

HeartAttack Prediction

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Heart Attack Analysis and Predictive Analysis

Introduction

Heart disease is the leading cause of death for men, women, and people of most racial and ethnic groups. One person dies every 36 seconds in the United States from cardiovascular disease. About 655,000 Americans die from heart disease each year—that's 1 in every 4 deaths. The goal of this project is to find out which factors influences the chances of getting a heart attack. I will be using Heart Attack Analysis & Prediction Dataset, which is a dataset for heart attack classification from kaggle. In addition i'll be using the following classification technique Decision Tree, to provide further analysis of which factors influence heart attacks.

Description of Dataset

Age : Age of the patient

Sex : Sex of the patient

exng: exercise induced angina (1 = yes; 0 = no)

caa: number of major vessels (0-3)

cp : Chest Pain type chest pain type

Value 1: typical angina Value 2: atypical angina Value 3: non-anginal pain Value 4: asymptomatic

trtbps : resting blood pressure (in mm Hg)

chol : cholestoral in mg/dl fetched via BMI sensor

fbs : (fasting blood sugar > 120 mg/dl) (1 = true; 0 = false)

rest_ecg : resting electrocardiographic results Value 0: normal Value 1: having ST-T wave abnormality (T wave inversions and/or ST elevation or depression of > 0.05 mV) Value 2: showing probable or definite left ventricular hypertrophy by Estes' criteria

thalach : maximum heart rate achieved

oldpeak: ST depression induced by exercise relative to rest

slp: the slope of the peak exercise ST segment (0 = upsloping; 1 = flat; 2 = downsloping)

thall: 1 = normal; 2 = fixed defect; 3 = reversable defect

target : 0= less chance of heart attack 1= more chance of heart attack

Here is a sample of the first 5 rows of the data

```
##   age sex cp trtbps chol fbs restecg thalachh exng oldpeak slp caa thall output
## 1  63  1  3   145  233   1         0      150   0    2.3   0  0    1      1
## 2  37  1  2   130  250   0         1      187   0    3.5   0  0    2      1
## 3  41  0  1   130  204   0         0      172   0    1.4   2  0    2      1
## 4  56  1  1   120  236   0         1      178   0    0.8   2  0    2      1
## 5  57  0  0   120  354   0         1      163   1    0.6   2  0    2      1
```

Here is the data types of the data set

```
## 'data.frame':   303 obs. of  14 variables:
## $ age      : int  63 37 41 56 57 57 56 44 52 57 ...
## $ sex      : int  1 1 0 1 0 1 0 1 1 1 ...
## $ cp       : int  3 2 1 1 0 0 1 1 2 2 ...
## $ trtbps   : int  145 130 130 120 120 140 140 120 172 150 ...
## $ chol     : int  233 250 204 236 354 192 294 263 199 168 ...
## $ fbs      : int  1 0 0 0 0 0 0 0 1 0 ...
## $ restecg  : int  0 1 0 1 1 1 0 1 1 1 ...
## $ thalachh : int  150 187 172 178 163 148 153 173 162 174 ...
## $ exng     : int  0 0 0 0 1 0 0 0 0 0 ...
## $ oldpeak  : num  2.3 3.5 1.4 0.8 0.6 0.4 1.3 0 0.5 1.6 ...
## $ slp      : int  0 0 2 2 2 1 1 2 2 2 ...
## $ caa      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ thall    : int  1 2 2 2 2 1 2 3 3 2 ...
## $ output   : int  1 1 1 1 1 1 1 1 1 1 ...
```

According to our dataset target which is output is our independent variable. We will use logistic regression since we are dealing with a categorical variable. We will also build two models one model which is an additive model and another model which includes interactions. We will evaluate both models performance and choose the best fitting model for further analysis.

Cleaning The Dataset

Based on the data set we have qualitative dependent variables and a qualitative independent variable so let's factor the qualitative variables and relabel them so they have meaningful names in the dataset to make it easier reading the data when analyzing the data.

```
##   age sex      cp trtbps chol   fbs      restecg thalachh
## 1  63  M asymptomatic   145  233  true      normal      150
## 2  37  M non-anginal pain   130  250 false ST-T wave abnormality      187
## 3  41  F atypical angina   130  204 false      normal      172
## 4  56  M atypical angina   120  236 false ST-T wave abnormality      178
## 5  57  F typical angina   120  354 false ST-T wave abnormality      163
##   exng oldpeak      slp caa      thall      output
## 1  No    2.3   upsloping  0      normal More Chance
## 2  No    3.5   upsloping  0 fixed defect More Chance
## 3  No    1.4  downsloping  0 fixed defect More Chance
## 4  No    0.8  downsloping  0 fixed defect More Chance
## 5  Yes   0.6  downsloping  0 fixed defect More Chance
```

Here is a basic summary of the factored data set

```
## 'data.frame':   303 obs. of  14 variables:
## $ age      : int  63 37 41 56 57 57 56 44 52 57 ...
## $ sex      : Factor w/ 2 levels "M","F": 1 1 2 1 2 1 2 1 1 1 ...
## $ cp       : Factor w/ 4 levels "typical angina",...: 4 3 2 2 1 1 2 2 3 3 ...
## $ trtbps   : int  145 130 130 120 120 140 140 120 172 150 ...
## $ chol     : int  233 250 204 236 354 192 294 263 199 168 ...
## $ fbs      : Factor w/ 2 levels "true","false": 1 2 2 2 2 2 2 1 2 ...
## $ restecg  : Factor w/ 3 levels "normal","ST-T wave abnormality",...: 1 2 1 2 2 2 1 2 2 2 ...
## $ thalachh : int  150 187 172 178 163 148 153 173 162 174 ...
## $ exng     : Factor w/ 2 levels "Yes","No": 2 2 2 2 1 2 2 2 2 2 ...
## $ oldpeak  : num  2.3 3.5 1.4 0.8 0.6 0.4 1.3 0 0.5 1.6 ...
## $ slp      : Factor w/ 3 levels "upsloping","flat",...: 1 1 3 3 3 2 2 3 3 3 ...
## $ caa      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ thall    : Factor w/ 3 levels "normal","fixed defect",...: 1 2 2 2 2 1 2 3 3 2 ...
## $ output   : Factor w/ 2 levels "Less Chance",...: 2 2 2 2 2 2 2 2 2 2 ...
```

```
##      age      sex      cp      trtbps      chol
## Min.   :29.00   M:207   typical angina :143   Min.    : 94.0   Min.    :126.0
## 1st Qu.:47.50   F: 96   atypical angina : 50   1st Qu.:120.0   1st Qu.:211.0
## Median :55.00           non-anginal pain: 87   Median :130.0   Median :240.0
## Mean   :54.37           asymptomatic   : 23   Mean    :131.6   Mean    :246.3
## 3rd Qu.:61.00                                3rd Qu.:140.0   3rd Qu.:274.5
## Max.   :77.00                                Max.    :200.0   Max.    :564.0
##      fbs      restecg      thalachh      exng
## true  : 45   normal           :147   Min.    : 71.0   Yes: 99
## false:258   ST-T wave abnormality :152   1st Qu.:133.5   No :204
##           left ventricular hypertrophy: 4   Median :153.0
##                                           Mean    :149.6
##                                           3rd Qu.:166.0
##                                           Max.    :202.0
##      oldpeak      slp      caa      thall
## Min.   :0.00   upsloping : 21   Min.    :0.0000   normal           : 18
## 1st Qu.:0.00   flat       :140   1st Qu.:0.0000   fixed defect     :166
## Median :0.80   downsloping:142   Median :0.0000   reversable defect:117
## Mean    :1.04                                Mean    :0.7294   NA's           : 2
## 3rd Qu.:1.60                                3rd Qu.:1.0000
## Max.    :6.20                                Max.    :4.0000
##      output
## Less Chance:138
## More Chance:165
##
##
##
##
```

removing the NA's from the dataset

```
##      age      sex      cp      trtbps      chol
## Min.   :29.00   M:206   typical angina :142   Min.    : 94.0   Min.    :126.0
## 1st Qu.:47.00   F: 95   atypical angina : 50   1st Qu.:120.0   1st Qu.:211.0
## Median :56.00           non-anginal pain: 86   Median :130.0   Median :241.0
## Mean    :54.38           asymptomatic   : 23   Mean    :131.6   Mean    :246.5
## 3rd Qu.:61.00                                3rd Qu.:140.0   3rd Qu.:275.0
```

```

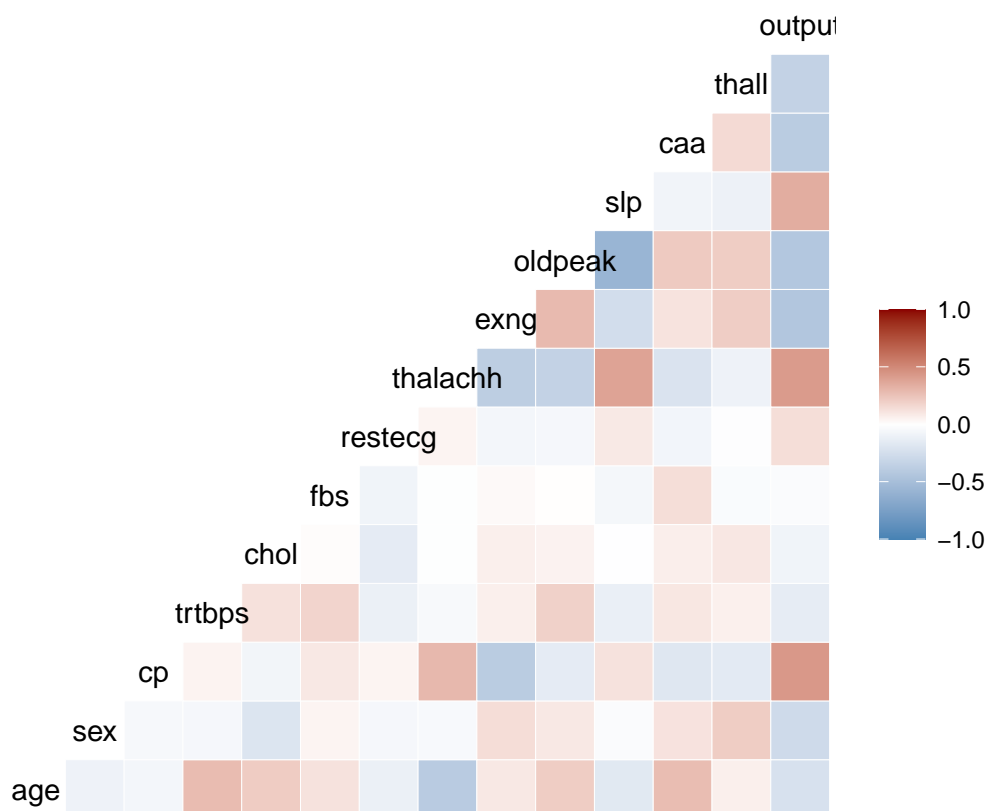
## Max.      :77.00                                Max.      :200.0    Max.      :564.0
##      fbs                                restecg      thalachh      exng
## true : 44    normal                                :146    Min.      : 71.0    Yes: 98
## false:257    ST-T wave abnormality                :151    1st Qu.:134.0    No :203
##              left ventricular hypertrophy: 4      Median :153.0
##                                                    Mean      :149.7
##                                                    3rd Qu.:166.0
##                                                    Max.      :202.0
##      oldpeak      slp      caa      thall
## Min.      :0.000    upsloping : 21    Min.      :0.0000    normal      : 18
## 1st Qu.:0.000    flat      :139    1st Qu.:0.0000    fixed defect :166
## Median :0.800    downsloping:141    Median :0.0000    reversable defect:117
## Mean      :1.043                                Mean      :0.7342
## 3rd Qu.:1.600                                3rd Qu.:1.0000
## Max.      :6.200                                Max.      :4.0000
##      output
## Less Chance:137
## More Chance:164
##
##
##
##

