# Return of the Devil in the Details: Delving Deep into Convolutional Nets

Ken Chatfield ken@robots.ox.ac.uk Karen Simonyan karen@robots.ox.ac.uk Andrea Vedaldi vedaldi@robots.ox.ac.uk

Andrew Zisserman az@robots.ox.ac.uk Visual Geometry Group Department of Engineering Science University of Oxford Oxford, UK

#### Abstract

The latest generation of Convolutional Neural Networks (CNN) have achieved impressive results in challenging benchmarks on image recognition and object detection, significantly raising the interest of the community in these methods. Nevertheless, it is still unclear how different CNN methods compare with each other and with previous state-of-the-art shallow representations such as the Bag-of-Visual-Words and the Improved Fisher Vector. This paper conducts a rigorous evaluation of these new techniques, exploring different deep architectures and comparing them on a common ground, identifying and disclosing important implementation details. We identify several useful properties of CNN-based representations, including the fact that the dimensionality of the CNN output layer can be reduced significantly without having an adverse effect on performance. We also identify aspects of deep and shallow methods that can be successfully shared. In particular, we show that the data augmentation techniques commonly applied to CNN-based methods can also be applied to shallow methods, and result in an analogous performance boost. Source code and models to reproduce the experiments in the paper is made publicly available.

## 1 Introduction

Perhaps the single most important design choice in current state-of-the-art image classification and object recognition systems is the choice of visual features, or image representation. In fact, most of the quantitative improvements to image understanding obtained in the past dozen years can be ascribed to the introduction of improved representations, from the *Bagof-Visual-Words* (BoVW) [6, 28] to the (*Improved*) Fisher Vector (IFV) [23]. A common characteristic of these methods is that they are largely handcrafted. They are also relatively simple, comprising dense sampling of local image patches, describing them by means of visual descriptors such as SIFT, encoding them into a high-dimensional representation, and then pooling over the image. Recently, these handcrafted approaches have been substantially outperformed by the introduction of the latest generation of *Convolutional Neural Networks* (CNNs) [19] to the computer vision field. These networks have a substantially more sophisticated structure than standard representations, comprising several layers of non-linear

feature extractors, and are therefore said to be *deep* (in contrast, classical representation will be referred to as *shallow*). Furthermore, while their structure is handcrafted, they contain a very large number of parameters learnt from data. When applied to standard image classification and object detection benchmark datasets such as ImageNet ILSVRC [7] and PASCAL VOC [9] such networks have demonstrated excellent performance [8, 11, 20, 25, 27], significantly better than standard image encodings [3].

Despite these impressive results, it remains unclear how different deep architectures compare to each other and to shallow computer vision methods such as IFV. Most papers did not test these representations extensively on a common ground, so a systematic evaluation of the effect of different design and implementation choices remains largely missing. As noted in our previous work [3], which compared the performance of various shallow visual encodings, the *performance of computer vision systems depends significantly on implementation details*. For example, state-of-the-art methods such as [17] not only involve the use of a CNN, but also include other improvements such as the use of very large scale datasets, GPU computation, and data augmentation (also known as data jittering or virtual sampling). These improvements could also transfer to shallow representations such as the IFV, potentially explaining a part of the performance gap [22].

In this study we analyse and empirically clarify these issues, conducting a large set of rigorous experiments (Sect. 4), in many ways picking up the story where it last ended in [3] with the comparison of shallow encoders. We focus on methods to construct *image representations*, *i.e.* encoding functions  $\phi$  mapping an image I to a vector  $\phi(I) \in \mathbb{R}^d$  suitable for analysis with a linear classifier, such as an SVM. We consider **three scenarios** (Sect. 2, Sect. 3): shallow image representations, deep representations pre-trained on outside data, and deep representation pre-trained and then fine-tuned on the target dataset. As part of our tests, we explore **generally-applicable best practices** that are nevertheless more often found in combination with CNNs [17] or, alternatively, with shallow encoders [3], porting them with mutual benefit. These are (Sect. 2): the use of *colour information*, feature *normalisation*, and, most importantly, the use of *substantial data augmentation*. We also determine **scenario-specific best-practices**, improving the ones in [3, 24] and others, including dimensionality reduction for deep features. Finally, we achieve **performance competitive with the state of the art [21, 30]** on PASCAL VOC classification using less additional training data and significantly simpler techniques. As in [3], the source code and models to reproduce all experiments in this paper is available on the project website 1.

## 2 Scenarios

This section introduces the three types of image representation  $\phi(I)$  considered in this paper, describing them within the context of three different scenarios. Having outlined details specific to each, general methodologies which apply to all three scenarios are reviewed, such as data augmentation and feature normalisation, together with the linear classifier (trained with a standard hinge loss). We also specify here the benchmark datasets used in the evaluation.

