

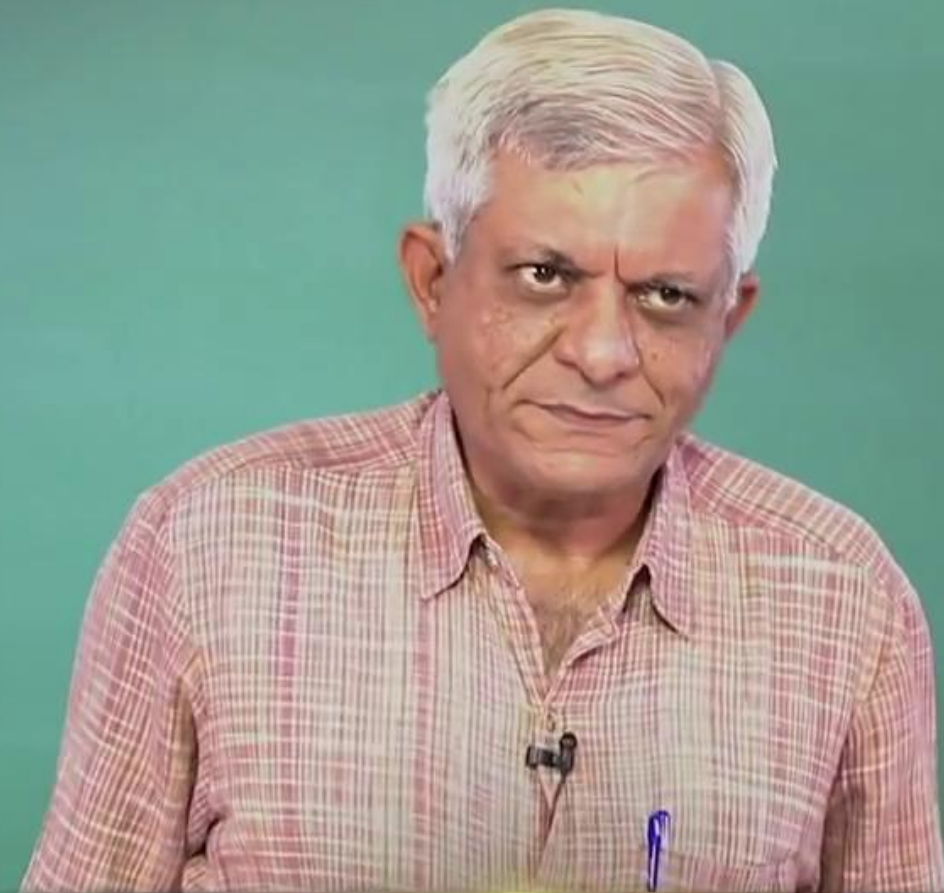
Video Lectures On Artificial Intelligence

Lecture 06 State Space Search Intro

Prof. Deepak Khemani

Department of Computer Science and Engineering
IIT Madras





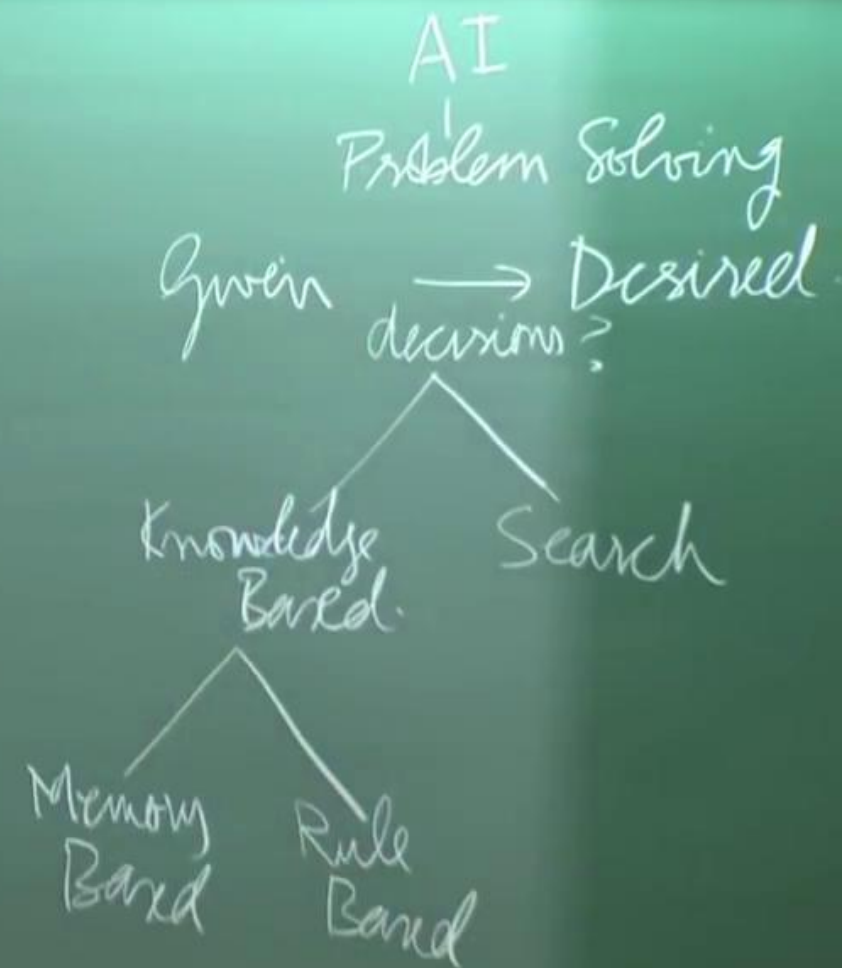
Prof . Deepak Khemani

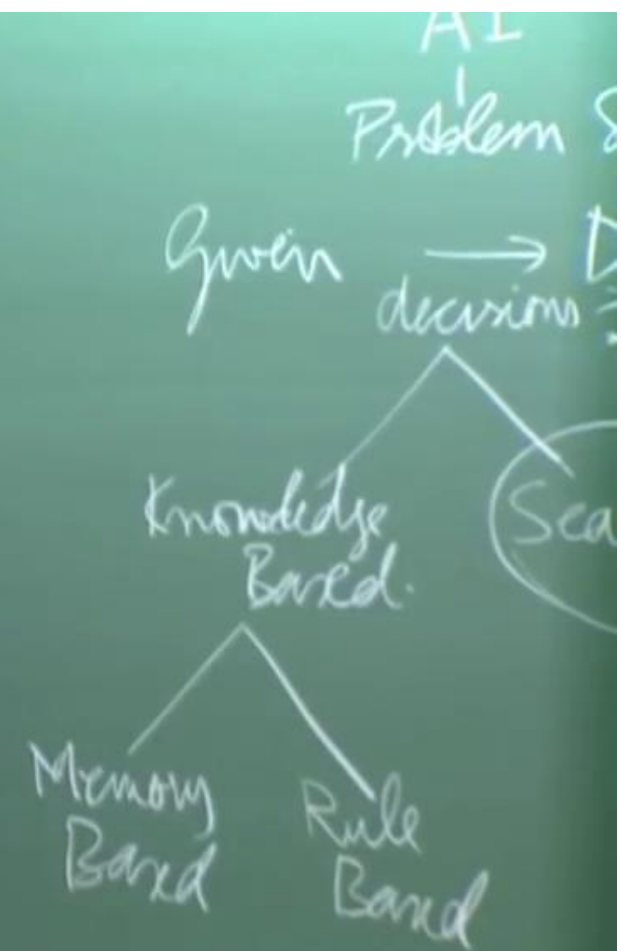
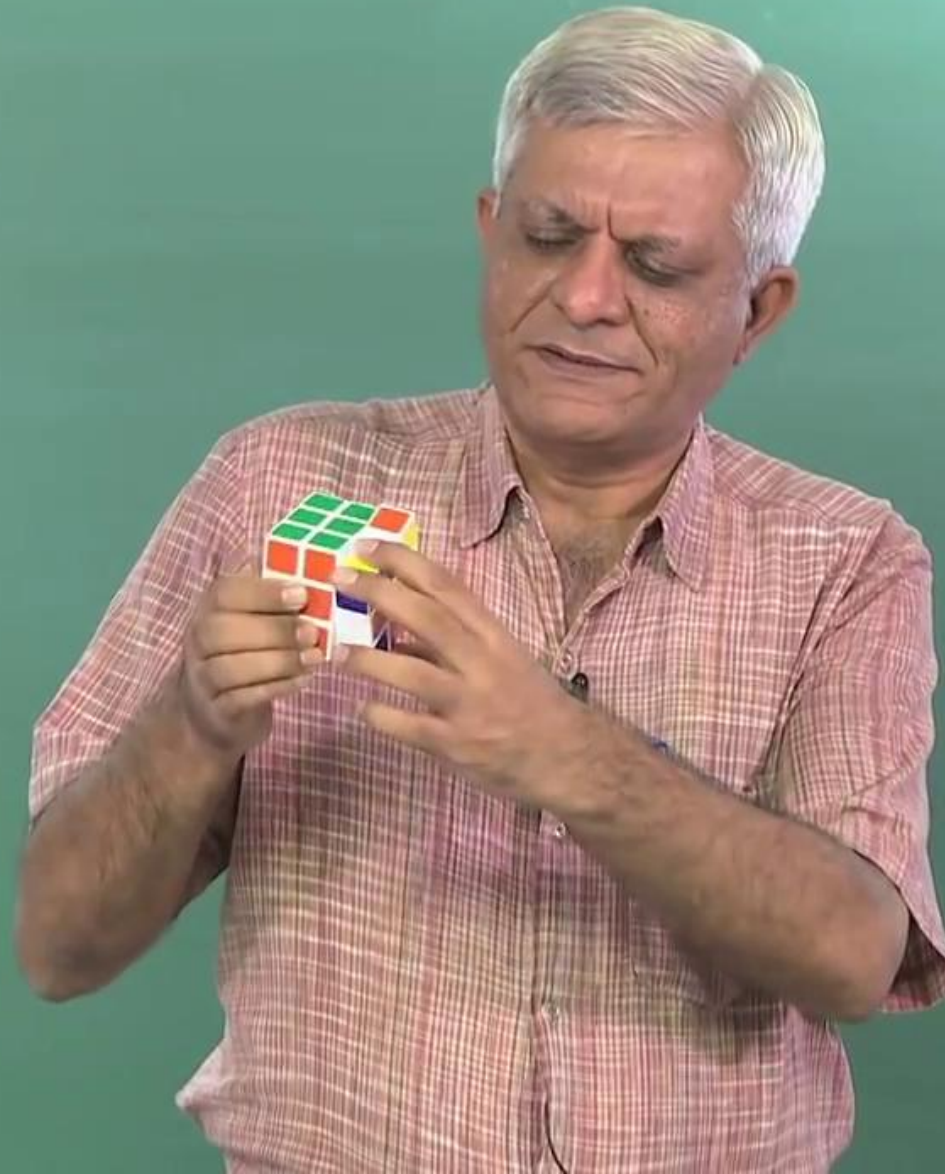
Dept . of . Computer Science and Engineering IIT Madras

