

Predicting NBA-All Stars Using Regression Analysis

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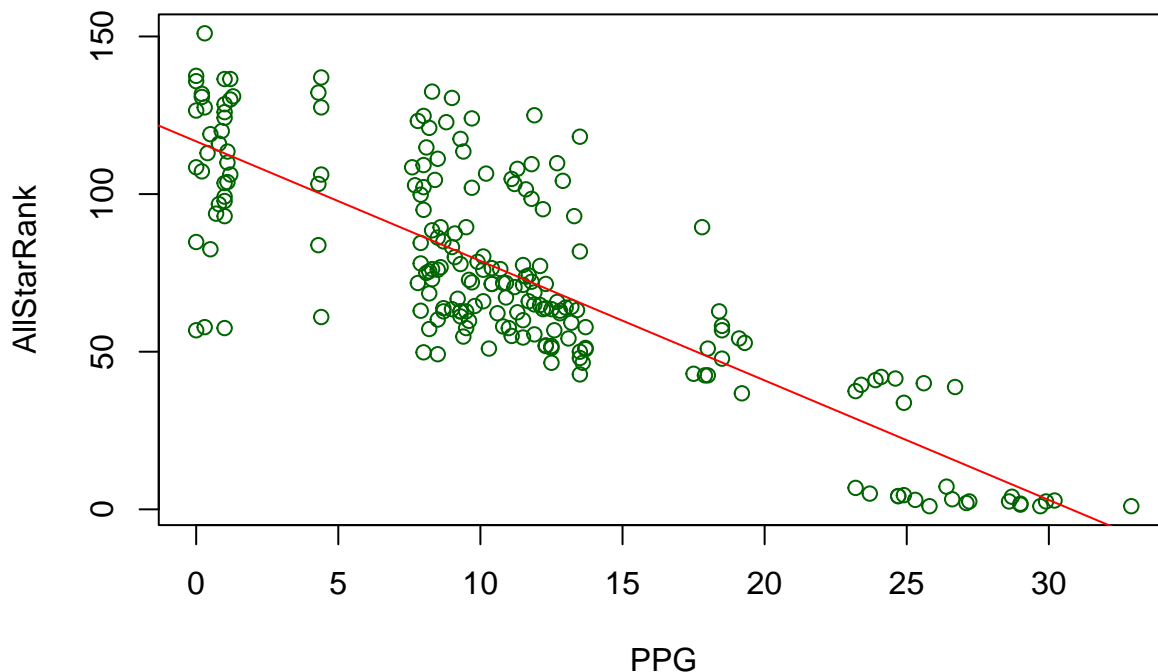
Appendix:

```
input=read.table("Data.csv",header=TRUE,fill=0,sep=',')
attach(input)
```

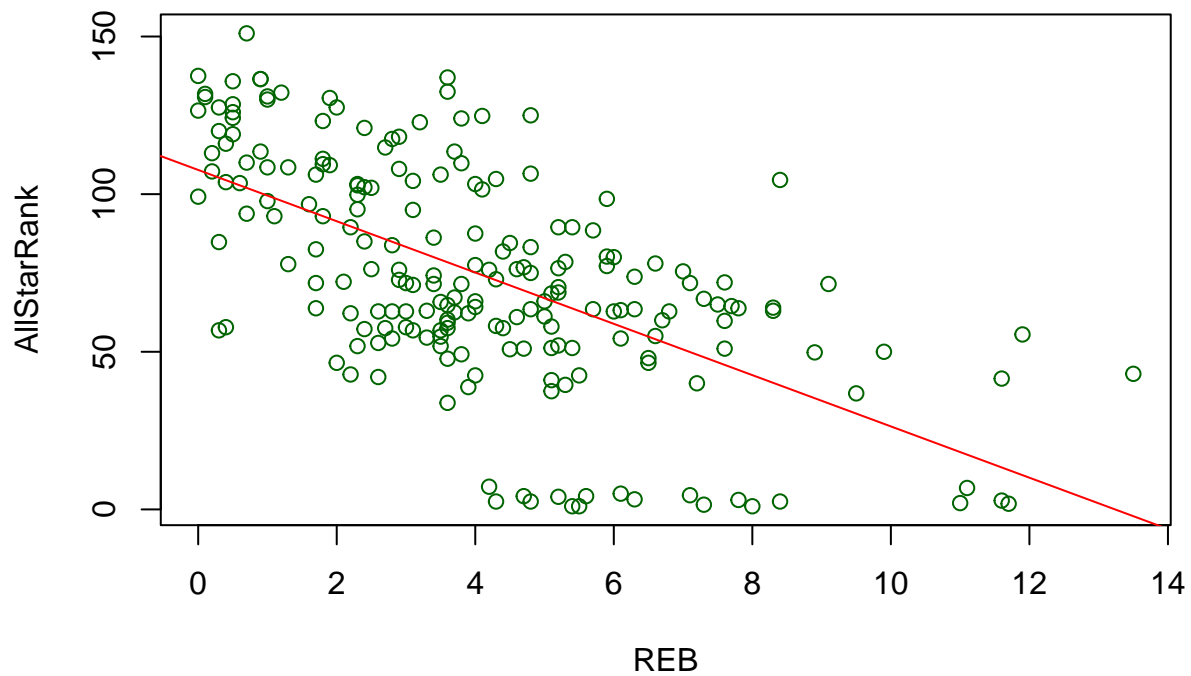
Variable Plot

Before we started any regression analysis, we wanted to plot the variables we believe will contribute most to All Star selection. These variables are the stereotypical “box-score” stats. These include Points per game, rebounds, assists, and we will also include Wins.

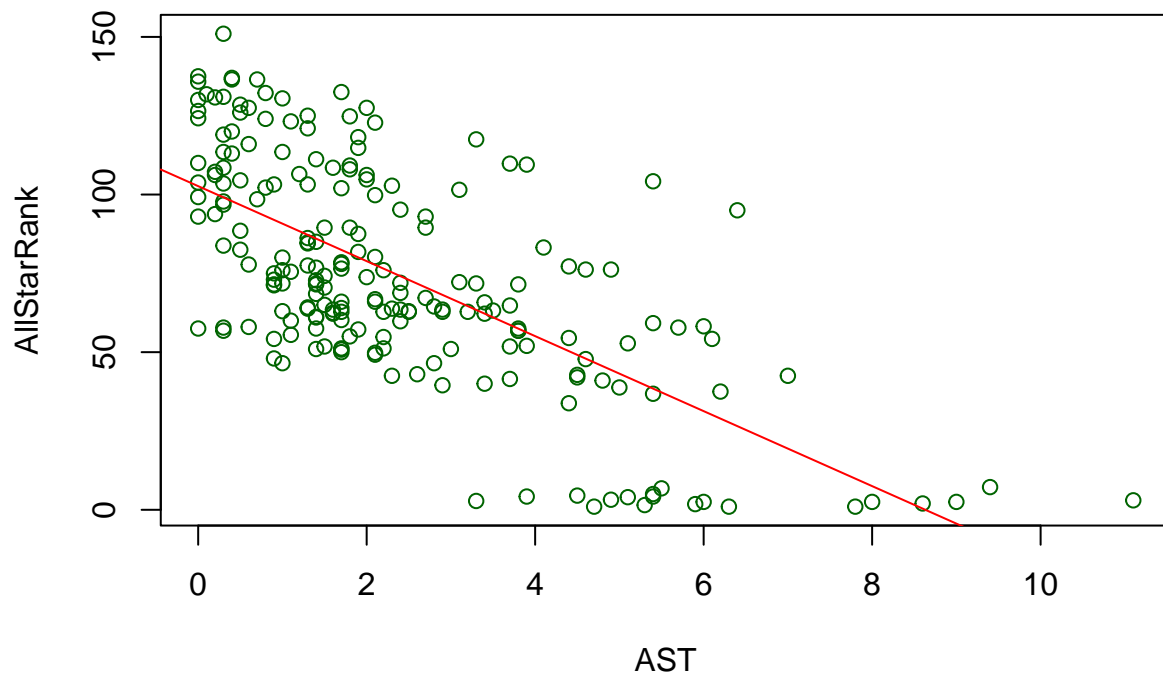
```
plot(PPG,AllStarRank,col='dark green')
PPGRankmodel=lm(AllStarRank~PPG)
abline(PPGRankmodel,col='red')
```



