

Here

$$N_C(p^2) = \int_{m_\pi}^{\sqrt{p^2}} dm \rho_h(m), \quad (71)$$

and in analogy to (53), $T_C(p^2)$ is a “life-time” factor giving the probability that a cluster of mass $m_C^2 = p^2$ decays within a time interval t in the laboratory frame,

$$T_C(p^2) = 1 - \exp\left[-\frac{t}{\tau_C(p^2)}\right], \quad (72)$$

where in this case we simply take $\tau_C(p^2) = E_C/p^2 = \gamma/m_C$ from the uncertainty principle. In order to find the value for the decay probability (70) for a given cluster of mass m_C , we sum over the possible decays for this cluster according to the particle data tables. The probability for a specific 2-body decay mode is taken to be a product of a flavor, a spin and a kinematical factor [38],

$$\Gamma_{C \rightarrow h_1 h_2}(m_C; m_1, m_2) := P_m(m_C, m_1 + m_2) P_s(j_1, j_2) P_k(m_C, m_1, m_2), \quad (73)$$

where $j_{1,2}$ ($m_{1,2}$) are the angular momenta (masses) of the two hadrons $h_{1,2}$. The factor

$$P_m(m_C, m_1 + m_2) = \left(1 + \frac{m_1^2 + m_2^2}{m_C^2}\right) \sqrt{1 - \frac{(m_1 + m_2)^2}{M_c^2}} \theta(m_C - m_1 - m_2) \quad (74)$$

is the two-body phase-space suppression function for the decay. The spin factor

$$P_s(j_1, j_2) = (2j_1 + 1) (2j_2 + 1) \quad (75)$$

takes into account the spin degeneracy with the allowed spins j_1 and j_2 of the two hadrons.

The kinematic factor

$$P_k(m_C, m_1, m_2) = \frac{\sqrt{\lambda(m_C^2, m_1^2, m_2^2)}}{m_C^2} \quad (76)$$

is the two-body phase-space factor, where $\lambda(a, b, c) = a^2 + b^2 + c^2 - 2(ab + ac + bc)$.

Thus, with the decay probability $\Gamma_{C \rightarrow h}$ of (70) evaluated in this fashion, the terms involving the \hat{D} and \hat{E} operators in the kinetic equations (48) and (49) can be expressed as

$$\begin{aligned} \hat{D}_\chi^U F_\chi &= F_\chi(r; x, p_\perp^2, p^2) \int dp'^2 \Gamma_{\chi \rightarrow U}(p^2, p'^2) \\ \hat{E}_\chi^h F_\chi &= F_\chi(r; x, p_\perp^2, p^2) \int dp'^2 \Gamma_{\chi \rightarrow h}(p^2, p'^2) \\ \hat{D}'_\chi^U F_\chi &= \int dp'^2 dp_\perp'^2 \frac{dx'}{x'} F_\chi(r; x, p_\perp'^2, p'^2) \Gamma_{\chi \rightarrow U}(p'^2, p^2) \\ \hat{E}'_U^h F_U &= F_U(r; x, p_\perp^2, p^2) \int dp'^2 \Gamma_{U \rightarrow h}(p^2, p'^2) \end{aligned} \quad (77)$$