```

Data Preperation

Correlation

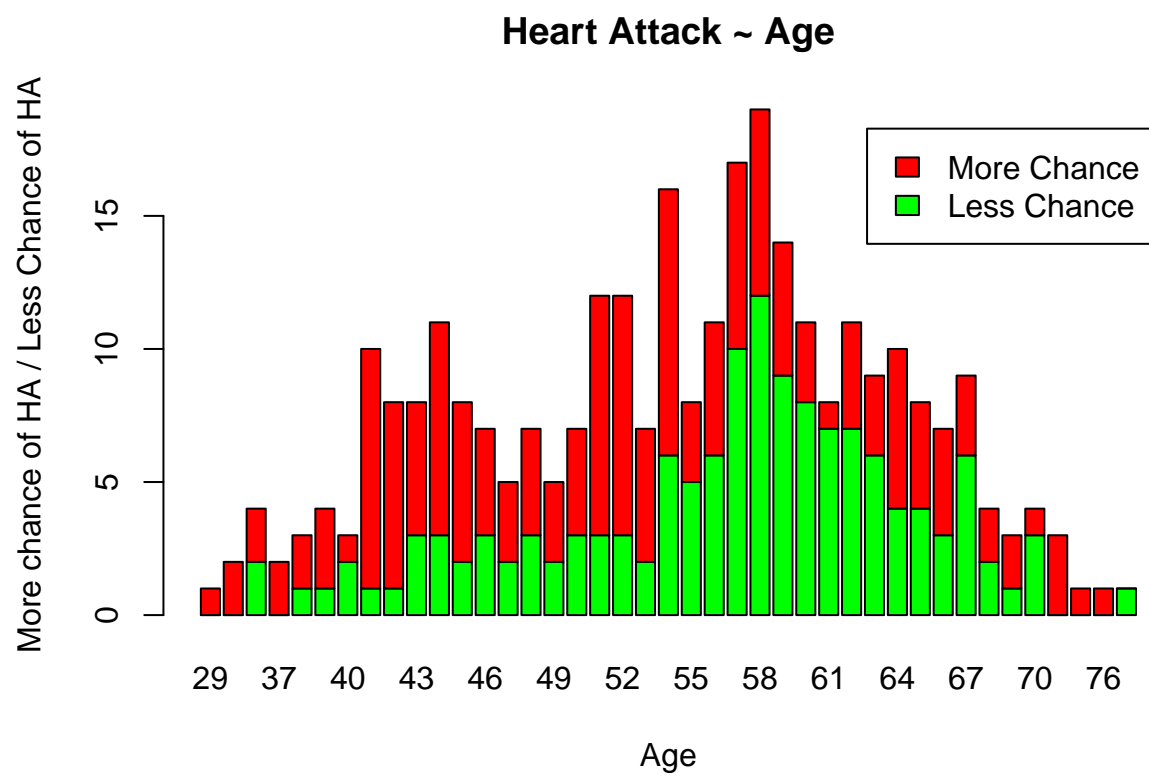
Lets see if there is any form of multicollinearity in the dataset by looking at the correlation plot of the data



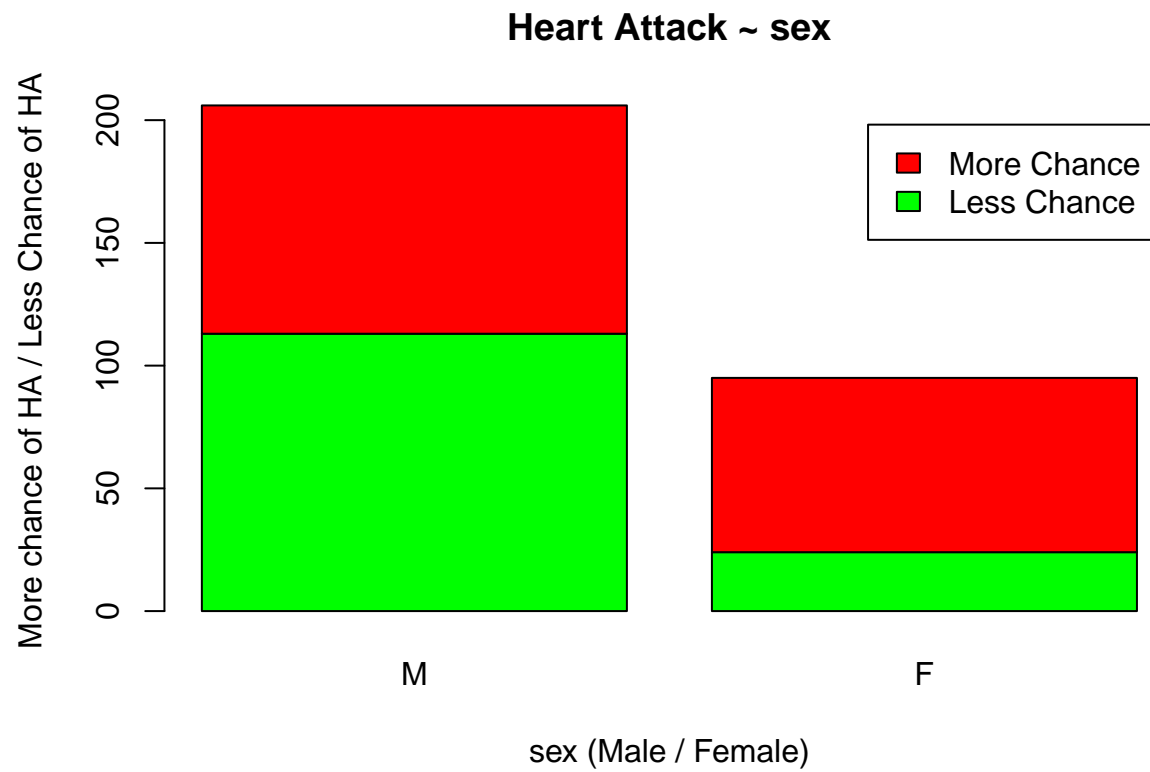
By looking at the following figure we can see that there is high correlation between the predictors cp, thalach and slp to tell whether or not a patient has a higher chance of a heart attack or less chance of a heart attack. This makes sense because cp is the type of chest pain, thalach the maximum heart rate achieved and slp the slope of the heart rate. These are major factors that help distinguish whether a patient is more likely or less likely to have a heart attack. We can also see that there is some aspects of multicollinearity in the model for there shows high significant amongst other predictors such as age and trtbps, cp and thalachh, thalach and slp, etc. These factors must be taken into account when building the model.

Data visualization

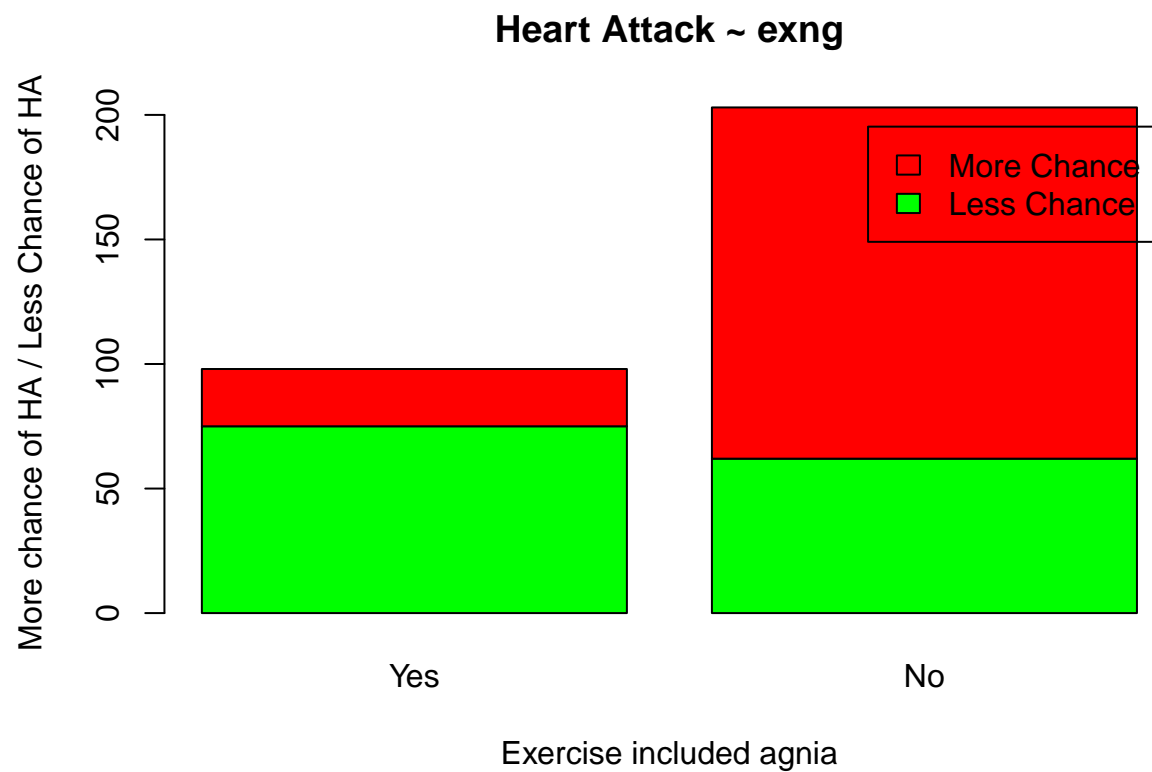
Lets use bar graphs to visualize the effects of the predictors on the independent variable output.



