

JEE EXPERT

ANSWER KEY & SOLUTIONS

Module Test - [MT - 01]

JEE ADV. Paper - 01

Batch : 12th (Zenith- 1820 - X01 & X02)

Date :[04.08.2019]

PHYSICS

| | | | | | | | |
|----|--------|----|--------|----|-----------|----|--------|
| 1 | (C) | 2 | (A) | 3 | (B) | 4 | (B) |
| 5 | (B, C) | 6 | (B, C) | 7 | (A, B, C) | 8 | (A, C) |
| 9 | (A, C) | 10 | (A, B) | 11 | (B, C) | 12 | (C, D) |
| 13 | (7) | 14 | (4) | 15 | (3) | 16 | (2) |
| 17 | (5) | 18 | (3) | | | | |

CHEMISTRY

| | | | | | | | |
|----|--------|----|--------|----|-----------|----|-----------|
| 19 | (A) | 20 | (A) | 21 | (B) | 22 | (D) |
| 23 | (B, C) | 24 | (B, C) | 25 | (B, C, D) | 26 | (B, C, D) |
| 27 | (A, B) | 28 | (C, D) | 29 | (B, C, D) | 30 | (B, B, D) |
| 31 | (4) | 32 | (8) | 33 | (4) | 34 | (6) |
| 35 | (4) | 36 | (2) | | | | |

MATHEMATICS

| | | | | | | | |
|----|--------|----|--------|----|--------|----|--------|
| 37 | (C) | 38 | (D) | 39 | (A) | 40 | (A) |
| 41 | (A, C) | 42 | (A, C) | 43 | (B, C) | 44 | (A, B) |
| 45 | (B, D) | 46 | (A) | 47 | (A, B) | 48 | (A, B) |
| 49 | (2) | 50 | (2) | 51 | (0) | 52 | (0) |
| 53 | (5) | 54 | (9) | | | | |

JEE EXPERT

SOLUTIONS

Module Test - [MT - 01]

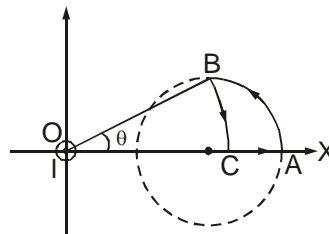
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PHYSICS

1. (C) Sol. Let segment OB = OC and arc BC is a circular arc with centre at origin. Since the shown closed path ABCA encloses no current, the path integral of magnetic field over this path is zero.



$$\text{Hence } \int_A^B \vec{B} \cdot d\vec{\ell} + \int_B^C \vec{B} \cdot d\vec{\ell} + \int_C^A \vec{B} \cdot d\vec{\ell} = 0.$$

Because \vec{B} is perpendicular to segment AC at all point, therefore $\int_C^A \vec{B} \cdot d\vec{\ell} = 0.$

$$\text{Hence } \int_A^B \vec{B} \cdot d\vec{\ell} = \int_C^B \vec{B} \cdot d\vec{\ell} = \frac{\mu_0 I}{2\pi} \frac{OB(\theta)}{OB} = \frac{\mu_0 I}{2\pi} \tan^{-1} \frac{1}{2}$$

2. (A) Sol. $B_{p_1} = \frac{\mu_0 I}{4\pi\ell} \left[0 + \frac{1}{\sqrt{2}} \right] \times 2 + \frac{\mu_0 I}{4\pi\ell} \left[\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right]$

$$B_{p_2} = \frac{\mu_0 I}{4r}$$

$$4\ell = \pi r \Rightarrow r = \frac{4\ell}{\pi}$$

$$B_{p_2} = \frac{\mu_0 I}{4 \left(\frac{4\ell}{\pi} \right)}$$

D? (B) Sol. $\frac{V_1}{V_2} = \frac{I_1}{I_2} = \frac{E'R_1/(R_1+r')}{E'R_2/(R_2+r')} = \frac{R_1(R_2+r')}{R_2(R_1+r')} \Rightarrow \frac{2}{3} = \frac{5(10+r')}{10(5+r')} \Rightarrow r' = 10\Omega$

4. (B) Sol. $C_{eq} = 3/2 F$

$$\text{Charge flow } q = C_{eq} \left(10 - \frac{15}{3} \right) = \frac{3}{2} \times 5 = 7.5 \mu C$$

SECTION-2

5. Sol. (B, C)

Applying Gauss theorem to volume containing cuboid indicated by ABCD $\frac{E}{k} A + \frac{0}{A} = \frac{q_{enc}}{\epsilon_0}$ or $q_{enc} = \frac{EA\epsilon_0}{A}$

$$\text{Electrostatic energy stored in dielectric medium} = \frac{1}{2} k\epsilon_0 \left(\frac{E}{k} \right)^2 At = \frac{\epsilon_0 E^2 At}{2k}$$

6. Sol. (B, C)

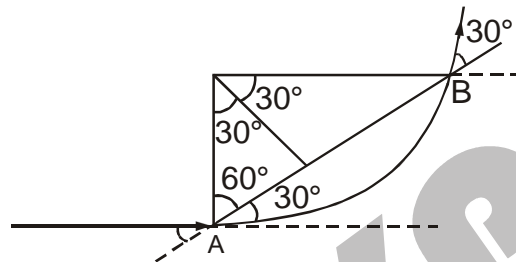
All elements are moving radially away with velocity K so.