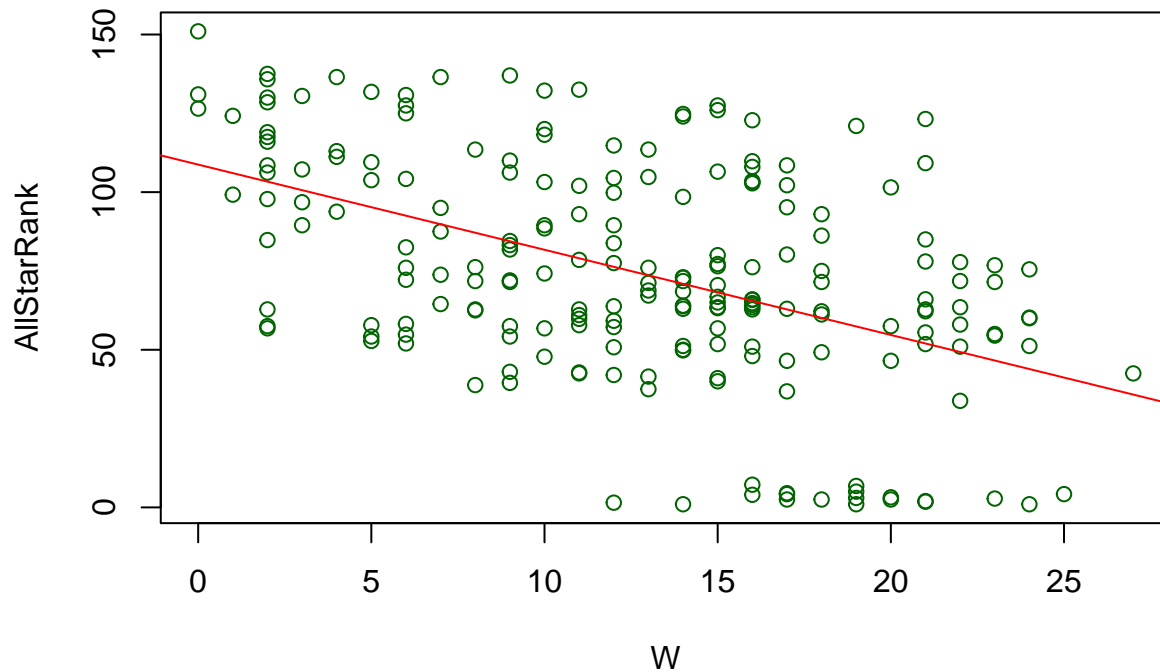
```
plot(REB,AllStarRank,col='dark green')
PPGRankmodel=lm(AllStarRank~REB)
abline(PPGRankmodel,col='red')
```



```
plot(AllStarRank, REB, col='dark green')
PPGRankmodel=lm(AllStarRank~REB)
abline(PPGRankmodel, col='red')
```



```
plot(AllStarRank, AST, col='dark green')
PPGRankmodel=lm(AllStarRank~AST)
abline(PPGRankmodel, col='red')
```



```
library(corrplot)

## corrplot 0.91 loaded

input = subset(input, select = -c(PPLAYER, ID, TEAM, FP, L))
model= lm(AllStarRank~. ,data = input)
correlation=cor(input);print(correlation)
```

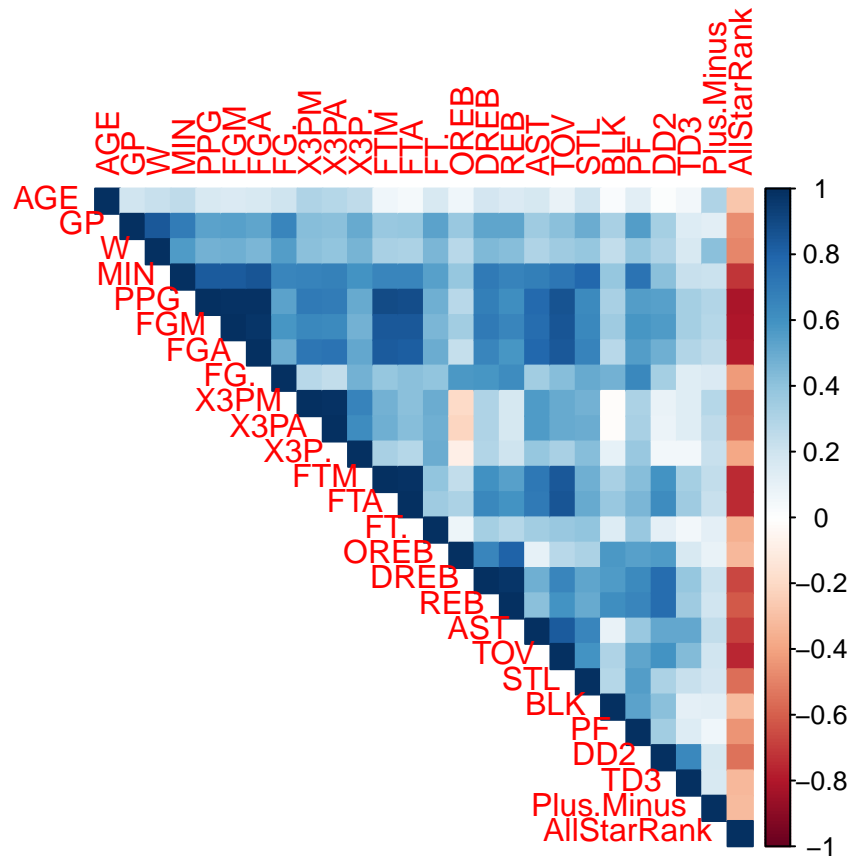
##	AGE	GP	W	MIN	PPG	FGM
## AGE	1.00000000	0.1960184	0.2206600	0.2554011	0.1638588	0.1530430
## GP	0.19601844	1.0000000	0.8430460	0.6999429	0.5326586	0.5478575
## W	0.22065998	0.8430460	1.0000000	0.5646752	0.4763017	0.4871001
## MIN	0.25540106	0.6999429	0.5646752	1.0000000	0.8344046	0.8391706
## PPG	0.16385884	0.5326586	0.4763017	0.8344046	1.0000000	0.9892973
## FGM	0.15304295	0.5478575	0.4871001	0.8391706	0.9892973	1.0000000
## FGA	0.16016681	0.5258974	0.4592597	0.8508604	0.9802938	0.9765680
## FG.	0.20398781	0.6578173	0.5503831	0.6586150	0.5391527	0.5832344
## X3PM	0.30527804	0.4238599	0.4189563	0.6669126	0.7004343	0.6430669
## X3PA	0.28957423	0.4197826	0.3970838	0.6785849	0.6926331	0.6348601
## X3P.	0.25408971	0.5052983	0.4622484	0.5992458	0.5035724	0.4774504
## FTM	0.06101227	0.3797010	0.3246686	0.6531541	0.8933259	0.8473570
## FTA	0.04258516	0.3842119	0.3157760	0.6564619	0.8829227	0.8485080
## FT.	0.16516005	0.5322275	0.4581832	0.5439303	0.4811442	0.4582974
## OREB	0.06284925	0.3769322	0.2764002	0.3806208	0.2761680	0.3493236
## DREB	0.18203052	0.5281877	0.4424720	0.7090804	0.6801467	0.7080265
## REB	0.15964312	0.5234976	0.4265316	0.6659781	0.6124132	0.6561864
## AST	0.17024999	0.3528948	0.3066789	0.6894887	0.7772246	0.7600915
## TOV	0.09745609	0.4127464	0.3523463	0.7213219	0.8642100	0.8502188
## STL	0.19574350	0.4977676	0.3802353	0.7813422	0.6363467	0.6495818
## BLK	0.02899747	0.3288669	0.2464631	0.3844737	0.3235164	0.3527511
## PF	0.12484034	0.5525904	0.3846378	0.7356304	0.5555703	0.5848503
## DD2	0.01359389	0.3377840	0.3076028	0.4148597	0.5484608	0.5653639
## TD3	0.05200609	0.1473457	0.1638558	0.2233516	0.3305992	0.3337188