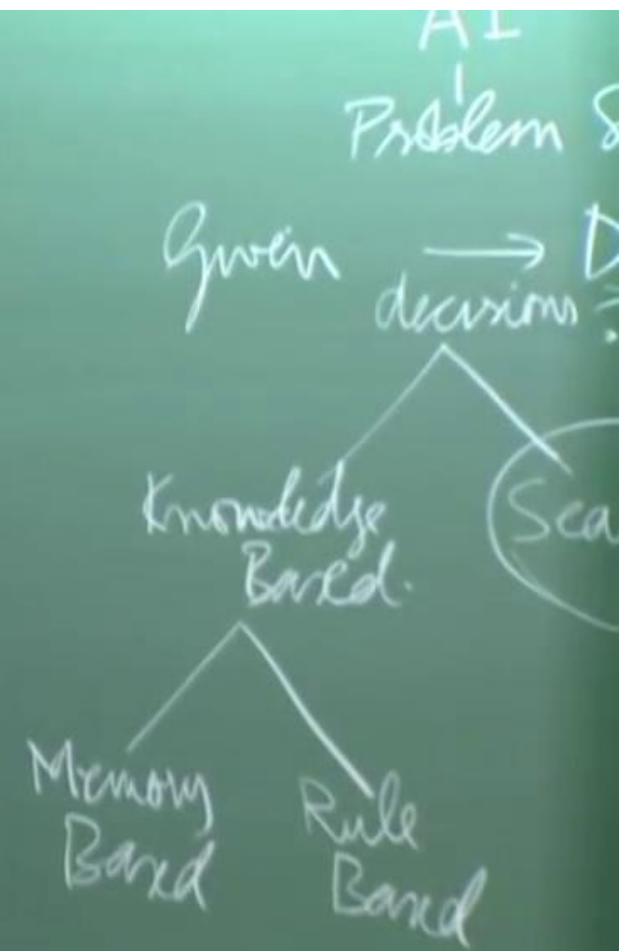
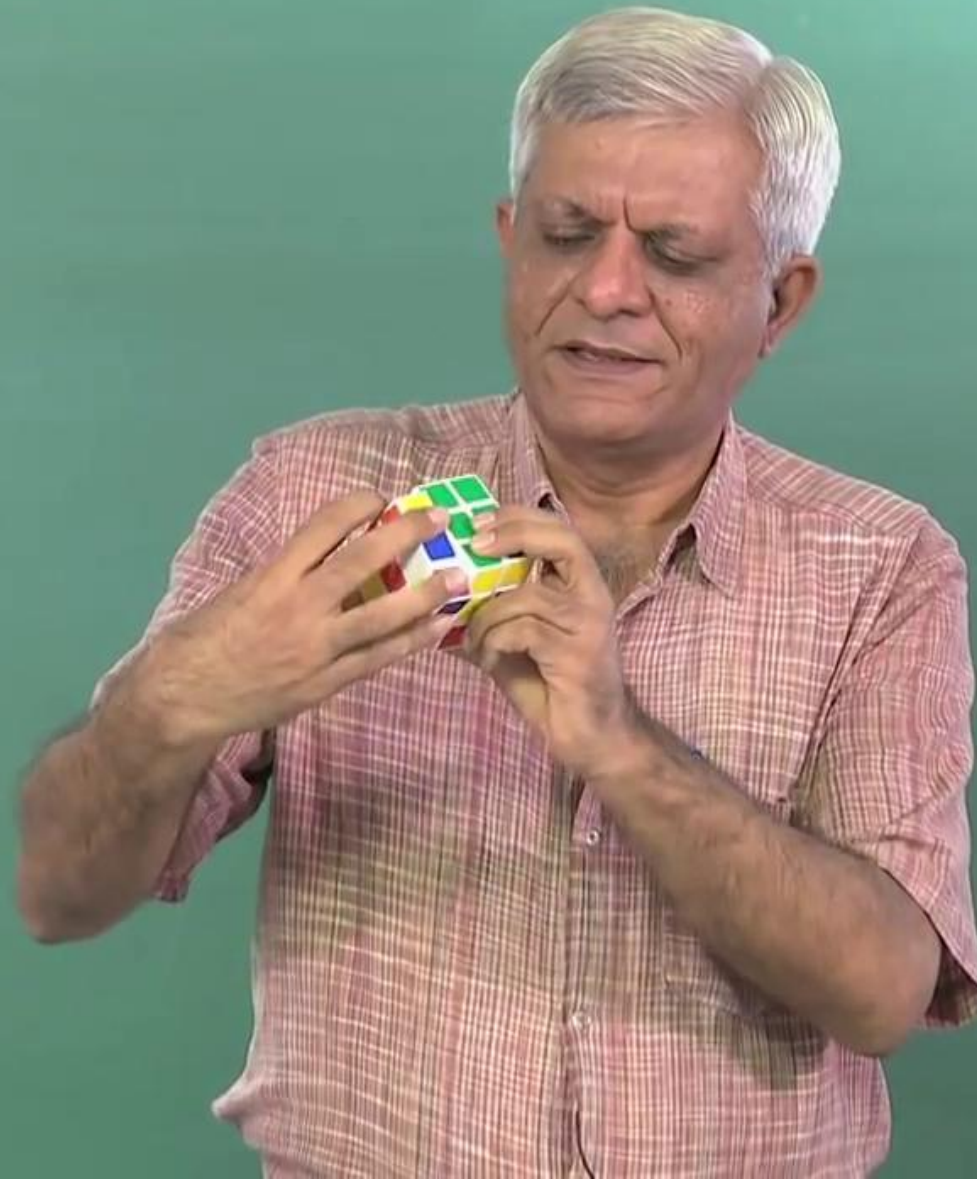


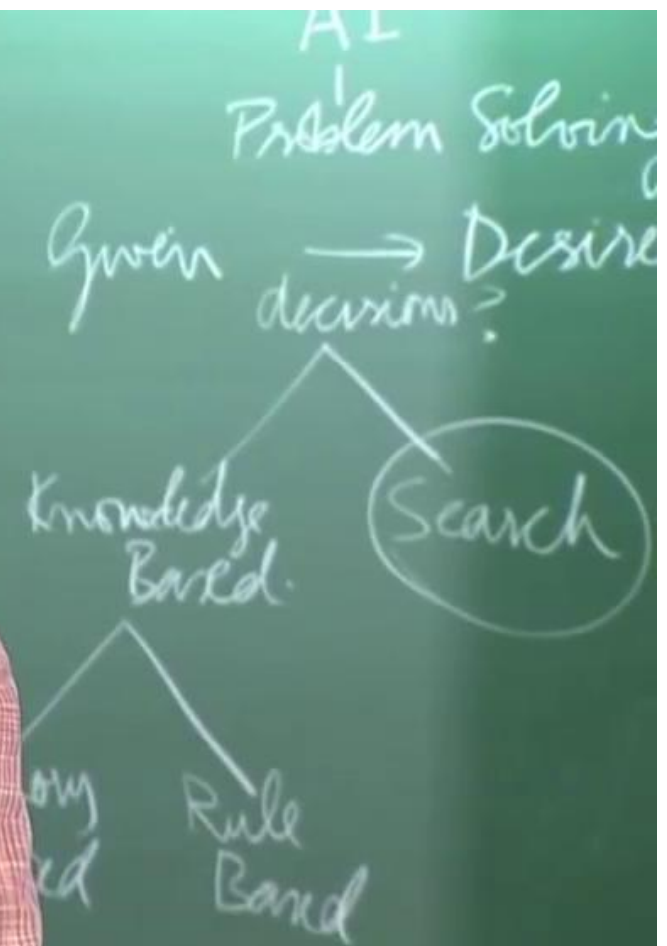
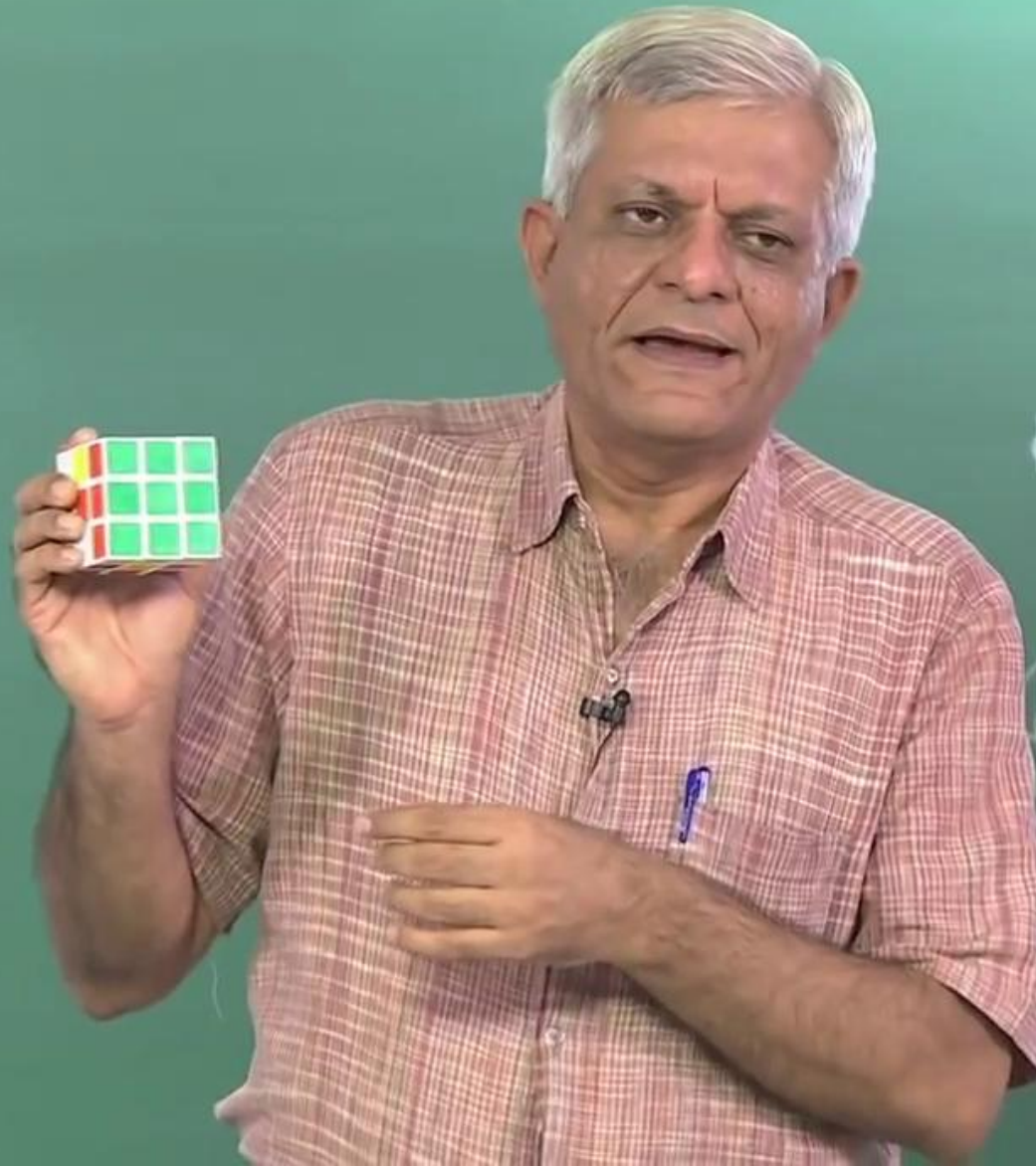
AI
Problem Solving
Given \rightarrow Desired
decision?