Scenario 1: Shallow representation (IFV). Our reference shallow image representation is the IFV [23]. Our choice is motivated by the fact that IFV usually outperforms related encoding methods such as BoVW, LLC [3], and VLAD [15]. Given an image I, the IFV  $\phi_{\text{FV}}(I)$  is obtained by extracting a dense collection of patches and corresponding local descriptors  $\mathbf{x}_i \in \mathbb{R}^D$  (e.g. SIFT) from the image at multiple scales. Each descriptor  $\mathbf{x}_i$  is then soft-quantized using a Gaussian Mixture Model with K components. First and second order differences between each descriptor  $\mathbf{x}_i$  and its Gaussian cluster mean  $\mu_k$  are accumulated

<sup>1</sup>http://www.robots.ox.ac.uk/~vgg/research/deep\_eval/

in corresponding blocks  $\mathbf{u}_k$ ,  $\mathbf{v}_k$  in the vector  $\phi_{\text{FV}}(I) \in \mathbb{R}^{2KD}$ , appropriately weighed by the Gaussian soft-assignments and covariance, leading to a 2KD-dimensional image representation  $\phi_{\text{FV}}(I) = [\mathbf{u}_1^\top, \mathbf{v}_1^\top, \dots \mathbf{u}_K^\top, \mathbf{v}_K^\top]^\top$ . The *improved* version of the Fisher vector involves post-processing  $\phi_{\text{FV}}$  by computing the signed square-root of its scalar components and normalising the result to a unit  $\ell^2$  norm. The details of this construction can be found in [23]; here we follow the notation of [3].

Scenario 2: Deep representation (CNN) with pre-training. Our deep representations are inspired by the success of the CNN of Krizhevsky *et al.* [17]. As shown in [8, 32], the vector of activities  $\phi_{\text{CNN}}(I)$  of the penultimate layer of a deep CNN, learnt on a large dataset such as ImageNet [7], can be used as a powerful image descriptor applicable to other datasets. Numerous CNN architectures that improve the previous state of the art obtained using shallow representations have been proposed, but choosing the best one remains an open question. Many are inspired by [17]: DeCAF [8, 11], Caffe [16], Oquab *et al.* [20]. Others use larger networks with a smaller stride of the first convolutional layer: Zeiler and Fergus [32] and OverFeat [25, 27]. Other differences include the CNN pre-training protocols. Here we adopt a single learning framework and experiment with architectures of different complexity exploring their performance-speed trade-off.

Scenario 3: Deep representation (CNN) with pre-training and fine-tuning. In Scenario 2 features are trained on one (large) dataset and applied to another (usually smaller). However, it was demonstrated [11] that fine-tuning a pre-trained CNN on the target data can significantly improve the performance. We consider this scenario separately from that of Scenario 2, as the image features become dataset-specific after the fine-tuning.

**Data augmentation.** Data augmentation is a method applicable to shallow and deep representations, but that has been so far mostly applied to the latter [17, 32]. By augmentation we mean perturbing an image I by transformations that leave the underlying class unchanged (e.g. cropping and flipping) in order to generate additional examples of the class. Augmentation can be applied at training time, at test time, or both. The augmented samples can either be taken as-is or combined to form a single feature, e.g. using sum/max-pooling or stacking.

**Linear predictors.** All the representations  $\phi(I)$  in the three scenarios are used to construct *linear predictors*  $\langle \mathbf{w}, \phi(I) \rangle$  for each class to be recognized. These predictors are learnt using Support Vector Machines (SVM) by fitting  $\mathbf{w}$  to the available training data by minimizing an objective function balancing a quadratic regularizer and the hinge-loss. The parameter C in the SVM, trading-off regularizer and loss, is determined using an held-off validation subset of the data. Here we use the same learning framework with all representations. It is common experience that linear classifiers are particularly sensitive to the *normalisation of the data* and that, in particular, SVMs tend to benefit from  $\ell^2$  normalisation [23] (an interpretation is that after normalisation the inner product corresponds to the cosine similarly).

Benchmark data. As reference benchmark we use the PASCAL VOC [9] data as already done in [3]. The VOC-2007 edition contains about 10,000 images split into train, validation, and test sets, and labelled with twenty object classes. A one-vs-rest SVM classifier for each class is learnt and evaluated independently and the performance is measured as mean Average Precision (mAP) across all classes. The VOC-2012 edition contains roughly twice as many images and does not include test labels; instead, evaluation uses the official PASCAL Evaluation Server. To train deep representations we use the ILSVRC-2012 challenge dataset. This contains 1,000 object categories from ImageNet [7] with roughly 1.2M training images, 50,000 validation images, and 100,000 test images. Performance is evaluated using the top-5 classification error. Finally, we also evaluate over the Caltech-101 and Caltech-

**256** image classification benchmarks [10, 12]. For Caltech-101, we followed the protocol of [3], and considered three random splits into training and testing data, each of which comprises 30 training and up to 30 testing images per class. For Caltech-256, two random splits were generated, each of which contains 60 training images per class, and the rest are used for testing. On both Caltech datasets, performance is measured using mean class accuracy.

#### 3 Details

#### 3.1 Improved Fisher Vector details

Our IFV representation uses a slightly improved setting compared to the best result of [3].

Computation starts by upscaling the image I by a factor of 2 [26], followed by SIFT features extraction with a stride of 3 pixels at 7 different scales with  $\sqrt{2}$  scale increments. These features are square-rooted as suggested by [1], and decorrelated and reduced in dimension from 128D to 80D using PCA. A GMM with K=256 components is learnt from features sampled from the training images. Hence the Fisher Vector  $\phi_{FV}(I)$  has dimension 2KD=40,960. Before use in classification, the vector is signed-square-rooted and  $I^2$ -normalised (square rooting correspond to the Hellinger's kernel map [29]). As in [3], square-rooting is applied twice, once to the raw encodings, and once again after sum pooling and normalisation. In order to capture weak geometrical information, the IFV representation is used in a *spatial pyramid* [18]. As in [3], the image is divided into  $1 \times 1$ ,  $3 \times 1$ , and  $2 \times 2$  spatial subdivisions and corresponding IFVs are computed and stacked with an overall dimension of  $8 \times 2KD = 327,680$  elements.

