.9

[Bohnet and Nivre 2012]

Multiplanarity

- ▶ Multiplanarity is based on the notion of planarity:
 - A dependency graph is planar if it has no crossing arcs
 - ► A dependency graph is k-planar if it can be decomposed into (at most) k planar graphs [Yli-Jyrä 2003]
- ► In most treebanks, well over 99% of the trees are at most 2-planar [Gómez-Rodríguez and Nivre 2010]
- \blacktriangleright We can parse k-planar graphs in linear time using k stacks

1-Planar Transition System

```
Configuration: (S, B, A) [S = Stack, B = Buffer, A = Arcs]
```

Initial: $([], [0, 1, ..., n], \{])$

Terminal: (S, [], A)

Shift:
$$(S, i|B, A) \Rightarrow (S|i, B, A)$$

Reduce:
$$(S|i, B, A) \Rightarrow (S, B, A)$$

Right-Arc(k):
$$(S|i,j|B,A) \Rightarrow (S|i,j|B,A \cup \{(i,j,k)\})$$
 $\neg h(j,A)$

Left-Arc(
$$k$$
): $(S|i,j|B,A) \Rightarrow (S|i,j|B,A \cup \{(j,i,k)\}) \neg h(i,A) \land i \neq 0$

- ▶ Similar to the arc-eager system except:
 - Reduce does not require popped node to have a head
 - ► **Left-Arc**/**Right-Arc** do not affect *S* or *B*

2-Planar Transition System

Configuration:
$$(S_1, S_2, B, A)$$
 $[S_1 = \text{Stack 1}, S_2 = \text{Stack 2}]$
Initial: $([\], [\], [0, 1, \dots, n], \{\ \})$
Terminal: $(S_1, S_2, [\], A)$

 $(S_1, S_2, i|B, A) \Rightarrow (S_1|i, S_2|i, B, A)$

Reduce:
$$(S_1|i, S_2, B, A) \Rightarrow (S_1, S_2, B, A)$$

Right-Arc(k): $(S_1|i, S_2, j|B, A) \Rightarrow (S_1|i, S_2, j|B, A \cup \{(i, j, k)\})$ $\neg h(i, A) \land i \neq 0$
Left-Arc(k): $(S_1|i, S_2, j|B, A) \Rightarrow (S_1|i, S_2, j|B, A \cup \{(j, i, k)\})$ $\neg h(i, A) \land i \neq 0$

Switch:
$$(S_1, S_2, B, A) \Rightarrow (S_2, S_1, B, A)$$

- Similar to 1-planar system except:
 - Shift pushes a node to both stacks
 - ▶ Left-Arc/Right-Arc/Reduce only affect S_1
 - **Switch** swaps S_1 and S_2

Shift:

```
[]S_1 [ROOT, A, hearing, is, scheduled, on, the, issue, today, .]B
```

```
ROOT
       Α
            hearing
                      is scheduled
                                           the
                                                issue
                                                       today
                                      on
ROOT
       det
             noun
                     verb
                             verb
                                      prep
                                            det
                                                 noun
                                                        adv
```

```
[ROOT]S_1 [A, hearing, is, scheduled, on, the, issue, today, .]B [ROOT]S_2
```

```
ROOT
       Α
          hearing
                  is scheduled
                                   on
                                        the issue
                                                  today
ROOT
      det
            noun
                   verb
                          verb
                                  prep
                                        det
                                             noun
                                                   adv
```

```
[ROOT, A]_{S_1} [hearing, is, scheduled, on, the, issue, today, .]_B [ROOT, A]_{S_2}
```

```
ROOT
       Α
           hearing
                   is scheduled
                                        the issue
                                                   today
                                   on
ROOT
      det
            noun
                   verb
                           verb
                                   prep
                                        det
                                             noun
                                                    adv
```

```
[ROOT, A]_{S_1} [hearing, is, scheduled, on, the, issue, today, .]_B [ROOT, A]_{S_2}
```

hearing is scheduled on the issue today ROOT ROOT det noun verb verb prep det noun adv

```
[ROOT]S_1 [hearing, is, scheduled, on, the, issue, today, .]B [ROOT, A]S_2
```



```
[ROOT, hearing]S_1 [is, scheduled, on, the, issue, today, .]B [ROOT, A, hearing]S_2
```



```
[ROOT, hearing, is]_{S_1} [scheduled, on, the, issue, today, .]_B [ROOT, A, hearing, is]_{S_2}
```