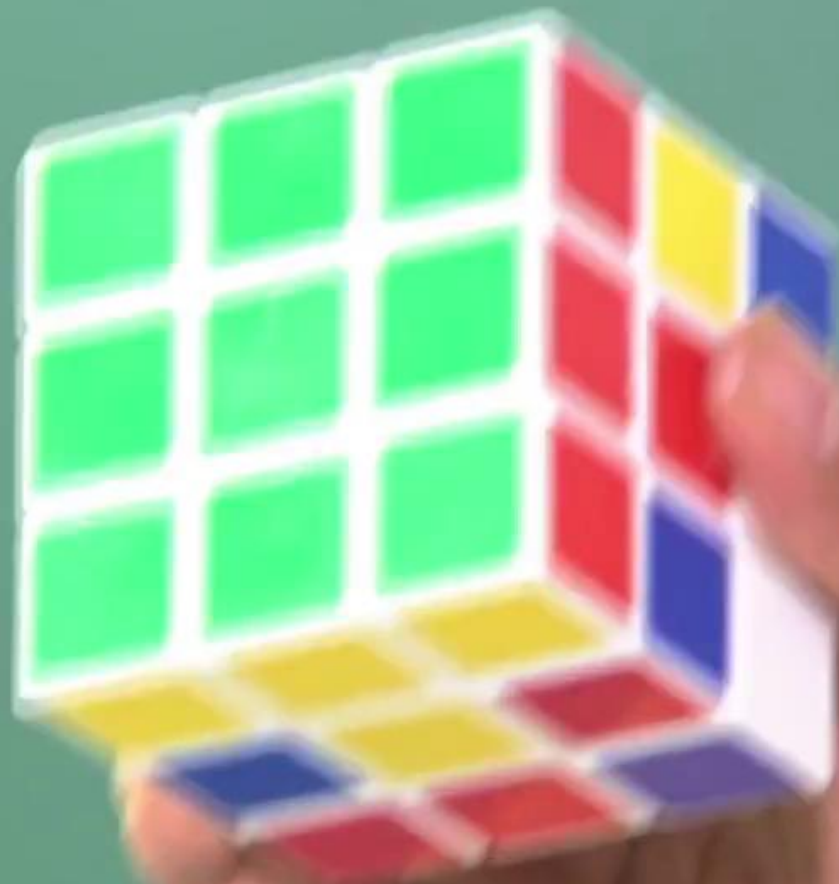
AI
Problem Solving
Given \rightarrow Desired
decisions?
Knowledge
Based. Search