In addition to this standard formulation, we experiment with a few modifications. The first one is the use of *intra-normalisation* of the descriptor blocks, an idea recently proposed for the VLAD descriptor [2]. In this case, the  $\ell^2$  normalisation is applied to the individual sub-blocks  $(\mathbf{u}_k, \mathbf{v}_k)$  of the vector  $\phi_{\text{FV}}(I)$ , which helps to alleviate the local feature burstiness [14]. In the case of the improved intra-normalised features, it was found that applying the square-rooting only once to the final encoding produced the best results.

The second modification is the use of *spatially-extended local descriptors* [26] instead of a spatial pyramid. Here descriptors  $\mathbf{x}_i$  are appended with their image location  $(x_i, y_i)$  before quantization with the GMM. Formally,  $\mathbf{x}_i$  is extended, after PCA projection, with its normalised spatial coordinates:  $[\mathbf{x}_i^\top, x_i/W - 0.5, y_i/H - 0.5]^\top$ , where  $W \times H$  are the dimensions of the image. Since the GMM quantizes both appearance and location, this allows for spatial information to be captured directly by the soft-quantization process. This method is significantly more memory-efficient than using a spatial pyramid. Specifically, the PCA-reduced SIFT features are spatially augmented by appending (x,y) yielding D=82 dimensional descriptors pooled in a 2KD=41,984 dimensional IFV.

The third modification is the use of colour features in addition to SIFT descriptors. While colour information is used in CNNs [17] and by the original FV paper [23], it was not explored in our previous comparison [3]. We do so here by adopting the same Local Colour Statistics (LCS) features as used by [23]. LCS is computed by dividing an input patch into a  $4 \times 4$  spatial grid (akin to SIFT), and computing the mean and variance of each of the *Lab* colour channels for each cell of the grid. The LCS dimensionality is thus  $4 \times 4 \times 2 \times 3 = 96$ . This is then encoded in a similar manner to SIFT.

#### 3.2 Convolutional neural networks details

The CNN-based features are based on three CNN architectures representative of the state of the art (shown in Table 1) each exploring a different accuracy/speed trade-off. To ensure a fair comparison between them, these networks are trained using the same training protocol

Arch.	conv1	conv2	conv3	conv4	conv5	full6	full7	full8
	64x11x11	256x5x5	256x3x3	256x3x3	256x3x3	4096	4096	1000
CNN-F	st. 4, pad 0	st. 1, pad 2	st. 1, pad 1	st. 1, pad 1	st. 1, pad 1	drop-	drop-	soft-
	LRN, x2 pool	LRN, x2 pool	-	-	x2 pool	out	out	max
	96x7x7	256x5x5	512x3x3	512x3x3	512x3x3	4096	4096	1000
CNN-M	st. 2, pad 0	st. 2, pad 1	st. 1, pad 1	st. 1, pad 1	st. 1, pad 1	drop-	drop-	soft-
	LRN, x2 pool	LRN, x2 pool	-	-	x2 pool	out	out	max
	96x7x7	256x5x5	512x3x3	512x3x3	512x3x3	4096	4096	1000
CNN-S	st. 2, pad 0	st. 1, pad 1	drop-	drop-	soft-			
	LRN, x3 pool	x2 pool	-	-	x3 pool	out	out	max

Table 1: **CNN architectures.** Each architecture contains 5 convolutional layers (conv 1–5) and three fully-connected layers (full 1–3). The details of each of the convolutional layers are given in three sub-rows: the first specifies the number of convolution filters and their receptive field size as "num x size x size"; the second indicates the convolution stride ("st.") and spatial padding ("pad"); the third indicates if Local Response Normalisation (LRN) [17] is applied, and the max-pooling downsampling factor. For full 1–3, we specify their dimensionality, which is the same for all three architectures. Full6 and full7 are regularised using dropout [17], while the last layer acts as a multi-way soft-max classifier. The activation function for all weight layers (except for full8) is the REctification Linear Unit (RELU) [17].

and the same implementation, which we developed based on the open-source Caffe framework [16].  $\ell^2$ -normalising the CNN features  $\phi_{\text{CNN}}(I)$  before use in the SVM was found to be important for performance.

Our **Fast** (CNN-F) architecture is similar to the one used by Krizhevsky *et al.* [17]. It comprises 8 learnable layers, 5 of which are convolutional, and the last 3 are fully-connected. The input image size is  $224 \times 224$ . Fast processing is ensured by the 4 pixel stride in the first convolutional layer. The main differences between our architecture and that of [17] are the reduced number of convolutional layers and the dense connectivity between convolutional layers ([17] used sparse connections to enable training on two GPUs).

Our **Medium** (CNN-M) architecture is similar to the one used by Zeiler and Fergus [32]. It is characterised by the decreased stride and smaller receptive field of the first convolutional layer, which was shown to be beneficial on the ILSVRC dataset. At the same time, conv2 uses larger stride (2 instead of 1) to keep the computation time reasonable. The main difference between our net and that of [32] is we use less filters in the conv4 layer (512 vs. 1024).

Our **Slow** (**CNN-S**) architecture is related to the 'accurate' network from the OverFeat package [27]. It also uses  $7 \times 7$  filters with stride 2 in conv1. Unlike CNN-M and [32], the stride in conv2 is smaller (1 pixel), but the max-pooling window in conv1 and conv5 is larger (3 × 3) to compensate for the increased spatial resolution. Compared to [27], we use 5 convolutional layers as in the previous architectures ([27] used 6), and less filters in conv5 (512 instead of 1024); we also incorporate an LRN layer after conv1 ([27] did not use contrast normalisation).

