HeartAttack Prediction

Ajanthan

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Heart Attack Analysis and Predictive Analysis

Introduction

Heart disease is the leading cause of death for men, women, and people of most racial and ethnic groups. One person dies every 36 seconds in the United States from cardiovascular disease. About 655,000 Americans die from heart disease each year—that's 1 in every 4 deaths. The goal of this project is to find out which factors influences the chances of getting a heart attack. I will be using Heart Attack Analysis & Prediction Dataset, which is a dataset for heart attack classification from kaggle. In addition i'll be using the following classification technique Decision Tree, to provide further analysis of which factors influence heart attacks.

Description of Dataset

Age: Age of the patient

Sex : Sex of the patient

ex
ng: exercise induced angina (1 = yes; 0 = no)

caa: number of major vessels (0-3)

cp: Chest Pain type chest pain type

Value 1: typical angina Value 2: atypical angina Value 3: non-anginal pain Value 4: asymptomatic

trtbps: resting blood pressure (in mm Hg)

chol: cholestoral in mg/dl fetched via BMI sensor

fbs: (fasting blood sugar > 120 mg/dl) (1 = true; 0 = false)

rest_ecg : resting electrocardiographic results Value 0: normal Value 1: having ST-T wave abnormality (T wave inversions and/or ST elevation or depression of > 0.05 mV) Value 2: showing probable or definite left ventricular hypertrophy by Estes' criteria

thalach: maximum heart rate achieved

oldpeak: ST depression induced by exercise relative to rest

slp: the slope of the peak exercise ST segment (0 = upsloping; 1 = flat; 2 = downsloping)

thall: 1 = normal; 2 = fixed defect; 3 = reversable defect

target: 0= less chance of heart attack 1= more chance of heart attack

Here is a sample of the first 5 rows of the data

```
age sex cp trtbps chol fbs restecg thalachh exng oldpeak slp caa thall output
##
## 1
             1
                             233
                                                                                  0
       63
                3
                       145
                                    1
                                              0
                                                      150
                                                               0
                                                                      2.3
                                                                             0
                                                                                          1
                                                                                          2
##
   2
       37
             1
                2
                       130
                             250
                                    0
                                              1
                                                      187
                                                               0
                                                                      3.5
                                                                             0
                                                                                  0
                                                                                                  1
                                                                             2
                                                                                  0
                                                                                         2
                                                                                                  1
##
   3
       41
             0
                1
                       130
                             204
                                    0
                                              0
                                                      172
                                                               0
                                                                      1.4
##
   4
       56
             1
                1
                       120
                             236
                                    0
                                              1
                                                      178
                                                               0
                                                                      0.8
                                                                             2
                                                                                  0
                                                                                          2
                                                                                                  1
             0
                                                                      0.6
                                                                             2
                                                                                  0
                                                                                          2
                                                                                                  1
## 5
       57
                0
                       120
                             354
                                    0
                                              1
                                                      163
                                                               1
```

Here is the data types of the data set

```
'data.frame':
                     303 obs. of
                                  14 variables:
    $ age
                      63 37 41 56 57 57 56 44 52 57 ...
##
               : int
##
    $
     sex
                int
                      1 1 0 1 0 1 0 1 1 1 ...
##
    $ ср
                      3 2 1 1 0 0 1 1 2 2 ...
                int
##
      trtbps
                 int
                      145 130 130 120 120 140 140 120 172 150 ...
##
    $ chol
                int
                      233 250 204 236 354 192 294 263 199 168 ...
##
    $ fbs
                      1 0 0 0 0 0 0 0 1 0 ...
               : int
##
    $ restecg : int
                      0 1 0 1 1 1 0 1 1 1 ...
##
    $ thalachh: int
                      150 187 172 178 163 148 153 173 162 174 ...
##
    $ exng
                      0 0 0 0 1 0 0 0 0 0 ...
               : int
##
    $ oldpeak : num
                      2.3 3.5 1.4 0.8 0.6 0.4 1.3 0 0.5 1.6 ...
                      0 0 2 2 2 1 1 2 2 2 ...
##
    $ slp
                int
                      0 0 0 0 0 0 0 0 0 0 ...
##
    $ caa
                int
                      1 2 2 2 2 1 2 3 3 2 ...
##
    $ thall
                int
    $ output
              : int
                      1 1 1 1 1 1 1 1 1 1 ...
```

According to our dataset target which is output is our independant variable. We will use logistic regression since we are dealing with a categorical variable. We will also build two models one model which is a additative model and another model which includes interactions. We will evaluate both models performance and choose the best fitting model for further analysis.

Cleaning The Dataset

Based on the data set we have qualititave dependent variables and a qualitative independent variable so lets factor the qualitative variables and relable them so they have meaningful names in the dataset to make it easier reading the data when analyzing the data.

```
##
                                               fbs
                                                                  restecg thalachh
     age sex
                            cp trtbps chol
## 1
      63
           М
                  asymptomatic
                                        233
                                                                   normal
                                                                                150
                                   145
                                              true
##
  2
      37
           M non-anginal pain
                                   130
                                        250 false ST-T wave abnormality
                                                                                187
## 3
      41
           F
               atypical angina
                                   130
                                        204 false
                                                                                172
                                                                   normal
## 4
      56
               atypical angina
                                   120
                                        236 false ST-T wave abnormality
                                                                                178
## 5
      57
           F
                typical angina
                                   120
                                        354 false ST-T wave abnormality
                                                                                163
##
     exng
          oldpeak
                                            thall
                                                       output
                            slp caa
## 1
       No
               2.3
                     upsloping
                                  0
                                          normal More Chance
## 2
       No
               3.5
                     upsloping
                                  O fixed defect More Chance
               1.4 downsloping
## 3
                                  O fixed defect More Chance
       No
## 4
       No
               0.8 downsloping
                                  O fixed defect More Chance
      Yes
               0.6 downsloping
                                  O fixed defect More Chance
```

Here is a basic summary of the factored data set

```
303 obs. of 14 variables:
## 'data.frame':
   $ age
              : int 63 37 41 56 57 57 56 44 52 57 ...
              : Factor w/ 2 levels "M", "F": 1 1 2 1 2 1 2 1 1 1 ...
              : Factor w/ 4 levels "typical angina",..: 4 3 2 2 1 1 2 2 3 3 ...
##
   $ ср
   $ trtbps : int 145 130 130 120 120 140 140 120 172 150 ...
##
              : int 233 250 204 236 354 192 294 263 199 168 ...
   $ chol
              : Factor w/ 2 levels "true", "false": 1 2 2 2 2 2 2 1 2 ...
   $ restecg : Factor w/ 3 levels "normal", "ST-T wave abnormality",..: 1 2 1 2 2 2 1 2 2 2 ...
##
   $ thalachh: int 150 187 172 178 163 148 153 173 162 174 ...
              : Factor w/ 2 levels "Yes", "No": 2 2 2 2 1 2 2 2 2 2 ...
   $ oldpeak : num 2.3 3.5 1.4 0.8 0.6 0.4 1.3 0 0.5 1.6 ...
              : Factor w/ 3 levels "upsloping", "flat", ...: 1 1 3 3 3 2 2 3 3 3 ...
##
   $ slp
              : int 0000000000...
   $ caa
              : Factor w/ 3 levels "normal", "fixed defect", ..: 1 2 2 2 2 1 2 3 3 2 ...
   $ output : Factor w/ 2 levels "Less Chance",..: 2 2 2 2 2 2 2 2 2 2 ...
##
                    sex
                                                       trtbps
                                                                         chol
         age
                                           ср
##
                    M:207
                                                         : 94.0
                                                                          :126.0
   Min.
          :29.00
                            typical angina :143
                                                                   Min.
                                                   Min.
   1st Qu.:47.50
                    F: 96
                            atypical angina: 50
                                                   1st Qu.:120.0
                                                                   1st Qu.:211.0
  Median :55.00
                                                   Median :130.0
                                                                   Median :240.0
                            non-anginal pain: 87
   Mean :54.37
                            asymptomatic
                                                   Mean :131.6
                                                                   Mean
                                                                          :246.3
                                           : 23
##
   3rd Qu.:61.00
                                                   3rd Qu.:140.0
                                                                   3rd Qu.:274.5
   Max.
          :77.00
                                                   Max.
                                                          :200.0
                                                                   Max.
                                                                          :564.0
##
                                                      thalachh
      fbs
                                                                    exng
                                        restecg
   true : 45
                                                   Min.
                                                         : 71.0
                                                                   Yes: 99
##
               normal
                                            :147
##
   false:258
               ST-T wave abnormality
                                            :152
                                                   1st Qu.:133.5
                                                                   No :204
                left ventricular hypertrophy: 4
                                                   Median :153.0
##
                                                   Mean
                                                         :149.6
                                                   3rd Qu.:166.0
##
##
                                                   Max.
                                                          :202.0
##
      oldpeak
                                                                    thall
                            slp
                                          caa
   Min. :0.00
                                            :0.0000
                                                                        : 18
##
                   upsloping : 21
                                     Min.
                                                      normal
   1st Qu.:0.00
                              :140
                                     1st Qu.:0.0000
                                                      fixed defect
                                                                       :166
                   flat
   Median:0.80
                                     Median :0.0000
                   downsloping:142
                                                      reversable defect:117
##
   Mean
         :1.04
                                     Mean
                                            :0.7294
                                                      NA's
                                                                       : 2
   3rd Qu.:1.60
##
                                     3rd Qu.:1.0000
##
   Max. :6.20
                                     Max.
                                            :4.0000
##
           output
##
   Less Chance: 138
##
   More Chance: 165
##
##
##
##
```