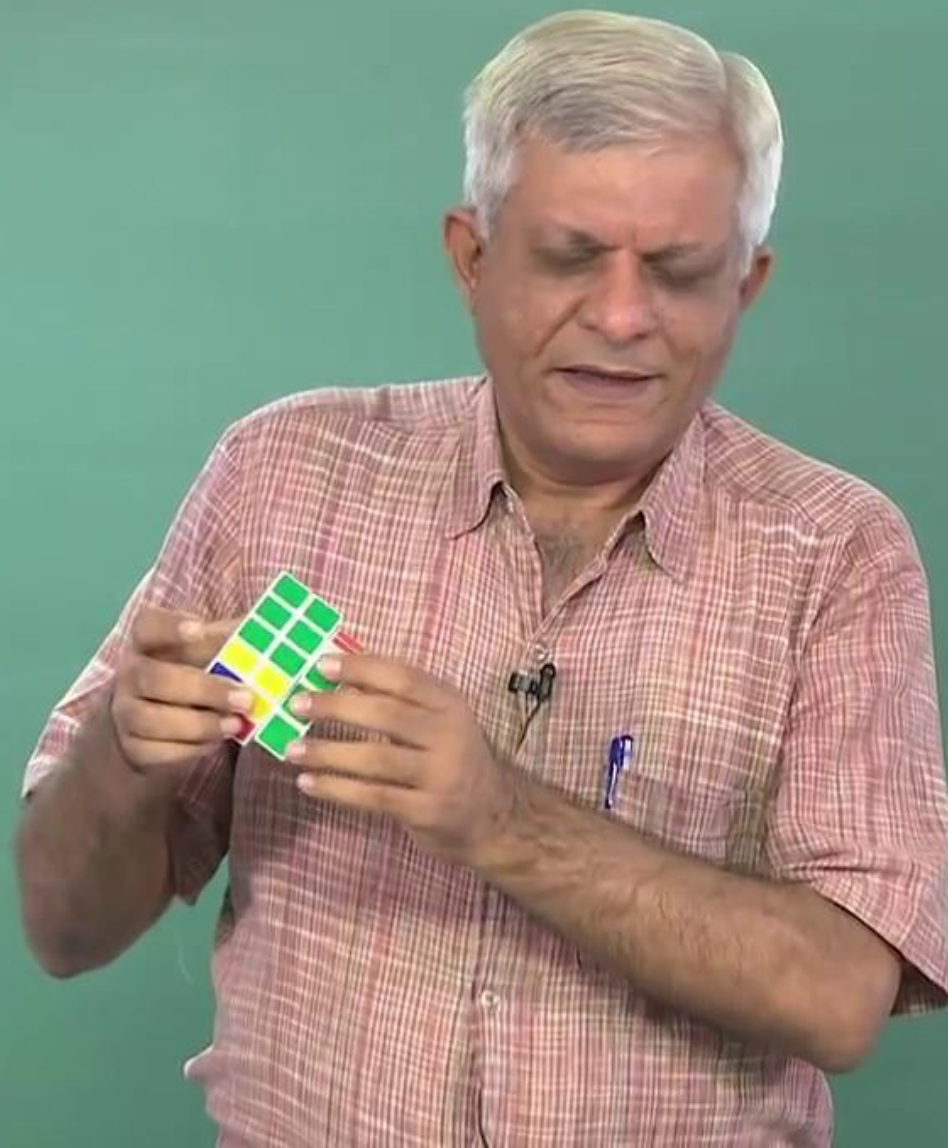


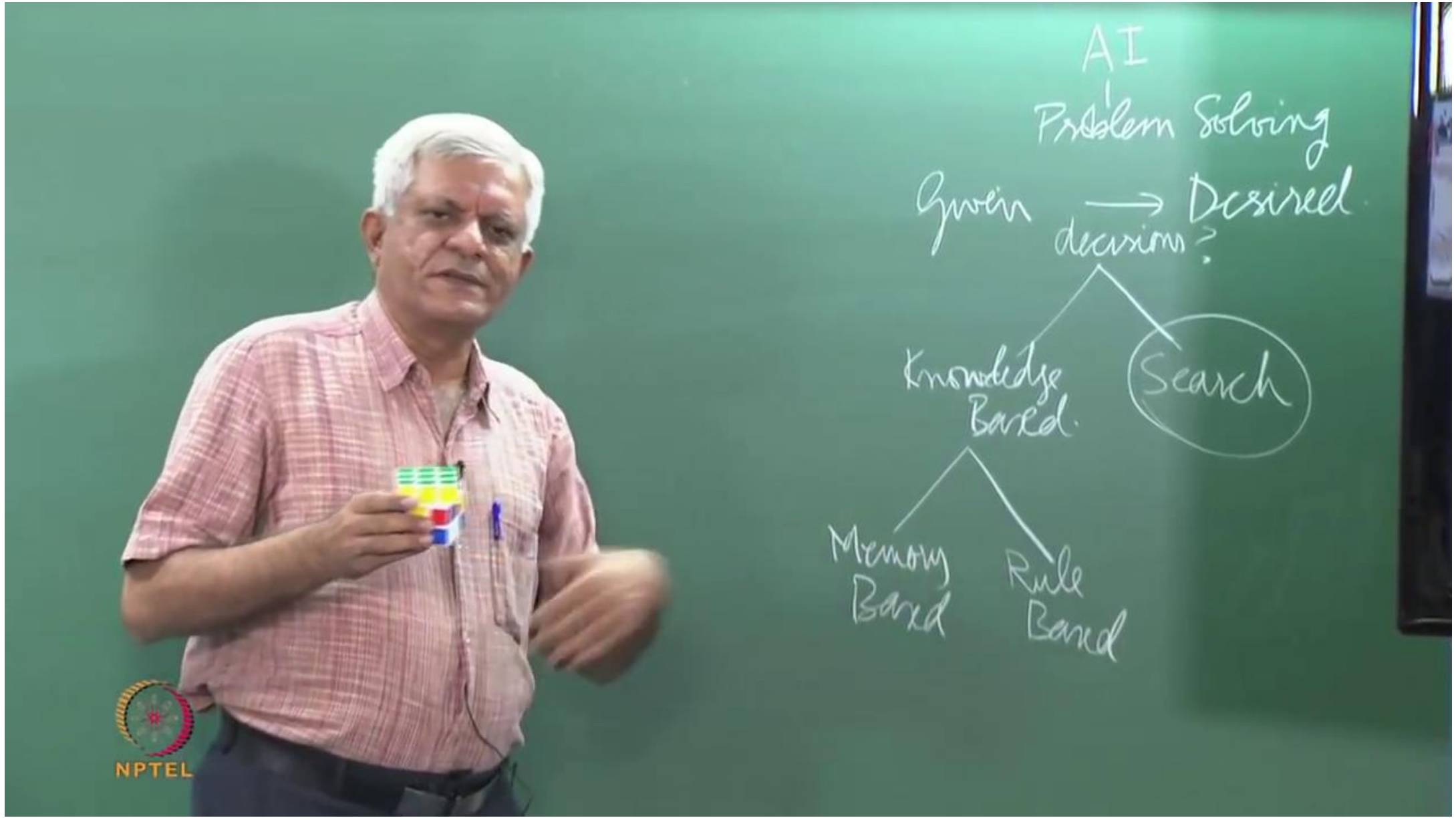




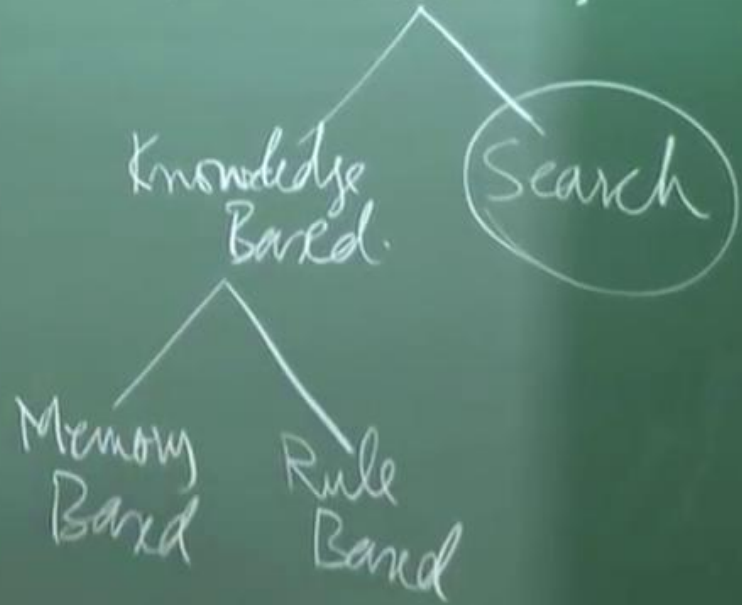






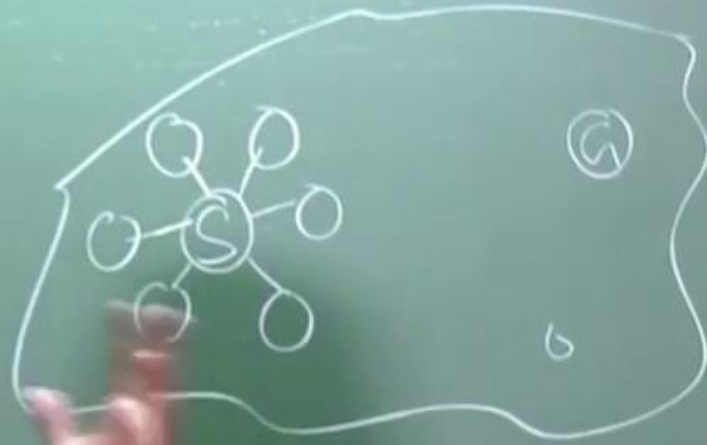


AI
Problem Solving
Given \rightarrow Desired
decision?



STATE SPACE SEARCH

STATE SPACE SEARCH



STATE SPACE SEARCH

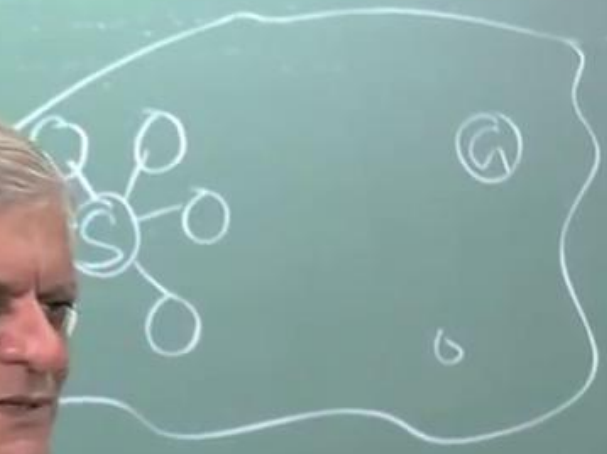


MoveGen(S)

8

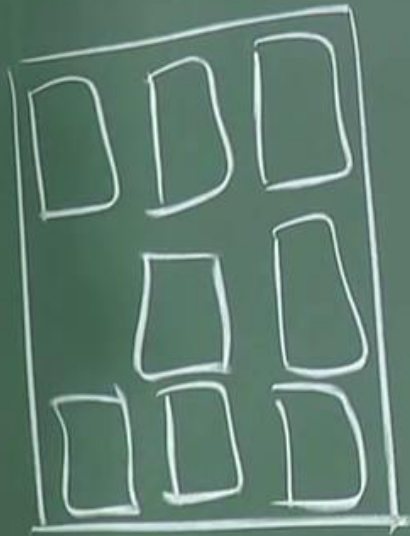
STATE SPACE SEARCH

8/15/24 puzzle



$Gen(S) \rightarrow$ set of neighbours

8/15/24 puzzle



STATE SPACE SEARCH

8/15/24 puzzle

Q

Q

3
6
7

Set of moves

1	2	3
8		4
7	6	5

Goal

8/15/24 puzzle

1	2	3
	4	6
8	5	7

1	2	3
8		4
7	6	5

Goal

8/15/24 puzzle



1	2	3
4	5	6
8	7	9

1	2	3
8		4
7	6	5

Goal.