**CNN training.** In general, our CNN training procedure follows that of [17], learning on ILSVRC-2012 using gradient descent with momentum. The hyper-parameters are the same as used by [17]: momentum 0.9; weight decay  $5 \cdot 10^{-4}$ ; initial learning rate  $10^{-2}$ , which is decreased by a factor of 10, when the validation error stop decreasing. The layers are initialised from a Gaussian distribution with a zero mean and variance equal to  $10^{-2}$ . We also employ similar data augmentation in the form of random crops, horizontal flips, and RGB colour jittering. Test time crop sampling is discussed in Sect. 3.3; at training time,  $224 \times 224$  crops are sampled randomly, rather than deterministically. Thus, the only notable difference to [17] is that the crops are taken from the whole training image  $P \times 256$ ,  $P \ge 256$ ,

rather than its  $256 \times 256$  centre. Training was performed on a single NVIDIA GTX Titan GPU and the training time varied from 5 days for CNN-F to 3 weeks for CNN-S.

CNN fine-tuning on the target dataset. In our experiments, we fine-tuned CNN-S using VOC-2007, VOC-2012, or Caltech-101 as the target data. Fine-tuning was carried out using the same framework (and the same data augmentation), as we used for CNN training on ILSVRC. The last fully-connected layer (conv8) has output dimensionality equal to the number of classes, which differs between datasets, so we initialised it from a Gaussian distribution (as used for CNN training above). Now we turn to dataset-specific fine-tuning details. **VOC-2007** and **VOC-2012.** Considering that PASCAL VOC is a multi-label dataset (i.e. a single image might have multiple labels), we replaced the softmax regression loss with a more appropriate loss function, for which we considered two options: one-vs-rest classification hinge loss (the same loss as used in the SVM experiments) and ranking hinge loss. Both losses define constraints on the scores of positive  $(I_{pos})$  and negative  $(I_{neg})$  images for each class:  $w_c \phi(I_{pos}) > 1 - \xi, w_c \phi(I_{neg}) < -1 + \xi$  for the classification loss,  $w_c \phi(I_{pos}) >$  $w_c \phi(I_{neg}) + 1 - \xi$  for the ranking loss ( $w_c$  is the c-th row of the last fully-connected layer, which can be seen as a linear classifier on deep features  $\phi(I)$ ;  $\xi$  is a slack variable). Our fine-tuned networks are denoted as "CNN S TUNE-CLS" (for the classification loss) and "CNN S TUNE-RNK" (for the ranking loss). In the case of both VOC datasets, the training and validation subsets were combined to form a single training set. Given the smaller size of the training data when compared to ILSVRC-2012, we controlled for over-fitting by using lower initial learning rates for the fine-tuned hidden layers. The learning rate schedule for the last layer / hidden layers was:  $10^{-2}/10^{-4} \rightarrow 10^{-3}/10^{-4} \rightarrow 10^{-4}/10^{-4} \rightarrow 10^{-5}/10^{-5}$ . Caltech-101 dataset contains a single class label per image, so fine-tuning was performed using the softmax regression loss. Other settings (including the learning rate schedule) were the same as used for the VOC fine-tuning experiments.

**Low-dimensional CNN feature training.** Our baseline networks (Table 1) have the same dimensionality of the last hidden layer (full7): 4096. This design choice is in accordance with the state-of-the-art architectures [17, 27, 32], and leads to a 4096-D dimensional image representation, which is already rather compact compared to IFV. We further trained three modifications of the CNN-M network, with lower dimensional full7 layers of: 2048, 1024, and 128 dimensions respectively. The networks were learnt on ILSVRC-2012. To speed-up training, all layers aside from full7/full8 were set to those of the CNN-M net and a lower initial learning rate of  $10^{-3}$  was used. The initial learning rate of full7/full8 was set to  $10^{-2}$ .

## 3.3 Data augmentation details

We explore three data augmentation strategies. The first strategy is to use **no augmentation**. In contrast to IFV, however, CNNs require images to be transformed to a fixed size ( $224 \times 224$ ) even when no augmentation is used. Hence the image is downsized so that the smallest dimension is equal to 224 pixels and a  $224 \times 224$  crop is extracted from the centre.<sup>2</sup> The second strategy is to use **flip augmentation**, mirroring images about the y-axis producing two samples from each image. The third strategy, termed **C+F augmentation**, combines cropping and flipping. For CNN-based representations, the image is downsized so that the smallest dimension is equal to 256 pixels. Then  $224 \times 224$  crops are extracted from the four corners and the centre of the image. Note that the crops are sampled from the whole image, rather than its  $256 \times 256$  centre, as done by [17]. These crops are then flipped about the y-axis, producing 10 perturbed samples per input image. In the case of the IFV encoding,

 $<sup>^2</sup>$ Extracting a 224 × 224 centre crop from a 256 × 256 image [17] resulted in worse performance.

