## Module 4: Optical Path Length of a Paraxial Lens

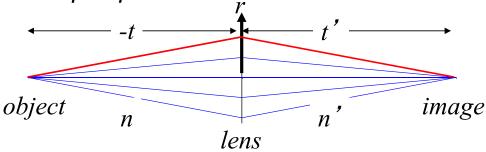
Course 1 of Optical Engineering: First Order Optical System Design

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## What is a lens? Paraxial thin lens via Fermat

Fermat's

Define a lens as a thin phase function that connects all the rays from object to image with equal phase.



**OPL** on axis

$$-nt + n't' = n\sqrt{t^2 + r^2} + n'\sqrt{t'^2 + r^2} + S_{lens}(r)$$
 Fermal's principle 
$$\approx -nt - \frac{r^2}{2} \frac{n}{t} + n't' + \frac{r^2}{2} \frac{n'}{t'} + S_{lens}(r)$$
 Binomial approx.

Solve for OPL of lens

$$S_{lens}(r) = -\frac{r^2}{2} \left( -\frac{n}{t} + \frac{n'}{t'} \right) = -\frac{r^2}{2f}$$

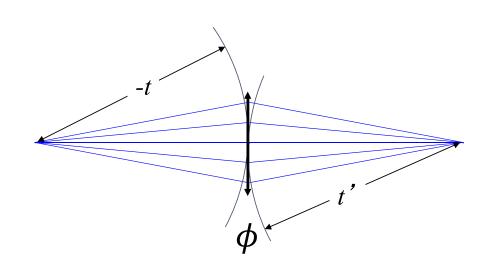
...using the Gaussian thin lens equation

$$\frac{1}{f} \equiv \phi = -\frac{n}{t} + \frac{n'}{t'}$$

## **Variables**

f Focal length of lens [m]  $\phi=1/f$  Power of lens [diopters]

## What is a lens? Transforms wavefront curvature



The power of a lens is the algebraic increment in curvature added to the incident wavefront.

$$\frac{1}{t'} = \frac{1}{t} + \phi$$
 In air