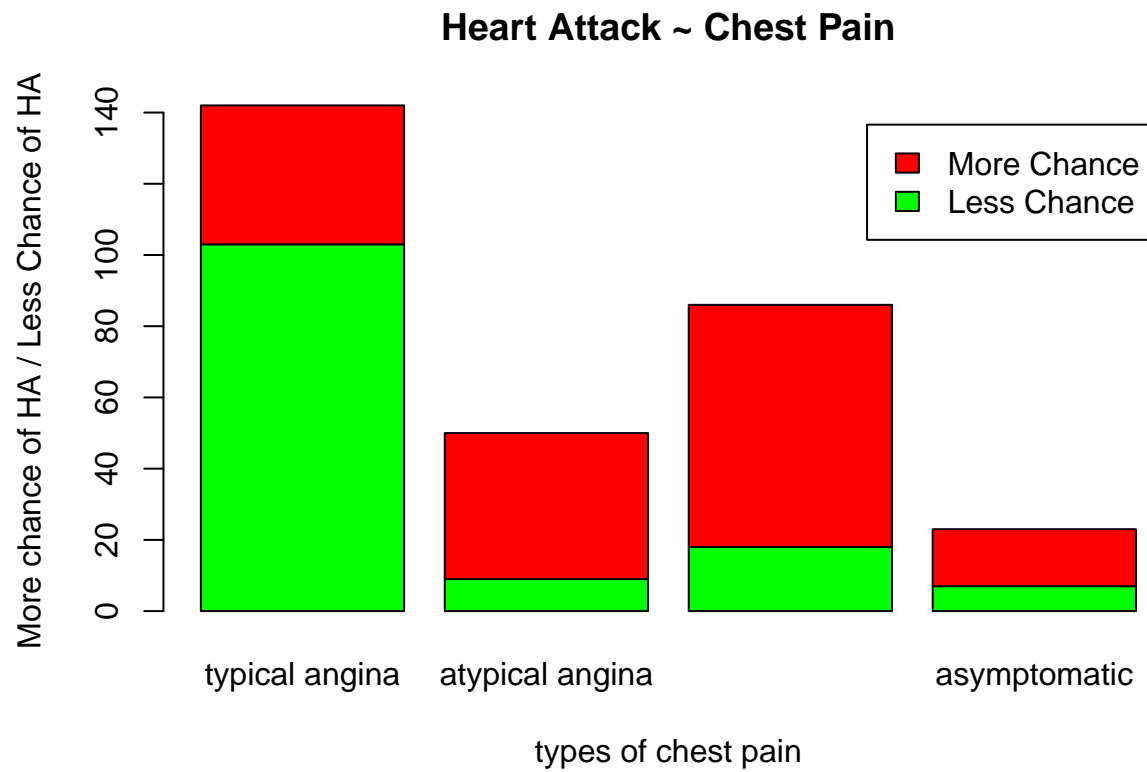
As the age increases we can see the chances of having a heart attack increases.



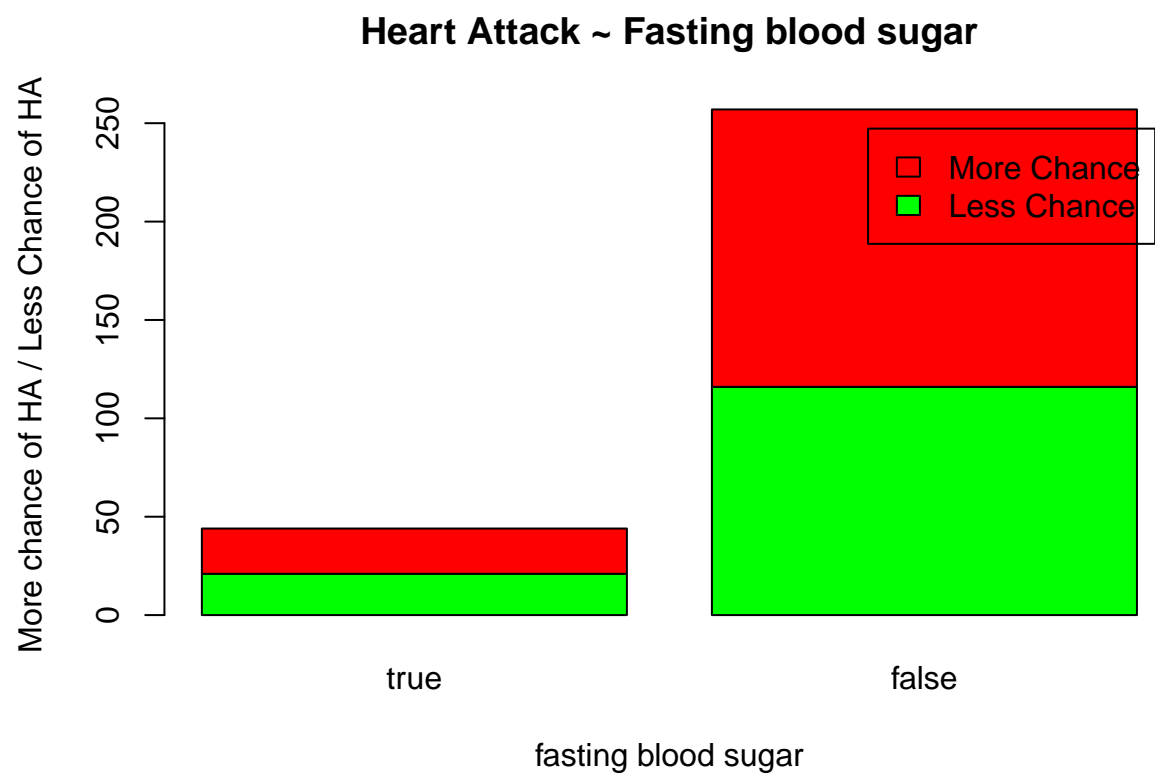
We can see most of the patients in the data set is male compared to females. The ratio of having a heart attack for males for having a higher chance of having a heart attack to a lower chance if having a heart attack is less than the ratio for females.



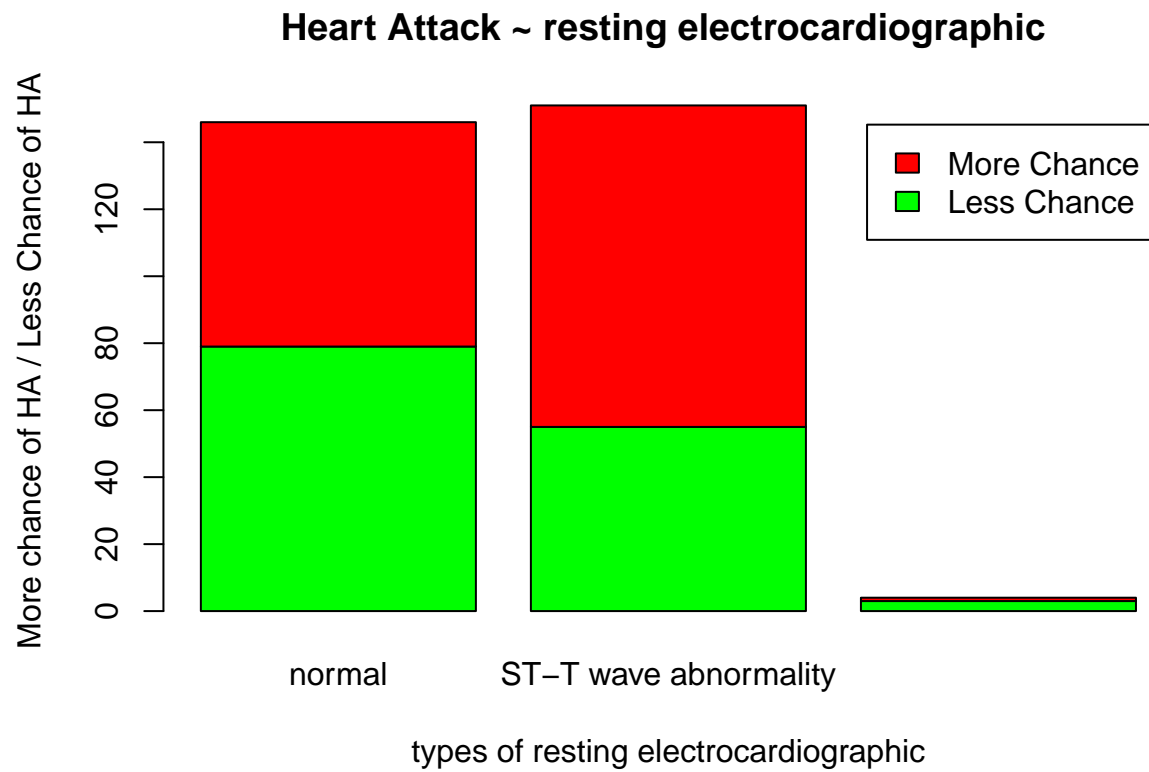
We can see that for patients who experience chest pain during exercise has a less chance of having a heart attack for patients who experienced chest pain when they were not exercising.