Method (I) FK BL (II) DECAF	spm –	(C) t t	Dim 327K 327K		79.0 87.4	67.4 79.3	51.9 84.1	70.9 78.4	30.8 42.3	72.2 73.7
(a) FK (b) FK IN	spm spm	_	327K 327K	63.66 64.18	83.4 82.1	68.8 69.7	59.6 59.7	74.1 75.2	35.7 35.7	71.2 71.3
(c) FK (d) FK IN (e) FK IN (f) FK IN (g) FK IN (h) FK IN 512 (i) FK IN 512 (j) FK IN COL 512 (k) FK IN 512 COL+ (l) FK IN 512 COL+	(x,y) (x,y) (x,y) (x,y) (x,y) (x,y) (x,y) - (x,y) (x,y)	- (F) f - (C) f s (C) s s - (C) f s - (C) f s	42K 42K 42K 42K 42K 84K 84K 82K 166K 166K	63.51 64.36 64.35 67.17 66.68 65.36 68.02 52.18 66.37 67.93	83.2 83.1 83.1 85.5 84.9 84.1 85.9 69.5 82.9 85.1	69.4 70.4 70.5 71.6 70.1 70.4 71.8 52.1 70.1 70.5	60.6 62.4 62.3 64.6 64.7 65.0 67.1 47.5 67.0	73.9 75.2 75.4 77.2 76.3 76.7 77.1 64.0 77.0 77.4	36.3 37.1 37.1 39.0 39.2 37.2 38.8 24.6 36.1 35.7	68.6 69.1 69.1 70.8 69.8 71.3 72.3 49.8 70.0 71.2
(m) CNN F (n) CNN S	- -	(C) f s (C) f s	4K 4K	77.38 79.74	88.7 90.7	83.9 85.7	87.0 88.9	84.7 86.6	46.9 50.5	77.5 80.1
(o) CNN M (p) CNN M (q) CNN M (r) CNN M (s) CNN M (t) CNN M (u) CNN M (v) CNN M GS (w) CNN M GS	- - - - - - -	(C) f s (C) f m (C) s s (C) t t (C) f - (F) f - (C) f s	4K 4K 4K 4K 41K 4K 4K 4K 4K	76.97 79.89 79.50 79.44 78.77 77.78 76.99 73.59 77.00	89.5 91.7 90.9 91.4 90.7 90.5 90.1 87.4 89.4	84.3 85.4 84.6 85.2 85.0 84.3 84.2 80.8 83.8	88.8 89.5 89.4 89.1 89.2 88.8 89.0 82.4 85.1	83.2 86.6 85.8 86.1 85.8 84.5 83.5 82.1 84.4	48.4 51.6 50.3 52.1 51.0 47.9 48.1 44.5 49.4	77.0 79.3 78.4 78.0 77.8 78.0 77.2 73.5 77.6
(x) CNN M 2048 (y) CNN M 1024 (z) CNN M 128	_ _ _	(C) f s (C) f s (C) f s	2K 1K 128	80.10 79.91 78.60	91.3 91.4 91.3	85.8 86.9 83.9	89.9 89.3 89.2	86.7 85.8 86.9	52.4 53.3 52.1	79.7 79.8 81.0
(α) FK+CNN F (β) FK+CNN M 2048 (γ) CNN S TUNE-RNK	(x,y) (x,y)	(C) f s (C) f s (C) f s	88K 86K 4K	77.95 80.14 82.42		83.1 85.9 90.4	87.1 88.8 92.5	84.5 85.5 89.6	48.0 52.3 54.4	79.4 81.4 81.9

Table 2: VOC 2007 results (continued overleaf). See Sect. 4 for details.

the same crops are extracted, but at the original image resolution.

## 4 Analysis

This section describes the experimental results, comparing different features and data augmentation schemes. The results are given in Table 2 for VOC-2007 and analysed next, starting from generally applicable methods such as augmentation and then discussing the specifics of each scenario. We then move onto other datasets and the state of the art in Sect. 4. **Data augmentation.** We experiment with no data augmentation (denoted  $Image\ Aug=-$  in Tab. 2), flip augmentation ( $Image\ Aug=F$ ), and C+F augmentation ( $Image\ Aug=C$ ). Augmented images are used as stand-alone samples (f), or by fusing the corresponding descriptors using sum (s) or max (m) pooling or stacking (t). So for example  $Image\ Aug=(C)\ f\ s$  in row [f] of Tab. 2 means that C+F augmentation is used to generate additional samples in training (f), and is combined with sum-pooling in testing (s).

Augmentation consistently improves performance by  $\sim 3\%$  for both IFV (e.g. [d] vs. [f]) and CNN (e.g. [o] vs. [p]). Using additional samples for training and sum-pooling for testing works best ([p]) followed by sum-pooling [r], max pooling [q], and stacking [s]. In terms of the choice of transformations, flipping improves only marginally ([o] vs. [u]), but using the more expensive C+F sampling improves, as seen, by about  $2 \sim 3\%$  ([o] vs. [p]). We experimented with sampling more transformations, taking a higher density of crops from the