## Plus.Minus	0.30118995	0.1275178	0.4181422	0.2156886	0.2948090	0.2836779
## AllStarRank	-0.27387112	-0.4610618	-0.4891655	-0.7129347	-0.8148292	-0.8029102
##	FGA	FG.	X3PM	X3PA	X3P.	
## AGE	0.1601668	0.2039878	0.30527804	0.28957423	0.25408971	
## GP	0.5258974	0.6578173	0.42385991	0.41978263	0.50529831	
## W	0.4592597	0.5503831	0.41895628	0.39708382	0.46224835	
## MIN	0.8508604	0.6586150	0.66691259	0.67858488	0.59924577	
## PPG	0.9802938	0.5391527	0.70043427	0.69263309	0.50357242	
## FGM	0.9765680	0.5832344	0.64306694	0.63486013	0.47745036	
## FGA	1.0000000	0.4990031	0.72507089	0.73589395	0.51123190	
## FG.	0.4990031	1.0000000	0.27680158	0.24151526	0.47499346	
## X3PM	0.7250709	0.2768016	1.00000000	0.98266956	0.66154889	
## X3PA	0.7358940	0.2415153	0.98266956	1.00000000	0.62217539	
## X3P.	0.5112319	0.4749935	0.66154889	0.62217539	1.00000000	
## FTM	0.8321297	0.3852716	0.47844595	0.48029390	0.32965117	
## FTA	0.8219124	0.4186366	0.41807964	0.42431260	0.28832830	
## FT.	0.4933646	0.3981259	0.49455797	0.48466353	0.49436998	
## OREB	0.2331225	0.5747246	-0.19583554	-0.21172082	-0.08238780	
## DREB	0.6585317	0.5833782	0.30561096	0.30353064	0.29750392	
## REB	0.5826006	0.6270052	0.17785297	0.17155265	0.20586421	
## AST	0.7801717	0.3438093	0.56745965	0.56934265	0.38233961	
## TOV	0.8483864	0.4205304	0.50306003	0.50813564	0.32222158	
## STL	0.6649665	0.5029862	0.47690802	0.49573276	0.42572635	
## BLK	0.2787101	0.4704382	-0.01473542	-0.01260028	0.10432052	
## PF	0.5534844	0.6454042	0.31324740	0.32282103	0.37684835	
## DD2	0.4873511	0.3349013	0.09912479	0.08587717	0.05524793	
## TD3	0.2909208	0.1351241	0.13833892	0.13429069	0.05562682	
## Plus.Minus	0.2584198	0.1526151	0.28603371	0.25572392	0.22390523	
## AllStarRank	-0.7850107	-0.4298340	-0.56003144	-0.54425949	-0.38084365	
##	FTM	FTA	FT.	OREB	DREB	
## AGE	0.06101227	0.04258516	0.16516005	0.06284925	0.1820305	
## GP	0.37970104	0.38421194	0.53222753	0.37693219	0.5281877	
## W	0.32466856	0.31577597	0.45818315	0.27640024	0.4424720	
## MIN	0.65315410	0.65646191	0.54393033	0.38062075	0.7090804	
## PPG	0.89332587	0.88292266	0.48114418	0.27616796	0.6801467	
## FGM	0.84735703	0.84850799	0.45829744	0.34932355	0.7080265	
## FGA	0.83212966	0.82191239	0.49336455	0.23312248	0.6585317	
## FG.	0.38527162	0.41863661	0.39812595	0.57472459	0.5833782	
## X3PM	0.47844595	0.41807964	0.49455797	-0.19583554	0.3056110	
## X3PA	0.48029390	0.42431260	0.48466353	-0.21172082	0.3035306	
## X3P.	0.32965117	0.28832830	0.49436998	-0.08238780	0.2975039	
## FTM	1.00000000	0.98654887	0.39330316	0.24242497	0.6026366	
## FTA	0.98654887	1.00000000	0.35090547	0.31570772	0.6464981	
## FT.	0.39330316	0.35090547	1.00000000	0.07352325	0.3354118	
## OREB	0.24242497	0.31570772	0.07352325	1.00000000	0.6517336	
## DREB	0.60263660	0.64649810	0.33541185	0.65173356	1.0000000	
## REB	0.54234049	0.59855635	0.28210885	0.80798180	0.9732708	
## AST	0.71165783	0.70027283	0.34622156	0.10939749	0.4897772	
## TOV	0.84817458	0.85853395	0.37860618	0.27823805	0.6576444	
## STL	0.48753833	0.50167217	0.39679066	0.31053184	0.5264741	
## BLK	0.32532011	0.37935776	0.14210380	0.57322316	0.5647516	
## PF	0.42925788	0.45944227	0.37846114	0.54453077	0.6353778	
## DD2	0.59295058	0.62873384	0.11640966	0.56140227	0.7645793	
## TD3	0.33411691	0.35862908	0.05426963	0.16910195	0.3893826	

