# COM SCI 132 Week 1

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# Compilers vs Interpreters

- Compilers compile all the code into an executable file, and later, the OS can run the program straight through
- Interpreters read and execute code at the same time.

# Compilers

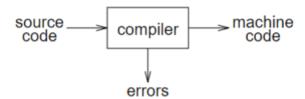
# Qualities

What are some important qualities of a compiler?

- 1. Correct code
- 2. Output runs fast
- 3. Compiler runs fast
- 4. Compile time proportional to program size
- 5. Support for separate compilation
- 6. Good diagnostics for syntax errors
- 7. Works well with the debugger
- 8. Good diagnostics for flow anomalies
- 9. Cross language calls
- 10. Consistent, predictable optimization

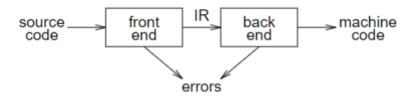
### Abstract view

- Implications:
  - recognize legal (and illegal) programs
  - generate correct code
  - manage storage of all variables and code
  - agreement on format for object (or assembly) code
  - Big step up from assembler to higher level notations



# Two-pass compilers

• Two pass compilers feature an \*intermediate representation\* (IR).



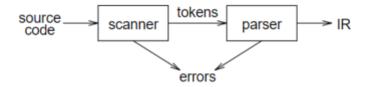
- Implications
  - Intermediate representation (IR)
  - Front end maps legal code into IR
  - Back end maps IR onto target machine
  - Simplify retargeting
  - Allows multiple front ends
  - Multiple passes  $\Rightarrow$  better code

### Front end

### Responsibilities:

- Recognize legal procedure
- Report errors
- Produce IR
- Preliminary storage map
- Shape the code for the back end

Much of front end construction can be automated.



#### Scanner:

• Maps characters into tokens - the basic unit of syntax

$$x = x + y;$$

becomes

$$=  + ;$$

- character string value for a token is a lexeme
- typical tokens: number, id, +, -, \*, /, do, end
- eliminates white space (tabs, blanks, comments)
- a key issue is speed  $\Rightarrow$  use specialized recognizer (as opposed to lex)

#### Parser:

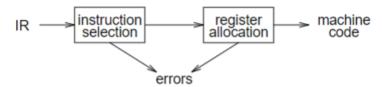
- recognize context-free syntax
- guide context-sensitive analysis
- construct IR(s)
- produce meaningful error messages
- ullet attempt error correction

Parser generators mechanize much of the work.

#### Back end

- translate IR into target machine code
- choose instructions for each IR operation
- decide what to keep in registers at each point
- ensure conformance with system interfaces

Automation has been less successful here.



#### Instruction Selection:

- produce compact, fast code
- use available addressing modes
- pattern matching problem
  - ad hoc techniques
  - tree pattern matching
  - string pattern matching
  - dynamic programming

### Register Allocation:

• have value in a register when used

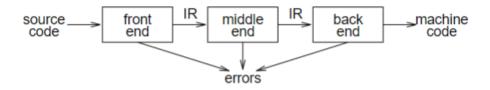
- limited resources
- changes instruction choices
- can move loads and stores
- optimal allocation is difficult

Modern allocators often use an analogy to graph coloring

# Optimizing compiler

Code improvement:

- $\bullet\,$  analyzes and changes IR
- goal is to reduce runtime
- must preserve values

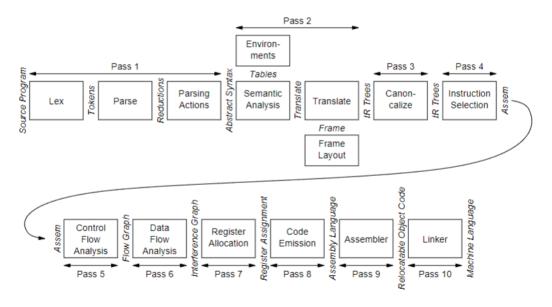


### Optimizer (middle end)

Modern optimizers are usually built as a set of passes. Typical passes:

- ullet constant propagation and folding
- code motion
- reduction of operator strength
- common subexpression elimination
- ullet redundant store elimination
- dead code elimination

# Compiler Example and Phases



Lex	Break source file into individual words, or tokens			
Parse	Analyse the phrase structure of program			
Parsing Actions	Build a piece of abstract syntax tree for each phrase			
Semantic Analysis	Determine what each phrase means, relate uses of variables to their definitions,			
	check types of expressions, request translation of each phrase			
Frame Layout	Place variables, function parameters, etc., into activation records (stack frames)			
	in a machine-dependent way			
Translate	Produce intermediate representation trees (IR trees), a notation that is not tie			
	to any particular source language or target machine			
Canonicalize	Hoist side effects out of expressions, and clean up conditional branches, for			
	convenience of later phases			
Instruction Selection	Group IR-tree nodes into clumps that correspond to actions of target-machine			
	instructions			
Control Flow Analysis	Analyse sequence of instructions into control flow graph showing all possible			
	flows of control program might follow when it runs			
Data Flow Analysis	Gather information about flow of data through variables of program; e.g., live-			
	ness analysis calculates places where each variable holds a still-needed (live)			
	value			
Register Allocation	Choose registers for variables and temporary values; variables not simultane-			
	ously live can share same register			
Code Emission	Replace temporary names in each machine instruction with registers			

# Lexical Analysis

# Patterns for the Scanner

Recall the scanner in the front end compiler.

A scanner must recognize various parts of the language's syntax For example, the easy parts: white space:

keywords and operators

comments:

Other parts are much harder: identifiers

• alphabetic followed by k alphanumerics  $(\_, \$, \&, ...)$ 

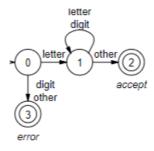
numbers

- integers: 0 or digit from 1-9 followed by digits from 0-9
- $\bullet$  decimals: integer '.' digits from 0-9
- reals: (integer or decimal) 'E' (+ or -) digits from 0-9
- complex: '(' real ',' real ')'

These can be done easily with REGEX.

# Recognizers

From a regular expression we can construct a deterministic finite automaton (DFA).



- letter  $\rightarrow (a|b|c|\dots|z|A|B|\dots|Z)$
- digit  $\to$  (0|1|2|...|9)
- id  $\rightarrow letter(letter|digit)^*$

### Tables for the Recognizer

To change languages, we can just change tables.

### **Automatic Construction**

Scanner generators automatically construct code from regular-expression-like descriptions

- construct a dfa
- use state minimization techniques
- emit code for the scanner (table driven or direct code)

A key issue in automation is an interface to the parser For example, lex is a scanner generator supplied with UNIX.

- emits C code for scanner
- provides macro definitions for each token (used in the parser)

# LL Parsing

Recall, the role of the Parser, the second part of the front-end compiler.

# Syntax Analysis

Context-free syntax is specified with a context-free grammar. Formally, a CFG G is a 4-tuple  $(V_t, V_n, S, P)$ , where

- $V_t$  is the set of terminal symbols in the grammar. For our purposes,  $V_t$  is the set of tokens returned by the scanner.
- $V_n$ , the nonterminals, is the set of syntactic variables that denote sets of (sub)strings occurring in the language. These are used to impose a structure on the grammar.
- S is the distinguished nonterminal  $(S \in V_n)$  denoting the entire set of strings in L(G). This is sometimes called a *goal symbol*.
- P is a finite set of productions specifying how terminals and non-terminals can be combined to form strings in the language. Each production must have a single non-terminal on its left hand side.

The set  $V = V_t \cup V_n$  is called the *vocabulary* of G.