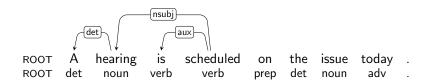
```
[ROOT, hearing, is]_{S_1} [scheduled, on, the, issue, today, .]_B [ROOT, A, hearing, is]_{S_2}
```



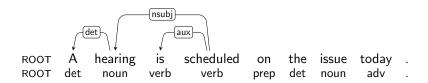
```
[ROOT, hearing]S_1 [scheduled, on, the, issue, today, .]B [ROOT, A, hearing, is]S_2
```



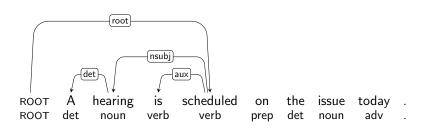
```
[ROOT, hearing]S_1 [scheduled, on, the, issue, today, .]B [ROOT, A, hearing, is]S_2
```



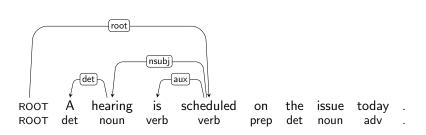
```
[ROOT]<sub>S<sub>1</sub></sub> [scheduled, on, the, issue, today, .]<sub>B</sub>
[ROOT, A, hearing, is]<sub>S<sub>2</sub></sub>
```



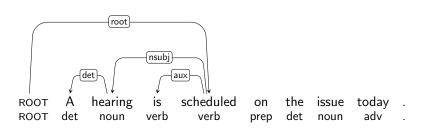
```
[ROOT]<sub>S1</sub> [scheduled, on, the, issue, today, .]<sub>B</sub>
[ROOT, A, hearing, is]<sub>S2</sub>
```



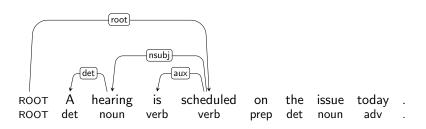
```
[ROOT, scheduled]S_1 [on, the, issue, today, .]B [ROOT, A, hearing, is, scheduled]S_2
```



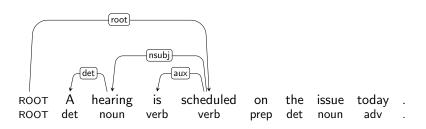
```
[ROOT, A, hearing, is, scheduled]_{S_1} [on, the, issue, today, .]_B [ROOT, scheduled]_{S_2}
```



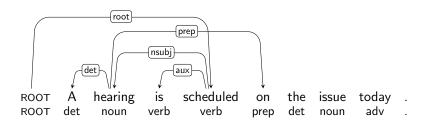
```
[ROOT, A, hearing, is]S_1 [on, the, issue, today, .]B [ROOT, scheduled]S_2
```



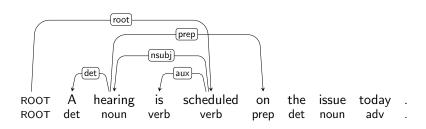
```
[ROOT, A, hearing]S_1 [on, the, issue, today, .]B [ROOT, scheduled]S_2
```



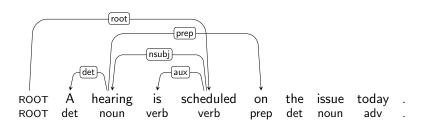
```
[ROOT, A, hearing]S_1 [on, the, issue, today, .]B [ROOT, scheduled]S_2
```