removing the NA's from the dataset

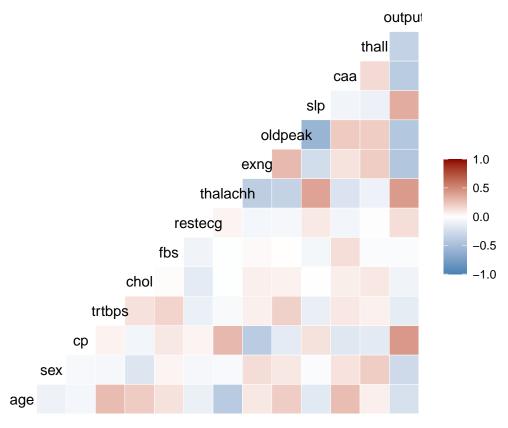
```
chol
##
                   sex
                                                      trtbps
        age
                                          ср
                                                                        :126.0
## Min.
          :29.00
                   M:206
                           typical angina :142
                                                  Min. : 94.0
                                                                  Min.
## 1st Qu.:47.00
                           atypical angina: 50
                                                  1st Qu.:120.0
                                                                  1st Qu.:211.0
                   F: 95
## Median :56.00
                           non-anginal pain: 86
                                                  Median :130.0
                                                                  Median :241.0
## Mean :54.38
                           asymptomatic
                                           : 23
                                                  Mean :131.6
                                                                  Mean :246.5
## 3rd Qu.:61.00
                                                                  3rd Qu.:275.0
                                                  3rd Qu.:140.0
```

```
:77.00
                                                                               :564.0
##
    Max.
                                                      Max.
                                                              :200.0
                                                                       Max.
                                                                         exng
##
       fbs
                                                          thalachh
                                          restecg
                 normal
                                                      Min.
                                                              : 71.0
##
    true : 44
                                               :146
                                                                       Yes: 98
    false:257
                 ST-T wave abnormality
                                               :151
                                                      1st Qu.:134.0
                                                                       No :203
##
##
                 left ventricular hypertrophy: 4
                                                      Median :153.0
##
                                                      Mean
                                                              :149.7
##
                                                      3rd Qu.:166.0
                                                      Max.
                                                              :202.0
##
##
       oldpeak
                               slp
                                              caa
                                                                          thall
           :0.000
                                : 21
                                                :0.0000
##
    Min.
                     upsloping
                                        Min.
                                                           normal
                                                                             : 18
##
    1st Qu.:0.000
                     flat
                                 :139
                                        1st Qu.:0.0000
                                                           fixed defect
                                                                             :166
                                        Median :0.0000
##
    Median :0.800
                     downsloping:141
                                                           reversable defect:117
           :1.043
                                                :0.7342
##
    Mean
                                        Mean
##
    3rd Qu.:1.600
                                        3rd Qu.:1.0000
##
    Max.
            :6.200
                                        Max.
                                                :4.0000
##
             output
##
    Less Chance: 137
    More Chance: 164
##
##
##
##
```

Data Preperation

Correlation

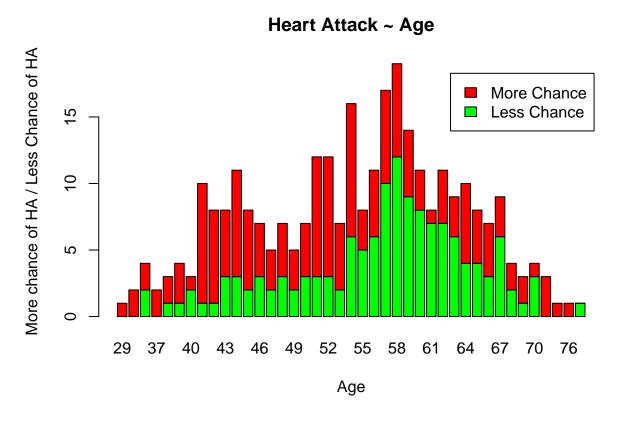
Lets see if there is any form of multicollinearity in the dataset by looking at the correlation plot of the data



By looking at the following figure we can see that there is high correlation between the predictors cp, thalach and slp to tell whether or not a patient has a higher chance of a heart attack or less chance of a heart attack. This makes sense because cp is the type of chest pain, thalach the maximum heart rate achieved and slp the slope of the heart rate. These are major factors that help distinguish whether a patient is more likely or less likely to have a hearth attack. We can also see that there is some aspects of multicollinearity in the model for there shows high significants amongst other predictors such as age and trtbps, cp and thalachh, thalach and slp, etc. These factors must be taken into account when building the model.

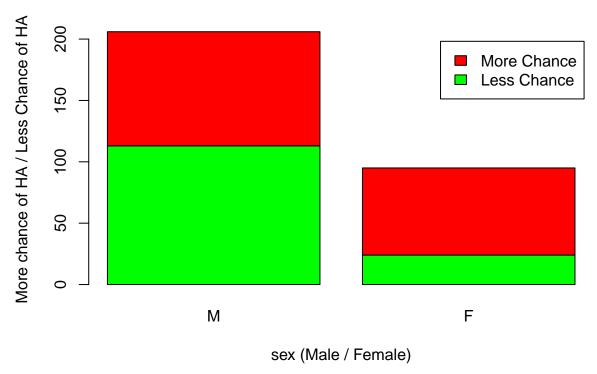
Data visualization

Lets use bar graphs to visualize the effects of the predictors on the independent variable output.



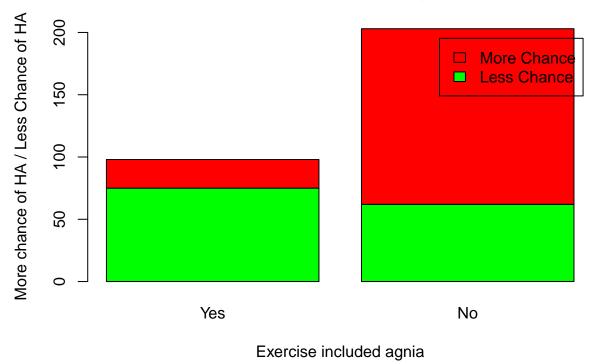
As the age increases we can see the chances of having a heart attack increases.