## Plus.Minus	0.24102986	0.22783390	0.11506400	0.09177158	0.2160332
## AllStarRank	-0.74475854	-0.74080654	-0.35572465	-0.32350050	-0.6660017
##	REB	AST	TOV	STL	BLK
## AGE	0.1596431	0.17024999	0.09745609	0.1957435	0.02899747
## GP	0.5234976	0.35289481	0.41274636	0.4977676	0.32886688
## W	0.4265316	0.30667885	0.35234628	0.3802353	0.24646314
## MIN	0.6659781	0.68948865	0.72132193	0.7813422	0.38447366
## PPG	0.6124132	0.77722462	0.86420999	0.6363467	0.32351644
## FGM	0.6561864	0.76009148	0.85021878	0.6495818	0.35275111
## FGA	0.5826006	0.78017168	0.84838645	0.6649665	0.27871009
## FG.	0.6270052	0.34380931	0.42053043	0.5029862	0.47043819
## X3PM	0.1778530	0.56745965	0.50306003	0.4769080	-0.01473542
## X3PA	0.1715527	0.56934265	0.50813564	0.4957328	-0.01260028
## X3P.	0.2058642	0.38233961	0.32222158	0.4257263	0.10432052
## FTM	0.5423405	0.71165783	0.84817458	0.4875383	0.32532011
## FTA	0.5985564	0.70027283	0.85853395	0.5016722	0.37935776
## FT.	0.2821088	0.34622156	0.37860618	0.3967907	0.14210380
## OREB	0.8079818	0.10939749	0.27823805	0.3105318	0.57322316
## DREB	0.9732708	0.48977720	0.65764440	0.5264741	0.56475159
## REB	1.0000000	0.41418001	0.59562834	0.5041075	0.61075459
## AST	0.4141800	1.00000000	0.83684786	0.6548433	0.09939696
## TOV	0.5956283	0.83684786	1.00000000	0.5954935	0.30029998
## STL	0.5041075	0.65484331	0.59549349	1.0000000	0.28336134
## BLK	0.6107546	0.09939696	0.30029998	0.2833613	1.00000000
## PF	0.6575017	0.37049994	0.52177035	0.5589262	0.53452351
## DD2	0.7642972	0.51275106	0.59942542	0.3194270	0.41609935
## TD3	0.3534395	0.51175547	0.43183295	0.2211978	0.11940796
## Plus.Minus	0.1967004	0.24532668	0.19736493	0.1899944	0.12956649
## AllStarRank	-0.6152969	-0.68272197	-0.75489942	-0.5538292	-0.31636803
##	PF	DD2	TD3	Plus.Minus	AllStarRank
## AGE	0.12484034	0.01359389	0.05200609	0.30118995	-0.2738711
## GP	0.55259039	0.33778400	0.14734565	0.12751781	-0.4610618
## W	0.38463778	0.30760277	0.16385582	0.41814216	-0.4891655
## MIN	0.73563039	0.41485973	0.22335158	0.21568858	-0.7129347
## PPG	0.55557026	0.54846079	0.33059918	0.29480895	-0.8148292
## FGM	0.58485032	0.56536390	0.33371879	0.28367792	-0.8029102
## FGA	0.55348439	0.48735106	0.29092078	0.25841977	-0.7850107
## FG.	0.64540422	0.33490130	0.13512410	0.15261513	-0.4298340
## X3PM	0.31324740	0.09912479	0.13833892	0.28603371	-0.5600314
## X3PA	0.32282103	0.08587717	0.13429069	0.25572392	-0.5442595
## X3P.	0.37684835	0.05524793	0.05562682	0.22390523	-0.3808436
## FTM	0.42925788	0.59295058	0.33411691	0.24102986	-0.7447585
## FTA	0.45944227	0.62873384	0.35862908	0.22783390	-0.7408065
## FT.	0.37846114	0.11640966	0.05426963	0.11506400	-0.3557246
## OREB	0.54453077	0.56140227	0.16910195	0.09177158	-0.3235005
## DREB	0.63537777	0.76457934	0.38938260	0.21603321	-0.6660017
## REB	0.65750168	0.76429719	0.35343951	0.19670038	-0.6152969
## AST	0.37049994	0.51275106	0.51175547	0.24532668	-0.6827220
## TOV	0.52177035	0.59942542	0.43183295	0.19736493	-0.7548994
## STL	0.55892617	0.31942704	0.22119780	0.18999436	-0.5538292
## BLK	0.53452351	0.41609935	0.11940796	0.12956649	-0.3163680
## PF	1.00000000	0.34254220	0.14675696	0.06328379	-0.4416425
## DD2	0.34254220	1.00000000	0.64332014	0.17410333	-0.5485662
## TD3	0.14675696	0.64332014	1.00000000	0.16025464	-0.3269609

```
## Plus.Minus 0.06328379 0.17410333 0.16025464 1.00000000 -0.3185606
## AllStarRank -0.44164252 -0.54856621 -0.32696095 -0.31856059 1.00000000
```

```
corrplot(correlation, method='color', type='upper')
```



```
library(car)
```

```
## Loading required package: carData
```

```
vif(model)
```

```
##      AGE      GP      W      MIN      PPG      FGM
## 1.332331 7.317597 6.069358 13.312547 10822.300808 5476.287641
##      FGA      FG.      X3PM      X3PA      X3P.      FTM
## 90.202559 3.976728 269.858197 66.741229 2.987555 629.323567
##      FTA      FT.      OREB      DREB      REB      AST
## 71.506122 1.915630 314.222811 2074.122110 3465.181111 7.176872
##      TOV      STL      BLK      PF      DD2      TD3
## 8.600731 3.118280 2.081541 3.388623 6.725222 2.505020
## Plus.Minus
## 2.068652
```

```
summary(model)
```

```
##
## Call:
## lm(formula = AllStarRank ~ ., data = input)
##
## Residuals:
```

```
##      Min      1Q  Median      3Q      Max
## -52.713 -10.429  -0.153  10.319  45.801
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 134.91940    9.87123  13.668 < 2e-16 ***
## AGE         -1.00997    0.34494   -2.928  0.00385 **
## GP           0.87435    0.32292    2.708  0.00742 **
## W           -2.06379    0.48888   -4.221 3.83e-05 ***
## MIN         -0.49162    0.46407   -1.059  0.29084
## PPG         -7.40654   17.38991   -0.426  0.67068
## FGM          7.60487   34.81910    0.218  0.82735
## FGA          2.77017    2.22935    1.243  0.21562
## FG.          0.45259    0.18547    2.440  0.01564 *
## X3PM         -4.18538   20.24226   -0.207  0.83643
## X3PA          2.07783    4.06922    0.511  0.61023
## X3P.          0.01376    0.14946    0.092  0.92676
## FTM          1.22565   18.56767    0.066  0.94744
## FTA          0.49676    5.20176    0.095  0.92402
## FT.          0.08997    0.07190    1.251  0.21245
## OREB         1.50240   27.90161    0.054  0.95712
## DREB         4.48605   27.90651    0.161  0.87247
## REB        -8.29419   27.95926   -0.297  0.76707
## AST        -2.49225    1.67652   -1.487  0.13886
## TOV        -3.91012    3.99588   -0.979  0.32911
## STL        -1.81771    5.44379   -0.334  0.73884
## BLK        -3.08453    4.22817   -0.730  0.46662
## PF          4.77374    2.65694    1.797  0.07404 .
## DD2          0.62583    0.60964    1.027  0.30599
## TD3          0.86632    1.92107    0.451  0.65256
## Plus.Minus   1.08048    0.52849    2.044  0.04235 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18.15 on 182 degrees of freedom
## Multiple R-squared:  0.7651, Adjusted R-squared:  0.7329
## F-statistic: 23.72 on 25 and 182 DF,  p-value: < 2.2e-16
```

```
library(leaps)
allmodels = regsubsets(AllStarRank~., input, nbest=2, method = "exhaustive")
allsummary = summary(allmodels)
r2 = round(allsummary$rsq*100 , 1)
r2_adj = round(allsummary$adjr2*100, 1)
CP = round(allsummary$cp, 1)
SSE = allsummary$rss
n = allmodels$nn
k = as.numeric(rownames(allsummary$which))
S = round(sqrt(allsummary$rss/(n-k-1)), 2)
cbind(r2, r2_adj, S, CP, allsummary$outmat)
```

```
##      r2      r2_adj S      CP      AGE GP  W  MIN PPG FGM FGA FG. X3PM X3PA
## 1  ( 1 ) "66.4" "66.2" "20.41" "56.4" " " " " " " " " " " " " " " " "
## 1  ( 2 ) "64.5" "64.3" "20.99" "71.3" " " " " " " " " " " " " " " " "
## 2  ( 1 ) "68.7" "68.4" "19.74" "40.4" " " " " " " " " " " " " " " " "
## 2  ( 2 ) "68.6" "68.3" "19.79" "41.6" " " " " " " " " " " " " " " " "
```

```
## 3 ( 1 ) "70.4" "69.9" "19.26" "29.7" "*" " " " " " " " " " " " " " " " " " " " " "
## 3 ( 2 ) "70.3" "69.8" "19.29" "30.2" "*" " " " " " " " " " " " " " " " " " " " " "
## 4 ( 1 ) "71.3" "70.8" "18.99" "24.2" "*" " " " " " " " " " " " " " " " " " " " " "
## 4 ( 2 ) "71.2" "70.7" "19.03" "25" "*" " " " " " " " " " " " " " " " " " " " " "
## 5 ( 1 ) "72.5" "71.9" "18.63" "16.8" "*" " " "*" " " " " " " " " " " " " " " " "
## 5 ( 2 ) "72.4" "71.7" "18.67" "17.7" "*" "*" "*" " " " " " " " " " " " " " " " "
## 6 ( 1 ) "73.4" "72.6" "18.38" "12.1" "*" "*" "*" " " " " " " " " " " " " " " " "
## 6 ( 2 ) "73.4" "72.6" "18.4" "12.5" "*" "*" "*" " " " " " " " " " " " " " " " "
## 7 ( 1 ) "74.1" "73.2" "18.17" "8.4" "*" "*" "*" " " " " " " " " " " " " " " " "
## 7 ( 2 ) "74.1" "73.2" "18.19" "8.8" "*" "*" "*" " " " " " " " " " " " " " " " "
## 8 ( 1 ) "74.6" "73.6" "18.05" "6.7" "*" "*" "*" " " " " " " " " " " " " " " " "
## 8 ( 2 ) "74.5" "73.5" "18.1" "7.8" "*" "*" "*" " " " " " " " " " " " " " " " "
##
##      X3P. FTM FTA FT. OREB DREB REB AST TOV STL BLK PF DD2 TD3 Plus.Minus
## 1 ( 1 ) " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " "
## 1 ( 2 ) " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " " "
## 2 ( 1 ) " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " " "
## 2 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 3 ( 1 ) " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " " "
## 3 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 4 ( 1 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 4 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 5 ( 1 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 5 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 6 ( 1 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 6 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 7 ( 1 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 7 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 8 ( 1 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
## 8 ( 2 ) " " " " " " " " " " " " " " "*" " " " " " " " " " " " " " " " " " " " "
```