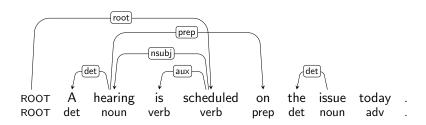
```
[ROOT, A, hearing, on]S_1 [the, issue, today, .]B [ROOT, scheduled, on]S_2
```



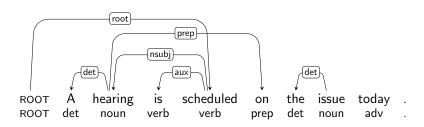
```
[ROOT, A, hearing, on, the] S_1 [issue, today, .] B [ROOT, scheduled, on, the] S_2
```



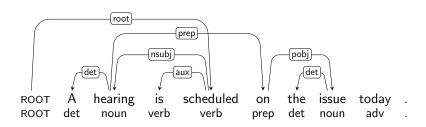
```
[ROOT, A, hearing, on, the] S_1 [issue, today, .] B [ROOT, scheduled, on, the] S_2
```



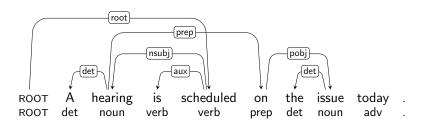
```
[ROOT, A, hearing, on]_{S_1} [issue, today, .]_B
[ROOT, scheduled, on, the]_{S_2}
```



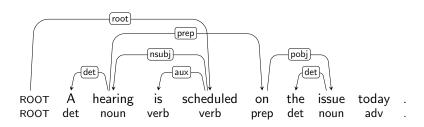
```
[ROOT, A, hearing, on]S_1 [issue, today, .]B
[ROOT, scheduled, on, the]S_2
```



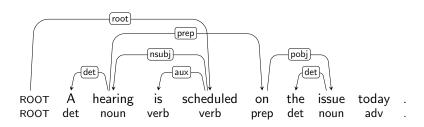
```
[ROOT, A, hearing, on, issue] S_1 [today, .] B [ROOT, scheduled, on, the, issue] S_2
```



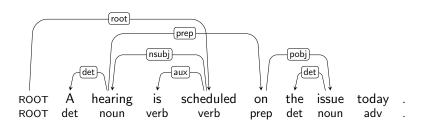
```
[ROOT, scheduled, on, the, issue] S_1 [today, .] S_2 [ROOT, A, hearing, on, issue] S_2
```



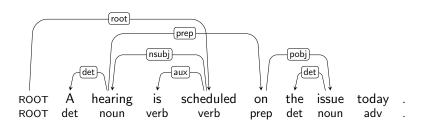
```
[ROOT, scheduled, on, the] S_1 [today, .] B [ROOT, A, hearing, on, issue] S_2
```



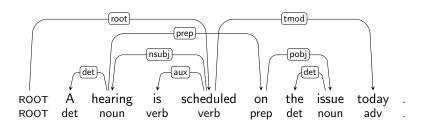
```
[ROOT, scheduled, on]S_1 [today, .]B
[ROOT, A, hearing, on, issue]S_2
```



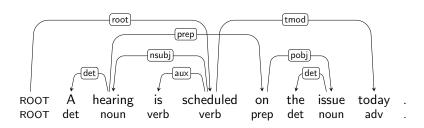
```
[ROOT, scheduled]S_1 [today, .]B [ROOT, A, hearing, on, issue]S_2
```



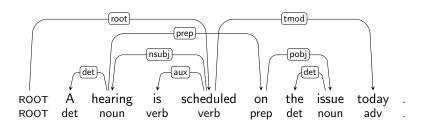
```
[ROOT, scheduled]S_1 [today, .]B [ROOT, A, hearing, on, issue]S_2
```



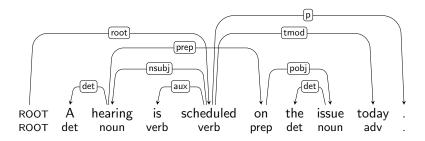
```
[ROOT, scheduled, today]_{S_1} [.]_B [ROOT, A, hearing, on, issue, today]_{S_2}
```