$$\text{Force} = d\theta kB$$

$$\text{torque} = d\theta kBr$$

$$\text{torque on ring} = dQkBr = 2\pi\lambda Bkr^2$$

7. Sol. (A, B, C)



$$\text{Arc } AB = \frac{\pi}{3} r = \frac{\pi m V}{3qB}$$

$$\text{Time 't'} = \left(\frac{T}{2\pi} \right) \cdot \left(\frac{\pi}{3} \right) = \frac{T}{6} = \frac{\pi m}{3qB}$$

8. Sol. (A, C)

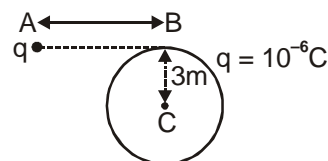
Solid neutral conducting sphere

$$\text{Potential at center} = \frac{9 \times 10^9 \times 10^{-6}}{5} = 1.8 \text{ kV}$$

$$\Rightarrow \text{Potential at B} = 1.8 \text{ kV}$$

$$V_{At B} = V_{\text{due to A}} + V_{\text{due to induced charges}}$$

$$V_{\text{due to induced charge}} = 1.8 \text{ kV} - 2.25 \text{ kV} = -0.45 \text{ kV}$$



9. Sol. (A, D)

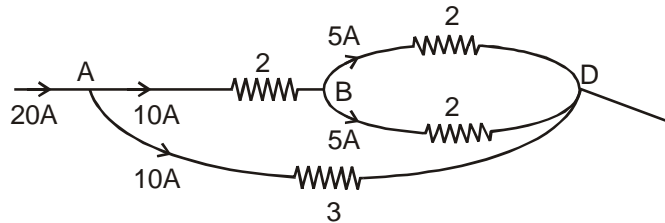
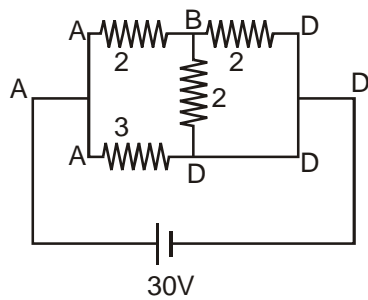
$$2T = F = \frac{\lambda q}{2\pi \epsilon_0 R}$$

11. (B), (C)

12. (C), (D)

SECTION - 3

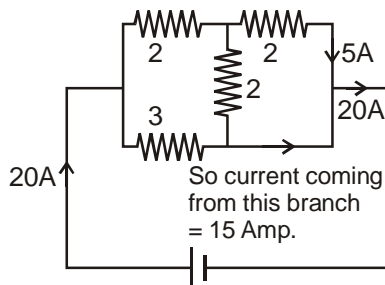
13. Sol. (7)



$$\Rightarrow R_{eq} = \frac{3}{2}$$

$$i = \frac{30}{3/2} = 20 \text{ Amp.}$$

From figure current through B \rightarrow D branch = 5 Amp.



therefore current in bd is 15 A = n + 8.

$$\Rightarrow n = 7$$

14. Sol. (4)

Assume positive and negative charge of density ρ in cavity. The electric field due to cylinder is

$$\frac{\rho r}{2\epsilon_0} \left(\text{where } r = \frac{R}{2} \right) \text{ and field due to spherical charge (-ve) is zero.}$$

15. Sol. (3)

$$\text{Resistance of cylinder } R = \int_0^1 \frac{1}{\sigma} \frac{dx}{a} = \frac{2\sqrt{l}}{3a\sigma_0}$$

$$I = \frac{E}{R}$$

$$\text{Electric field} = \frac{J}{\sigma} = \frac{I}{a\sigma} = \frac{E\sqrt{x}}{Ra\sigma_0 l} = \frac{E(\sqrt{l})}{\frac{2\sqrt{l}}{3a\sigma_0} a\sigma_0 l} = \frac{3E}{2l}$$

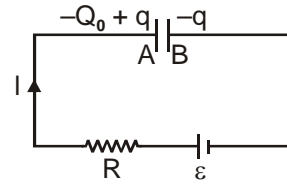
16. Sol. (2)

Let at any time t charge flown through the plate B to plate A is q and instantaneous current is ℓ .

From loop theorem $\left(\frac{2q - Q_0}{2C}\right) + \ell R - \varepsilon = 0$

$$\Rightarrow R \frac{dq}{dt} = \frac{-2q + 2\varepsilon C + Q_0}{2C}$$

$$\Rightarrow \frac{dq}{2\varepsilon C + Q_0 - 2q} = \frac{dt}{2RC}$$



Now for charge on plate A to be zero $q = Q_0$.

$$\text{Integrating } \int_0^{Q_0} \frac{dq}{2\varepsilon C + Q_0 - 2q} = \int_0^t \frac{dt}{2RC}$$

$$= t = RC \ln \left[\frac{2\varepsilon C + Q_0}{2\varepsilon C - Q_0} \right]$$

Putting the value of C , Q_0 , ε and R

We get $t = 2$ seconds.

17. Sol. (5)

At terminal stage, torque applied on the smaller disc by the rope = mga

current to the disc = $\frac{B\omega r^2}{2R}$ (where ω is terminal angular velocity)

Torque applied by magnetic field = $\frac{B^2\omega r^4}{4R}$

$$\text{So, } \frac{B^2\omega r^4}{4R} = mga$$

$$\omega = 100 \text{ rad/sec}$$

18. Sol. (3)

$$R_{\text{Voltmeter}} = 6, R_{\text{ammeter}} = 0.5$$

$$R_{\text{eq}} = 10$$

$$I = \frac{30}{10} = 3A$$

Reading of voltmeter = $1 \times 3 = 3$ volt.