

# JEE EXPERT

## ANSWER KEY & SOLUTIONS

Module Test - [MT - 01]

JEE ADV. Paper - 01

Batch : 12th (Zenith- 1820 - X01 & X02)

Date :[04.08.2019]

### PHYSICS

1	(C)	2	(A)	3	(B)	4	(B)
5	(B, C)	6	(B, C)	7	(A, B, C)	8	(A, C)
9	(A, C)	10	(A, B)	11	(B, C)	12	(C, D)
13	(7)	14	(4)	15	(3)	16	(2)
17	(5)	18	(3)				

### CHEMISTRY

19	(A)	20	(A,D)	21	(B)	22	(D)
23	(B, C)	24	(B, C)	25	(B, C, D)	26	(B, C, D)
27	(A, B)	28	(C, D)	29	(B, C, D)	30	(A, B, D)
31	(4)	32	(8)	33	(4)	34	(6)
35	(4)	36	(2)				

### MATHEMATICS

37	(C)	38	(D)	39	(A)	40	(A)
41	(A, C)	42	(A, C)	43	(B, C)	44	(A, B)
45	(B, D)	46	(A)	47	(A, B)	48	(A, B)
49	(2)	50	(2)	51	(0)	52	(0)
53	(5)	54	(9)				

# JEE EXPERT

## SOLUTIONS

Module Test - [MT - 01]

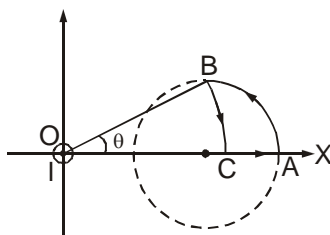
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## PHYSICS

1. **(C) Sol.** Let segment  $OB = OC$  and arc  $BC$  is a circular arc with centre at origin. Since the shown closed path  $ABCA$  encloses no current, the path integral of magnetic field over this path is zero.



$$\text{Hence } \int_A^B \vec{B} \cdot d\vec{\ell} + \int_B^C \vec{B} \cdot d\vec{\ell} + \int_C^A \vec{B} \cdot d\vec{\ell} = 0.$$

Because  $\vec{B}$  is perpendicular to segment  $AC$  at all point, therefore  $\int_C^A \vec{B} \cdot d\vec{\ell} = 0.$

$$\text{Hence } \int_A^B \vec{B} \cdot d\vec{\ell} = \int_C^B \vec{B} \cdot d\vec{\ell} = \frac{\mu_0 I}{2\pi} \frac{OB(\theta)}{OB} = \frac{\mu_0 I}{2\pi} \tan^{-1} \frac{1}{2}$$

2. **(A) Sol.**  $B_{p_1} = \frac{\mu_0 i}{4\pi \ell} \left[ 0 + \frac{1}{\sqrt{2}} \right] \times 2 + \frac{\mu_0 i}{4\pi \ell} \left[ \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right]$

$$B_{p_2} = \frac{\mu_0 i}{4r}$$

$$4\ell = \pi r \Rightarrow r = \frac{4\ell}{\pi}$$

$$B_{p_2} = \frac{\mu_0 i}{4 \left( \frac{4\ell}{\pi} \right)}$$

D? **(B) Sol.**  $\frac{V_1}{V_2} = \frac{l_1}{l_2} = \frac{E'R_1/(R_1+r')}{E'R_2/(R_2+r')} = \frac{R_1(R_2+r')}{R_2(R_1+r')} \Rightarrow \frac{2}{3} = \frac{5(10+r')}{10(5+r')} \Rightarrow r' = 10\Omega$

4. (B) Sol.  $C_{eq} = 3/2 F$

$$\text{Charge flow } q = C_{eq} \left( 10 - \frac{15}{3} \right) = \frac{3}{2} \times 5 = 7.5 \mu C$$

### SECTION-2

5. Sol. (B, C)

Applying Gauss theorem to volume containing cuboid indicated by ABCD  $\frac{E}{k} A + \frac{0}{A} = \frac{q_{enc}}{\epsilon_0}$  or  $q_{enc} = \frac{EA\epsilon_0}{A}$

$$\text{Electrostatic energy stored in dielectric medium} = \frac{1}{2} k \epsilon_0 \left( \frac{E}{k} \right)^2 At = \frac{\epsilon_0 E^2 At}{2k}$$

6. Sol. (B, C)

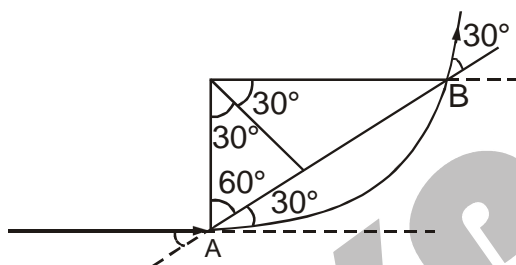
All elements are moving radially away with velocity  $K$  so.

$$\text{Force} = d\theta kB$$

$$\text{torque} = d\theta kBr$$

$$\text{torque on ring} = dQkBr = 2\pi\lambda Bkr^2$$

7. Sol. (A, B, C)



$$\text{Arc } AB = \frac{\pi}{3} r = \frac{\pi m V}{3qB}$$

$$\text{Time 't'} = \left( \frac{T}{2\pi} \right) \cdot \left( \frac{\pi}{3} \right) = \frac{T}{6} = \frac{\pi m}{3qB}$$