www

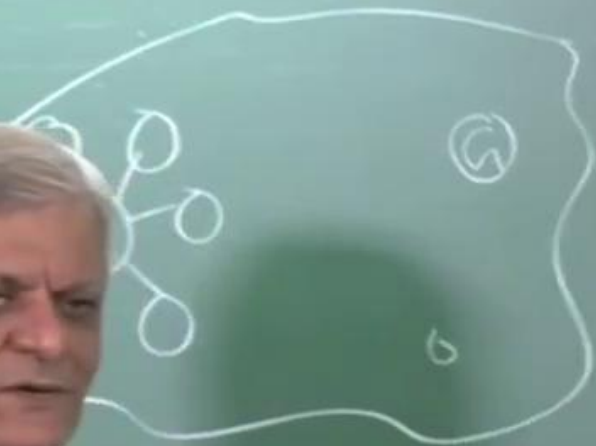
S



NPTEL

STATE SPACE SEARCH

8/15/24 puzzle



⇒ set of neighbours

1	2	3
	4	6
8	5	7

s

1	2	3
4		6
8	5	7

1	2	3
8		4
7	6	5

Goal

STATE SPACE SEARCH

8/15/24 puzzle



1	2	3
	4	6
8	5	7

U
D

1	2	3
4		6
8	5	7

1	2	3
8		4
7	6	5

Goal

8/15/24

(S) \rightarrow set of neighbours

Goal
in Cabbage puzzle

1	2	3
	4	6
5	1	2

U

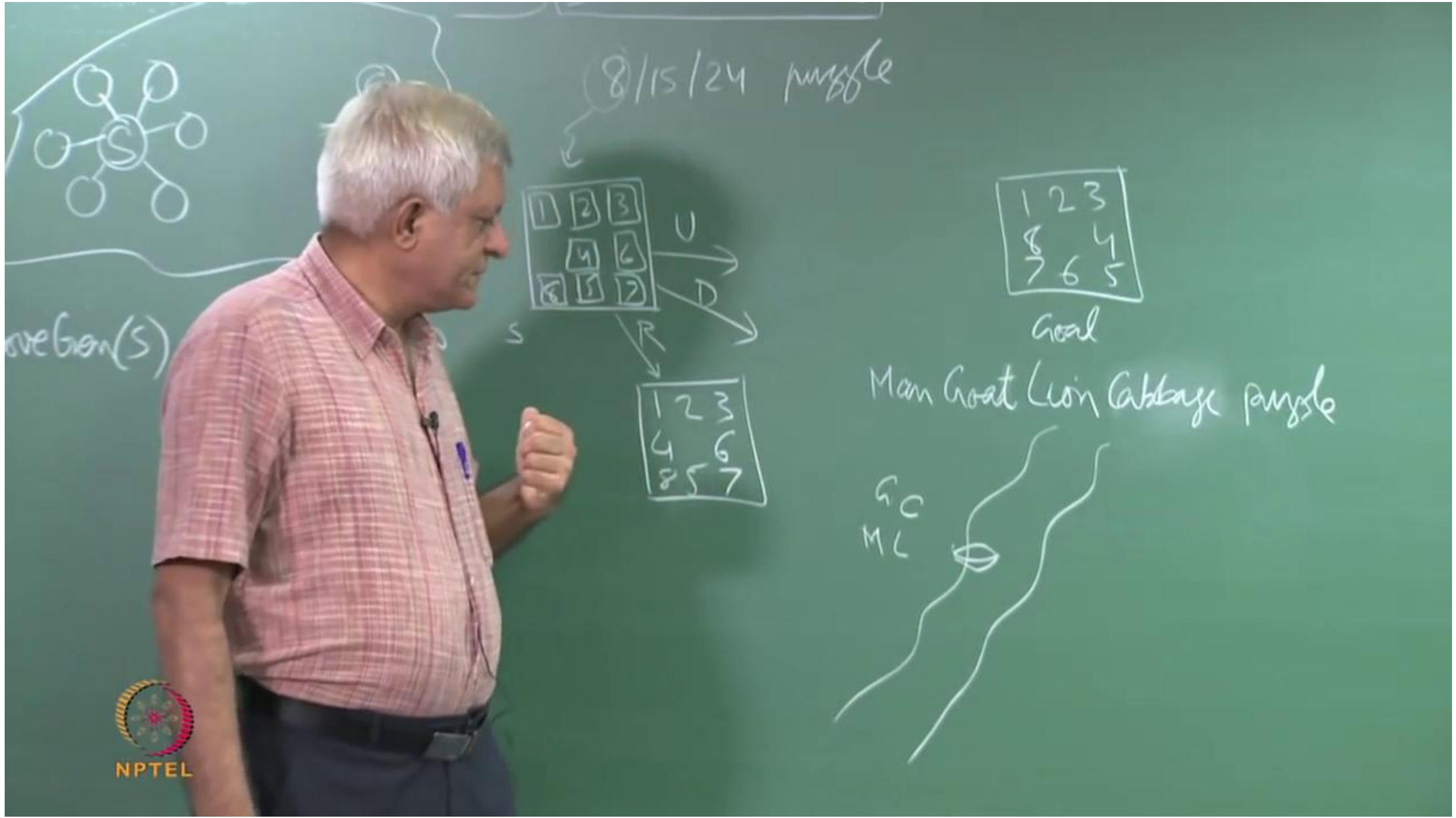
D

1	2	3
8		4
7	6	5

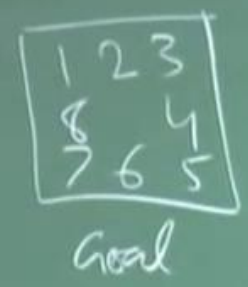
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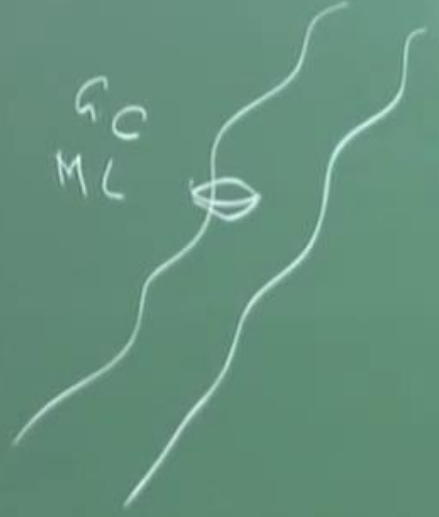
NPTel



8/15/24 puzzle



Man Goat Lion Cabbage puzzle



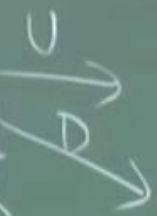
reGen(S)

STATE SPACE SEARCH

8/15/24 puzzle



1	2	3
	4	6
8	5	7



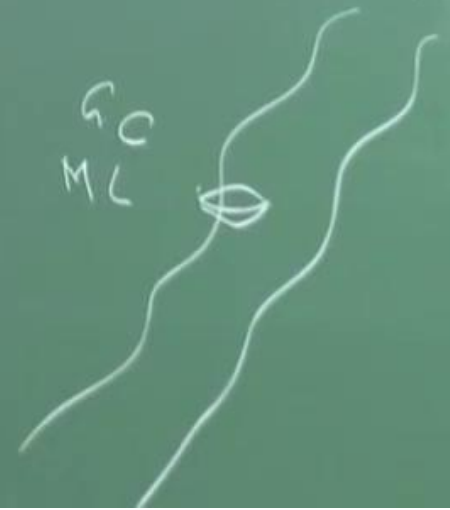
1	2	3
4		6
8	5	7

1	2	3
8		4
7	6	5

Goal

Man Goat Lion Cabbage

G C
M L



STATE SPACE SEARCH

8/15/24 puzzle

1	2	3
4	5	6
7	8	9

1	2	3
8		4
7	6	5

Goal

Man Goat Lion Cabbage puzzle

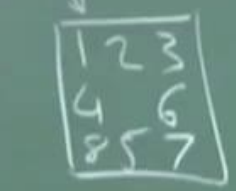
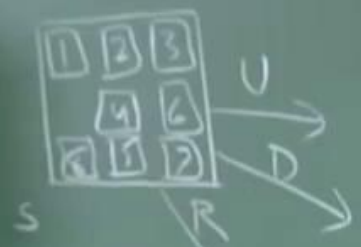
GC
ML

L	B	R

STATE SPACE SEARCH

8/15/24 puzzle

→ set of neighbours



((MGLC)())

((())(MGLC))



Goal

Man Goat Lion Cabbage puzzle



L	B	R

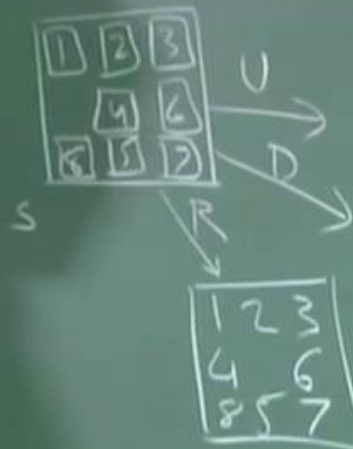
STATE SPACE SEARCH

8/15/24 puzzle



MoveGen

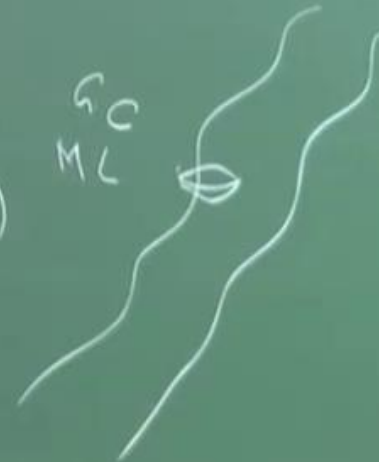
known



Goal

Man Goat Lion Cabbage puzzle

GC
ML



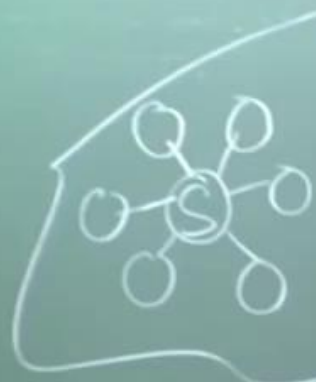
L B R



(()) (MGLC)

STATE SPACE SEARCH

8/15/24 puzzle



MoveGen(S)

1	2	3
	4	6
8	5	7

U
D

1	2	3
4		6
8	5	7

1	2	3
8		4
7	6	5

Goal

Man Goat Lion Cabbage puzzle

GC
ML

L B R

((MGLC)())

((GC)(ML))

((())(MGLC))

STATE SPACE SEARCH

8/15/24 puzzle

1	2	3
4	6	
8	5	7

U

D

R

1	2	3
4	6	
8	5	7

1	2	3
8		4
7	6	5

Goal

Man Goat Lion Cabbage puzzle

GC
ML

L B R

((MGLC))

((GC)(ML))

(())(MGLC)

→ set of neighbours



NPTEL

STATE SPACE SEARCH

(8/15/24 puzzle)



$neigh(S) \rightarrow$ set of neighbours

1	2	3
4	5	6
7	8	9

U
D
R

1	2	3
4	5	6
7	8	9

1	2	3
8	4	5
7	6	9

Goal

Man Goat Lion Cabbage puzzle

(Left G/L)

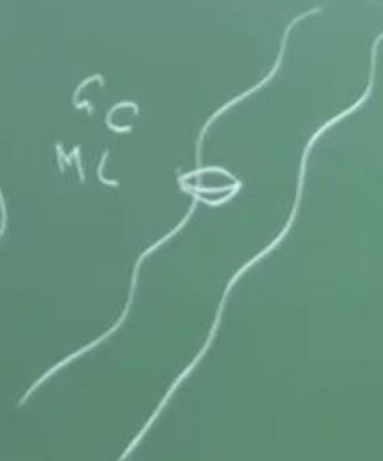
(Right G)

((M G/L)())

((G/L)(M))

((())(M G/L))

G/L
M/L



L B R



NPTEL

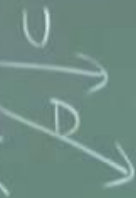
STATE SPACE SEARCH

8/15/24 puzzle



$Neigh(S) \rightarrow$ set of neighbours

1	2	3
4	5	6
7	8	9

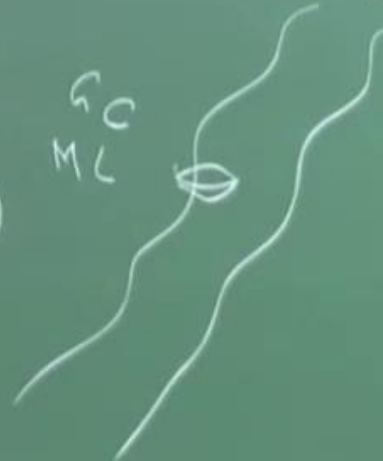


1	2	3
8		4
7	6	5

Goal

1	2	3
4		6
8	5	7

Man Goat Lion Cabbage puzzle



L	B	R

(Left GLC)