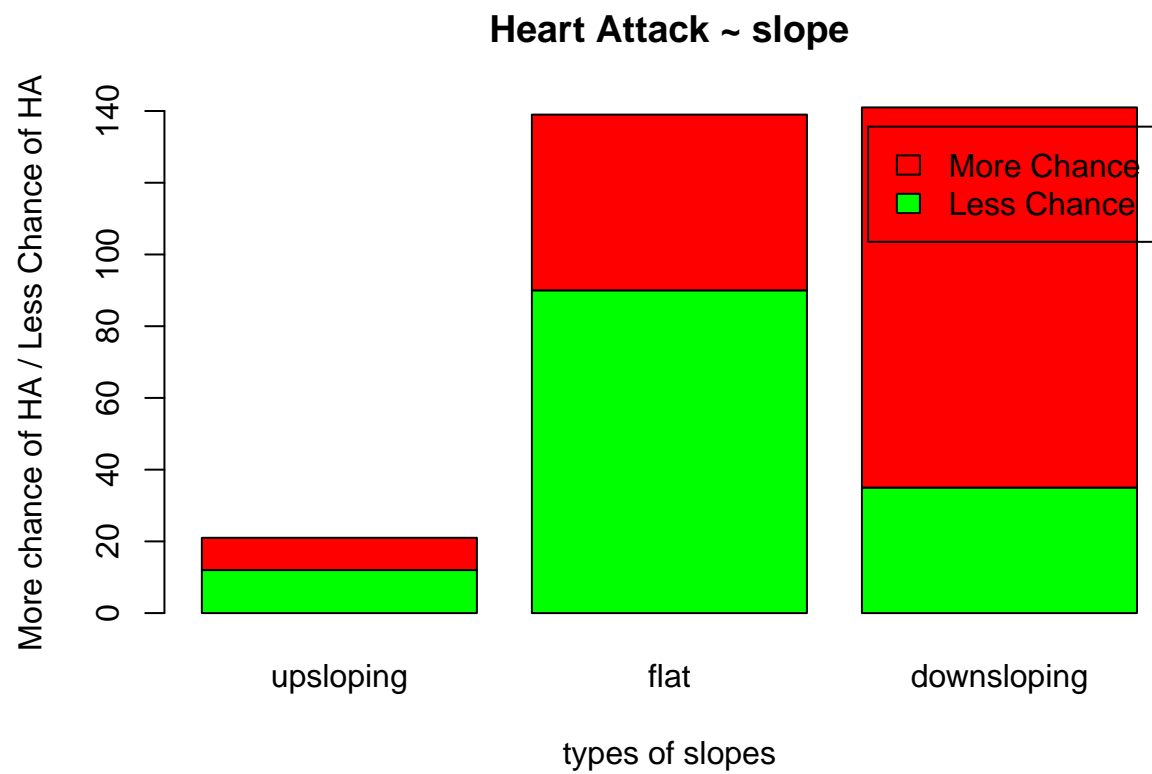
We can see patients who experienced non-anginal pain in there chest have more chance of a heart attack than patients who experienced typical chest pains. Therefore non-anginal pain in the chest is a significant factor to having a higher chance of heart attack.



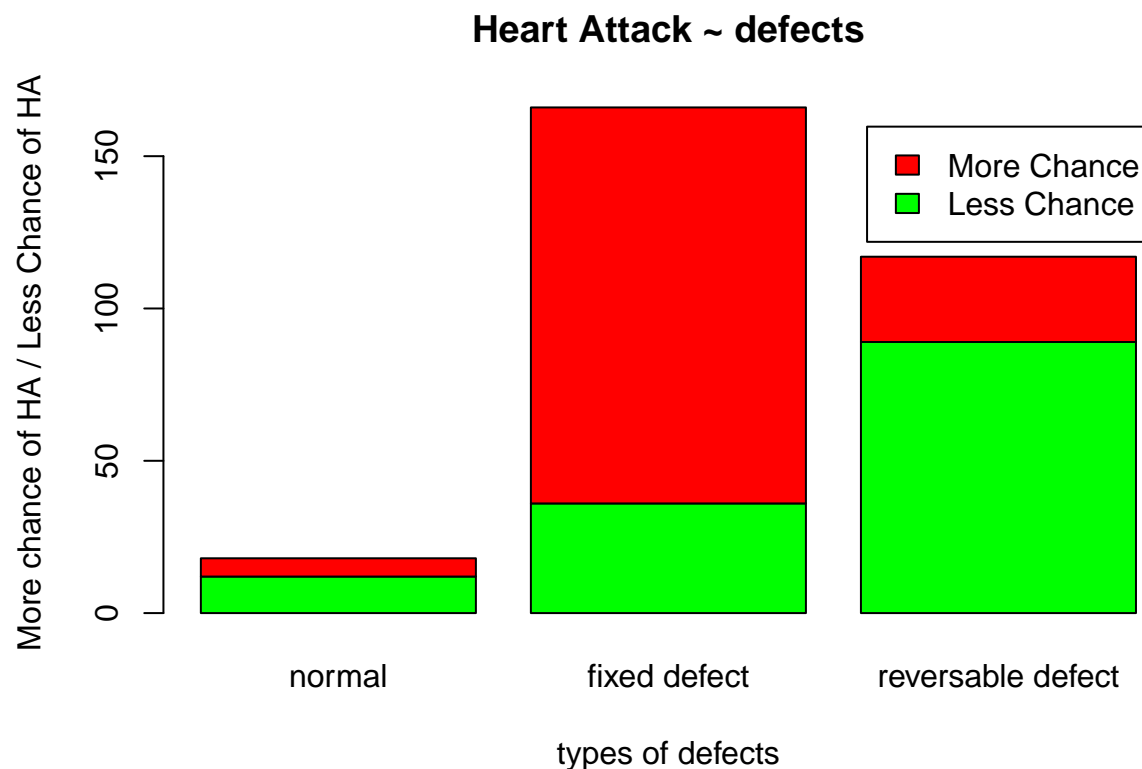
We can see that if the fasting blood sugar is less than 120 mg/dl, there is more of a chance of having a heart attack compared to someone with fasting blood sugar greater than 120 mg/dl.



We can see patients who's resting electrocardiographic is showing forms of ST-T wave abnormality have a higher chance of having a heart attack compared to patients who show left ventricular hypertrophy. Having a normal reading doesn't give enough information of whether the patient has a higher chance of having a heart to less of chance because the ratio of more chance to less chance of having a heart attack is one to one.



We can see if the slope of the cardiac machine is downwards sloping there it shows that there is more of a chance to have a heart attack compared to seeing an upward slope or a flat slope on the machine.



We can see that if it is a fixed defect there is more chance of a heart attack to occur compared to a reversible defect or a normal defect.

Model Selection

Additive Model

Based on the data set lets first evaluate the additive model

```
##
## Call:
## glm(formula = output ~ age + sex + cp + trtbps + chol + fbs +
##      restecg + thalachh + exng + oldpeak + slp + caa + thall,
##      family = "binomial", data = newheart)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.7668  -0.3527   0.1548   0.5312   2.5923
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    7.071e-01  2.695e+00   0.262  0.79308
## age           -2.299e-05  2.353e-02  -0.001  0.99922
## sexF           1.477e+00  5.231e-01   2.823  0.00475 **
## cpatypical angina  9.769e-01  5.636e-01   1.733  0.08301 .
## cpnon-anginal pain 1.909e+00  4.794e-01   3.982 6.83e-05 ***
```

```
## cpasymptomatic      1.985e+00  6.508e-01  3.050  0.00229 **
## trtbps              -1.712e-02  1.068e-02  -1.603  0.10890
## chol                -4.303e-03  3.877e-03  -1.110  0.26705
## fbsfalse            -2.134e-01  5.692e-01  -0.375  0.70774
## restecgST-T wave abnormality  5.885e-01  3.755e-01  1.567  0.11704
## restecgleft ventricular hypertrophy -2.395e-01  2.246e+00  -0.107  0.91507
## thalachh            1.782e-02  1.079e-02  1.652  0.09857 .
## exngNo              7.468e-01  4.260e-01  1.753  0.07958 .
## oldpeak            -4.861e-01  2.254e-01  -2.157  0.03103 *
## slpflat             -7.007e-01  8.622e-01  -0.813  0.41637
## slpdownsloping      1.875e-01  9.372e-01  0.200  0.84144
## caa                -8.302e-01  2.036e-01  -4.077  4.55e-05 ***
## thallfixed defect    6.695e-02  7.714e-01  0.087  0.93084
## thallreversible defect -1.326e+00  7.572e-01  -1.751  0.08003 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 414.85  on 300  degrees of freedom
## Residual deviance: 201.19  on 282  degrees of freedom
## AIC: 239.19
##
## Number of Fisher Scoring iterations: 6

## [1] "R-squared: 0.515021967180605"
```

