

Untitled

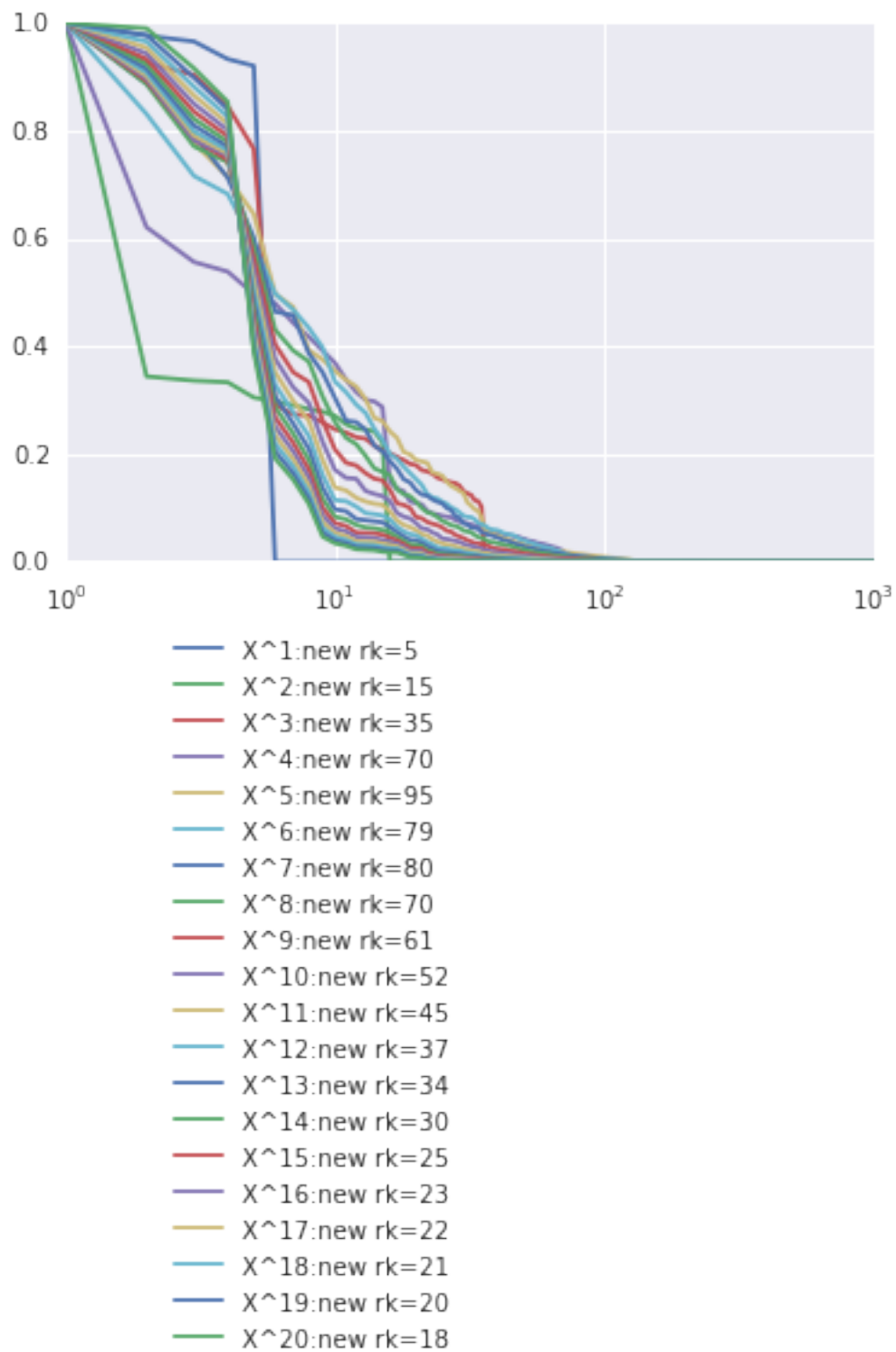
October 2, 2015

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline

In [3]: n=1000
rk=5
U=np.random.randn(n,rk)
V=np.random.randn(n,rk)
X=U.dot(V.T)

for i in range(1,21):
    Xp=X**i
    Sp=np.linalg.svd(Xp)[1]
    s=Sp/np.max(Sp)
    r=np.nonzero(s<=1e-2)[0][0]
    plt.plot(np.arange(1,len(s)+1),s,label=('X^%d:new rk=%r' %(i,r)))
plt.xscale('log')
plt.legend(loc='upper right', bbox_to_anchor=(0.5,-0.1))