We choose model 1 that contains 8 variables. This has the highest adjusted R^2 value and lowest C_p . The 8 variables are Age, Games Played, Wins, Points per Game, Field Goals Attempted, Field Goal Percentage, Rebounds, Assists.

```
model8var=lm(AllStarRank~AGE+GP+W+PPG+FGA+FG.+REB+AST)
vif(model8var)
```

```
##      AGE      GP      W      PPG      FGA      FG.      REB      AST
## 1.075780 4.523346 3.579074 29.854102 27.831255 2.322817 2.033955 2.667912
```

```
step_backward=step(model, direction='backward')
```

```
## Start: AIC=1230.15
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + X3P. + FTM + FTA + FT. + OREB + DREB + REB + AST +
##      TOV + STL + BLK + PF + DD2 + TD3 + Plus.Minus
##
##      Df Sum of Sq  RSS    AIC
## - OREB      1      1.0 59979 1228.2
## - FTM       1      1.4 59979 1228.2
## - X3P.      1      2.8 59980 1228.2
## - FTA       1      3.0 59981 1228.2
## - DREB      1      8.5 59986 1228.2
## - X3PM      1     14.1 59992 1228.2
## - FGM       1     15.7 59993 1228.2
## - REB       1     29.0 60007 1228.2
```



```

## - STL          1      36.7 60014 1228.3
## - PPG          1      59.8 60037 1228.4
## - TD3          1      67.0 60045 1228.4
## - X3PA         1      85.9 60063 1228.5
## - BLK          1     175.4 60153 1228.8
## - TOV          1     315.6 60293 1229.2
## - DD2          1     347.3 60325 1229.3
## - MIN          1     369.8 60347 1229.4
## - FGA          1     508.8 60486 1229.9
## - FT.          1     516.0 60494 1229.9
## <none>                59978 1230.2
## - AST          1      728.3 60706 1230.7
## - PF           1    1063.8 61041 1231.8
## - Plus.Minus   1    1377.5 61355 1232.9
## - FG.          1    1962.3 61940 1234.8
## - GP           1    2416.0 62394 1236.4
## - AGE          1    2825.3 62803 1237.7
## - W            1    5872.8 65850 1247.6
##
## Step:  AIC=1228.15
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + X3P. + FTM + FTA + FT. + DREB + REB + AST + TOV +
##      STL + BLK + PF + DD2 + TD3 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - FTM      1      1.5 59980 1226.2
## - X3P.      1      2.7 59981 1226.2
## - FTA       1      3.1 59982 1226.2
## - X3PM      1     13.7 59992 1226.2
## - FGM       1     16.1 59995 1226.2
## - STL       1     38.3 60017 1226.3
## - PPG       1     60.6 60039 1226.4
## - TD3       1     67.9 60046 1226.4
## - X3PA      1     85.3 60064 1226.5
## - BLK       1    174.7 60153 1226.8
## - DREB      1    180.9 60159 1226.8
## - TOV       1    317.9 60296 1227.2
## - DD2       1    347.6 60326 1227.4
## - MIN       1    370.9 60349 1227.4
## - FGA       1    508.2 60487 1227.9
## - FT.       1    516.9 60495 1227.9
## <none>                59979 1228.2
## - AST       1    728.8 60707 1228.7
## - PF        1   1069.1 61048 1229.8
## - REB       1   1233.2 61212 1230.4
## - Plus.Minus 1   1386.3 61365 1230.9
## - FG.       1   1965.6 61944 1232.9
## - GP        1   2415.6 62394 1234.4
## - AGE       1   2825.5 62804 1235.7
## - W         1   5889.6 65868 1245.6
##
## Step:  AIC=1226.16
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + X3P. + FTA + FT. + DREB + REB + AST + TOV + STL +

```

```

##      BLK + PF + DD2 + TD3 + Plus.Minus
##
##      Df Sum of Sq  RSS    AIC
## - X3P.      1      2.9 59983 1224.2
## - FTA       1      5.2 59985 1224.2
## - STL       1     39.1 60019 1224.3
## - TD3       1     66.7 60047 1224.4
## - X3PM      1     68.0 60048 1224.4
## - FGM       1     70.0 60050 1224.4
## - X3PA      1     86.8 60067 1224.5
## - DREB      1    180.5 60161 1224.8
## - BLK       1    185.6 60166 1224.8
## - TOV       1    327.4 60307 1225.3
## - DD2       1    351.8 60332 1225.4
## - MIN       1    375.5 60356 1225.5
## - PPG       1    414.8 60395 1225.6
## - FGA       1    506.8 60487 1225.9
## - FT.       1    543.1 60523 1226.0
## <none>              59980 1226.2
## - AST       1    736.4 60716 1226.7
## - PF        1   1069.2 61049 1227.8
## - REB       1   1231.7 61212 1228.4
## - Plus.Minus 1   1384.9 61365 1228.9
## - FG.       1   1964.3 61944 1230.9
## - GP        1   2415.0 62395 1232.4
## - AGE       1   2827.9 62808 1233.7
## - W         1   5889.3 65869 1243.6
##
## Step:  AIC=1224.17
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + FTA + FT. + DREB + REB + AST + TOV + STL + BLK + PF +
##      DD2 + TD3 + Plus.Minus
##
##      Df Sum of Sq  RSS    AIC
## - FTA       1      4.9 59988 1222.2
## - STL       1     39.0 60022 1222.3
## - X3PM      1     65.3 60048 1222.4
## - TD3       1     67.5 60050 1222.4
## - FGM       1     67.8 60051 1222.4
## - X3PA      1     85.5 60068 1222.5
## - BLK       1    184.8 60168 1222.8
## - DREB      1    224.0 60207 1222.9
## - TOV       1    343.4 60326 1223.4
## - DD2       1    354.0 60337 1223.4
## - MIN       1    377.3 60360 1223.5
## - PPG       1    412.4 60395 1223.6
## - FGA       1    533.2 60516 1224.0
## - FT.       1    546.9 60530 1224.1
## <none>              59983 1224.2
## - AST       1    740.2 60723 1224.7
## - PF        1   1083.0 61066 1225.9
## - Plus.Minus 1   1416.8 61400 1227.0
## - REB       1   1481.9 61465 1227.2
## - FG.       1   2231.0 62214 1229.8

```

```

## - GP          1      2450.5 62433 1230.5
## - AGE         1      2827.2 62810 1231.8
## - W           1      5914.4 65897 1241.7
##
## Step:  AIC=1222.19
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + FT. + DREB + REB + AST + TOV + STL + BLK + PF + DD2 +
##      TD3 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - STL      1      37.4 60025 1220.3
## - TD3      1      73.4 60061 1220.4
## - X3PA     1      94.6 60082 1220.5
## - X3PM     1     159.4 60147 1220.7
## - FGM      1     161.9 60150 1220.8
## - BLK      1     182.0 60170 1220.8
## - DREB     1     224.2 60212 1221.0
## - TOV      1     341.0 60329 1221.4
## - DD2      1     349.3 60337 1221.4
## - MIN      1     378.3 60366 1221.5
## - FGA      1     528.8 60517 1222.0
## - FT.      1     546.2 60534 1222.1
## <none>                59988 1222.2
## - AST      1     751.9 60740 1222.8
## - PF       1    1079.5 61067 1223.9
## - Plus.Minus 1    1426.0 61414 1225.1
## - REB      1    1478.0 61466 1225.2
## - FG.      1    2268.7 62256 1227.9
## - GP       1    2477.0 62465 1228.6
## - AGE      1    2878.1 62866 1229.9
## - PPG      1    3283.5 63271 1231.3
## - W        1    6021.5 66009 1240.1
##
## Step:  AIC=1220.32
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + FT. + DREB + REB + AST + TOV + BLK + PF + DD2 + TD3 +
##      Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - TD3      1      74.4 60100 1218.6
## - X3PA     1      90.4 60116 1218.6
## - X3PM     1     152.6 60178 1218.8
## - FGM      1     155.5 60181 1218.8
## - BLK      1     192.2 60217 1219.0
## - DREB     1     241.9 60267 1219.2
## - TOV      1     333.9 60359 1219.5
## - DD2      1     365.0 60390 1219.6
## - FGA      1     517.9 60543 1220.1
## - MIN      1     524.4 60550 1220.1
## - FT.      1     540.3 60565 1220.2
## <none>                60025 1220.3
## - AST      1     913.3 60939 1221.5
## - PF       1    1089.8 61115 1222.1
## - Plus.Minus 1    1399.0 61424 1223.1