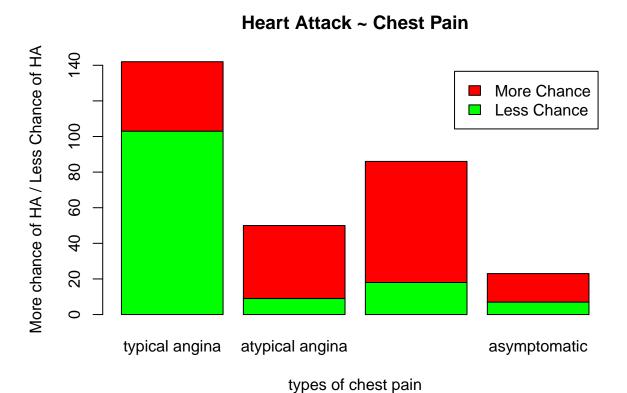


We can see most of the patients in the data set is male compared to females. The ratio of having a heart attack for males for having a higher chance of having a heart attack to a lower chance if having a heart attack is less than the ratio for females.



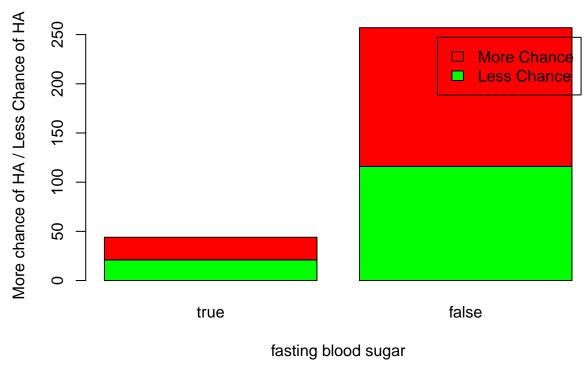


We can see that for patients who experience chest pain during exercise has a less chance of having a heart attack for patients who experienced chest pain when they were not exercising.



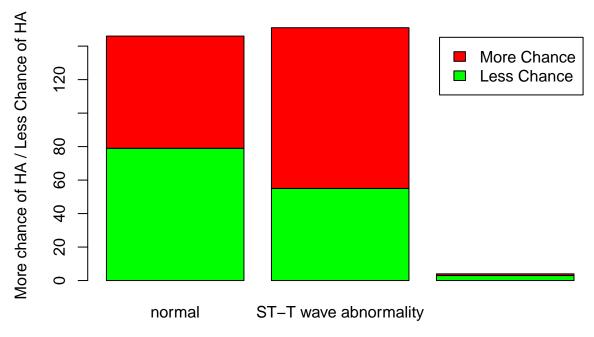
We can see patients who experienced non-anginal pain in there chest have more chance of a heart attack than patients who experienced typical chest pains. Therefore non-anginal pain in the chest is a significant factor to having a higher chance of heart attack.





We can see that if the fasting blood sugar is less than 120 mg/dl, there is more of a chance of having a heart attack compared to someone with fasting blood sugar greater than 120 mg/dl.

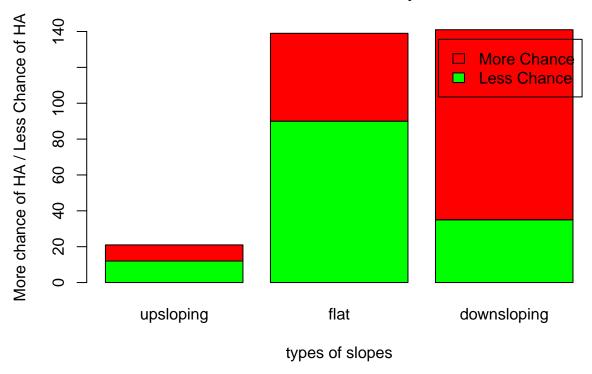
Heart Attack ~ resting electrocardiographic



types of resting electrocardiographic

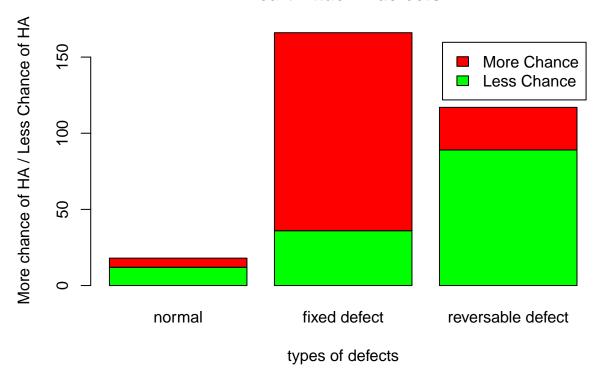
We can see patients who's resting electrocardiographic is showing forms of ST-T wave abnormality have a higher chance of having a heart attack compared to patients who show left venticular hypertrophy. Having a normal reading doesn't give enough information of whether the patient has a higher chance of having a heart to less of chance because the ratio of more chance to less chance of having a heart attack is one to one.

Heart Attack ~ slope



We can see if the slope of the cardiactric machine is downwards slopping there it shows that there is more of a chance to have a heartattack compared to seeing a upward slope or a flat slope on the machine.

Heart Attack ~ defects



We can see that if it is a fixed defect there is more chance of a heart attack to occur compared to a reversable defect or a normal defect.

Model Selection ### Additative Model Based on the data set lets first evaluate the additative model

```
##
## Call:
  glm(formula = output ~ age + sex + cp + trtbps + chol + fbs +
       restecg + thalachh + exng + oldpeak + slp + caa + thall,
##
       family = "binomial", data = newheart)
##
##
  Deviance Residuals:
##
       Min
                 10
                      Median
                                   3Q
                                           Max
  -2.7668
                      0.1548
                               0.5312
                                        2.5923
##
           -0.3527
##
## Coefficients:
                                         Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                        7.071e-01
                                                   2.695e+00
                                                                0.262 0.79308
                                       -2.299e-05
## age
                                                   2.353e-02 -0.001
                                                                      0.99922
## sexF
                                        1.477e+00 5.231e-01
                                                               2.823
                                                                      0.00475 **
## cpatypical angina
                                        9.769e-01
                                                   5.636e-01
                                                               1.733
                                                                      0.08301
                                        1.909e+00
                                                   4.794e-01
                                                                3.982 6.83e-05
## cpnon-anginal pain
## cpasymptomatic
                                        1.985e+00
                                                   6.508e-01
                                                                3.050
                                                                      0.00229 **
## trtbps
                                       -1.712e-02 1.068e-02
                                                             -1.603
                                                                      0.10890
## chol
                                       -4.303e-03 3.877e-03 -1.110
                                                                       0.26705
## fbsfalse
                                       -2.134e-01 5.692e-01
                                                              -0.375
                                                                       0.70774
                                        5.885e-01 3.755e-01
## restecgST-T wave abnormality
                                                              1.567 0.11704
```

```
## restecgleft ventricular hypertrophy -2.395e-01 2.246e+00 -0.107
                                                                      0.91507
## thalachh
                                        1.782e-02
                                                  1.079e-02
                                                               1.652
                                                                      0.09857
                                                                      0.07958
## exngNo
                                       7.468e-01
                                                  4.260e-01
                                                               1.753
## oldpeak
                                       -4.861e-01
                                                  2.254e-01
                                                             -2.157
                                                                      0.03103
## slpflat
                                       -7.007e-01
                                                  8.622e-01
                                                             -0.813
                                                                      0.41637
## slpdownsloping
                                       1.875e-01
                                                  9.372e-01
                                                               0.200
                                                                     0.84144
                                       -8.302e-01
                                                  2.036e-01
                                                             -4.077 4.55e-05 ***
## thallfixed defect
                                       6.695e-02
                                                  7.714e-01
                                                              0.087
                                                                      0.93084
## thallreversable defect
                                       -1.326e+00 7.572e-01 -1.751 0.08003 .
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 414.85 on 300
                                     degrees of freedom
## Residual deviance: 201.19
                            on 282
                                     degrees of freedom
  AIC: 239.19
##
## Number of Fisher Scoring iterations: 6
## [1] "R-squared: 0.515021967180605"
```