8. Sol. (A,C)

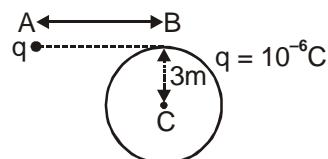
Solid neutral conducting sphere

$$\text{Potential at center} = \frac{9 \times 10^9 \times 10^{-6}}{5} = 1.8 \text{ kV}$$

$$\Rightarrow \text{Potential at B} = 1.8 \text{ kV}$$

$$V_{At B} = V_{\text{due to A}} + V_{\text{due to induced charges}}$$

$$V_{\text{due to induced charge}} = 1.8 \text{ kV} - 2.25 \text{ kV} = -0.45 \text{ kV}$$



9. Sol. (A, D)

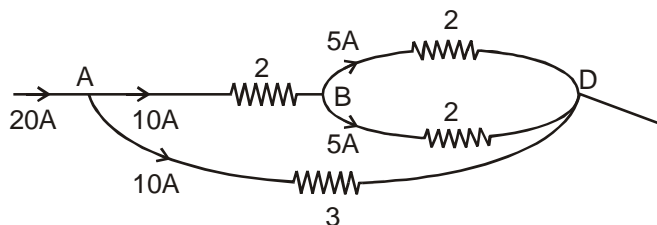
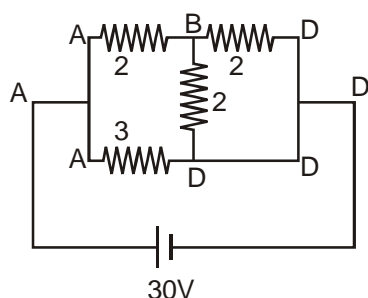
$$2T = F = \frac{\lambda q}{2\pi \epsilon_0 R}$$

11. (B), (C)

12. (C), (D)

## SECTION - 3

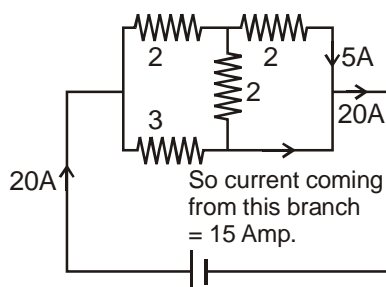
13. Sol. (7)



$$\Rightarrow R_{eq} = \frac{3}{2}$$

$$i = \frac{30}{3/2} = 20 \text{ Amp.}$$

From figure current through B → D branch = 5 Amp.



therefore current in bd is  $15 \text{ A} = n + 8$ .

$$\Rightarrow n = 7$$

14. Sol. (4)

Assume positive and negative charge of density  $\rho$  in cavity. The electric field due to cylinder is

$$\frac{\rho r}{2\epsilon_0} \left( \text{where } r = \frac{R}{2} \right) \text{ and field due to spherical charge (–ve) is zero.}$$

15. Sol. (3)

$$\text{Resistance of cylinder } R = \int_0^1 \frac{1}{\sigma} \frac{dx}{a} = \frac{2\sqrt{l}}{3a\sigma_0}$$

$$I = \frac{E}{R}$$

$$\text{Electric field} = \frac{J}{\sigma} = \frac{I}{a\sigma} = \frac{E\sqrt{x}}{Ra\sigma_0 l} = \frac{E(\sqrt{l})}{\frac{2\sqrt{l}}{3a\sigma_0} a\sigma_0 l} = \frac{3E}{2l}$$

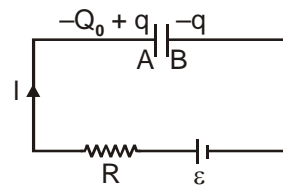
## 16. Sol. (2)

Let at any time  $t$  charge flown through the plate B to plate A is  $q$  and instantaneous current is  $\ell$ .

From loop theorem  $\left(\frac{2q - Q_0}{2C}\right) + \ell R - \varepsilon = 0$

$$\Rightarrow R \frac{dq}{dt} = \frac{-2q + 2\varepsilon C + Q_0}{2C}$$

$$\Rightarrow \frac{dq}{2\varepsilon C + Q_0 - 2q} = \frac{dt}{2RC}$$



Now for charge on plate A to be zero  $q = Q_0$ .

$$\text{Integrating } \int_0^{Q_0} \frac{dq}{2\varepsilon C + Q_0 - 2q} = \int_0^t \frac{dt}{2RC}$$

$$= t = RC \ln \left[ \frac{2\varepsilon C + Q_0}{2\varepsilon C - Q_0} \right]$$

Putting the value of  $C$ ,  $Q_0$ ,  $\varepsilon$  and  $R$

We get  $t = 2$  seconds.

## 17. Sol. (5)

At terminal stage, torque applied on the smaller disc by the rope =  $mga$

current to the disc =  $\frac{B\omega r^2}{2R}$  (where  $\omega$  is terminal angular velocity)

Torque applied by magnetic field =  $\frac{B^2 \omega r^4}{4R}$

$$\text{So, } \frac{B^2 \omega r^4}{4R} = mga$$

$$\omega = 100 \text{ rad/sec}$$

## 18. Sol. (3)

$$R_{\text{Voltmeter}} = 6, R_{\text{ammeter}} = 0.5$$

$$R_{\text{eq}} = 10$$

$$I = \frac{30}{10} = 3A$$

Reading of voltmeter =  $1 \times 3 = 3$  volt.