```

```

## - REB          1      1532.0 61557 1223.6
## - FG.          1      2262.0 62287 1226.0
## - GP           1      2461.9 62487 1226.7
## - AGE          1      2863.9 62889 1228.0
## - PPG          1      3246.2 63271 1229.3
## - W            1      5985.2 66010 1238.1
##
## Step:  AIC=1218.57
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      X3PA + FT. + DREB + REB + AST + TOV + BLK + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - X3PA      1      130.1 60230 1217.0
## - X3PM      1      183.7 60283 1217.2
## - BLK       1      198.1 60298 1217.3
## - FGM       1      228.4 60328 1217.4
## - DREB      1      281.5 60381 1217.5
## - TOV       1      316.9 60417 1217.7
## - FGA       1      456.1 60556 1218.2
## - FT.       1      568.1 60668 1218.5
## - MIN       1      571.0 60671 1218.5
## <none>              60100 1218.6
## - DD2       1      676.7 60776 1218.9
## - AST       1      838.9 60939 1219.5
## - PF        1     1157.4 61257 1220.5
## - Plus.Minus 1     1423.3 61523 1221.4
## - REB       1     1689.6 61789 1222.3
## - FG.       1     2278.9 62379 1224.3
## - GP        1     2447.7 62547 1224.9
## - AGE       1     2849.3 62949 1226.2
## - PPG       1     3552.7 63652 1228.5
## - W         1     5987.1 66087 1236.3
##
## Step:  AIC=1217.02
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + X3PM +
##      FT. + DREB + REB + AST + TOV + BLK + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - X3PM      1       66.2 60296 1215.2
## - FGM       1      137.0 60367 1215.5
## - BLK       1      175.2 60405 1215.6
## - DREB      1      314.5 60544 1216.1
## - TOV       1      341.8 60572 1216.2
## - FT.       1      496.1 60726 1216.7
## - MIN       1      504.6 60734 1216.8
## <none>              60230 1217.0
## - DD2       1      717.2 60947 1217.5
## - AST       1      891.7 61121 1218.1
## - FGA       1     1151.3 61381 1219.0
## - PF        1     1216.2 61446 1219.2
## - Plus.Minus 1     1461.5 61691 1220.0
## - REB       1     1822.1 62052 1221.2
## - FG.       1     2218.2 62448 1222.5
## - GP        1     2586.7 62816 1223.8

```

```

## - AGE          1      2803.2 63033 1224.5
## - PPG          1      3551.8 63781 1226.9
## - W            1      6109.3 66339 1235.1
##
## Step:  AIC=1215.25
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + FT. +
##      DREB + REB + AST + TOV + BLK + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - BLK      1      147.2 60443 1213.8
## - DREB     1      257.7 60554 1214.1
## - FGM      1      281.6 60578 1214.2
## - TOV      1      281.8 60578 1214.2
## - FT.      1      500.1 60796 1215.0
## <none>                60296 1215.2
## - MIN      1      599.1 60895 1215.3
## - DD2      1      751.2 61047 1215.8
## - AST      1      910.5 61206 1216.4
## - FGA      1     1085.2 61381 1217.0
## - PF       1     1185.5 61481 1217.3
## - Plus.Minus 1     1429.8 61726 1218.1
## - REB      1     1786.4 62082 1219.3
## - FG.      1     2178.0 62474 1220.6
## - GP       1     2617.8 62914 1222.1
## - AGE      1     3089.4 63385 1223.7
## - PPG      1     5015.5 65311 1229.9
## - W       1     6307.7 66604 1234.0
##
## Step:  AIC=1213.76
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + FT. +
##      DREB + REB + AST + TOV + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - DREB     1      265.9 60709 1212.7
## - FGM      1      286.3 60729 1212.7
## - TOV      1      314.8 60758 1212.8
## - FT.      1      516.9 60960 1213.5
## <none>                60443 1213.8
## - MIN      1      621.9 61065 1213.9
## - DD2      1      721.5 61165 1214.2
## - AST      1      803.6 61247 1214.5
## - PF       1     1070.2 61513 1215.4
## - FGA      1     1174.7 61618 1215.8
## - Plus.Minus 1     1343.4 61786 1216.3
## - REB      1     1904.4 62348 1218.2
## - FG.      1     2101.4 62545 1218.9
## - GP       1     2584.0 63027 1220.5
## - AGE      1     3000.8 63444 1221.8
## - PPG      1     5187.2 65630 1228.9
## - W       1     6198.1 66641 1232.1
##
## Step:  AIC=1212.67
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGM + FGA + FG. + FT. +
##      REB + AST + TOV + PF + DD2 + Plus.Minus

```

```

##
##           Df Sum of Sq  RSS    AIC
## - FGM      1    141.6 60851 1211.2
## - TOV      1    324.0 61033 1211.8
## - FT.      1    566.5 61275 1212.6
## <none>                60709 1212.7
## - MIN      1    607.5 61316 1212.7
## - DD2      1    750.0 61459 1213.2
## - AST      1    770.5 61480 1213.3
## - PF       1    974.4 61683 1214.0
## - Plus.Minus 1   1263.1 61972 1215.0
## - FGA      1   1572.5 62282 1216.0
## - FG.      1   1957.0 62666 1217.3
## - GP       1   2460.3 63169 1218.9
## - AGE      1   2895.6 63605 1220.4
## - REB      1   4491.8 65201 1225.5
## - PPG      1   4924.4 65633 1226.9
## - W        1   5990.6 66700 1230.2
##
## Step:  AIC=1211.16
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGA + FG. + FT. + REB +
##           AST + TOV + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - TOV      1    411.5 61262 1210.6
## - FT.      1    462.7 61313 1210.7
## <none>                60851 1211.2
## - AST      1    725.7 61576 1211.6
## - DD2      1    747.6 61598 1211.7
## - MIN      1    787.3 61638 1211.8
## - PF       1   1054.4 61905 1212.7
## - Plus.Minus 1   1235.3 62086 1213.3
## - GP       1   2420.7 63271 1217.3
## - FGA      1   2558.6 63409 1217.7
## - FG.      1   2769.7 63620 1218.4
## - AGE      1   3085.1 63936 1219.4
## - REB      1   4377.1 65228 1223.6
## - W        1   5892.0 66743 1228.4
## - PPG      1   7624.6 68475 1233.7
##
## Step:  AIC=1210.56
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGA + FG. + FT. + REB +
##           AST + PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - FT.      1    448.1 61710 1210.1
## <none>                61262 1210.6
## - MIN      1    618.9 61881 1210.7
## - DD2      1    816.6 62079 1211.3
## - PF       1    830.5 62093 1211.4
## - Plus.Minus 1   1530.8 62793 1213.7
## - AST      1   2138.3 63400 1215.7
## - GP       1   2567.4 63829 1217.1
## - FGA      1   2708.8 63971 1217.6