Wald Test Evaluation

This is the Wald test for additive model. A wald test is conducted in logistic regression is to check whether a predictor is significant or not. From looking at the wald test we see that some of the p-values are high which indicates that there are some variables that are not significant to the model. Doing a quick glance we see that age, fbs, and restecg at the left ventricular hypertrophy has high p-values showing that they are insignificant to the model. This doesn't mean we should drop them right away, we shall do further analysis on the model to get a clearer idea on whether or not these variables are significant to showing the patient has a lower or higher chance of getting a heart attack.

```
## numDF denDF F.value p.value
## 19 282 4.34943 <.00001
##
## Estimate Std.Error DF t-value p-value
## (Intercept) 0.707054 2.695471 282 0.262312 0.79327
## age -0.000023 0.023533 282 -0.000977 0.99922
## sexF 1.476875 0.523100 282 2.823315 0.00509
## cpatypical angina 0.976943 0.563577 282 1.733468 0.08411
## cpnon-anginal pain 1.908910 0.479388 282 3.981973 0.00009
## cpasymptomatic 1.985185 0.650795 282 3.050401 0.00250
## trtbps -0.017119 0.010678 282 -1.603164 0.11002
## chol -0.004303 0.003877 282 -1.109892 0.26799
## fbsfalse -0.213385 0.569199 282 -0.374886 0.70803
## restecgST-T wave abnormality 0.588548 0.375510 282 1.567329 0.11816
## restecgleft ventricular hypertrophy -0.239541 2.246060 282 -0.106649 0.91514
## thalachh 0.017820 0.010788 282 1.651829 0.09968
## exngNo 0.746836 0.426008 282 1.753105 0.08067
```

```
## oldpeak -0.486090 0.225392 282 -2.156649 0.03188
## slpflat -0.700728 0.862186 282 -0.812734 0.41706
## slpdownsloping 0.187488 0.937188 282 0.200054 0.84158
## caa -0.830169 0.203604 282 -4.077363 0.00006
## thallfixed defect 0.066946 0.771424 282 0.086783 0.93091
## thallreversable defect -1.325557 0.757231 282 -1.750530 0.08111
## Lower 0.95 Upper 0.95
## (Intercept) -4.598742 6.012851
## age -0.046346 0.046300
## sexF 0.447200 2.506551
## cpatypical angina -0.132409 2.086296
## cpnon-anginal pain 0.965277 2.852543
## cpasymptomatic 0.704153 3.266217
## trtbps -0.038138 0.003900
## chol -0.011934 0.003328
## fbsfalse -1.333803 0.907033
## restecgST-T wave abnormality -0.150611 1.327708
## restecgleft ventricular hypertrophy -4.660711 4.181630
## thalachh -0.003415 0.039055
## exngNo -0.091722 1.585394
## oldpeak -0.929754 -0.042427
## slpflat -2.397864 0.996409
## slpdownsloping -1.657284 2.032260
## caa -1.230946 -0.429392
## thallfixed defect -1.451534 1.585426
## thallreversable defect -2.816100 0.164987
```

Stepwise Regression

Stepwise regression is a modification of the forward selection so that after each step in which a variable was added, all candidate variables in the model are checked to see if their significance has been reduced below the specified tolerance level. If a nonsignificant variable is found, it is removed from the model. Applying stepwise regression both backward and forward leaves us with output ~ sex + cp + trtbps + chol + thalachh + exng + oldpeak + slp + caa + thall

```
## Start: AIC=239.19
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
## exng + oldpeak + slp + caa + thall
##
## Df Deviance AIC
## - age 1 201.19 237.19
## - fbs 1 201.33 237.33
## - restecg 2 203.75 237.75
## - chol 1 202.41 238.41
## <none> 201.19 239.19
## - slp 2 205.37 239.37
## - trtbps 1 203.81 239.81
## - thalachh 1 204.02 240.02
## - exng 1 204.23 240.23
## - oldpeak 1 206.14 242.14
## - sex 1 209.80 245.80
## - thall 2 214.12 248.12
## - cp 3 222.08 254.08
```

```

## - caa      1   219.17 255.17
##
## Step: AIC=237.19
## output ~ sex + cp + trtbps + chol + fbs + restecg + thalachh +
##      exng + oldpeak + slp + caa + thall
##
##           Df Deviance   AIC
## - fbs      1   201.34 235.34
## - restecg  2   203.77 235.77
## - chol     1   202.45 236.45
## <none>      201.19 237.19
## - slp      2   205.37 237.37
## - trtbps   1   203.94 237.94
## - exng     1   204.24 238.24
## - thalachh 1   204.49 238.49
## + age      1   201.19 239.19
## - oldpeak  1   206.14 240.14
## - sex      1   209.94 243.94
## - thall    2   214.16 246.16
## - cp       3   222.08 252.08
## - caa      1   219.92 253.92
##
## Step: AIC=235.34
## output ~ sex + cp + trtbps + chol + restecg + thalachh + exng +
##      oldpeak + slp + caa + thall
##
##           Df Deviance   AIC
## - restecg  2   203.88 233.88
## - chol     1   202.55 234.55
## <none>      201.34 235.34
## - slp      2   205.46 235.46
## - trtbps   1   203.97 235.97
## - exng     1   204.30 236.30
## - thalachh 1   204.64 236.64
## + fbs      1   201.19 237.19
## + age      1   201.33 237.33
## - oldpeak  1   206.46 238.46
## - sex      1   209.99 241.99
## - thall    2   214.57 244.57
## - cp       3   223.57 251.57
## - caa      1   219.99 251.99
##
## Step: AIC=233.88
## output ~ sex + cp + trtbps + chol + thalachh + exng + oldpeak +
##      slp + caa + thall
##
##           Df Deviance   AIC
## <none>      203.88 233.88
## - chol     1   205.93 233.93
## - slp      2   208.63 234.63
## - exng     1   206.75 234.75
## - trtbps   1   206.96 234.96
## + restecg  2   201.34 235.34
## - thalachh 1   207.44 235.44

```



```
## + fbs      1  203.77 235.77
## + age      1  203.86 235.86
## - oldpeak  1  209.12 237.12
## - sex      1  213.78 241.78
## - thall    2  216.18 242.18
## - cp       3  226.06 250.06
## - caa      1  222.65 250.65

##
## Call:  glm(formula = output ~ sex + cp + trtbps + chol + thalachh +
##          exng + oldpeak + slp + caa + thall, family = "binomial",
##          data = newheart)
##
## Coefficients:
##          (Intercept)                sexF          cpatypical angina
##              1.025922                1.535349                1.000189
##    cpnon-anginal pain          cpasymptomatic          trtbps
##              1.943932                1.965324             -0.017488
##              chol                thalachh          exngNo
##             -0.005343                0.018627                0.722047
##              oldpeak          slpflat          slpdownsloping
##             -0.484829             -0.711536                0.228519
##              caa          thallfixed defect  thallreversible defect
##             -0.817229             -0.032660             -1.345274
##
## Degrees of Freedom: 300 Total (i.e. Null);  286 Residual
## Null Deviance:          414.8
## Residual Deviance: 203.9      AIC: 233.9
```

Model with interactions

```
##
## Call:
## glm(formula = output ~ age + sex + cp + trtbps + chol + fbs +
##       restecg + thalachh + exng + oldpeak + slp + caa + thall +
##       age * sex + age * cp + trtbps * age + chol * age + fbs *
##       age + exng * age + sex * chol + chol * cp + chol * fbs +
##       chol * exng, family = "binomial", data = newheart)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8295  -0.3641   0.1254   0.4979   2.6450
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    7.129e+00  1.417e+01  0.503 0.614769
## age           -3.171e-02  2.490e-01 -0.127 0.898648
## sexF           2.733e-01  4.001e+00  0.068 0.945546
## cpatypical angina  6.375e+00  4.942e+00  1.290 0.197078
## cpnon-anginal pain  4.903e+00  4.084e+00  1.201 0.229902
## cpasymptomatic    6.266e+00  6.493e+00  0.965 0.334525
## trtbps           1.619e-02  7.928e-02  0.204 0.838210
## chol           -2.187e-02  3.155e-02 -0.693 0.488213
```

```

## fbsfalse -9.888e+00 6.110e+00 -1.618 0.105587
## restecgST-T wave abnormality 6.448e-01 4.029e-01 1.600 0.109506
## restecgleft ventricular hypertrophy 5.637e-01 1.868e+00 0.302 0.762825
## thalachh 1.676e-02 1.117e-02 1.501 0.133293
## exngNo -3.486e+00 3.680e+00 -0.947 0.343556
## oldpeak -5.458e-01 2.451e-01 -2.227 0.025962 *
## slpflat -3.739e-01 9.492e-01 -0.394 0.693661
## slpdownsloping 4.920e-01 1.055e+00 0.467 0.640817
## caa -8.771e-01 2.349e-01 -3.734 0.000189 ***
## thallfixed defect 3.013e-01 8.280e-01 0.364 0.715938
## thallreversible defect -1.107e+00 7.948e-01 -1.393 0.163617
## age:sexF -1.492e-02 5.244e-02 -0.285 0.775986
## age:cpatypical angina -2.248e-02 6.621e-02 -0.339 0.734235
## age:cpnon-anginal pain -6.404e-02 6.200e-02 -1.033 0.301641
## age:cpasymptomatic 2.177e-02 7.251e-02 0.300 0.764009
## age:trtbps -5.562e-04 1.391e-03 -0.400 0.689337
## age:chol -4.015e-05 5.378e-04 -0.075 0.940496
## age:fbsfalse 1.082e-01 8.910e-02 1.215 0.224524
## age:exngNo 4.046e-02 5.202e-02 0.778 0.436661
## sexF:chol 8.117e-03 1.078e-02 0.753 0.451553
## cpatypical angina:chol -1.602e-02 1.571e-02 -1.020 0.307925
## cpnon-anginal pain:chol 2.073e-03 1.190e-02 0.174 0.861672
## cpasymptomatic:chol -2.238e-02 2.176e-02 -1.028 0.303742
## chol:fbsfalse 1.280e-02 1.241e-02 1.032 0.302217
## chol:exngNo 8.572e-03 1.114e-02 0.770 0.441566
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 414.85 on 300 degrees of freedom
## Residual deviance: 191.63 on 268 degrees of freedom
## AIC: 257.63
##
## Number of Fisher Scoring iterations: 6

## [1] "R-squared: 0.538066697274319"

```

Wald test for interactive model

```

## numDF denDF F.value p.value
## 33 268 2.39469 7e-05
##
## Estimate Std.Error DF t-value p-value
## (Intercept) 7.129284 14.165714 268 0.503277 0.61518
## age -0.031709 0.248955 268 -0.127370 0.89874
## sexF 0.273257 4.000752 268 0.068301 0.94560
## cpatypical angina 6.375048 4.942201 268 1.289921 0.19819
## cpnon-anginal pain 4.903159 4.083889 268 1.200610 0.23096
## cpasymptomatic 6.265785 6.492777 268 0.965039 0.33540
## trtbps 0.016188 0.079281 268 0.204184 0.83837
## chol -0.021866 0.031545 268 -0.693154 0.48881
## fbsfalse -9.887685 6.109733 268 -1.618350 0.10676
## restecgST-T wave abnormality 0.644823 0.402909 268 1.600418 0.11068