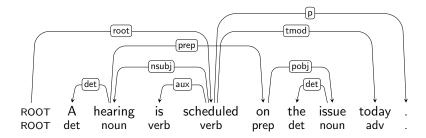
```
[ROOT, scheduled]S_1 [.]B [ROOT, A, hearing, on, issue, today]S_2
```



```
[ROOT, scheduled]S_1 [.]B [ROOT, A, hearing, on, issue, today]S_2
```



```
[ROOT, scheduled, .]_{S_1} []_B [ROOT, A, hearing, on, issue, today, .]_{S_2}
```



Morphology and Syntax

- Morphological analysis in dependency parsing:
 - Crucially assumed as input, not predicted by the parser
 - Pipeline approach may lead to error propagation
 - Most PCFG-based parsers at least predict their own tags
- Recent interest in joint models for morphology and syntax:
 - ► Graph-based [McDonald 2006, Lee et al. 2011, Li et al. 2011]
 - ► Transition-based [Hatori et al. 2011, Bohnet and Nivre 2012]
- Can improve both morphology and syntax

Transition System for Morphology and Syntax

```
Configuration: (S, B, M, A) [M = Morphology]
```

Initial: $([], [0, 1, ..., n], \{], \{])$

Terminal: ([0], [], M, A)

Shift(p):
$$(S, i|B, M, A) \Rightarrow (S|i, B, M \cup \{(i, m)\}, A)$$

Right-Arc(
$$k$$
): $(S|i|j, B, M, A) \Rightarrow (S|i, B, M, A \cup \{(i, j, k)\})$

Left-Arc(k):
$$(S|i|j, B, M, A) \Rightarrow (S|j, B, M, A \cup \{(j, i, k)\})$$
 $i \neq 0$

Swap:
$$(S|i|j, B, M, A) \Rightarrow (S|j, i|B, M, A)$$
 $0 < i < j$

Transition System for Morphology and Syntax

```
Configuration: (S, B, M, A)  [M = Morphology]
Initial: ([], [0, 1, ..., n], \{ \}, \{ \})
Terminal: ([0], [], M, A)
Shift(p): (S, i|B, M, A) \Rightarrow (S|i, B, M \cup \{(i, m)\}, A)
Right-Arc(k): (S|i|j, B, M, A) \Rightarrow (S|i, B, M, A \cup \{(i, j, k)\})
Left-Arc(k): (S|i|j, B, M, A) \Rightarrow (S|j, B, M, A \cup \{(j, i, k)\}) i \neq 0
Swap: (S|i|j, B, M, A) \Rightarrow (S|j, i|B, M, A) 0 < i < j
```

- ► Transition-based parsing with three interleaved processes:
 - Assign morphology when words are shifted onto the stack
 - ► Optionally sort words into projective order <_p
 - ▶ Build dependency tree *T* by connecting adjacent subtrees

Parsing Richly Inflected Languages

- ► Full morphological analysis: lemma + postag + features
 - Beam search and structured predication
 - \triangleright Parser selects from k best tags + features
 - Rule-based morphology provides additional features
- Evaluation metrics:
 - ▶ PM = morphology (postag + features)
 - ► LAS = labeled attachment score

	Czech		Finnish		German		Hungarian		Russian	
	PM	LAS	PM	LAS	PM	LAS	PM	LAS	PM	LAS
Pipeline	93.0	83.1	88.88	79.9	89.1	91.8	96.1	88.4	92.6	87.4
Joint	94.4	83.5	91.6	82.5	91.2	92.1	97.4	89.1	95.1	88.0

[Bohnet et al. 2013]

Summary

- Transition-based parsing:
 - Efficient parsing using heuristic inference
 - Unconstrained history-based feature models
- Recent advances in synergy:
 - Beam search and structured prediction
 - Easy-first parsing and dynamic oracles
 - Online reordering for non-projective trees
 - Joint morphological and syntactic analysis

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