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(e) 80.5 66.8 51.0 54.1 62.2 51.5 80.4 68.2 86.0 37.3 55.1 54.2 83.3 59.2 (f) 82.4 71.6 52.8 62.4 63.4 57.1 81.6 70.9 86.9 41.2 61.2 56.9 85.2 61.5 (g) 81.9 71.0 52.8 61.6 62.2 56.8 81.8 70.0 86.5 41.5 61.0 56.5 84.3 60.9 (h) 81.1 67.9 52.6 55.4 61.4 51.2 80.5 69.1 86.4 41.2 56.0 56.2 83.7 59.9 (i) 82.5 73.2 54.7 62.7 64.5 56.6 82.2 71.3 87.5 43.0 62.0 59.3 85.7 62.4 (j) 66.1 46.6 42.5 35.8 41.1 45.5 75.4 58.3 83.9 39.8 47.3 35.6 69.2 49.0 (k) 80.0 65.9 52.8 56.1 61.0 56.9 81.4 69.6 88.4 49.0 59.2 56.4 84.7 62.8 (l) 81.6 70.8 52.9 59.6 63.1 59.9 82.1 70.5 88.9 50.6 63.7 57.5 86.1 64.1 (m) 87.8 88.3 61.3 74.8 74.7 87.2 89.0 83.7 92.3 58.8 80.5 69.4 90.5 74.0 (o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.0 58.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (v) 87.8 88.6 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (2) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (c) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.5 (d) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.5 (d) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	` /														
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(i) 66.1 46.6 42.5 35.8 41.1 45.5 75.4 58.3 83.9 39.8 47.3 35.6 69.2 49.0 (k) 80.0 65.9 52.8 56.1 61.0 56.9 81.4 69.6 88.4 49.0 59.2 56.4 84.7 62.8 (l) 81.6 70.8 52.9 59.6 63.1 59.9 82.1 70.5 88.9 50.6 63.7 57.5 86.1 64.1 (m) 86.3 85.4 58.6 71.0 72.6 82.0 87.9 80.7 91.8 58.5 77.4 66.3 89.1 71.3 (n) 87.8 88.3 61.3 74.8 74.7 87.2 89.0 83.7 92.3 58.8 80.5 69.4 90.5 74.0 (o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (2) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	. ,														
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(I) 81.6 70.8 52.9 59.6 63.1 59.9 82.1 70.5 88.9 50.6 63.7 57.5 86.1 64.1 (m) 86.3 85.4 58.6 71.0 72.6 82.0 87.9 80.7 91.8 58.5 77.4 66.3 89.1 71.3 (n) 87.8 88.3 61.3 74.8 74.7 87.2 89.0 83.7 92.3 58.8 80.5 69.4 90.5 74.0 (o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(j)														
(m) 86.3 85.4 58.6 71.0 72.6 82.0 87.9 80.7 91.8 58.5 77.4 66.3 89.1 71.3 (n) 87.8 88.3 61.3 74.8 74.7 87.2 89.0 83.7 92.3 58.8 80.5 69.4 90.5 74.0 (o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(k)														
(n) 87.8 88.3 61.3 74.8 74.7 87.2 89.0 83.7 92.3 58.8 80.5 69.4 90.5 74.0 (o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(l)	81.6	70.8	52.9	59.6	63.1	59.9	82.1	70.5	88.9	50.6	63.7	57.5	86.1	64.1
(o) 85.1 87.4 58.1 70.4 73.1 83.5 85.5 80.9 90.8 54.1 78.9 61.1 89.0 70.4 (p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(m)	86.3	85.4	58.6	71.0	72.6	82.0	87.9	80.7	91.8	58.5	77.4	66.3	89.1	71.3
(p) 87.7 88.6 60.3 80.1 74.4 85.9 88.2 84.6 92.1 60.3 80.5 66.2 91.3 73.5 (q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(n)	87.8	88.3	61.3	74.8	74.7	87.2	89.0	83.7	92.3	58.8	80.5	69.4	90.5	74.0
(q) 87.6 88.6 60.7 78.2 73.6 86.0 87.4 83.8 92.3 59.3 81.0 66.8 91.3 74.0 (r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(o)														
(r) 87.5 88.1 60.4 76.9 74.8 85.8 88.1 84.3 92.2 59.5 79.3 65.8 90.8 73.5 (s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(p)														
(s) 87.3 87.6 60.1 72.3 75.3 85.2 86.9 82.6 91.9 58.5 77.9 66.5 90.5 73.4 (t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(q)														
(t) 85.7 87.9 58.3 74.2 73.9 84.7 86.6 82.0 91.0 55.8 79.2 62.1 89.3 71.0 (u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(r)														
(u) 85.3 87.3 58.1 70.0 73.4 83.5 86.0 80.8 90.9 53.9 78.1 61.2 88.8 70.6 (v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	. ,														
(v) 85.0 84.9 57.8 65.9 69.8 79.5 82.9 77.4 89.2 42.8 71.7 60.2 86.3 67.8 (w) 87.2 86.5 59.5 72.4 74.1 81.7 86.0 82.3 90.8 48.9 73.7 66.8 89.6 71.0 (x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(t)														
(w)   87.2   86.5   59.5   72.4   74.1   81.7   86.0   82.3   90.8   48.9   73.7   66.8   89.6   71.0     (x)   87.6   88.4   60.2   76.9   75.4   85.5   88.0   83.4   92.1   61.1   83.1   68.5   91.9   74.2     (y)   87.8   88.6   59.0   77.2   73.1   85.9   88.3   83.5   91.8   59.9   81.4   68.3   93.0   74.1     (z)   86.6   87.5   59.1   70.0   72.9   84.6   86.7   83.6   89.4   57.0   81.5   64.8   90.4   73.4     (α)   86.8   85.6   59.9   72.0   73.4   81.4   88.6   80.5   92.1   60.6   77.3   66.4   89.3   73.3     (β)   87.7   88.4   61.2   76.9   76.6   84.9   89.1   82.9   92.4   61.9   80.9   68.7   91.5   75.1	(u)														
(x) 87.6 88.4 60.2 76.9 75.4 85.5 88.0 83.4 92.1 61.1 83.1 68.5 91.9 74.2 (y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(v)														
(y) 87.8 88.6 59.0 77.2 73.1 85.9 88.3 83.5 91.8 59.9 81.4 68.3 93.0 74.1 (z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4 (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(w)	87.2	86.5	59.5	72.4	74.1	81.7	86.0	82.3	90.8	48.9	73.7	66.8	89.6	71.0
(z) 86.6 87.5 59.1 70.0 72.9 84.6 86.7 83.6 89.4 57.0 81.5 64.8 90.4 73.4   (α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3   (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(x)	87.6	88.4	60.2	76.9	75.4	85.5	88.0	83.4	92.1	61.1	83.1	68.5	91.9	74.2
(α) 86.8 85.6 59.9 72.0 73.4 81.4 88.6 80.5 92.1 60.6 77.3 66.4 89.3 73.3 (β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(y)	87.8	88.6	59.0	77.2	73.1	85.9	88.3	83.5	91.8	59.9	81.4	68.3	93.0	74.1
(β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(z)	86.6	87.5	59.1	70.0	72.9	84.6	86.7	83.6	89.4	57.0	81.5	64.8	90.4	73.4
(β) 87.7 88.4 61.2 76.9 76.6 84.9 89.1 82.9 92.4 61.9 80.9 68.7 91.5 75.1	(a)	86.8	85.6	59.9	72.0	73.4	81.4	88.6	80.5	92.1	60.6	77.3	66.4	89.3	73.3
(Y) 91.5 91.9 64.1 76.3 74.9 89.7 92.2 86.9 95.2 60.7 82.9 68.0 95.5 74.4		87.7	88.4	61.2	76.9	76.6	84.9	89.1	82.9	92.4	61.9	80.9	68.7	91.5	75.1
	(γ)	91.5	91.9	64.1	76.3	74.9	89.7	92.2	86.9	95.2	60.7	82.9	68.0	95.5	74.4