```

## restecgleft ventricular hypertrophy	0.563728	1.868053	268	0.301773	0.76306
## thalachh	0.016764	0.011166	268	1.501241	0.13447
## exngNo	-3.485743	3.680194	268	-0.947163	0.34441
## oldpeak	-0.545767	0.245092	268	-2.226781	0.02679
## slpflat	-0.373894	0.949231	268	-0.393891	0.69397
## slpdownsloping	0.492027	1.054593	268	0.466557	0.64120
## caa	-0.877077	0.234917	268	-3.733559	0.00023
## thallfixed defect	0.301297	0.827982	268	0.363893	0.71622
## thallreversible defect	-1.107233	0.794850	268	-1.393009	0.16477
## age:sexF	-0.014921	0.052437	268	-0.284554	0.77621
## age:cpatypical angina	-0.022477	0.066208	268	-0.339498	0.73450
## age:cpnon-anginal pain	-0.064039	0.061998	268	-1.032920	0.30257
## age:cpasymptomatic	0.021770	0.072515	268	0.300220	0.76424
## age:trtbps	-0.000556	0.001391	268	-0.399755	0.68966
## age:chol	-0.000040	0.000538	268	-0.074647	0.94055
## age:fbsfalse	0.108222	0.089102	268	1.214587	0.22559
## age:exngNo	0.040463	0.052019	268	0.777843	0.43735
## sexF:chol	0.008117	0.010782	268	0.752829	0.45221
## cpatypical angina:chol	-0.016020	0.015713	268	-1.019587	0.30884
## cpnon-anginal pain:chol	0.002073	0.011897	268	0.174246	0.86180
## cpasymptomatic:chol	-0.022379	0.021760	268	-1.028442	0.30467
## chol:fbsfalse	0.012805	0.012412	268	1.031691	0.30315
## chol:exngNo	0.008572	0.011140	268	0.769552	0.44224
##	Lower 0.95	Upper 0.95			
## (Intercept)	-20.760956	35.019525			
## age	-0.521866	0.458447			
## sexF	-7.603644	8.150158			
## cpatypical angina	-3.355430	16.105527			
## cpnon-anginal pain	-3.137427	12.943745			
## cpasymptomatic	-6.517553	19.049123			
## trtbps	-0.139904	0.172280			
## chol	-0.083974	0.040242			
## fbsfalse	-21.916863	2.141494			
## restecgST-T wave abnormality	-0.148447	1.438092			
## restecgleft ventricular hypertrophy	-3.114198	4.241655			
## thalachh	-0.005222	0.038749			
## exngNo	-10.731513	3.760027			
## oldpeak	-1.028318	-0.063216			
## slpflat	-2.242791	1.495004			
## slpdownsloping	-1.584313	2.568368			
## caa	-1.339595	-0.414559			
## thallfixed defect	-1.328880	1.931474			
## thallreversible defect	-2.672177	0.457711			
## age:sexF	-0.118161	0.088319			
## age:cpatypical angina	-0.152830	0.107876			
## age:cpnon-anginal pain	-0.186104	0.058026			
## age:cpasymptomatic	-0.121000	0.164541			
## age:trtbps	-0.003296	0.002183			
## age:chol	-0.001099	0.001019			
## age:fbsfalse	-0.067207	0.283652			
## age:exngNo	-0.061956	0.142882			
## sexF:chol	-0.013111	0.029346			
## cpatypical angina:chol	-0.046956	0.014916			
## cpnon-anginal pain:chol	-0.021351	0.025497			

```
## cpasymptomatic:chol          -0.065221  0.020463
## chol:fbsfalse                -0.011632  0.037242
## chol:exngNo                  -0.013360  0.030505
```

Stepwise regression for model with interactions

```
## Start:  AIC=257.63
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##          exng + oldpeak + slp + caa + thall + age * sex + age * cp +
##          trtbps * age + chol * age + fbs * age + exng * age + sex *
##          chol + chol * cp + chol * fbs + chol * exng
##
##              Df Deviance    AIC
## - age:cp      3   193.11 253.11
## - cp:chol     3   194.15 254.15
## - age:chol    1   191.64 255.64
## - age:sex     1   191.71 255.71
## - age:trtbps  1   191.79 255.79
## - sex:chol    1   192.21 256.21
## - chol:exng   1   192.23 256.23
## - age:exng    1   192.24 256.24
## - restecg     2   194.25 256.25
## - slp         2   194.70 256.70
## - chol:fbs    1   192.71 256.71
## - age:fbs     1   193.08 257.08
## <none>        191.63 257.63
## - thalachh    1   193.94 257.94
## - oldpeak     1   196.97 260.97
## - thall       2   201.97 263.97
## - caa         1   207.81 271.81
##
## Step:  AIC=253.11
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##          exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##          age:chol + age:fbs + age:exng + sex:chol + cp:chol + chol:fbs +
##          chol:exng
##
##              Df Deviance    AIC
## - cp:chol     3   195.40 249.40
## - age:chol    1   193.12 251.12
## - age:sex     1   193.35 251.35
## - age:trtbps  1   193.38 251.38
## - age:exng    1   193.40 251.40
## - chol:exng   1   193.71 251.71
## - sex:chol    1   193.79 251.79
## - slp         2   196.04 252.04
## - chol:fbs    1   194.15 252.15
## - restecg     2   196.35 252.35
## - age:fbs     1   194.49 252.49
## <none>        193.11 253.11
## - thalachh    1   195.46 253.46
## - oldpeak     1   198.97 256.97
## + age:cp      3   191.63 257.63
## - thall       2   205.82 261.82
```

```

## - caa          1    208.37 266.37
##
## Step: AIC=249.4
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##          exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##          age:chol + age:fbs + age:exng + sex:chol + chol:fbs + chol:exng
##
##              Df Deviance    AIC
## - age:chol    1    195.41 247.41
## - chol:exng   1    195.70 247.70
## - age:sex     1    195.73 247.73
## - age:trtbps  1    195.73 247.73
## - age:exng    1    195.82 247.82
## - restecg     2    198.48 248.48
## - slp         2    198.52 248.52
## - age:fbs     1    196.54 248.54
## - sex:chol    1    196.91 248.91
## - chol:fbs    1    197.01 249.01
## <none>        195.40 249.40
## - thalachh    1    198.18 250.18
## + cp:chol     3    193.11 253.11
## - oldpeak     1    201.40 253.40
## + age:cp      3    194.15 254.15
## - thall       2    209.82 259.82
## - cp          3    215.74 263.74
## - caa         1    211.75 263.75
##
## Step: AIC=247.41
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##          exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##          age:fbs + age:exng + sex:chol + chol:fbs + chol:exng
##
##              Df Deviance    AIC
## - chol:exng   1    195.70 245.70
## - age:trtbps  1    195.74 245.74
## - age:sex     1    195.74 245.74
## - age:exng    1    195.84 245.84
## - restecg     2    198.49 246.49
## - slp         2    198.53 246.53
## - age:fbs     1    196.59 246.59
## - chol:fbs    1    197.02 247.02
## - sex:chol    1    197.35 247.35
## <none>        195.41 247.41
## - thalachh    1    198.18 248.18
## + age:chol    1    195.40 249.40
## + cp:chol     3    193.12 251.12
## - oldpeak     1    201.44 251.44
## + age:cp      3    194.15 252.15
## - thall       2    209.83 257.83
## - cp          3    215.91 261.91
## - caa         1    212.28 262.29
##
## Step: AIC=245.7
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +

```

```

##      exng + oldpeak + slp + caa + thall + age:sex + age:trtbps +
##      age:fbs + age:exng + sex:chol + chol:fbs
##
##           Df Deviance    AIC
## - age:sex      1   196.00 244.00
## - age:trtbps   1   196.05 244.05
## - age:exng     1   196.24 244.24
## - restecg      2   198.74 244.74
## - age:fbs      1   196.80 244.80
## - slp          2   198.87 244.87
## - chol:fbs     1   197.23 245.23
## <none>         195.70 245.70
## - sex:chol     1   197.93 245.93
## - thalachh     1   198.51 246.51
## + chol:exng    1   195.41 247.41
## + age:chol     1   195.70 247.70
## + cp:chol      3   193.71 249.71
## - oldpeak      1   201.82 249.82
## + age:cp       3   194.51 250.51
## - thall        2   210.42 256.42
## - cp           3   216.37 260.37
## - caa          1   212.95 260.95
##
## Step:  AIC=244
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##      exng + oldpeak + slp + caa + thall + age:trtbps + age:fbs +
##      age:exng + sex:chol + chol:fbs
##
##           Df Deviance    AIC
## - age:trtbps   1   196.33 242.33
## - age:exng     1   196.55 242.55
## - restecg      2   198.80 242.80
## - slp          2   198.97 242.97
## - age:fbs      1   197.09 243.09
## - chol:fbs     1   197.51 243.51
## <none>         196.00 244.00
## - sex:chol     1   198.05 244.05
## - thalachh     1   198.78 244.78
## + age:sex      1   195.70 245.70
## + chol:exng    1   195.74 245.74
## + age:chol     1   195.99 245.99
## + cp:chol      3   193.96 247.96
## - oldpeak      1   202.26 248.26
## + age:cp       3   194.62 248.62
## - thall        2   210.53 254.53
## - cp           3   216.44 258.44
## - caa          1   213.43 259.43
##
## Step:  AIC=242.33
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##      exng + oldpeak + slp + caa + thall + age:fbs + age:exng +
##      sex:chol + chol:fbs
##
##           Df Deviance    AIC