Grammars are often written in Backus-Naur form (BNF). For example:

This describes simple expressions over numbers and identifiers. In a BNF for a grammar, we represent

- 1. non-temrinals with angle brackets or capital letters
- 2. terminals with typewriter font or underline
- 3. productions as in the example

# Scanning vs. Parsing - where do we draw the line?

Regular expressions are used to classify:

- identifiers, numbers, keywords
- REs are more concise and simpler for tokens than a grammar
- more efficient scanners can be built from REs (DFAs) than grammars

Context-free grammars are used to count:

- brackets: (), begin...end, if...then...else
- imparting structure: expressions

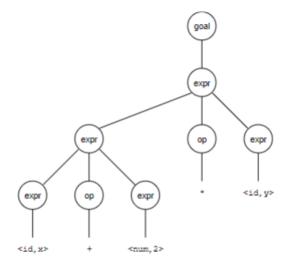
Syntactic analysis is complicated enough: grammar for C has around 200 productions. Factoring out lexical analysis as a separate phase makes the compiler more manageable.

### **Derivations**

We can view the productions of a CFG as rewriting rules. Using our exmple CFG:

- We have derived the sentence x + 2 \* y.
- We denote this <goal>=>\* id + num \* id.
- Such a sequence of rewrites is a derivation or a parse.
- The process of discovering a derivation is called *parsing*.
- At each step, we chose a non-terminal to replace.
- This choice can lead to different derivations.
- Two are of particular interest:
  - leftmost derivation: the leftmost non-terminal is replaced at each step
  - rightmost derivation: the rightmost non-terminal is replaced at each step
- The previous example was a leftmost derivation.

### Precedence



A tree can be generated using the CFG. However, for the tree shown here, the *treewalk evaluation* computes (x + 2) \* y - the wrong answer!

The two derivations point out a problem with the grammar: it has no notion of precedence, or *implied order* or evaluation. To add precedence takes additional machinery:

This grammar enforces a precedence on the derivation:

- $\bullet$  terms *must* be derived from expressions
- forces the "correct" tree

# **Ambiguity**

If a grammar has more than one derivation for a single sentential form, then it is **ambiguous**. Example:

Consider deriving the sentential form:

if 
$$E_1$$
 then if  $E_2$  then  $S_1$  else  $S_2$ 

This has two derivations, which leads to ambiguity that is purely grammatical. It is a *context-free* ambiguity.

### Eliminating Ambiguity

It may be possible to eliminate ambiguities by rearranging the grammar:

if <expr> then <matched> else <unmatched>

This generates the same language as the ambiguous grammar, but applies the common sense rule:

match each else with the closest unmatched then

This is most likely the language designer's intent.

### Overloading

Ambiguity is often due to confusion in the context-free specification. Context-sensitive confusions can arise from *overloading*. For example:

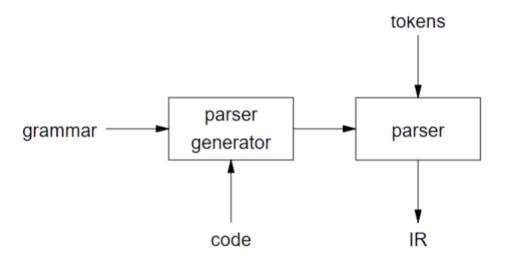
$$a = f(17)$$

In many Algol-like languages, **f** could be a function or subscripted variable. Disambiguating this statement requires context:

- need values of declarations
- not context-free
- really an issue of type

Rather than complicate parsing, we will handle this separately.

### Parsing: the big picture



Our goal is a flexible parser generator system.

# Top-Down vs. Bottom-Up Parsing

Top-down parsers:

- start at the root of derivation tree and fill in
- picks a production and tries to match the input
- may require backtracking
- some grammars are backtrack-free (predictive)

Bottom-up parsers:

- start at the leaves and fill in
- start in a state valid for legal first tokens
- as input is consumed, change state to encode possibilities (recognize valid prefixes)
- use a stack to store both state and sentential forms

# **Top-down Parsing**

A top-down parser starts with the root of the parse tree, labelled with the start or goal symbol of the grammar. To build a parse, it repeats the following steps until the fringe of the parse tree matches the input string

- 1. At a node labelled A, select a production  $A \to \alpha$  and construct the appropriate child for each symbol of  $\alpha$
- 2. When a terminal is added to the fringe that doesn't match the input string, backtrack.
- 3. Find the next node to be expanded (must have a label in  $V_n$ )