Wald Test Evaluation

This is the Wald test for additative model. A wald test is conducted in logistic regression is to check whether a predictor is significant or not. From looking at the wald test we see that some of the p-values are high which indicates that there are some variables that are not significant to the model. Doing a quick glance we see that age, fbs, and restec at the left verticular hypertrophy has high p-values showing that they are insignificant to the model. This doesnt mean we should drop them right away, we shall do further analysis on the model to get a clearer idea on whether or not these variables are significant to showing the patient has a lower or higher chance of getting a heart attack.

```
numDF denDF F.value p.value
            282 4.34943 <.00001
##
       19
##
                                       Estimate Std.Error DF t-value
                                                                          p-value
## (Intercept)
                                        0.707054 2.695471 282 0.262312 0.79327
## age
                                       -0.000023 0.023533
                                                           282 -0.000977 0.99922
                                                           282
## sexF
                                        1.476875 0.523100
                                                                2.823315 0.00509
## cpatypical angina
                                        0.976943 0.563577
                                                           282
                                                                1.733468 0.08411
## cpnon-anginal pain
                                        1.908910 0.479388
                                                           282 3.981973 0.00009
## cpasymptomatic
                                        1.985185 0.650795
                                                           282 3.050401 0.00250
## trtbps
                                       -0.017119 0.010678
                                                           282 -1.603164 0.11002
                                       -0.004303 0.003877
## chol
                                                           282 -1.109892 0.26799
## fbsfalse
                                       -0.213385 0.569199
                                                           282 -0.374886 0.70803
## restecgST-T wave abnormality
                                        0.588548 0.375510
                                                           282
                                                               1.567329 0.11816
## restecgleft ventricular hypertrophy -0.239541 2.246060
                                                           282 -0.106649 0.91514
                                                           282 1.651829 0.09968
## thalachh
                                        0.017820 0.010788
## exngNo
                                        0.746836 0.426008
                                                           282 1.753105 0.08067
                                                           282 -2.156649 0.03188
## oldpeak
                                       -0.486090 0.225392
## slpflat
                                       -0.700728 0.862186
                                                           282 -0.812734 0.41706
                                        0.187488 0.937188
## slpdownsloping
                                                           282 0.200054 0.84158
                                       -0.830169 0.203604
                                                           282 -4.077363 0.00006
## caa
## thallfixed defect
                                        0.066946 0.771424 282 0.086783 0.93091
```

```
## thallreversable defect
                                       -1.325557 0.757231 282 -1.750530 0.08111
##
                                       Lower 0.95 Upper 0.95
## (Intercept)
                                       -4.598742
                                                   6.012851
                                       -0.046346
                                                   0.046300
## age
## sexF
                                        0.447200
                                                   2.506551
## cpatypical angina
                                       -0.132409
                                                   2.086296
## cpnon-anginal pain
                                        0.965277
                                                   2.852543
## cpasymptomatic
                                        0.704153
                                                   3.266217
## trtbps
                                       -0.038138
                                                   0.003900
## chol
                                       -0.011934
                                                   0.003328
## fbsfalse
                                       -1.333803
                                                   0.907033
## restecgST-T wave abnormality
                                       -0.150611
                                                   1.327708
## restecgleft ventricular hypertrophy -4.660711
                                                   4.181630
## thalachh
                                                   0.039055
                                       -0.003415
## exngNo
                                       -0.091722
                                                   1.585394
## oldpeak
                                       -0.929754 -0.042427
## slpflat
                                       -2.397864
                                                   0.996409
## slpdownsloping
                                       -1.657284
                                                   2.032260
                                       -1.230946 -0.429392
## caa
## thallfixed defect
                                       -1.451534
                                                   1.585426
## thallreversable defect
                                       -2.816100
                                                   0.164987
```

Stepwise Regression

Stepwise regression is a modification of the forward selection so that after each step in which a variable was added, all candidate variables in the model are checked to see if their significance has been reduced below the specified tolerance level. If a nonsignificant variable is found, it is removed from the model. Applying stepwise regression both backward and forward leaves us with output \sim sex + cp + trtbps + chol + thalachh + exng + oldpeak + slp + caa + thall

```
## Start: AIC=239.19
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##
       exng + oldpeak + slp + caa + thall
##
##
              Df Deviance
                             AIC
                  201.19 237.19
## - age
               1
## - fbs
               1
                   201.33 237.33
## - restecg
                  203.75 237.75
                  202.41 238.41
## - chol
               1
## <none>
                   201.19 239.19
                  205.37 239.37
## - slp
               2
## - trtbps
                  203.81 239.81
               1
## - thalachh 1
                  204.02 240.02
                   204.23 240.23
## - exng
               1
## - oldpeak
               1
                  206.14 242.14
## - sex
               1
                  209.80 245.80
## - thall
               2
                   214.12 248.12
## - cp
               3
                   222.08 254.08
                   219.17 255.17
## - caa
               1
##
## Step: AIC=237.19
## output ~ sex + cp + trtbps + chol + fbs + restecg + thalachh +
##
       exng + oldpeak + slp + caa + thall
```

```
##
##
            Df Deviance AIC
           1 201.34 235.34
## - fbs
## - restecg 2 203.77 235.77
## - chol 1 202.45 236.45
                201.19 237.19
## <none>
## - slp 2 205.37 237.37
## - trtbps
           1 203.94 237.94
## - exng
             1 204.24 238.24
## - thalachh 1 204.49 238.49
## + age 1 201.19 239.19
            1 206.14 240.14
## - oldpeak
            1 209.94 243.94
## - sex
             2 214.16 246.16
## - thall
## - ср
             3 222.08 252.08
             1 219.92 253.92
## - caa
##
## Step: AIC=235.34
## output ~ sex + cp + trtbps + chol + restecg + thalachh + exng +
     oldpeak + slp + caa + thall
##
##
            Df Deviance
## - restecg 2 203.88 233.88
## - chol 1 202.55 234.55
## <none>
               201.34 235.34
## - slp
             2 205.46 235.46
## - trtbps
             1 203.97 235.97
             1 204.30 236.30
## - exng
## - thalachh 1 204.64 236.64
## + fbs
           1 201.19 237.19
             1 201.33 237.33
## + age
## - oldpeak 1 206.46 238.46
## - sex 1 209.99 241.99
             2 214.57 244.57
## - thall
             3 223.57 251.57
## - cp
## - caa
            1 219.99 251.99
##
## Step: AIC=233.88
## output ~ sex + cp + trtbps + chol + thalachh + exng + oldpeak +
##
      slp + caa + thall
##
##
            Df Deviance
                        AIC
## <none>
               203.88 233.88
## - chol
            1 205.93 233.93
## - slp
             2 208.63 234.63
             1 206.75 234.75
## - exng
             1 206.96 234.96
## - trtbps
## + restecg
             2 201.34 235.34
## - thalachh 1 207.44 235.44
## + fbs
             1 203.77 235.77
## + age
            1 203.86 235.86
## - oldpeak 1 209.12 237.12
## - sex
             1 213.78 241.78
           2 216.18 242.18
## - thall
```

```
## - ср
                   226.06 250.06
## - caa
                   222.65 250.65
               1
##
## Call: glm(formula = output ~ sex + cp + trtbps + chol + thalachh +
       exng + oldpeak + slp + caa + thall, family = "binomial",
##
##
       data = newheart)
##
## Coefficients:
##
              (Intercept)
                                              sexF
                                                          cpatypical angina
##
                 1.025922
                                          1.535349
                                                                   1.000189
##
       cpnon-anginal pain
                                    cpasymptomatic
                                                                      trtbps
##
                 1.943932
                                          1.965324
                                                                   -0.017488
##
                      chol
                                          thalachh
                                                                      exngNo
##
                -0.005343
                                          0.018627
                                                                   0.722047
##
                  oldpeak
                                           slpflat
                                                             slpdownsloping
##
                -0.484829
                                         -0.711536
                                                                    0.228519
##
                                 thallfixed defect thallreversable defect
                      caa
##
                -0.817229
                                         -0.032660
                                                                  -1.345274
##
## Degrees of Freedom: 300 Total (i.e. Null); 286 Residual
## Null Deviance:
                         414.8
## Residual Deviance: 203.9
                                 AIC: 233.9
```