Table 2: VOC 2007 results (continued from previous page)

centre of the image, but observed no benefit.

**Colour.** Colour information can be added and subtracted in CNN and IFV. In IFV replacing SIFT with the colour descriptors of [23] (denoted COL in Method) yields significantly worse performance ([j] vs. [h]). However, when SIFT and colour descriptors are combined by stacking the corresponding IFVs (COL+) there is a small but significant improvement of around  $\sim 1\%$  in the non-augmented case (e.g. [h] vs. [k]) but little impact in the augmented case (e.g. [i] vs. [l]). For CNNs, retraining the network after converting all the input images to grayscale (denoted GS in Methods) has a more significant impact, resulting in a performance drop of  $\sim 3\%$  ([w] vs. [p], [v] vs. [o]).

Scenario 1: Shallow representation (IFV). The baseline IFV encoding using a spatial pyramid [a] performs slightly better than the results [I] taken from Chatfield *et al.* [3], primarily due to a larger number of spatial scales being used during SIFT feature extraction, and the resultant SIFT features being square-rooted. *Intra-normalisation*, denoted as *IN* in the *Method* column of the table, improves the performance by  $\sim 1\%$  (*e.g.* [c] *vs.* [d]). More interestingly, switching from spatial pooling (denoted *spm* in the *SPool* column) to feature spatial augmentation (SPool=(x,y)) has either little effect on the performance or results in a marginal increase ([a] *vs.* [c], [b] *vs.* [d]), whilst resulting in a representation which is over  $10\times$  smaller. We also experimented with augmenting with scale in addition to position as

(a) FK IN 512	ILSVRC-2012 (top-5 error)	VOC-2007 (mAP) 68.0	VOC-2012 (mAP)	Caltech-101 (accuracy)	Caltech-256 (accuracy)
(b) CNN F	16.7	77.4	79.9	_	_
(c) CNN M	13.7	79.9	82.5	$87.15 \pm 0.80$	$77.03 \pm 0.46$
(d) CNN M 2048	13.5	80.1	82.4	$86.64 \pm 0.53$	$76.88 \pm 0.35$
(e) CNN S	13.1	79.7	82.9	$87.76 \pm 0.66$	$77.61 \pm 0.12$
(f) CNN S TUNE-CLS	13.1	-	83.0	$\textbf{88.35} \pm \textbf{0.56}$	$77.33 \pm 0.56$
(g) CNN S TUNE-RNK	13.1	82.4	83.2	_	
(h) Zeiler & Fergus [32]	16.1	-	79.0	$86.5 \pm 0.5$	$74.2 \pm 0.3$
(i) Razavian <i>et al</i> . [25, 27]	14.7	77.2	_	_	_
(j) Oquab <i>et al</i> . [20]	18	77.7	78.7 (82.8 <sup>*</sup> )	_	_
(k) Oquab <i>et al</i> . [21]	-	-	86.3*	_	_
(l) Wei <i>et al</i> . [30]	-	81.5 ( <b>85.2</b> *)	81.7 ( <b>90.3</b> *)	_	_
(m) He <i>et al</i> . [13]	13.6	80.1	-	$\textbf{91.4} \pm \textbf{0.7}$	_

Table 3: **Comparison with the state of the art** on ILSVRC2012, VOC2007, VOC2012, Caltech-101, and Caltech-256. Results marked with \* were achieved using models pretrained on the *extended* ILSVRC datasets (1512 classes in [20, 21], 2000 classes in [30]). All other results were achieved using CNNs pre-trained on ILSVRC-2012 (1000 classes).

in [26] but observed no improvement. Finally, we investigate pushing the parameters of the representation setting K = 512 (rows [h]-[l]). Increasing the number of GMM centres in the model from K = 256 to 512 results in a further performance increase (e.g. [h] vs. [d]), but at the expense of higher-dimensional codes (125K dimensional).

