

1. The derivative of  $\tan^{-1}(x^2)$  w.r.t.  $x$  is:

- (a)  $\frac{x}{1+x^4}$
- (b)  $\frac{2x}{1+x^4}$
- (c)  $-\frac{2x}{1+x^4}$
- (d)  $\frac{1}{1+x^4}$

2. Overspeeding increases fuel consumption and decreases fuel economy as a result of tyre rolling friction and air resistance. While vehicles reach optimal fuel economy at different speeds, fuel mileage usually decreases rapidly at speeds above 80km/h.

The relation between fuel consumption  $F$ (l/100 km) and speed  $V$ (km/h)

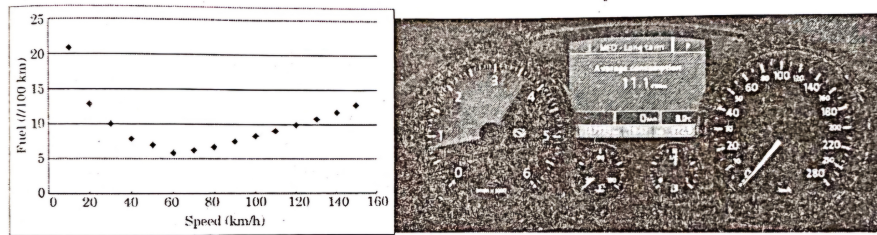


Figure 1: 1

under some constraints is given as  $F = \frac{V^2}{500} - \frac{V}{4} + 14$ .

On the basis of the above information, answer the following questions:

- (i) Find  $F$ , when  $V = 40 \text{ km/h}$ .
- (ii) Find  $\frac{dF}{dV}$ .
- (iii) Find the speed  $V$  for which fuel consumption  $F$  is minimum.
- (iv) Find the quantity of fuel required to travel 600 km at the speed  $V$  at which  $\frac{dF}{dV} = -0.01$ .