Model with interactions

```
##
## Call:
## glm(formula = output ~ age + sex + cp + trtbps + chol + fbs +
##
      restecg + thalachh + exng + oldpeak + slp + caa + thall +
      age * sex + age * cp + trtbps * age + chol * age + fbs *
##
##
      age + exng * age + sex * chol + chol * cp + chol * fbs +
##
      chol * exng, family = "binomial", data = newheart)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -2.8295 -0.3641
                    0.1254
                              0.4979
                                       2.6450
##
## Coefficients:
                                        Estimate Std. Error z value Pr(>|z|)
                                       7.129e+00 1.417e+01 0.503 0.614769
## (Intercept)
## age
                                      -3.171e-02 2.490e-01 -0.127 0.898648
                                       2.733e-01 4.001e+00 0.068 0.945546
## sexF
                                       6.375e+00 4.942e+00
                                                             1.290 0.197078
## cpatypical angina
                                       4.903e+00 4.084e+00 1.201 0.229902
## cpnon-anginal pain
## cpasymptomatic
                                       6.266e+00 6.493e+00 0.965 0.334525
                                       1.619e-02 7.928e-02
## trtbps
                                                            0.204 0.838210
                                      -2.187e-02 3.155e-02 -0.693 0.488213
## chol
## fbsfalse
                                      -9.888e+00 6.110e+00 -1.618 0.105587
## restecgST-T wave abnormality
                                       6.448e-01 4.029e-01
                                                            1.600 0.109506
## restecgleft ventricular hypertrophy
                                       5.637e-01 1.868e+00
                                                              0.302 0.762825
## thalachh
                                       1.676e-02 1.117e-02
                                                            1.501 0.133293
## exngNo
                                      -3.486e+00 3.680e+00 -0.947 0.343556
```

```
## oldpeak
                                      -5.458e-01 2.451e-01 -2.227 0.025962 *
                                      -3.739e-01 9.492e-01 -0.394 0.693661
## slpflat
## slpdownsloping
                                                            0.467 0.640817
                                      4.920e-01 1.055e+00
                                      -8.771e-01 2.349e-01 -3.734 0.000189 ***
## caa
## thallfixed defect
                                      3.013e-01 8.280e-01
                                                             0.364 0.715938
## thallreversable defect
                                     -1.107e+00 7.948e-01 -1.393 0.163617
                                     -1.492e-02 5.244e-02 -0.285 0.775986
## age:sexF
                                     -2.248e-02 6.621e-02 -0.339 0.734235
## age:cpatypical angina
## age:cpnon-anginal pain
                                     -6.404e-02 6.200e-02 -1.033 0.301641
## age:cpasymptomatic
                                      2.177e-02 7.251e-02 0.300 0.764009
## age:trtbps
                                      -5.562e-04 1.391e-03 -0.400 0.689337
                                      -4.015e-05 5.378e-04 -0.075 0.940496
## age:chol
## age:fbsfalse
                                      1.082e-01 8.910e-02 1.215 0.224524
## age:exngNo
                                      4.046e-02 5.202e-02 0.778 0.436661
## sexF:chol
                                      8.117e-03 1.078e-02
                                                             0.753 0.451553
## cpatypical angina:chol
                                      -1.602e-02 1.571e-02 -1.020 0.307925
## cpnon-anginal pain:chol
                                      2.073e-03 1.190e-02
                                                             0.174 0.861672
## cpasymptomatic:chol
                                      -2.238e-02 2.176e-02 -1.028 0.303742
## chol:fbsfalse
                                      1.280e-02 1.241e-02
                                                            1.032 0.302217
## chol:exngNo
                                      8.572e-03 1.114e-02
                                                             0.770 0.441566
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 414.85 on 300 degrees of freedom
## Residual deviance: 191.63 on 268 degrees of freedom
## AIC: 257.63
##
## Number of Fisher Scoring iterations: 6
## [1] "R-squared: 0.538066697274319"
```

Wald test for interactive model

```
numDF denDF F.value p.value
##
           268 2.39469 7e-05
      33
                                     Estimate Std.Error DF t-value
                                                                     p-value
##
## (Intercept)
                                     7.129284 14.165714 268 0.503277 0.61518
## age
                                     -0.031709 0.248955 268 -0.127370 0.89874
## sexF
                                     0.273257 4.000752 268 0.068301 0.94560
## cpatypical angina
                                     6.375048 4.942201 268 1.289921 0.19819
## cpnon-anginal pain
                                     4.903159 4.083889 268 1.200610 0.23096
                                     6.265785 6.492777 268 0.965039 0.33540
## cpasymptomatic
## trtbps
                                     0.016188 0.079281 268
                                                            0.204184 0.83837
## chol
                                     -0.021866 0.031545 268 -0.693154 0.48881
## fbsfalse
                                     -9.887685 6.109733 268 -1.618350 0.10676
## restecgST-T wave abnormality
                                      ## restecgleft ventricular hypertrophy 0.563728 1.868053 268
                                                            0.301773 0.76306
## thalachh
                                      0.016764 0.011166 268 1.501241 0.13447
## exngNo
                                     -3.485743 3.680194 268 -0.947163 0.34441
                                     -0.545767  0.245092  268  -2.226781  0.02679
## oldpeak
## slpflat
                                     -0.373894 0.949231 268 -0.393891 0.69397
```

```
## slpdownsloping
                                     0.492027 1.054593 268 0.466557 0.64120
                                    -0.877077 0.234917 268 -3.733559 0.00023
## caa
                                     ## thallfixed defect
                                    -1.107233 0.794850 268 -1.393009 0.16477
## thallreversable defect
## age:sexF
                                    -0.014921 0.052437 268 -0.284554 0.77621
                                    -0.022477 0.066208 268 -0.339498 0.73450
## age:cpatypical angina
## age:cpnon-anginal pain
                                    -0.064039 0.061998 268 -1.032920 0.30257
                                    0.021770 0.072515 268 0.300220 0.76424
## age:cpasymptomatic
                                    -0.000556 0.001391 268 -0.399755 0.68966
## age:trtbps
                                    -0.000040 0.000538 268 -0.074647 0.94055
## age:chol
## age:fbsfalse
                                     0.108222 0.089102 268 1.214587 0.22559
                                     0.040463 0.052019 268 0.777843 0.43735
## age:exngNo
## sexF:chol
                                     -0.016020 0.015713 268 -1.019587 0.30884
## cpatypical angina:chol
## cpnon-anginal pain:chol
                                    0.002073 0.011897 268 0.174246 0.86180
## cpasymptomatic:chol
                                    -0.022379 0.021760 268 -1.028442 0.30467
                                     ## chol:fbsfalse
## chol:exngNo
                                     0.008572 0.011140 268 0.769552 0.44224
                                    Lower 0.95 Upper 0.95
##
## (Intercept)
                                    -20.760956 35.019525
## age
                                     -0.521866 0.458447
## sexF
                                     -7.603644 8.150158
                                     -3.355430 16.105527
## cpatypical angina
## cpnon-anginal pain
                                     -3.137427 12.943745
## cpasymptomatic
                                     -6.517553 19.049123
## trtbps
                                     -0.139904 0.172280
## chol
                                     -0.083974 0.040242
## fbsfalse
                                    -21.916863 2.141494
## restecgST-T wave abnormality
                                     -0.148447 1.438092
## restecgleft ventricular hypertrophy -3.114198 4.241655
## thalachh
                                     -0.005222 0.038749
## exngNo
                                    -10.731513 3.760027
## oldpeak
                                     -1.028318 -0.063216
                                     -2.242791 1.495004
## slpflat
## slpdownsloping
                                     -1.584313 2.568368
                                     -1.339595 -0.414559
## caa
## thallfixed defect
                                     -1.328880 1.931474
## thallreversable defect
                                     -2.672177 0.457711
## age:sexF
                                     -0.118161 0.088319
## age:cpatypical angina
                                     -0.152830 0.107876
## age:cpnon-anginal pain
                                     -0.186104 0.058026
## age:cpasymptomatic
                                     -0.121000 0.164541
## age:trtbps
                                     -0.003296 0.002183
                                     -0.001099 0.001019
## age:chol
## age:fbsfalse
                                     -0.067207 0.283652
## age:exngNo
                                     -0.061956 0.142882
## sexF:chol
                                     -0.013111 0.029346
## cpatypical angina:chol
                                     -0.046956 0.014916
## cpnon-anginal pain:chol
                                     -0.021351 0.025497
## cpasymptomatic:chol
                                     -0.065221 0.020463
## chol:fbsfalse
                                     -0.011632 0.037242
## chol:exngNo
                                     -0.013360 0.030505
```