(Right L)

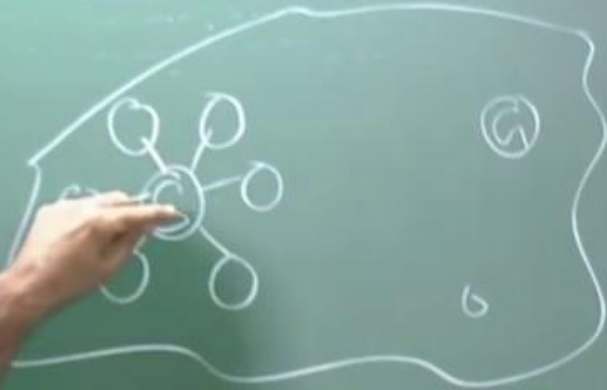
((MGLC)())

((GL)(ML))

((())(MGLC))

STATE SPACE SEARCH

8/15/24 puzzle



$\text{MoveGen}(S) \rightarrow \text{set of neighbours}$

1	2	3
4	6	
8	5	7

U
D
R

1	2	3
8	4	
7	6	5

Goal

Mam Goat Lion Cabbage pny

(Left G/L)

((M G/L)())

(Right L)

((G/L)(M))

((())(M G/L))

G
M
L

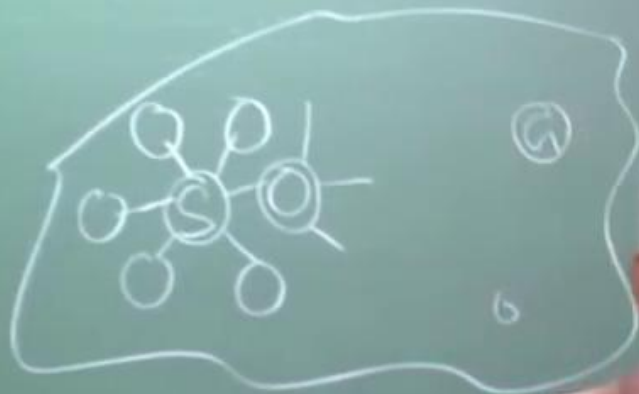
L B



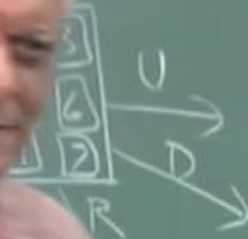
NPTEL

STATE SPACE SEARCH

8/15/24 puzzle



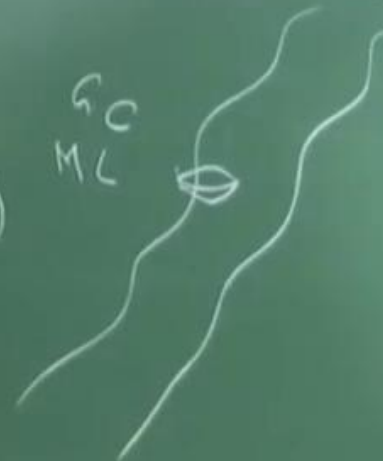
MoveGen(S) → set of



Goal

Man Goat Lion Cabbage puzzle

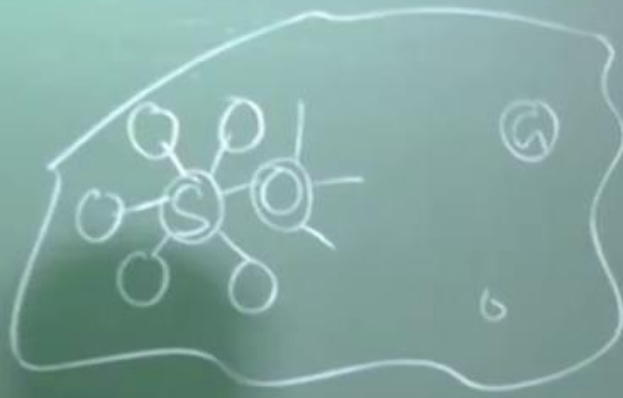
GC
ML



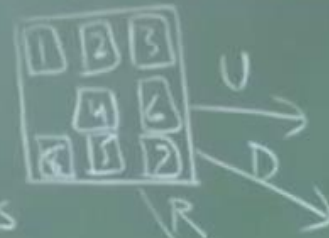
L	B	R

STATE SPACE SEARCH

8/15/24 puzzle



$\text{MoveGen}(S) \rightarrow \text{set of neighbours}$



Goal

Mom Goat Lion Cabbage p

Generate & Test

Generate a candidate
Test whether it is the solution

(Left GLC)

(Right L)

((MGLC)())

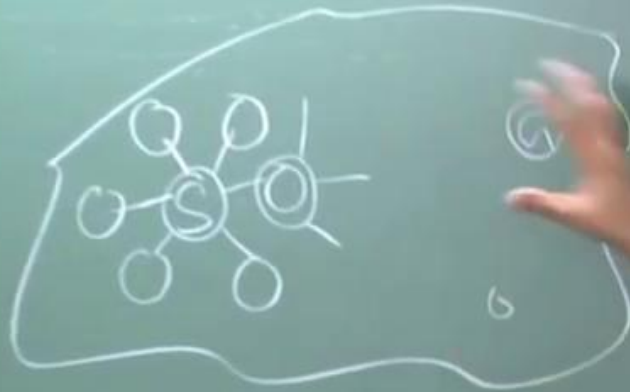
((GC)(ML))

((())(MGLC))

GC
ML



STATE SPACE SEARCH



(8/15/24) puzzle

1	2	3
4	5	6
7	8	9

1	2	3
8	4	
7	6	5

MoveGen(s) \rightarrow set of neighbours s

Goal

at Lion Cabbage puzzle

Generate & Test

Generate a candidate
Test whether it is the solution

(Left G/C)

(Right L)

(G/C)

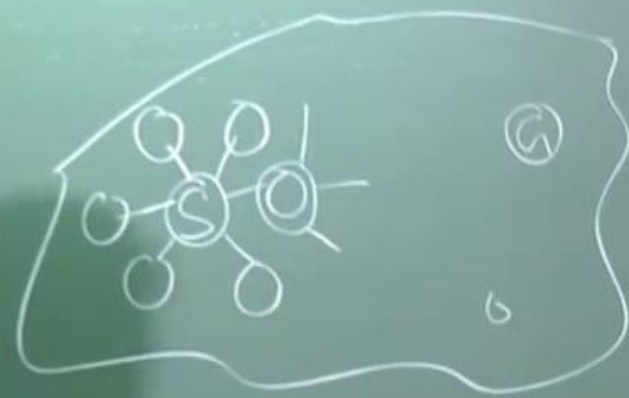
L B R



NPTEL

STATE SPACE SEARCH

(8/15/24) puzzle



MoveGen(s) \rightarrow set of neighbours

GoalTest(s)

Generate & Test

\rightarrow Generate a candidate

Test whether it is the solution

(Left GLC)

(Right L)

((MGLC)())

((GC)(ML))

((())(MGLC))

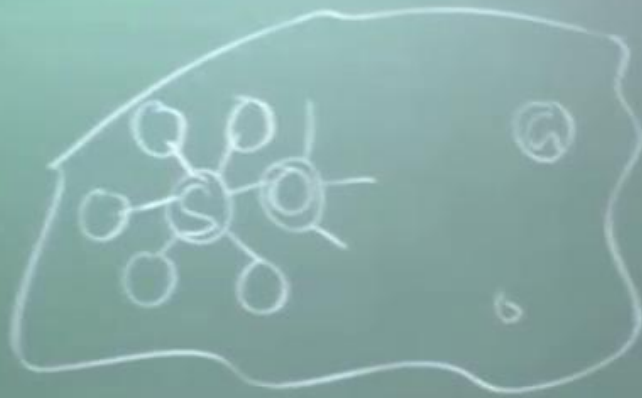
Man Goat Lion Cabbage

GC
ML

L



STATE SPACE SEARCH



8/15/24

1	2	3
4	5	6
7	8	9

U
D

1	2	3
8		4
7	6	5

Goal

Levin Gabbage puzzle

MoveGen(s) \rightarrow set of neighbours

GoalTest(s) \rightarrow Y/N

Generate & Test

(Left G/L)

(Right L)

\rightarrow Generate a candidate

Test whether it is the solution

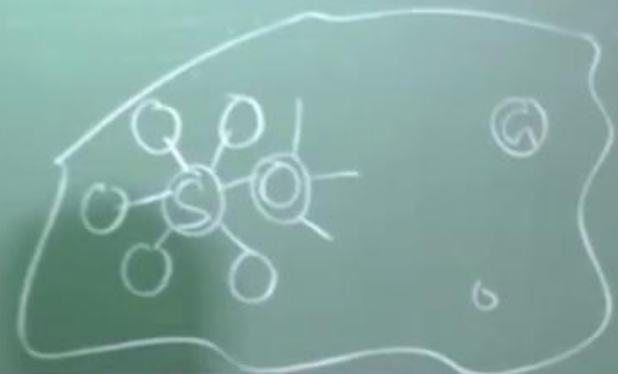
L	B	R



NPTEL

STATE SPACE SEARCH

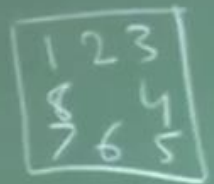
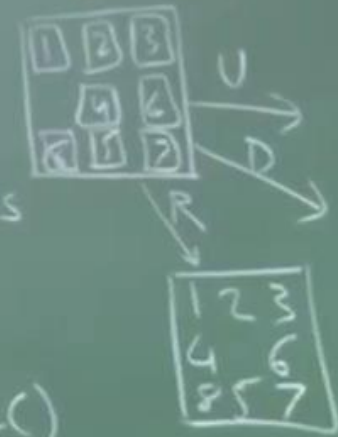
8/15/24 puzzle