The key in selecting the right production in step  $1 \Rightarrow$  should be guided by input string Example using x - 2 \* y:

Prod'n	Sentential form	Inpu	Input				
_	(goal)	†x	_	2	*	у	
1	(expr)	↑x	_	2	*	У	
2	$\langle expr \rangle + \langle term \rangle$	↑x	_	2	*	у	
4	$\langle \text{term} \rangle + \langle \text{term} \rangle$	↑x	_	2	*	у	
7	$\langle factor \rangle + \langle term \rangle$	↑x	_	2	*	У	
9	id + (term)	†x	_	2	*	у	
_	id + (term)	X	<b>↑</b> -	2	*	у	
_	(expr)	↑x	_	2	*	у	
3	$\langle expr \rangle - \langle term \rangle$	↑x	_	2	*	у	
4	$\langle \text{term} \rangle - \langle \text{term} \rangle$	↑x	_	2	*	у	
7	$\langle factor \rangle - \langle term \rangle$	↑x	_	2	*	У	
9	id – (term)	↑x	_	2	*	У	
_	id — (term)	х	1-	2	*	у	
_	id – (term)	х	_	↑2	*	У	
7	id — (factor)	х	_	↑2	*	У	
8	id — num	х	_	↑2	*	У	
_	id - num	X	_	2	↑*	у	
_	id — (term)	Х	_	↑2	*	У	
5	id - (term) * (factor)	x	_	↑2	*	У	
7	id - (factor) * (factor)	x	_	↑2	*	У	
8	id — num ∗ ⟨factor⟩	X	_	†2	*	У	
_	id — num * (factor)	x	_	2	<b>↑</b> *	У	
_	id — num * (factor)	X	_	2	*	↑у	
9	id - num * id	X	_	2	*	1у	
-	id - num * id	X	_	2	*	У	1

Another possible parse for x - 2 \* y

Prod'n	Sentential form	Input
_	⟨goal⟩	↑x - 2 * y
1	⟨expr⟩	↑x - 2 * y
2	$\langle \exp r \rangle + \langle \text{term} \rangle$	↑x - 2 * y
2	$\langle \exp r \rangle + \langle \text{term} \rangle + \langle \text{term} \rangle$	↑x - 2 * y
2	$\langle \exp r \rangle + \langle \text{term} \rangle + \cdots$	↑x - 2 * y
2	$\langle \exp r \rangle + \langle \text{term} \rangle + \cdots$	↑x - 2 * y
2		↑x - 2 * y

If the parser makes the worng choices, expansion doesn't terminate. This isn't a good property for a parser to have. (Parsers should terminate!)

# Left-recursion

Top-down parsers cannot handle left-recursion in a grammar. Formally, a grammar is left-recursive if:

$$\exists A \in V_n \text{ such that } A \Rightarrow^+ A\alpha \text{ for some string } \alpha$$

Our simple expression grammar is left-recursive.

### Eliminating left-recursion

To remove left-recursion, we can transform the grammar. Consider the grammar fragment:

where  $\alpha$  and  $\beta$  do not start with <foo>

We can rewrite this as:

where <br/> <br/> is a new non-terminal. This fragment contains no left-recursion.

**Example:** Our expression grammar contaions two cases of left-recursion.

Applying the transformation gives:

With this grammar, a top-down parser will:

- terminate
- backtrack on some inputs

Although it is longer and harder to read, it factors out left-recursion.

### How much lookahead is needed?

We saw that top-down parsers may need to backtrack when they select the wrong production. Do we need arbitrary lookahead to parse CFGs?

- in general, yes
- use the Earley or Cocke-Younger, Kasami algorithms

Fortunately,

- large subclasses of CFGs can be parsed with limited lookahead
- most programming language constructs can be expressed in a grammar that falls in these subclasses

Among the interesting subclasses are:

- LL(1): left to right scan, left-most derivation, 1-token lookahead
- LR(1): left to right scan, **right**-most derivation, 1-token lookahead

### **Predictive Parsing**

**Basic idea:** For any two productions  $A \to \alpha | \beta$ , we would like a distinct way of choosing the correct production to expand.