Stepwise regression for model with interactions

```
## Start: AIC=257.63
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
      exng + oldpeak + slp + caa + thall + age * sex + age * cp +
      trtbps * age + chol * age + fbs * age + exng * age + sex *
##
##
      chol + chol * cp + chol * fbs + chol * exng
##
               Df Deviance
                              AIC
                    193.11 253.11
## - age:cp
                3
## - cp:chol
                3
                    194.15 254.15
## - age:chol
                1
                    191.64 255.64
## - age:sex
                    191.71 255.71
                1
                    191.79 255.79
## - age:trtbps 1
## - sex:chol
                1
                    192.21 256.21
## - chol:exng
               1
                    192.23 256.23
                    192.24 256.24
## - age:exng
                1
## - restecg
                2
                    194.25 256.25
                2
                    194.70 256.70
## - slp
## - chol:fbs
              1
                    192.71 256.71
## - age:fbs
                1 193.08 257.08
## <none>
                    191.63 257.63
## - thalachh
              1
                  193.94 257.94
## - oldpeak
               1
                   196.97 260.97
## - thall
                2 201.97 263.97
                1
                    207.81 271.81
## - caa
##
## Step: AIC=253.11
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
      exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##
      age:chol + age:fbs + age:exng + sex:chol + cp:chol + chol:fbs +
##
      chol:exng
##
##
               Df Deviance
                              AIC
                    195.40 249.40
## - cp:chol
                    193.12 251.12
## - age:chol
                1
## - age:sex
                    193.35 251.35
                1
                    193.38 251.38
## - age:trtbps 1
## - age:exng
                1
                    193.40 251.40
## - chol:exng
                    193.71 251.71
               1
## - sex:chol
                1
                    193.79 251.79
## - slp
                2 196.04 252.04
## - chol:fbs
                    194.15 252.15
              1
## - restecg
                2 196.35 252.35
                   194.49 252.49
## - age:fbs
## <none>
                    193.11 253.11
## - thalachh
                1
                    195.46 253.46
                    198.97 256.97
## - oldpeak
                1
## + age:cp
                3
                    191.63 257.63
                2
                    205.82 261.82
## - thall
## - caa
                1
                    208.37 266.37
##
## Step: AIC=249.4
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##
      exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##
      age:chol + age:fbs + age:exng + sex:chol + chol:fbs + chol:exng
```

```
##
##
               Df Deviance
                              ATC
## - age:chol
                    195.41 247.41
                    195.70 247.70
## - chol:exng 1
## - age:sex
                    195.73 247.73
                    195.73 247.73
## - age:trtbps 1
## - age:exng
                    195.82 247.82
                1
                    198.48 248.48
## - restecg
                2
## - slp
                2
                    198.52 248.52
                   196.54 248.54
## - age:fbs
                1
## - sex:chol
              1
                   196.91 248.91
              1 197.01 249.01
## - chol:fbs
## <none>
                    195.40 249.40
## - thalachh
              1 198.18 250.18
## + cp:chol
                3
                   193.11 253.11
## - oldpeak
                1
                    201.40 253.40
                3
                    194.15 254.15
## + age:cp
## - thall
                2
                    209.82 259.82
## - cp
                3
                    215.74 263.74
                    211.75 263.75
## - caa
                1
##
## Step: AIC=247.41
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
      exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##
      age:fbs + age:exng + sex:chol + chol:fbs + chol:exng
##
##
               Df Deviance
                              AIC
                    195.70 245.70
## - chol:exng
                1
## - age:trtbps 1
                    195.74 245.74
## - age:sex
                1
                    195.74 245.74
## - age:exng
                1
                    195.84 245.84
## - restecg
                2
                   198.49 246.49
                2 198.53 246.53
## - slp
               1 196.59 246.59
## - age:fbs
## - chol:fbs
                   197.02 247.02
              1 197.35 247.35
## - sex:chol
## <none>
                    195.41 247.41
## - thalachh
              1
                   198.18 248.18
## + age:chol
                1
                    195.40 249.40
## + cp:chol
                    193.12 251.12
                3
## - oldpeak
                    201.44 251.44
                1
## + age:cp
                3
                    194.15 252.15
## - thall
                2
                    209.83 257.83
## - ср
                3
                    215.91 261.91
## - caa
                    212.28 262.29
##
## Step: AIC=245.7
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##
      exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##
      age:fbs + age:exng + sex:chol + chol:fbs
##
               Df Deviance
##
                              AIC
## - age:sex
               1 196.00 244.00
## - age:trtbps 1 196.05 244.05
```

```
## - age:exng
                    196.24 244.24
                1
                    198.74 244.74
## - restecg
                2
## - age:fbs
                    196.80 244.80
                2 198.87 244.87
## - slp
## - chol:fbs
                   197.23 245.23
## <none>
                    195.70 245.70
## - sex:chol
                  197.93 245.93
## - thalachh
                   198.51 246.51
                1
## + chol:exng
               1
                    195.41 247.41
                    195.70 247.70
## + age:chol
                1
## + cp:chol
                3
                   193.71 249.71
                    201.82 249.82
## - oldpeak
                1
## + age:cp
                3
                   194.51 250.51
## - thall
                2
                   210.42 256.42
## - ср
                3
                    216.37 260.37
## - caa
                1
                    212.95 260.95
##
## Step: AIC=244
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
      exng + oldpeak + slp + caa + thall + age:trtbps + age:fbs +
##
      age:exng + sex:chol + chol:fbs
##
##
               Df Deviance
                              AIC
                   196.33 242.33
## - age:trtbps 1
## - age:exng
                1
                    196.55 242.55
## - restecg
                2
                   198.80 242.80
## - slp
                   198.97 242.97
## - age:fbs
                   197.09 243.09
                1
              1 197.51 243.51
## - chol:fbs
                    196.00 244.00
## <none>
                  198.05 244.05
## - sex:chol
## - thalachh
                1
                   198.78 244.78
                   195.70 245.70
## + age:sex
## + chol:exng
                    195.74 245.74
              1
## + age:chol
                1
                    195.99 245.99
## + cp:chol
                3
                    193.96 247.96
## - oldpeak
                1
                    202.26 248.26
## + age:cp
                3
                    194.62 248.62
## - thall
                2
                    210.53 254.53
                   216.44 258.44
## - cp
                3
## - caa
                    213.43 259.43
##
## Step: AIC=242.33
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
      exng + oldpeak + slp + caa + thall + age:fbs + age:exng +
##
      sex:chol + chol:fbs
##
##
               Df Deviance
                              AIC
## - age:exng
                1
                   196.84 240.84
                2
## - restecg
                    199.21 241.21
## - slp
                2
                   199.40 241.40
                   197.63 241.63
## - age:fbs
               1
## - chol:fbs
              1 197.78 241.78
## - sex:chol
              1 198.23 242.23
```

```
## <none>
                     196.33 242.33
## - trtbps
                    198.57 242.57
                1
## - thalachh
                    199.29 243.29
## + age:trtbps 1
                    196.00 244.00
## + chol:exng 1
                    196.05 244.05
## + age:sex
                    196.05 244.05
                1
## + age:chol
                    196.32 244.32
                1
## + cp:chol
                    194.23 246.23
                 3
## - oldpeak
                1
                     202.42 246.42
                    194.84 246.84
## + age:cp
                 3
## - thall
                 2
                    211.22 253.22
                    216.90 256.90
## - ср
                 3
                    213.53 257.53
## - caa
                 1
##
## Step: AIC=240.84
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##
       exng + oldpeak + slp + caa + thall + age:fbs + sex:chol +
##
       chol:fbs
##
               Df Deviance
##
                              AIC
## - restecg
                2
                    199.47 239.47
## - slp
                2
                    200.00 240.00
                    198.09 240.09
## - age:fbs
               1
## - chol:fbs
                    198.20 240.20