```

```

## - age:exng      1    196.84 240.84
## - restecg      2    199.21 241.21
## - slp          2    199.40 241.40
## - age:fbs      1    197.63 241.63
## - chol:fbs     1    197.78 241.78
## - sex:chol     1    198.23 242.23
## <none>         196.33 242.33
## - trtbps      1    198.57 242.57
## - thalachh    1    199.29 243.29
## + age:trtbps  1    196.00 244.00
## + chol:exng   1    196.05 244.05
## + age:sex     1    196.05 244.05
## + age:chol    1    196.32 244.32
## + cp:chol     3    194.23 246.23
## - oldpeak     1    202.42 246.42
## + age:cp      3    194.84 246.84
## - thall       2    211.22 253.22
## - cp          3    216.90 256.90
## - caa         1    213.53 257.53
##
## Step: AIC=240.84
## output ~ age + sex + cp + trtbps + chol + fbs + restecg + thalachh +
##          exng + oldpeak + slp + caa + thall + age:fbs + sex:chol +
##          chol:fbs
##
##           Df Deviance    AIC
## - restecg   2    199.47 239.47
## - slp       2    200.00 240.00
## - age:fbs   1    198.09 240.09
## - chol:fbs  1    198.20 240.20
## - sex:chol  1    198.72 240.72
## <none>      196.84 240.84
## - trtbps   1    199.15 241.15
## - thalachh  1    199.68 241.68
## - exng     1    199.84 241.84
## + age:exng  1    196.33 242.33
## + chol:exng 1    196.46 242.46
## + age:sex   1    196.54 242.54
## + age:trtbps 1    196.55 242.55
## + age:chol  1    196.83 242.83
## - oldpeak   1    202.57 244.57
## + cp:chol   3    194.66 244.66
## + age:cp    3    195.77 245.77
## - thall     2    211.25 251.25
## - cp        3    217.75 255.75
## - caa       1    214.58 256.58
##
## Step: AIC=239.47
## output ~ age + sex + cp + trtbps + chol + fbs + thalachh + exng +
##          oldpeak + slp + caa + thall + age:fbs + sex:chol + chol:fbs
##
##           Df Deviance    AIC
## - age:fbs   1    200.68 238.68
## - chol:fbs  1    201.00 239.00

```

```

## - sex:chol      1    201.10 239.10
## - slp           2    203.16 239.16
## <none>          199.47 239.47
## - trtbps        1    202.14 240.14
## - thalachh       1    202.35 240.35
## - exng           1    202.47 240.47
## + restecg        2    196.84 240.84
## + age:trtbps     1    199.11 241.11
## + chol:exng       1    199.13 241.13
## + age:exng        1    199.21 241.21
## + age:sex         1    199.41 241.41
## + age:chol        1    199.47 241.47
## - oldpeak        1    205.22 243.22
## + cp:chol         3    197.38 243.38
## + age:cp          3    197.94 243.94
## - thall           2    212.82 248.82
## - cp              3    220.30 254.30
## - caa             1    216.99 254.99
##
## Step:  AIC=238.68
## output ~ age + sex + cp + trtbps + chol + fbs + thalachh + exng +
##          oldpeak + slp + caa + thall + sex:chol + chol:fbs
##
##           Df Deviance    AIC
## - age      1    200.71 236.71
## - sex:chol  1    202.15 238.15
## - chol:fbs  1    202.33 238.33
## - slp       2    204.65 238.65
## <none>      200.68 238.68
## + age:fbs   1    199.47 239.47
## - exng      1    203.53 239.53
## - trtbps    1    203.71 239.71
## - thalachh  1    203.74 239.74
## + restecg   2    198.09 240.09
## + age:trtbps 1    200.11 240.11
## + chol:exng  1    200.43 240.43
## + age:exng   1    200.44 240.44
## + age:sex    1    200.62 240.62
## + age:chol   1    200.63 240.63
## - oldpeak    1    206.13 242.13
## + cp:chol    3    198.88 242.88
## + age:cp     3    199.03 243.03
## - thall      2    213.14 247.14
## - cp         3    221.07 253.07
## - caa        1    217.76 253.76
##
## Step:  AIC=236.7
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
##          slp + caa + thall + sex:chol + chol:fbs
##
##           Df Deviance    AIC
## - sex:chol  1    202.19 236.19
## - chol:fbs  1    202.34 236.34
## - slp       2    204.68 236.68

```



```

## <none>          200.71 236.71
## - exng          1   203.54 237.54
## - trtbps        1   203.96 237.96
## + restecg       2   198.09 238.09
## + chol:exng     1   200.46 238.46
## - thalachh      1   204.49 238.49
## + age           1   200.68 238.68
## - oldpeak       1   206.16 240.16
## + cp:chol       3   198.93 240.93
## - thall         2   213.23 245.23
## - cp            3   221.08 251.08
## - caa           1   218.80 252.80
##
## Step:  AIC=236.19
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
##         slp + caa + thall + chol:fbs
##
##           Df Deviance    AIC
## - chol:fbs   1   203.77 235.77
## <none>        202.19 236.19
## + sex:chol   1   200.71 236.71
## - exng       1   205.00 237.00
## - slp        2   207.10 237.10
## - trtbps     1   205.57 237.57
## + chol:exng  1   201.74 237.74
## + restecg    2   199.80 237.80
## - thalachh   1   205.80 237.80
## + age        1   202.15 238.15
## - oldpeak    1   207.14 239.14
## + cp:chol    3   199.58 239.58
## - thall      2   214.32 244.32
## - sex        1   212.73 244.73
## - cp         3   223.47 251.47
## - caa        1   220.29 252.29
##
## Step:  AIC=235.77
## output ~ sex + cp + trtbps + chol + fbs + thalachh + exng + oldpeak +
##         slp + caa + thall
##
##           Df Deviance    AIC
## - fbs        1   203.88 233.88
## <none>        203.77 235.77
## - chol       1   205.86 235.86
## + chol:fbs   1   202.19 236.19
## + sex:chol   1   202.34 236.34
## - slp        2   208.59 236.59
## - exng       1   206.71 236.71
## - trtbps     1   206.95 236.95
## + restecg    2   201.19 237.19
## - thalachh   1   207.31 237.31
## + chol:exng  1   203.45 237.45
## + age        1   203.75 237.75
## + cp:chol    3   200.74 238.74
## - oldpeak    1   208.83 238.83

```

```

## - sex          1    213.77 243.77
## - thall        2    215.83 243.83
## - cp           3    224.60 250.60
## - caa          1    222.60 252.60
##
## Step:  AIC=233.88
## output ~ sex + cp + trtbps + chol + thalachh + exng + oldpeak +
##      slp + caa + thall
##
##           Df Deviance    AIC
## <none>          203.88 233.88
## - chol          1    205.93 233.93
## + sex:chol      1    202.46 234.46
## - slp           2    208.63 234.63
## - exng          1    206.75 234.75
## - trtbps        1    206.96 234.96
## + restecg       2    201.34 235.34
## - thalachh      1    207.44 235.44
## + chol:exng     1    203.59 235.59
## + fbs           1    203.77 235.77
## + age           1    203.86 235.86
## + cp:chol       3    201.08 237.08
## - oldpeak       1    209.12 237.12
## - sex           1    213.78 241.78
## - thall         2    216.18 242.18
## - cp            3    226.06 250.06
## - caa           1    222.65 250.65
##
##
## Call:  glm(formula = output ~ sex + cp + trtbps + chol + thalachh +
##      exng + oldpeak + slp + caa + thall, family = "binomial",
##      data = newheart)
##
## Coefficients:
##      (Intercept)                sexF          cpatypical angina
##           1.025922                1.535349                1.000189
##      cpnon-anginal pain          cpasymptomatic                trtbps
##           1.943932                1.965324                -0.017488
##           chol                thalachh                exngNo
##          -0.005343                0.018627                0.722047
##          oldpeak                slpflat                slpdownsloping
##          -0.484829                -0.711536                0.228519
##           caa          thallfixed defect  thallreversible defect
##          -0.817229                -0.032660                -1.345274
##
## Degrees of Freedom: 300 Total (i.e. Null);  286 Residual
## Null Deviance:          414.8
## Residual Deviance: 203.9    AIC: 233.9

```

Model Comparision

I noticed when adding interactions to the model the significance of the variables in the model became less effective. We can see this by looking at the both the p-values in the wald test. All the p-values for the model

with interactions are significantly more higher than the additive model. We can also see that When running step wise regression on the model with interactions. It eliminated all the interaction terms because they were insignificant to the model and gave us back the additive model. This is telling us that the additive model will be more viable to use for the analysis. Thus after evaluating both models we will stick with the additive model for further analysis.

```
## [1] "R-squared: 0.508545330225056"
```

Model evaluation

VIF

Since our selected model is the additive model we can now use the model to answer the question. Which predictor influences the factors of having a heart attack. As mentioned before during the correlation test we notice there was some aspects of multicollinearity in the dataset. Lets check the VIF of the additive model. In statistics, the variance inflation factor is the quotient of the variance in a model with multiple terms by the variance of a model with one term alone. It quantifies the severity of multicollinearity in an ordinary least squares regression analysis

##		GVIF	Df	$GVIF^{1/(2*Df)}$
##	sex	1.491120	1	1.221114
##	cp	1.569147	3	1.077980
##	trtbps	1.094189	1	1.046035
##	chol	1.187864	1	1.089892
##	thalachh	1.318093	1	1.148082
##	exng	1.176216	1	1.084535
##	oldpeak	1.502516	1	1.225772
##	slp	1.805862	2	1.159234
##	caa	1.150145	1	1.072448
##	thall	1.312593	2	1.070367

Since the VIF score of our predictors are less than 10. There is no aspects of multicollinearity in our model.