```

```

## - AGE          1    2930.2 64192 1218.3
## - FG.          1    3243.1 64505 1219.3
## - REB          1    5285.1 66547 1225.8
## - W            1    6216.1 67478 1228.7
## - PPG          1    9451.4 70713 1238.4
##
## Step:  AIC=1210.07
## AllStarRank ~ AGE + GP + W + MIN + PPG + FGA + FG. + REB + AST +
##      PF + DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - MIN      1      559.9 62270 1210.0
## <none>                      61710 1210.1
## - DD2      1      690.8 62401 1210.4
## - PF       1      828.9 62539 1210.8
## - Plus.Minus 1    1476.7 63187 1213.0
## - AST      1    2130.5 63841 1215.1
## - FGA      1    2759.7 64470 1217.2
## - AGE      1    2871.4 64582 1217.5
## - GP       1    2936.8 64647 1217.7
## - FG.      1    3224.4 64935 1218.7
## - REB      1    5307.1 67017 1225.2
## - W        1    6098.8 67809 1227.7
## - PPG      1    9300.6 71011 1237.3
##
## Step:  AIC=1209.95
## AllStarRank ~ AGE + GP + W + PPG + FGA + FG. + REB + AST + PF +
##      DD2 + Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## - PF       1      467.3 62737 1209.5
## <none>                      62270 1210.0
## - DD2      1    1281.3 63551 1212.2
## - Plus.Minus 1    1437.8 63708 1212.7
## - FGA      1    2321.4 64591 1215.6
## - GP       1    2427.0 64697 1215.9
## - FG.      1    3131.2 65401 1218.2
## - AGE      1    3230.7 65501 1218.5
## - AST      1    3512.0 65782 1219.4
## - W        1    5916.9 68187 1226.8
## - REB      1    7070.0 69340 1230.3
## - PPG      1    9069.7 71340 1236.2
##
## Step:  AIC=1209.51
## AllStarRank ~ AGE + GP + W + PPG + FGA + FG. + REB + AST + DD2 +
##      Plus.Minus
##
##           Df Sum of Sq  RSS    AIC
## <none>                      62737 1209.5
## - DD2      1      971.0 63708 1210.7
## - Plus.Minus 1    1377.2 64114 1212.0
## - FGA      1    2369.8 65107 1215.2
## - GP       1    2898.4 65636 1216.9
## - AST      1    3363.2 66100 1218.4

```

```
## - AGE      1      3439.9 66177 1218.6
## - FG.      1      3743.5 66481 1219.6
## - W        1      6444.0 69181 1227.8
## - REB      1      6796.0 69533 1228.9
## - PPG      1      8985.7 71723 1235.3
```

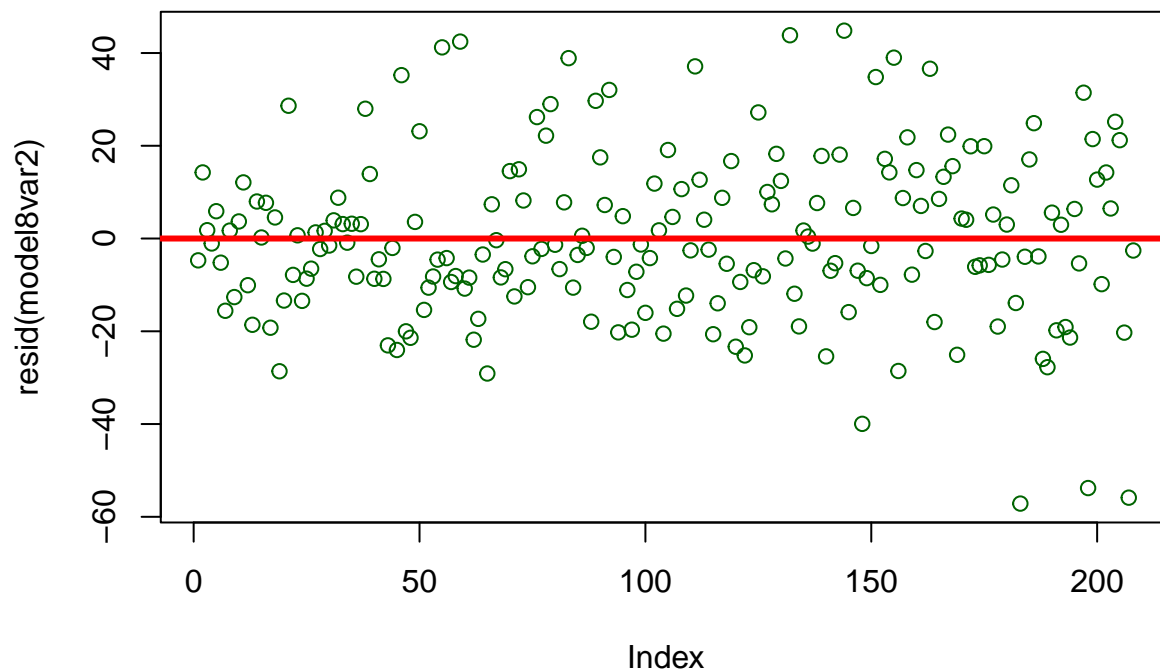
```
model8var2=lm(AllStarRank~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
vif(model8var2)
```

```
##      AGE      GP      W      PPG      FG.      REB      AST
##  1.198464  6.010411  5.535492  3.865659  2.442023  4.437507  2.977787
##      DD2 Plus.Minus
##  3.280499  1.829877
```