                1
## - sex:chol
              1 198.72 240.72
## <none>
                    196.84 240.84
## - trtbps
                1
                   199.15 241.15
                    199.68 241.68
## - thalachh
                1
                    199.84 241.84
## - exng
                1
                    196.33 242.33
## + age:exng
                1
## + chol:exng
                 1
                    196.46 242.46
## + age:sex
                 1
                    196.54 242.54
                    196.55 242.55
## + age:trtbps 1
## + age:chol
                    196.83 242.83
                 1
## - oldpeak
                 1
                     202.57 244.57
                 3
                    194.66 244.66
## + cp:chol
## + age:cp
                 3
                    195.77 245.77
## - thall
                2
                    211.25 251.25
## - ср
                3
                     217.75 255.75
## - caa
                 1
                    214.58 256.58
##
## Step: AIC=239.47
## output ~ age + sex + cp + trtbps + chol + fbs + thalachh + exng +
##
       oldpeak + slp + caa + thall + age:fbs + sex:chol + chol:fbs
##
                Df Deviance
##
                              AIC
                     200.68 238.68
## - age:fbs
## - chol:fbs
                     201.00 239.00
## - sex:chol
                1
                     201.10 239.10
                2
## - slp
                     203.16 239.16
## <none>
                     199.47 239.47
                    202.14 240.14
## - trtbps
## - thalachh
                1
                    202.35 240.35
                 1 202.47 240.47
## - exng
```

```
196.84 240.84
## + restecg
## + age:trtbps 1
                    199.11 241.11
## + chol:exng 1
                    199.13 241.13
                   199.21 241.21
## + age:exng
                1
## + age:sex
                1
                    199.41 241.41
## + age:chol
                   199.47 241.47
                1
## - oldpeak
                    205.22 243.22
                1
                   197.38 243.38
## + cp:chol
                3
## + age:cp
                3
                   197.94 243.94
## - thall
                2
                   212.82 248.82
## - ср
                3
                   220.30 254.30
                    216.99 254.99
## - caa
                1
## Step: AIC=238.68
## output ~ age + sex + cp + trtbps + chol + fbs + thalachh + exng +
##
      oldpeak + slp + caa + thall + sex:chol + chol:fbs
##
               Df Deviance
##
                              AIC
## - age
                    200.71 236.71
                1
                    202.15 238.15
## - sex:chol
## - chol:fbs
              1
                    202.33 238.33
## - slp
                2 204.65 238.65
                    200.68 238.68
## <none>
## + age:fbs
                  199.47 239.47
                1
                1 203.53 239.53
## - exng
## - trtbps
                1
                    203.71 239.71
              1
## - thalachh
                    203.74 239.74
                2
                   198.09 240.09
## + restecg
                    200.11 240.11
## + age:trtbps 1
                    200.43 240.43
## + chol:exng
                1
                    200.44 240.44
## + age:exng
                1
## + age:sex
                1
                    200.62 240.62
                    200.63 240.63
## + age:chol
                    206.13 242.13
## - oldpeak
                1
## + cp:chol
                3
                   198.88 242.88
## + age:cp
                3
                   199.03 243.03
## - thall
                2
                   213.14 247.14
## - ср
                3 221.07 253.07
                    217.76 253.76
## - caa
##
## Step: AIC=236.7
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
      slp + caa + thall + sex:chol + chol:fbs
##
              Df Deviance
                   202.19 236.19
## - sex:chol
               1
                   202.34 236.34
## - chol:fbs
               1
## - slp
                   204.68 236.68
## <none>
                   200.71 236.71
                   203.54 237.54
## - exng
               1
                   203.96 237.96
## - trtbps
               1
               2 198.09 238.09
## + restecg
## + chol:exng 1
                   200.46 238.46
## - thalachh 1
                   204.49 238.49
```

```
200.68 238.68
## + age
             1
## - oldpeak 1
                 206.16 240.16
## + cp:chol 3 198.93 240.93
## - thall
              2 213.23 245.23
## - ср
              3
                 221.08 251.08
## - caa
                 218.80 252.80
              1
## Step: AIC=236.19
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
      slp + caa + thall + chol:fbs
##
##
             Df Deviance
                          AIC
## - chol:fbs 1 203.77 235.77
                 202.19 236.19
## <none>
## + sex:chol 1 200.71 236.71
            1 205.00 237.00
## - exng
## - slp
             2 207.10 237.10
## - trtbps 1 205.57 237.57
## + chol:exng 1
                 201.74 237.74
             2 199.80 237.80
## + restecg
## - thalachh 1 205.80 237.80
## + age 1 202.15 238.15
## - oldpeak 1 207.14 239.14
## + cp:chol
             3 199.58 239.58
## - thall 2 214.32 244.32
## - sex
            1
                 212.73 244.73
## - ср
              3 223.47 251.47
              1 220.29 252.29
## - caa
##
## Step: AIC=235.77
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
##
      slp + caa + thall
##
##
             Df Deviance
                           AIC
             1 203.88 233.88
## - fbs
## <none>
                 203.77 235.77
## - chol
            1 205.86 235.86
## + chol:fbs 1 202.19 236.19
## + sex:chol 1
                 202.34 236.34
## - slp
            2 208.59 236.59
## - exng
            1 206.71 236.71
## - trtbps 1 206.95 236.95
## + restecg 2 201.19 237.19
## - thalachh 1
                 207.31 237.31
## + chol:exng 1
                 203.45 237.45
                 203.75 237.75
## + age
              1
                 200.74 238.74
## + cp:chol
              3
## - oldpeak
                 208.83 238.83
            1
            1
## - sex
                 213.77 243.77
              2
## - thall
                 215.83 243.83
## - cp
              3
                 224.60 250.60
                 222.60 252.60
## - caa
##
## Step: AIC=233.88
```

```
## output ~ sex + cp + trtbps + chol + thalachh + exng + oldpeak +
       slp + caa + thall
##
##
               Df Deviance
##
                               AIC
## <none>
                     203.88 233.88
                     205.93 233.93
## - chol
                1
                     202.46 234.46
## + sex:chol
                1
## - slp
                     208.63 234.63
                2
## - exng
                1
                     206.75 234.75
## - trtbps
                1
                     206.96 234.96
## + restecg
                2
                     201.34 235.34
                     207.44 235.44
## - thalachh
                1
## + chol:exng
                1
                     203.59 235.59
## + fbs
                1
                     203.77 235.77
## + age
                     203.86 235.86
                1
## + cp:chol
                3
                     201.08 237.08
## - oldpeak
                     209.12 237.12
                1
## - sex
                1
                     213.78 241.78
## - thall
                     216.18 242.18
                2
## - ср
                3
                     226.06 250.06
## - caa
                1
                     222.65 250.65
##
##
  Call: glm(formula = output ~ sex + cp + trtbps + chol + thalachh +
       exng + oldpeak + slp + caa + thall, family = "binomial",
##
       data = newheart)
##
##
##
   Coefficients:
##
              (Intercept)
                                               sexF
                                                           cpatypical angina
##
                 1.025922
                                           1.535349
                                                                    1.000189
##
       cpnon-anginal pain
                                     cpasymptomatic
                                                                      trtbps
                 1.943932
                                           1.965324
                                                                   -0.017488
##
##
                      chol
                                           thalachh
                                                                      exngNo
##
                -0.005343
                                           0.018627
                                                                    0.722047
##
                  oldpeak
                                            slpflat
                                                              slpdownsloping
                -0.484829
##
                                          -0.711536
                                                                    0.228519
##
                                 thallfixed defect
                                                    thallreversable defect
                       caa
##
                -0.817229
                                          -0.032660
                                                                   -1.345274
##
## Degrees of Freedom: 300 Total (i.e. Null); 286 Residual
## Null Deviance:
                         414.8
## Residual Deviance: 203.9
                                 AIC: 233.9
```

