

# Module 5: Example of ABCD matrices

**Course 1 of *Optical Engineering*: First Order Optical System Design**

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# Example: Doublet lens

Using ABCD matrices:

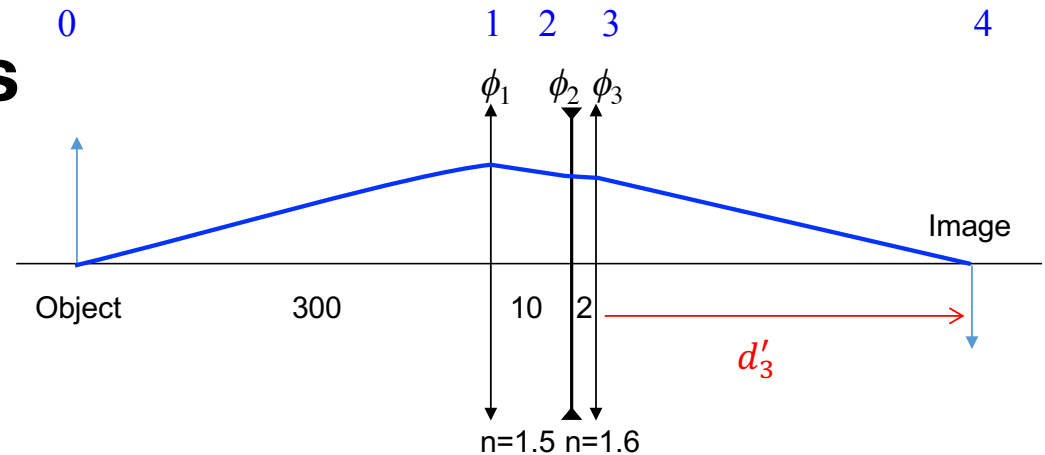
$$\begin{bmatrix} y_4 \\ u'_4 \end{bmatrix} = \mathbf{T}_3 \mathbf{R}_3 \mathbf{T}_2 \mathbf{R}_2 \mathbf{T}_1 \mathbf{R}_1 \mathbf{T}_0 \begin{bmatrix} y_0 \\ u'_0 \end{bmatrix} \quad \text{Note reverse order!}$$

$$\mathbf{T}_k = \begin{bmatrix} 1 & d'_k \\ 0 & 1 \end{bmatrix} \quad \mathbf{R}_k = \begin{bmatrix} 1 & 0 \\ -\phi_k/n'_k & n_k/n'_k \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ u'_4 \end{bmatrix} = \begin{bmatrix} 1 & d'_3 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1.6 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0.00125 & 0.9375 \end{bmatrix} \begin{bmatrix} 1 & 10 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -0.0067 & 0.667 \end{bmatrix} \begin{bmatrix} 1 & 300 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1.5 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2.8488 - 0.01427 d'_3 \\ -0.01427 \end{bmatrix}$$

$$d'_3 = 199.685 \quad \checkmark$$



Surface $k$		0	1	2	3	4
Surfaces	$c$		0.02	-0.02	0	
	$n'$		1	1.5	1.6	1
System	$\phi_k = 1/f$		0.01	-0.002	0	
	$d'_k$		300	10	2	199.7
Axial ray	$y_k$	0	3	2.8667	2.8488	0
	$u'_k$		.01	-.0133	-0.0089	-0.0143