Out[3]: <matplotlib.legend.Legend at 0x7f4a75b519d0>
```



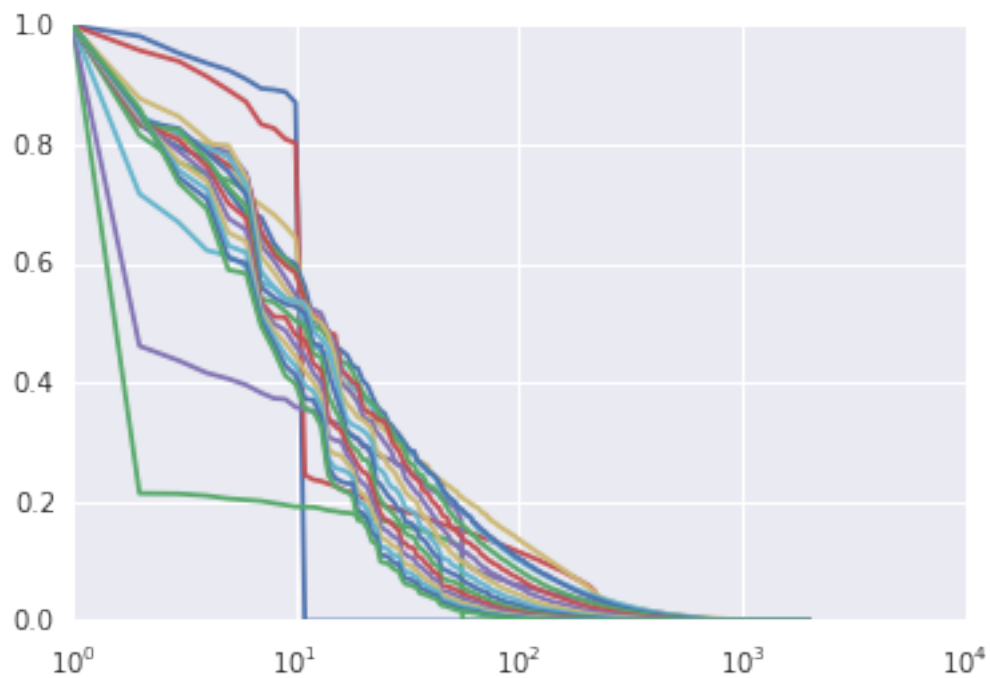
```
In [7]: n=2000
        rk=10
        U=np.random.randn(n,rk)
```

```

V=np.random.randn(n,rk)
X=U.dot(V.T)
#Xp=0
#plt.rc('text', usetex=True)
for i in range(1,21):
    Xp=X**i
    Sp=np.linalg.svd(Xp)[1]
    s=Sp/np.max(Sp)
    r=np.nonzero(s<=1e-2)[0][0]
    plt.plot(np.arange(1,len(s)+1),s,label=('X^%d:new rk=%i' %(i,r)))
plt.xscale('log')
plt.legend(loc='upper right', bbox_to_anchor=(0.5,-0.1))

```

Out[7]: <matplotlib.legend.Legend at 0x7f4a75cc6990>



- X^1 :new rk=10
- X^2 :new rk=55
- X^3 :new rk=220
- X^4 :new rk=493
- X^5 :new rk=498
- X^6 :new rk=483
- X^7 :new rk=429
- X^8 :new rk=375
- X^9 :new rk=319
- X^{10} :new rk=271
- X^{11} :new rk=227
- X^{12} :new rk=190
- X^{13} :new rk=163
- X^{14} :new rk=139
- X^{15} :new rk=117
- X^{16} :new rk=104
- X^{17} :new rk=93
- X^{18} :new rk=82
- X^{19} :new rk=76
- X^{20} :new rk=68