Scenario 2: Deep representation (CNN) with pre-training. CNN-based methods consistently outperform the shallow encodings, even after the improvements discussed above, by a large  $\sim 10\%$  mAP margin ([i] vs. [p]). Our small architecture CNN-F, which is similar to DeCAF [8], performs significantly better than the latter ([II] vs. [s]), validating our implementation. Both medium CNN-M [m] and slow CNN-S [p] outperform the fast CNN-F [m] by a significant  $2 \sim 3\%$  margin. Since the accuracy of CNN-S and CNN-M is nearly the same, we focus on the latter as it is simpler and marginally ( $\sim 25\%$ ) faster. Remarkably, these good networks work very well even with no augmentation [o]. Another advantage of CNNs compared to IFV is the small dimensionality of the output features, although IFV can be compressed to an extent. We explored retraining the CNNs such that the final layer was of a lower dimensionality, and reducing from 4096 to 2048 actually resulted in a marginal performance boost ([x] vs. [p]). What is surprising is that we can reduce the output dimensionality further to 1024D [v] and even 128D [z] with only a drop of  $\sim 2\%$  for codes that are  $32\times$  smaller ( $\sim 650\times$  smaller than our best performing IFV [i]). Note,  $\ell^2$ -normalising the features accounted for up to  $\sim 5\%$  of their performance over VOC 2007; it should be applied before input to the SVM and after pooling the augmented descriptors (where applicable).

Scenario 3: Deep representation (CNN) with pre-training and fine-tuning. We fine-tuned our CNN-S architecture on VOC-2007 using the ranking hinge loss, and achieved a significant improvement: 2.7% ([ $\gamma$ ] vs. [n]). This demonstrates that in spite of the small amount of VOC training data (5,011 images), fine-tuning is able to adjust the learnt deep representation to better suit the dataset in question.

**Combinations.** For the CNN-M 2048 representation [x], stacking deep and shallow representations to form a higher-dimensional descriptor makes little difference ([x] vs. [ $\beta$ ]). For the weaker CNN-F it results in a small boost of  $\sim 0.8\%$  ([m] vs. [ $\alpha$ ]).

Comparison with the state of the art. In Table 3 we report our results on ILSVRC-2012, VOC-2007, VOC-2012, Caltech-101, and Caltech-256 datasets, and compare them to the

state of the art. First, we note that the ILSVRC error rates of our CNN-F, CNN-M, and CNN-S networks are better than those reported by [17], [32], and [27] for the related configurations. This validates our implementation, and the difference is likely to be due to the sampling of image crops from the uncropped image plane (instead of the centre). When using our CNN features on other datasets, the relative performance generally follows the same pattern as on ILSVRC, where the nets are trained – the CNN-F architecture exhibits the worst performance, with CNN-M and CNN-S performing considerably better.

Further fine-tuning of CNN-S on the VOC datasets turns out to be beneficial; on VOC-2012, using the ranking loss is marginally better than the classification loss ([g] vs. [f]), which can be explained by the ranking-based VOC evaluation criterion. Fine-tuning on Caltech-101 also yields a small improvement, but no gain is observed over Caltech-256.

Our CNN-S net is competitive with recent CNN-based approaches [13, 20, 21, 25, 30, 32] and on a number of datasets (VOC-2007, VOC-2012, Caltech-101, Caltech-256) and sets the state of the art on VOC-2007 and VOC-2012 across methods pre-trained solely on ILSVRC-2012 dataset. While the CNN-based methods of [21, 30] achieve better performance on VOC (86.3% and 90.3% respectively), they were trained using extended ILSVRC datasets, enriched with additional categories semantically close to the ones in VOC. Additionally, [30] used a significantly more complex classification pipeline, driven by bounding box proposals [5], pre-trained on ILSVRC-2013 detection dataset. Their best reported result on VOC-2012 (90.3%) was achieved by the late fusion with a complex hand-crafted method of [31]; without fusion, they get 84.2%. On Caltech-101, [13] achieves the state of the art using spatial pyramid pooling of conv5 layer features, while we used full7 layer features consistently across all datasets (for full7 features, they report 87.08%).

In addition to achieving performance comparable to the state of the art with a very simple approach (but powerful CNN-based features), with the modifications outlined in the paper (primarily the use of data augmentation similar to the CNN-based methods) we are able to improve the performance of shallow IFV to 68.02% (Table 2, [i]).

**Timings and dimensionality.** One of our best-performing CNN representations CNN-M-2048 [x] is  $\sim$  42× more compact than the best performing IFV [i] (84K vs. 2K) and CNN-M features are also  $\sim$  50× faster to compute ( $\sim$  120s vs.  $\sim$  2.4s per image with augmentation enabled, over a single CPU core). Non-augmented CNN-M features [o] take around 0.3s per image, compared to  $\sim$  0.4s for CNN-S features and  $\sim$  0.13s for CNN-F features.

## 5 Conclusion

In this paper we presented a rigorous empirical evaluation of CNN-based methods for image classification, along with a comparison with more traditional shallow feature encoding methods. We have demonstrated that the performance of shallow representations can be significantly improved by adopting data augmentation, typically used in deep learning. In spite of this improvement, deep architectures still outperform the shallow methods by a large margin. We have shown that the performance of deep representations on the ILSVRC dataset is a good indicator of their performance on other datasets, and that fine-tuning can further improve on already very strong results achieved using the combination of deep representations and a linear SVM. Source code and CNN models to reproduce the experiments presented in the paper are available on the project website [4] in the hope that it would provide common ground for future comparisons, and good baselines for image representation research.

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