MoveGen(S) \rightarrow set of neighbours
 GoalTest(S) \rightarrow Y/N

Generate & Test

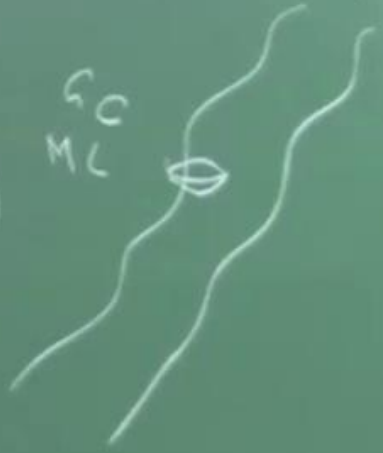
\rightarrow Generate a candidate
 Test whether it is the solution



Goal

Man Goat Lion Cabbage puzzle

(Left G/LC)
 (Right L)
 ((MGLC)())
 ((GC)(ML))
 (())(MGLC)



STATE SPACE SEARCH

Simple Search 1

8/15/24 Monday

2	3
4	6
1	2

U

1	2	3
8		4
7	6	5

Goal

rat Lion Cabbage puzzle

L B R



NPTEL

Simple Search 1

OPEN $\leftarrow \{s\}$

Simple Search 1

OPEN $\leftarrow \{S\}$

While GoalTest(S) \neq true

Remove S from OPEN

Simple Search 1

OPEN $\leftarrow \{S\}$

While GoalTest(S) \neq true

Remove S from OPEN

OPEN \leftarrow OPEN \cup MoveGen(S)

CH

Simple Search 1

$OPEN \leftarrow \{S\}$

Pick some node N
from $OPEN$

→ While $GoalTest(S) \neq true$

Remove S from $OPEN$

$OPEN \leftarrow OPEN \cup MoveGen(S)$

2	3
	4
6	5

Goal



NPTEL

CH

Simple Search 1

$OPEN \leftarrow \{S\}$

Pick some node N
from $OPEN$

→ While $GoalTest(N) \neq true$

Remove N from $OPEN$

$OPEN \leftarrow OPEN \cup MoveGen(N)$

2	3
8	4
7	6
	5

CH

Simple Search 1

$OPEN \leftarrow \{S\}$

Pick some node N
from $OPEN$

→ While $GoalTest(N) \neq true$

Remove N from $OPEN$

$OPEN \leftarrow OPEN \cup MoveGen(N)$

E) SEARCH

style

Simple Search 1

OPEN $\leftarrow \{S\}$

den
OPEN

While GoalTest(N) \neq true

Remove N from OPEN

OPEN \leftarrow OPEN \cup MoveGen(N)

Search Tree

1	2	3
8		
7	6	

Main Goal

style

GC
ML

R



TE SPACE SEARCH

5/24 puzzle

U
D

2 3
4 6
5 7

16(1)(

1(1)

(16(1)

Simple Search 1

Pick some node N from OPEN \rightarrow OPEN $\leftarrow \{S\}$
While GoalTest(N) \neq true
Remove N from OPEN
OPEN \leftarrow OPEN \cup MoveGen(N)

Search Tree

1	2	3
8		4
7	6	

Goal

Cabbage puzzle

	B	R



NPTEL

TE SPACE SEARCH

5/24

Simple Search 1

Pick some node N from OPEN \rightarrow While $\text{GoalTest}(N) \neq \text{true}$
Remove N from OPEN
 $\text{OPEN} \leftarrow \text{OPEN} \cup \text{MoveGen}(N)$

Search Tree

1	2	3
8		4
7	6	5

Goal

8-puzzle

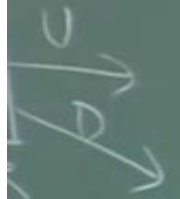
L B R



NPTEL

TE SPACE SEARCH

15/24 puzzle



1	2	3
4	6	
8	5	7

1G(C())

1G()

1G(C)

Simple Search 1

Search mode = state
Search Tree

OPEN $\leftarrow \{S\}$

remove N
from OPEN

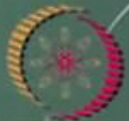
While GoalTest(N) \neq true

Remove N from OPEN

OPEN \leftarrow OPEN \cup MoveGen(N)

puzzle

B R



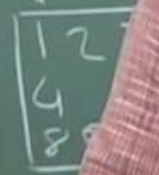
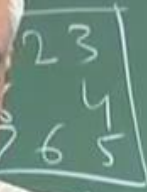
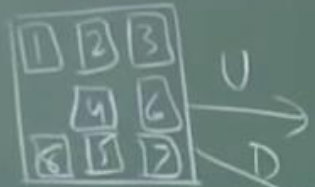
NPTEL

STATE SPACE SEARCH

Simple Search 1

$OPEN \leftarrow \{S\}$
 Pick some node N from $OPEN$ \rightarrow While $GoalTest(N) \neq true$
 Remove N from $OPEN$
 $OPEN \leftarrow OPEN \cup Move$

8/15/24 puzzle



8/15/24 puzzle



set of neighbours
Y/N

(Left GLC)

(Right L)

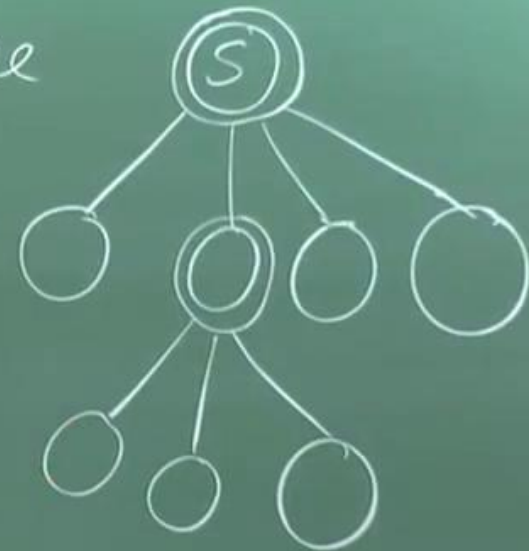
(M) (GLC) (M)

(I) (MGLC)

Simple Search 1

Take some node N from OPEN \rightarrow While GoalTest(N)
Remove N from OPEN
OPEN \leftarrow OPEN \cup children(N)

Search mode = state
Search Tree



State space

L B R



SEARCH

Simple Search 1

Search node = state

Search Tree

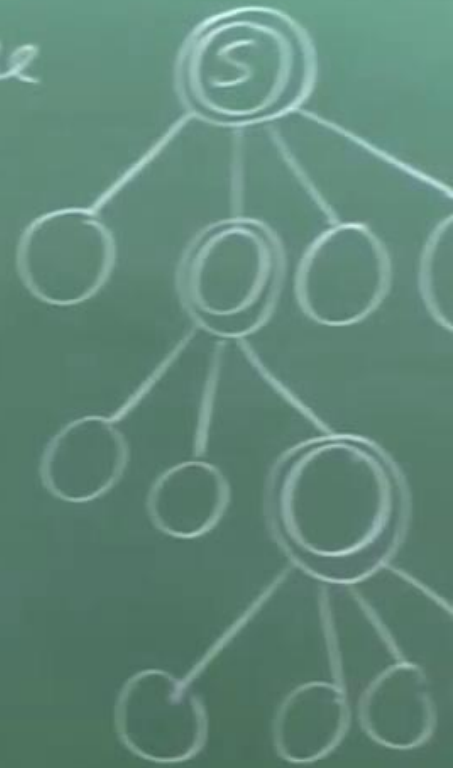
OPEN \leftarrow SET
Pick a node N
from OPEN \rightarrow whole f
time
OPEN \leftarrow U MinHeap(N)