Model Comparision

I noticed when adding interactions to the model the significance of the variables in the model became less effective. We can see this by looking at the both the p-values in the wald test. All the p-values for the model with interactions are significantly more higher than the additative model. We can also see that When running step wise regression on the model with interactions. It eliminated all the interaction terms because they were insigificant to the model and gave us back the additative model. This is telling us that the additative model will be more viable to use for the analysis. Thus after evaluating both models we will stick with the additative model for further analysis.

```
## [1] "R-squared: 0.508545330225056"
```

#Model evaluation

VIF

Since our selected model is the additative model we can now use the model to answer the question. Which predictor influences the factors of having a heart attack. As metioned before during the correlation test we notice there was some aspects of multicollinearity in the dataset. Lets check the VIF of the additative model. In statistics, the variance inflation factor is the quotient of the variance in a model with multiple terms by the variance of a model with one term alone. It quantifies the severity of multicollinearity in an ordinary least squares regression analysis

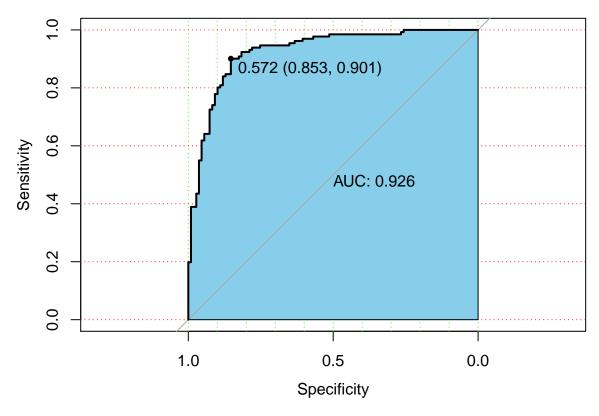
```
##
                 GVIF Df GVIF^(1/(2*Df))
## sex
            1.491120
                       1
                                 1.221114
                                 1.077980
## ср
            1.569147
                       3
## trtbps
            1.094189
                       1
                                 1.046035
## chol
            1.187864
                       1
                                 1.089892
## thalachh 1.318093
                                 1.148082
                                 1.084535
## exng
            1.176216
                       1
## oldpeak
            1.502516
                                 1.225772
## slp
            1.805862
                       2
                                 1.159234
## caa
            1.150145
                       1
                                 1.072448
## thall
            1.312593
                                 1.070367
```

Since the VIF score of our predictors are less than 10. There is no aspects of multicollinearity in our model. #Model Analysis

ROC Curve for Logistic Regression

The ROC curve shows the trade-off between sensitivity (or TPR) and specificity (1 - FPR). Classifiers that give curves closer to the top-left corner indicate a better performance. As a baseline, a random classifier is expected to give points lying along the diagonal (FPR = TPR). The closer the curve comes to the 45-degree diagonal of the ROC space, the less accurate the test. To compare different classifiers, it can be useful to summarize the performance of each classifier into a single measure. One common approach is to calculate the area under the ROC curve, which is abbreviated to AUC

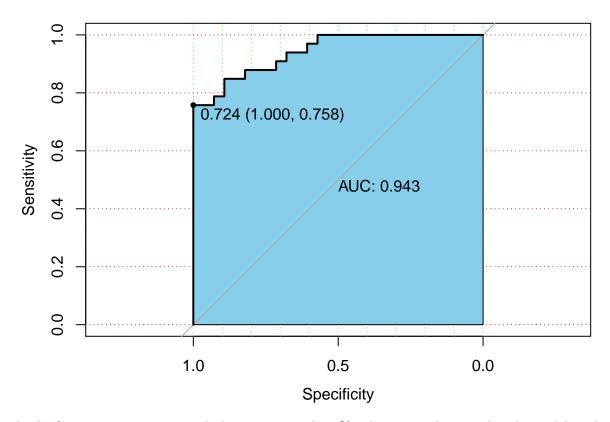
```
## Setting levels: control = Less Chance, case = More Chance
## Setting direction: controls < cases</pre>
```



The AUC on training set is 0.918 which is approximately 92%, This is an indication that the model prediction performance is good.

```
## Setting levels: control = Less Chance, case = More Chance
```

Setting direction: controls < cases

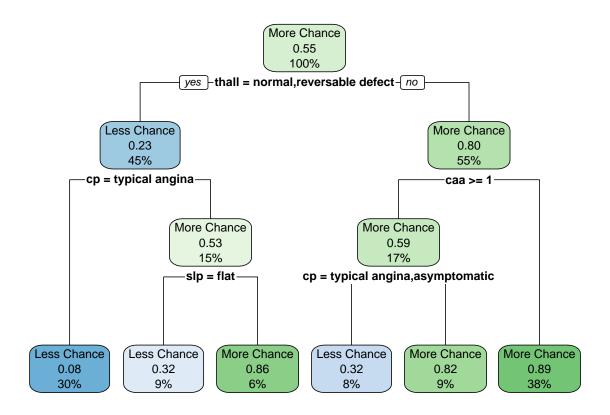


The AUC on testing set is 0.974 which is approximetly 97%. This is an indication that the model prediction performance is good.

Overall comparing the model performance on both the testing and training set we get similar performances which tells us that the model we have is able to classify whether the patient is highly in risk of having a heart attack or less in risk of having a heart attack, based on logistic regression.

Decision Tree Classification

We will use our aditative model for decision tree classification also. The Decision tree builds classification or regression models in the form of a tree structure. It breaks down a dataset into smaller and smaller subsets while at the same time an associated decision tree is incrementally developed. the Decision trees can handle both categorical and numerical data



At the top is the overal percentage of patients getting heart attacks. It shows the porportion of patients who have a higher chance of recieving a heart attack to patients having a less chance of recieving a heart attack. 53% of the patients have a higher chance of recieving a heart attack. You can keep going down the nodes to understand what features impact the chances of having a higher chance of a heart attack to having a less chance of having a heart attack. For example, if its a fixed defect and if the chest pain type is asymptomatic then there is a 91% chance of having a heart attack.

Making A Prediction

Accuracy of test set

##	<pre>predict_unseen</pre>					
##			Less	Chance	${\tt More}$	Chance
##	Less	${\tt Chance}$		24		4
##	More	Chance		8		25

Confusion matrix of the patients who have more chance of a heart attack and the patients who have a less chance of a heart attack using the testing data set.

[1] "Accuracy for test 0.80327868852459"

The accuracy of the testing set is approximatly 85%. Which is good because it tells us that 82% of the predictions made are correct based on the testing set.

Accuracy of training set

```
## predict_unseen1
## Less Chance More Chance
## Less Chance 93 16
## More Chance 19 112
```

[1] "Accuracy for train 0.85416666666667"

The accuracy of the training set is approximatly 84%. This is good because it tells us that 84% of the predictions made are correct based on the training set.

#Conclusion

Comparing the performance of our model through logistic regression and using the decision tree method we can see that the model performs well to predict whether the patient is classified in having a higher chance of getting a heart attack to having a less chance of having a heart attack. We can also see that Logistic regression seems to be more viable since it has a higher chance of prediciting more or less chance of having a heart attack compared to the decision tree method. Finally, we see that the predictors that show the most influence to our independant variable 'output' is sex, cp, trtbps, chol, thalachh, exng, oldpeak, slp, caa and the thall. Theoretically speaking this makes sense. Factors such as chest pain, cholesterol levels, etc, are related to heart attacks. Some recommendations that will probably improve the performance of the model is having more meaningful predictors in the data set for detecting heart attacks.