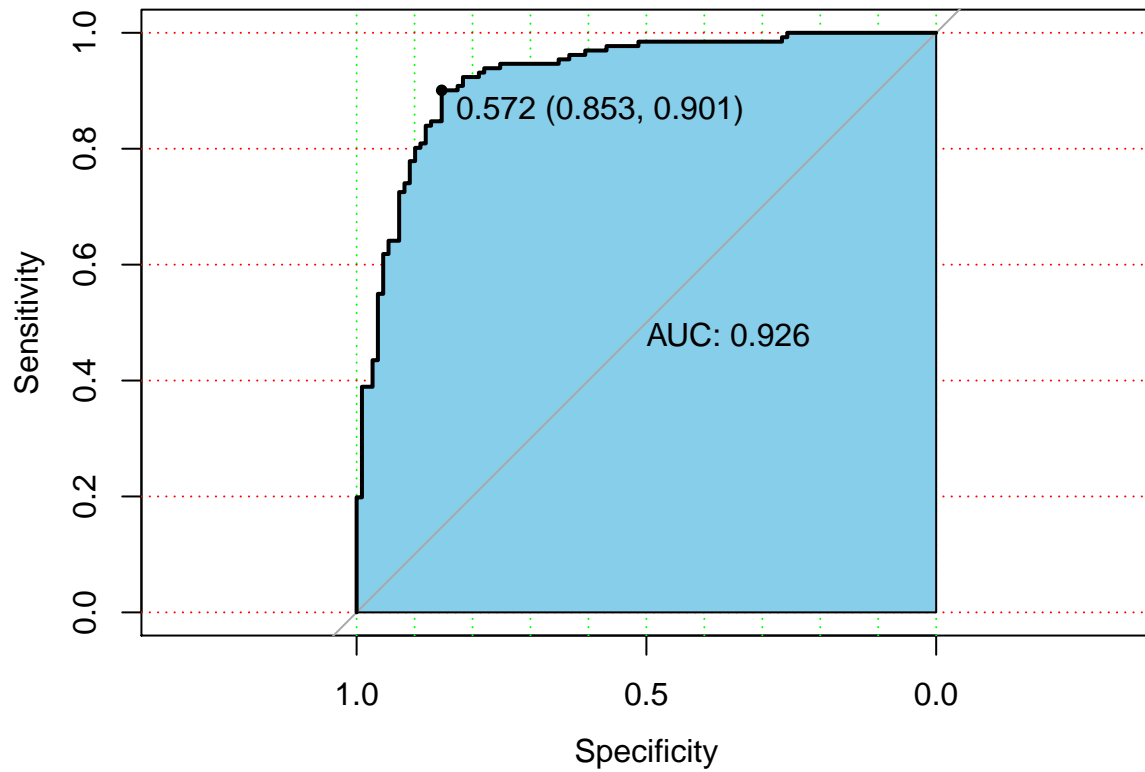
Model Analysis

ROC Curve for Logistic Regression

The ROC curve shows the trade-off between sensitivity (or TPR) and specificity ($1 - \text{FPR}$). Classifiers that give curves closer to the top-left corner indicate a better performance. As a baseline, a random classifier is expected to give points lying along the diagonal ($\text{FPR} = \text{TPR}$). The closer the curve comes to the 45-degree diagonal of the ROC space, the less accurate the test. To compare different classifiers, it can be useful to summarize the performance of each classifier into a single measure. One common approach is to calculate the area under the ROC curve, which is abbreviated to AUC

```
## Setting levels: control = Less Chance, case = More Chance
```

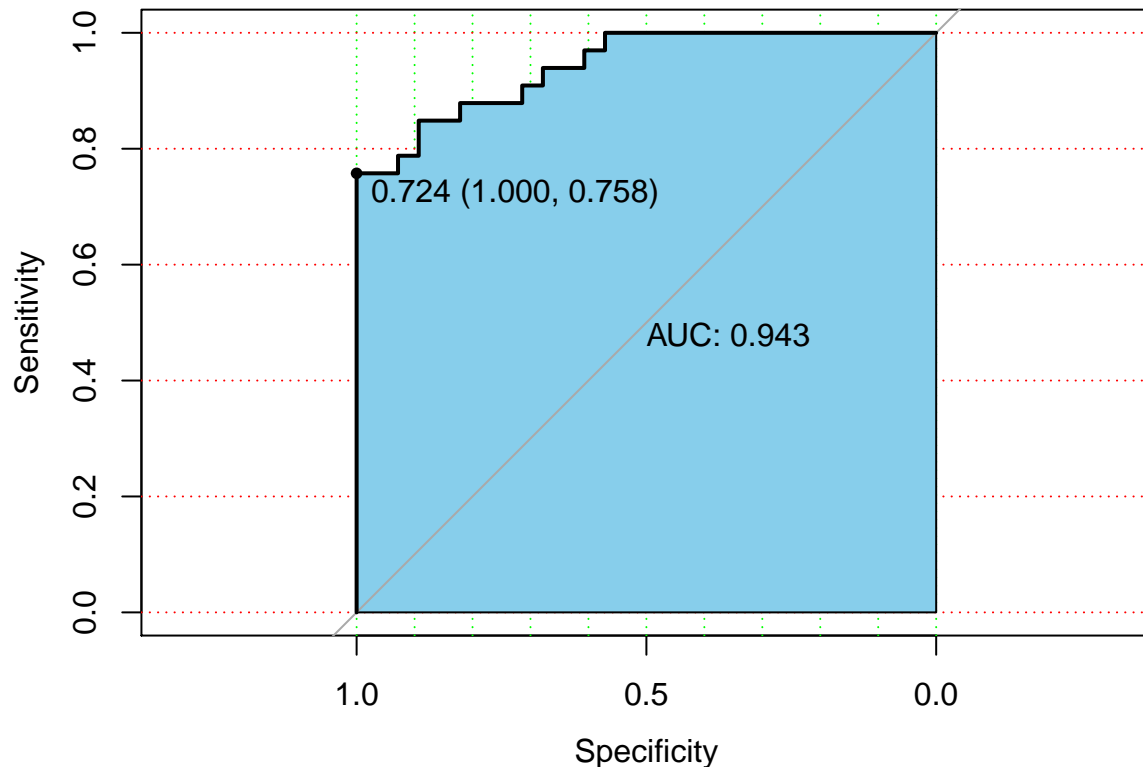
```
## Setting direction: controls < cases
```



The AUC on training set is 0.918 which is approximately 92%, This is an indication that the model prediction performance is good.

```
## Setting levels: control = Less Chance, case = More Chance
```

```
## Setting direction: controls < cases
```

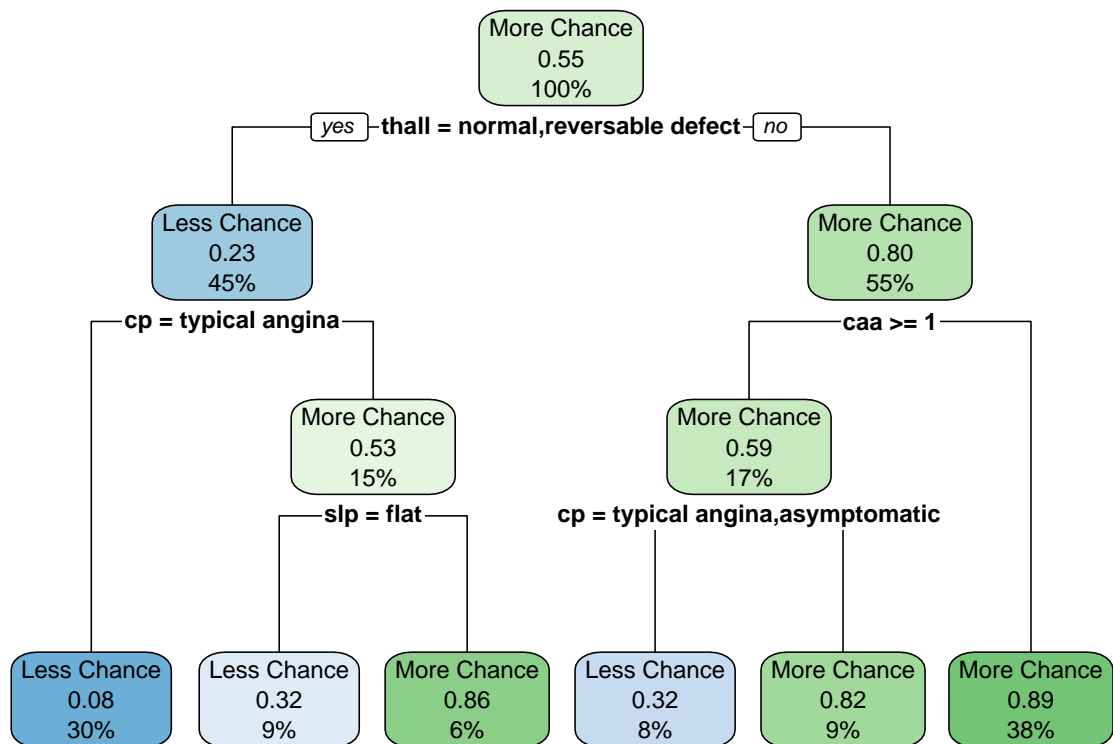


The AUC on testing set is 0.943 which is approximately 94%. This is an indication that the model prediction performance is good.

Overall comparing the model performance on both the testing and training set we get similar performances which tells us that the model we have is able to classify whether the patient is highly in risk of having a heart attack or less in risk of having a heart attack, based on logistic regression.

Decision Tree Classification

We will use our additive model for decision tree classification also. The Decision tree builds classification or regression models in the form of a tree structure. It breaks down a dataset into smaller and smaller subsets while at the same time an associated decision tree is incrementally developed. The Decision trees can handle both categorical and numerical data.



At the top is the overall percentage of patients getting heart attacks. It shows the proportion of patients who have a higher chance of receiving a heart attack to patients having a less chance of receiving a heart attack. 53% of the patients have a higher chance of receiving a heart attack. You can keep going down the nodes to understand what features impact the chances of having a higher chance of a heart attack to having a less chance of having a heart attack. For example, if it's a fixed defect and if the chest pain type is asymptomatic then there is a 91% chance of having a heart attack.

Making A Prediction

Accuracy of test set

```
##          predict_unseen
##          Less Chance More Chance
## Less Chance          24          4
## More Chance           8          25
```

Confusion matrix of the patients who have more chance of a heart attack and the patients who have a less chance of a heart attack using the testing data set.

```
## [1] "Accuracy for test 0.80327868852459"
```

Accuracy of training set

```
##          predict_unseen1
##          Less Chance More Chance
```

##	Less Chance	93	16
##	More Chance	19	112

```
## [1] "Accuracy for train 0.8541666666666667"
```

Conclusion

Comparing the performance of our model through logistic regression and using the decision tree method we can see that the model performs well to predict whether the patient is classified in having a higher chance of getting a heart attack to having a less chance of having a heart attack. We can also see that Logistic regression seems to be more viable since it has a higher chance of predicting more or less chance of having a heart attack compared to the decision tree method. Finally, we see that the predictors that show the most influence to our independent variable 'output' is sex, cp, trtbps, chol, thalachh, exng, oldpeak, slp, caa and the thall. Theoretically speaking this makes sense. Factors such as chest pain, cholesterol levels, etc, are related to heart attacks. Some recommendations that will probably improve the performance of the model is having more meaningful predictors in the data set for detecting heart attacks leading to more accuracy in model performance.