For some RHS  $\alpha \in G$ , define FIRST( $\alpha$ ) as the set of tokens that appear first in some string derived form  $\alpha$ . That is, for some  $w \in V_t^*$ ,  $w \in \text{FIRST}(\alpha)$  if and only if  $\alpha \Rightarrow^* w\gamma$ .

**Key property:** Whenever two productions  $A \to \alpha$  and  $A \to \beta$  both appear in the grammar, we would like

$$FIRST(\alpha) \cap FIRST(\beta) = \phi$$

This would allow the parser to make a correct choice with a lookahead of only one symbol! The example grammar has this property!

If a grammar does not have this property, we can transform it to have the property through a process called **left factoring**:

- For each non-terminal A find the longest prefix  $\alpha$  common to two or more of its alternatives.
- if  $\alpha \neq \epsilon$  then replace all of the A productions  $A \to \alpha \beta_1 |\alpha \beta_2| \cdots |\alpha \beta_n|$  with:

$$A \to \alpha A'$$
$$A' \to \beta_1 |\beta_2| \cdots |\beta_n|$$

- where A' is a new non-terminal
- Repeat until no two altrernatives for a single non-terminal have a common prefix.

### Example:

Consider a right-recursive version of the expression grammar:

```
<goal>
             ::= <expr>
             ::= <term> + <expr>
                <term> - <expr>
31
41
                 <term>
5|
             ::= <factor> * <term>
    <term>
6|
              | <factor> / <term>
7|
                <factor>
              1
81
    <factor> ::= num
91
              id
```

To choose between productions 2, 3, and 4, the parser must see past the num or id and look at the +, -, \*, or /.

$$FIRST(2) \cap FIRST(3) \cap FIRST(4) \neq \Phi$$

This grammar fails the test. There are two non-terminals that must be left factored: <expr> and <term>. Applying left factoring gives:

Substituting this back makes it so selection requires only a single token lookahead.

# Generality

Question:

• By left factoring and eliminating left-recursion, can we transform an arbitrary context-free grammar to a form where it can be predictively parsed with a single token lookahead?

Answer:

• Given a context-free grammar that doesn't meet our conditions, it is undecidable whether an equivalent grammar exists that does meet our conditions.

Many context-free languages do not have such a grammar:

$$\{a^n 0b^n | n \ge 1\} \bigcup \{a^n 1b^{2n} | n \ge 1\}$$

Must look past an arbitrary number of a's to discover the 0 or the 1 and so determine the derivation.

# Recursive Descent Parsing

Now, we can produce a simple recursive descent parser from the (right-associative) grammar.

```
Token token;
void eat(char a) {
    if (token == a) {token = next.token(); }
    else { error(); }
void goal() { token = next.token(); expr(); eat(EOF); }
void expr() { term(); expr_prime(); }
void expr_prime() {
    if (token == PLUS) { eat(PLUS); expr(); }
    else if (token == MINUS) { eat(MINUS); expr(); }
    else { }
}
void term() { factor(); term_prime(); }
void term prime() {
    if (token = MULT) { eat(MULT); term(); }
    else if (token = DIV) { eat(DIV); term(); }
    else { }
}
void factor() {
    if (token = NUM) { eat(NUM); }
    else if (token = ID) { eat(ID); }
    else error();
}
```

### **NULLABLE**

For a string  $\alpha$  with grammar symbols, define NULLABLE( $\alpha$ ) as  $\alpha$  can go to  $\epsilon$ .