1	2	3
8		4
7	6	5

Goal

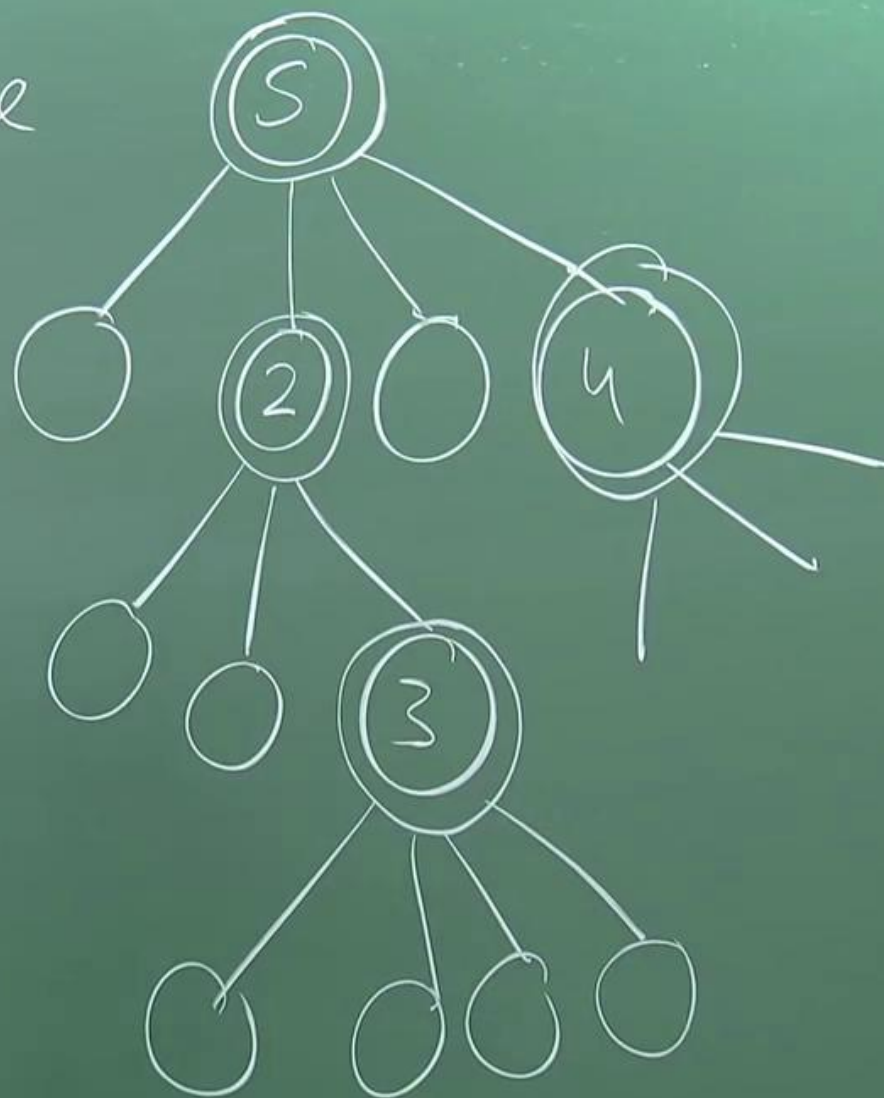
Goal Lion Gabbage puzzle

L B



h node = state
Search Tree

$O(N)$



Given

Knowledge Base

Memory Based

Run



NPTEL

ARCH

Simple Search 1

Search mode = state
Search Tree

Pick some node N
from OPEN

OPEN

Which

≠ time
OPEN

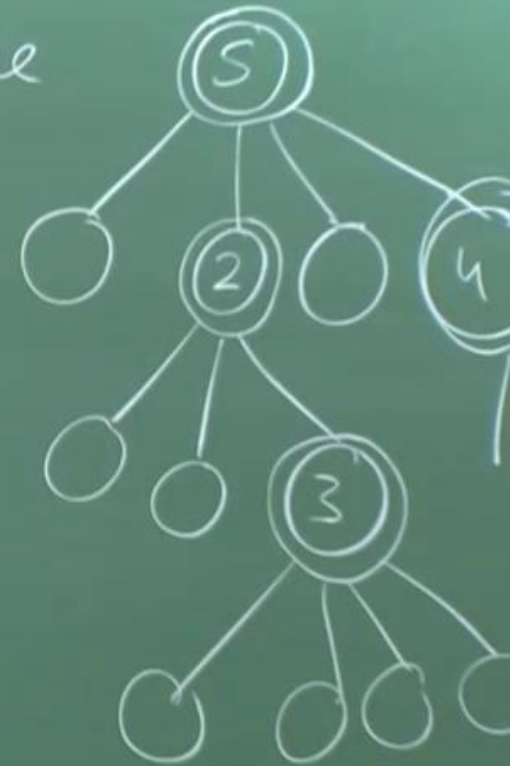
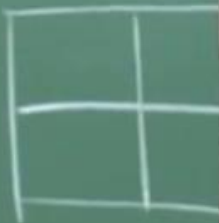
U Move(N)

1	2	3
8		4
7	6	5

Goal

at Lion Cabbage puzzle

L B



STATE SPACE SEARCH

Simple Search 1

Pick some node N from OPEN
 OPEN ← S
 While Goal
 Remove
 OPEN

1	2	3
4	5	6
7	8	9

1	2	3
8	4	
7	6	5

Goal

Great Lion Cabbage puzzle

L	B	R



Move Gen(S) → set of neighbours
 Goal Test(S) → Y/N

Generate & Test

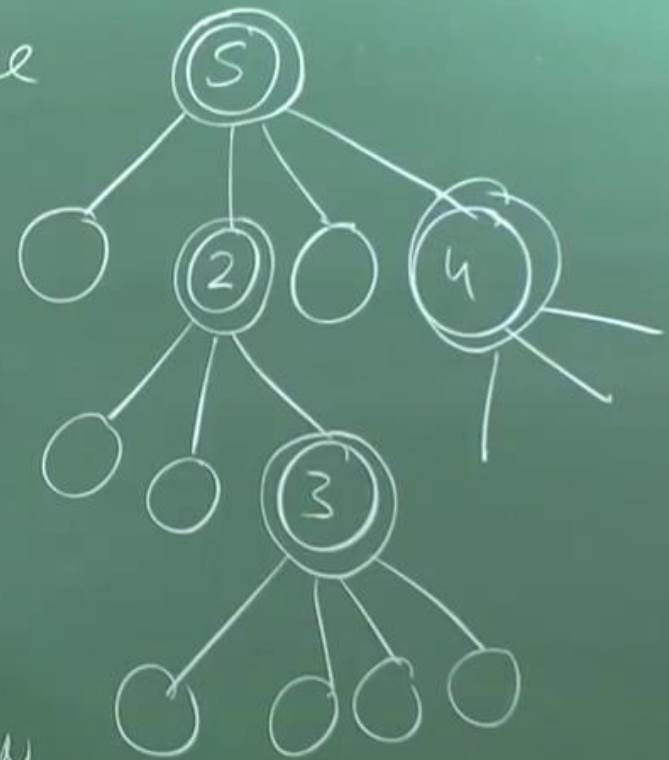
→ Generate a candidate
 Test whether it is the solution



Simple Search 1

Pick some node N from OPEN \rightarrow While GoalTest(N) \neq true
Remove N from OPEN
OPEN \leftarrow OPEN

Search node = state
Search Tree



Cabbage puzzle

L	B	R

SS2

OPEN \leftarrow {S}
CLOSED \leftarrow { }
Pick some node from OPEN
Add it to CLOSED

SS2

OPEN $\leftarrow \{S\}$

CLOSED $\leftarrow \{ \}$

Pick some node for OPEN

Add it to CLOSED

If goalTest(N) then return(N)

STATE SPACE SEARCH

Simple Search 1

Search mode = state Search

$OPEN \leftarrow \{S\}$

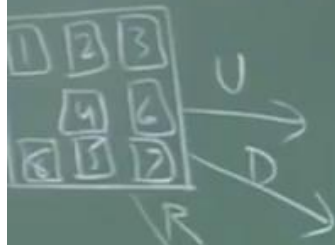
While $GoalTest(N) \neq true$

Remove N from $OPEN$

$OPEN \leftarrow OPEN \cup MoveGen(N)$

Pick some

8/15/24 puzzle



Goal

Main Goal

GC
ML



SS2

$OPEN \leftarrow \{S\}$

$CLOSED \leftarrow \{ \}$

Pick some node for

Add it to

if $GoalTest(N)$

Else

$OPEN \leftarrow$



NPTEL

SEARCH

Simple Search 1

$OPEN \leftarrow \{S\}$

Pick some node from

if $GoalTest(N) \neq true$

Remove N from $OPEN$

$OPEN \leftarrow OPEN \cup MoveGen(N)$

Search mode = state

Search Tree



1	2	3
8	4	
7	6	5

Goal

Main Goal List

GOAL



SS2

$OPEN \leftarrow \{S\}$

$CLOSED \leftarrow \{ \}$

Pick some node from $OPEN$

Add it to $CLOSED$

if $GoalTest(N)$ then return (N)

Else

$OPEN \leftarrow OPEN \cup \{ MoveGen(N) \}$

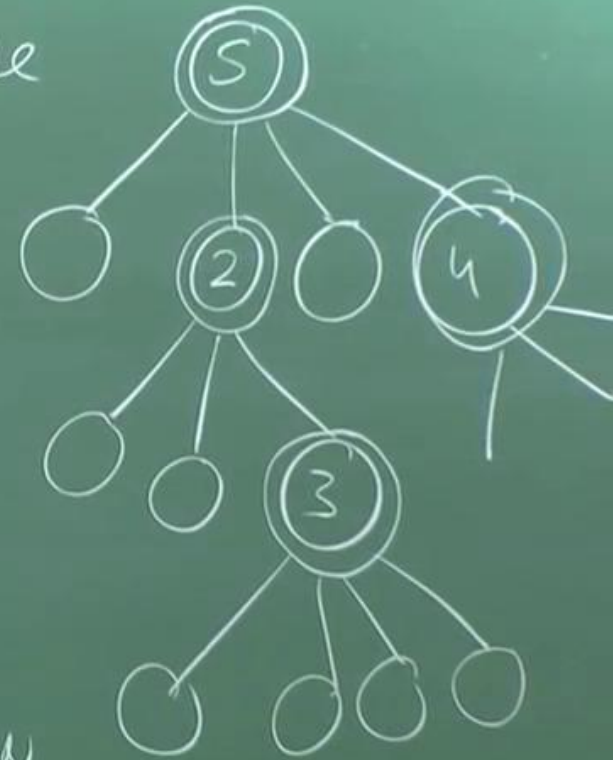


NPTEL

Simple Search 1

Search node = state
Search Tree

Pick some node N from OPEN
 $OPEN \leftarrow \{S\}$
 While GoalTest(N) \neq true
 Remove N from OPEN
 $OPEN \leftarrow OPEN \cup \text{children}(N)$



SS2

$OPEN \leftarrow \{S\}$
 $CLOSED \leftarrow \{\}$
 Pick some node from OPEN
 Add it to CLOSED
 If GoalTest(N) then return(N)
 Else
 $OPEN \leftarrow OPEN \cup \text{MoveGen}(N) \setminus \{OPEN \cup \text{CLOSED}\}$

2 3
4
6 5

Goal
win Cabbage puzzle



STATE SPACE SEARCH

8/15/24 puzzle

Simple

Pick some node N from OPEN



1	2	3
	4	6
8	5	7

U
D
R

1	2	3
4		6
8	5	7

1	2	3
8		4
7	6	5

Goal

Man Goat Lion Cabbage puzzle

GC
ML

L B R

neighbours

GLC()

(Right L)

((MGLC)())

((GC)(ML))

((())(MGLC))

früh



NPTEL

STATE SPACE SEARCH

8/15/24 puzzle



Simple Search 1

Search mode = state Search

$OPEN \leftarrow \{S\}$

While $GoalTest(N) \neq true$

Remove N from OPEN

$OPEN \leftarrow OPEN \cup MoveGen(N)$

SS2

$OPEN \leftarrow \{S\}$
 $CLOSED \leftarrow \emptyset$

Pick some node

Add it
 if $GoalTest(N)$
 Else

$OPEN \leftarrow$