NULLABLE(
$$\alpha$$
) if and only if ( $\alpha \Rightarrow^* \epsilon$ )

How to compute NULLABLE(U), for  $U \in V_t \cup V_n$ :

- 1. For each U, let NULLABLE(U) be a Boolean variable
- 2. Derive the following constraints:
  - (a) if  $a \in V_t$ , then NULLABLE(a) = false.
  - (b) if  $A \to Y_1 \dots Y_k$  is a production, then  $[\text{NULLABLE}(Y_1) \land \dots \land \text{NULLABLE}(Y_k)] \Rightarrow \text{NULLABLE}(A)$
- 3. Solve the constraints.

$$NULLABLE(X_1 ... X_k) = NULLABLE(X_1) \land \cdots \land NULLABLE(X_k)$$

#### **FIRST**

For a string  $\alpha$  with grammar symbols, define FIRST( $\alpha$ ) as the set of terminal symbols that begin strings derived from  $\alpha$ .

$$FIRST(\alpha) = \{ a \in V_t | \alpha \Rightarrow^* a\beta \}$$

How to compute FIRST(U), for  $U \in V_t \cup V_n$ :

- 1. For each U, let FIRST(U) be a set variable.
- 2. Derive the following constraints:
  - (a) if  $a \in V_t$ , then FIRST(a) = a
  - (b) if  $A \to Y_1 Y_2 \cdots Y_k$  is a production, then

- $FIRST(Y_1) \subseteq FIRST(A)$
- $\forall i : 1 < i \le k$ , if NULLABLE $(Y_1 \cdots Y_{i-1})$ , then FIRST $(Y_i) \subseteq \text{FIRST}(A)$
- 3. Solve the constraints. Go for the  $\subseteq$ -least solution.

$$FIRST(X_1 \cdots X_k) = \bigcup_{i:1 \le i \le k \land NULLABLE(X_1 \cdots X_{i-1})} FIRST(X_i)$$

#### **FOLLOW**

For a non-terminal B, define FOLLOW(B) as the set of terminals that can appear immediately to the right of B in some sentential form.

$$FOLLOW(B) = \{ a \in V_t | G \Rightarrow^* \alpha B \beta \land a \in FIRST(\beta \$) \}$$

How to compute FOLLOW(B):

- 1. For each non-terminal B, let FOLLOW(B) be a set variable.
- 2. Derive the following constraints:
  - (a) if G is the start symbol and \$ is the end-of-file marker, then  $\{\$\}\subseteq FOLLOW(G)$
  - (b) if  $A \to \alpha B\beta$  is a production, then:
    - $FIRST(\beta) \subseteq FOLLOW(B)$
    - if  $NULLABLE(\beta)$ , then  $FOLLOW(A) \subseteq FOLLOW(B)$
- 3. Solve the constraints. Go for the  $\subseteq$ -least solution.

#### LL1 Grammars

**Intuition:** A grammar G is LL(1) if and only if:

• for all non-terminals A, each distinct pair of productions  $(A \to \beta)$  and  $(A \to \gamma)$  satisfies the condition  $FIRST(\beta) \cap FIRST(\gamma) = \emptyset$ .

**Question:** What if NULLABLE(A)?

**Definition:** A grammar G is LL(1) if and only if for each set of productions  $A \to \alpha_1 |\alpha_2| \cdots |\alpha_n|$ 

- 1.  $FIRST(\alpha_1)$ ,  $FIRST(\alpha_2)$ , ...,  $FIRST(\alpha_n)$  are pairwise disjoint, and
- 2. If NULLABLE( $\alpha_i$ ), then for all j, such that  $1 \leq j \leq n \land j \neq i$ : FIRST( $\alpha_j$ ) $\cap$ FOLLOW(A) =  $\emptyset$

If G is  $\epsilon$ -free, condition 1 is sufficient.

Provable facts about LL(1) grammars:

- 1. No left-recursive grammar is LL(1)
- 2. No ambiguous grammar is LL(1)
- 3. Some languages have no LL(1) grammar
- 4. A  $\epsilon$ -free grammar where each alternative expansion for A begins with a distinct terminal is a *simple* LL(1) *grammar*.

#### Example:

$$S \to aS|a$$

is not LL(1) because  $FIRST(aS) = FIRST(a) = \{a\}$ 

$$S \to aS'$$

$$S' \to aS' | \epsilon$$

accepts the same language and is LL(1).