Took out FGA because that VIF was over 60. Added DD2 and Plus.Minus because the backwards step-wise regression showed that these variables were useful the model. Above are the updated VIF models and now there is no apparent multicollinearity because no VIF score is over 10.

```
summary(model8var2)
```

```
##
## Call:
## lm(formula = AllStarRank ~ AGE + GP + W + PPG + FG. + REB + AST +
##      DD2 + Plus.Minus)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -57.149 -10.173  -1.816   10.193   44.815
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  142.4542     8.9336   15.946 < 2e-16 ***
## AGE          -1.0971     0.3268   -3.357 0.000944 ***
## GP           0.9021     0.2923    3.086 0.002321 **
## W            -1.9941     0.4664   -4.276 2.96e-05 ***
## PPG          -2.7343     0.3283   -8.329 1.34e-14 ***
## FG.           0.3815     0.1452    2.628 0.009269 **
## REB          -3.8755     0.9994   -3.878 0.000143 ***
## AST          -2.7045     1.0787   -2.507 0.012975 *
## DD2           0.2329     0.4253    0.548 0.584598
## Plus.Minus    0.7955     0.4965    1.602 0.110688
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 18.13 on 198 degrees of freedom
## Multiple R-squared:  0.745, Adjusted R-squared:  0.7335
## F-statistic: 64.29 on 9 and 198 DF, p-value: < 2.2e-16
plot(resid(model8var2),col='dark green')
abline(0,0,col='red',lwd=3)
```

```
library(nortest)
y=AllStarRank
y1=sqrt(y)
y2=y^(0.25)
y3=log(y)

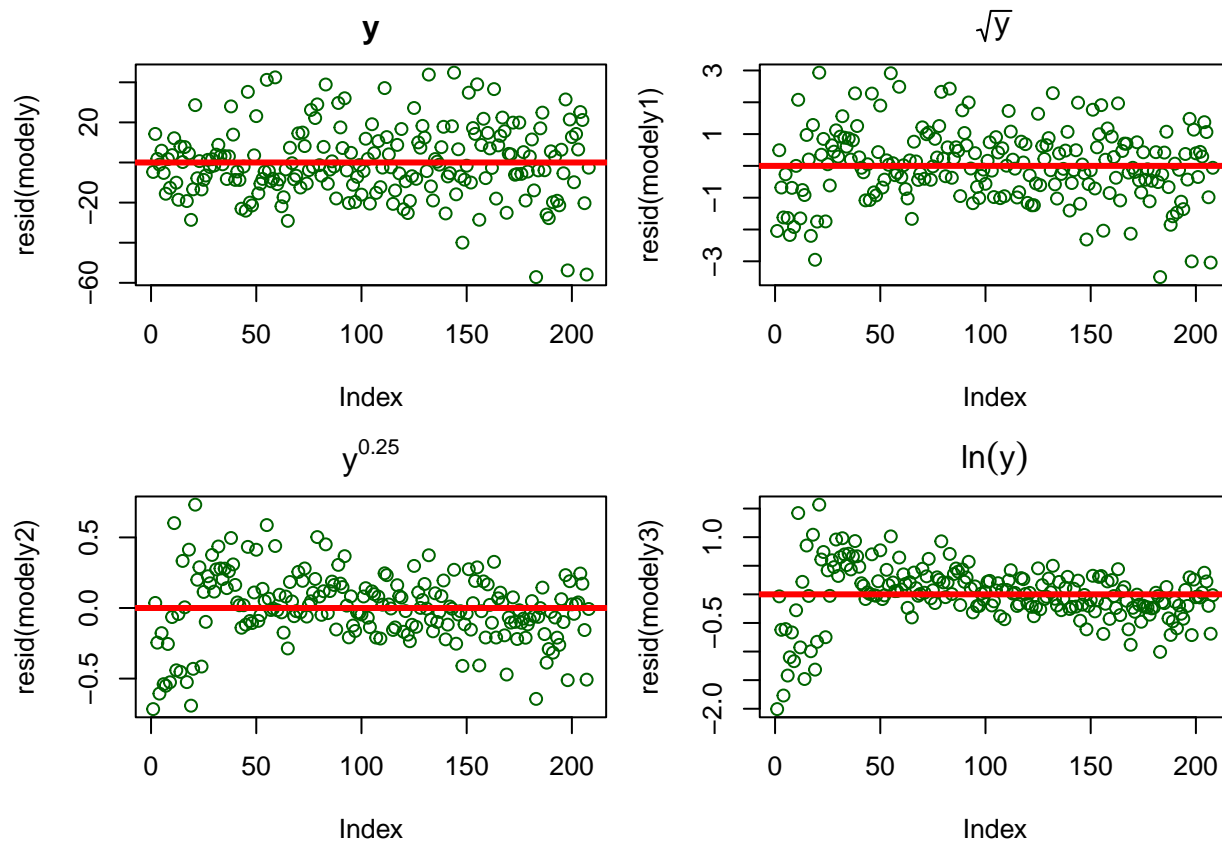
modely=lm(y~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely1=lm(y1~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely2=lm(y2~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely3=lm(y3~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
par(mfrow=c(2,2),mai=c(0.7,0.7,0.4,0.1))

plot(resid(modely),col='dark green',main='y')
abline(0,0,col='red',lwd=3)

plot(resid(modely1),col='dark green',main=bquote(sqrt(y)))
abline(0,0,col='red',lwd=3)

plot(resid(modely2),col='dark green',main=bquote(y^0.25))
abline(0,0,col='red',lwd=3)

plot(resid(modely3),col='dark green',main=bquote(ln(y)))
abline(0,0,col='red',lwd=3)
```



```
library(nortest)
y=AllStarRank
y1=sqrt(y)
y2=y^(0.25)
y3=log(y)

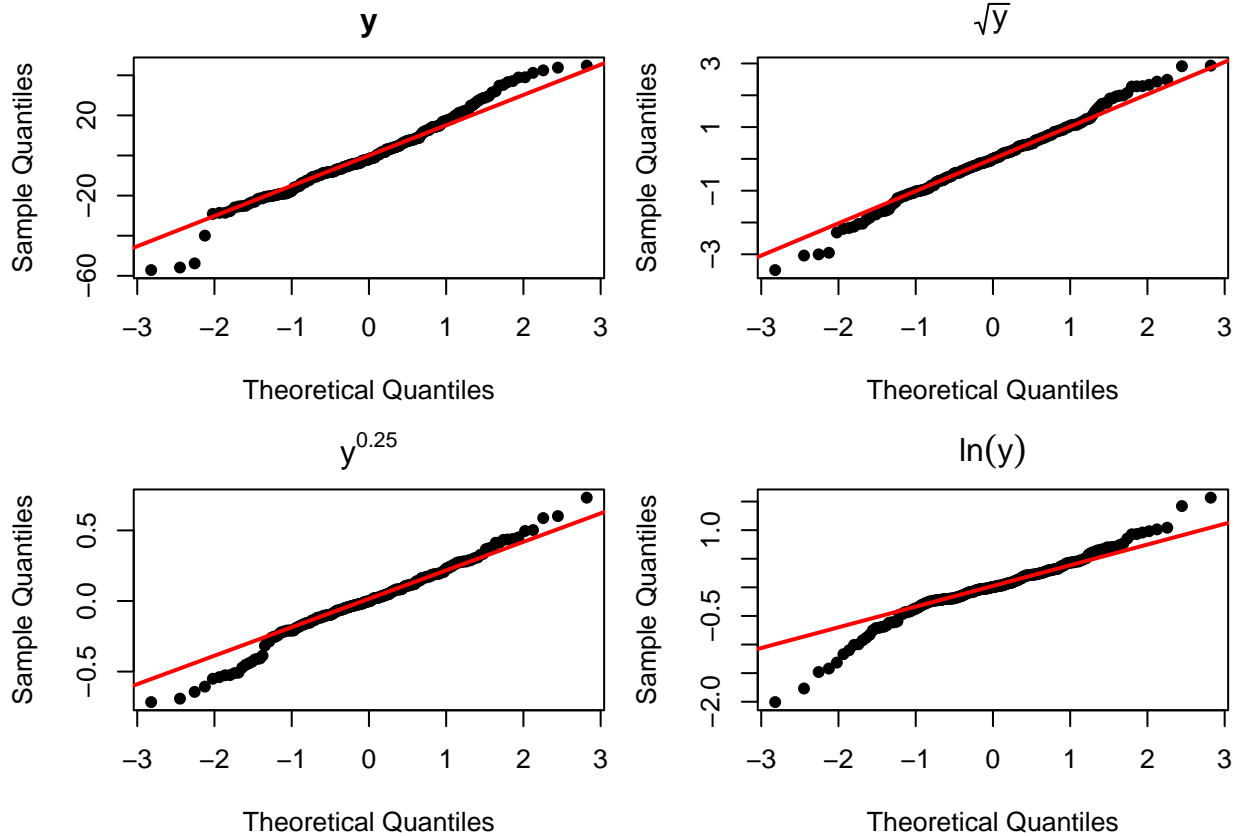
modely=lm(y~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely1=lm(y1~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely2=lm(y2~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)
modely3=lm(y3~AGE+GP+W+PPG+FG.+REB+AST+DD2+Plus.Minus)

par(mfrow=c(2,2),mai=c(0.7,0.7,0.4,0.1))
qqnorm(resid(modely),pch=16, main='y')
qqline(resid(modely),col='red', lwd=2)

qqnorm(resid(modely1),pch=16, main=bquote(sqrt(y)))
qqline(resid(modely1),col='red', lwd=2)

qqnorm(resid(modely2),pch=16, main=bquote(y^0.25))
qqline(resid(modely2),col='red', lwd=2)

qqnorm(resid(modely3),pch=16, main=bquote(ln(y)))
qqline(resid(modely3),col='red', lwd=2)
```



```
ad.test(resid(modely))
```

```
##
## Anderson-Darling normality test
##
## data: resid(modely)
## A = 0.94685, p-value = 0.01633
```

```
ad.test(resid(modely1))
```

```
##
## Anderson-Darling normality test
##
## data: resid(modely1)
## A = 0.45017, p-value = 0.2733
```

```
ad.test(resid(modely2))
```

```
##
## Anderson-Darling normality test
##
## data: resid(modely2)
## A = 1.171, p-value = 0.004561
```

```
ad.test(resid(modely3))
```

```
##
## Anderson-Darling normality test
##
```

```
## data: resid(modely3)
## A = 2.372, p-value = 5.069e-06
```

We selected modely1 which took the square root of y. We chose this model because after running the Anderson-Darling test, we discovered it had the highest p-value. Based off the images above, the data points are most closely aligned to the qqnorm line.

```
k=9
n = length(AllStarRank)
LV_cutoff = 2*(k+1)/n
Hat_i = hatvalues(modely1)
Hat_i[Hat_i > LV_cutoff]
```

```
##          1          2          5          10          13          16          21
## 0.10036467 0.13564050 0.10669667 0.19285459 0.12873161 0.18174767 0.15400890
##          30          39          73          118          157          174          188
## 0.09671702 0.12036058 0.10411135 0.10769084 0.12994419 0.10764578 0.11944982
```

Above are the outliers with respect to the independent variables.

```
k=9
ds = rstudent(modely1)
a = qt(.995,n-k-2)
b = qt(.975,n-k-2)
print(ds[abs(ds)>a])
```

```
##          19          21          55          183          198          207
## -2.630673  2.799746  2.659600 -3.142106 -2.675935 -2.747921
```

```
print(ds[abs(ds)>b])
```

```
##          19          21          38          46          55          59          79          83
## -2.630673  2.799746  2.032860  2.005310  2.659600  2.187781  2.079804  2.139746
##          132          148          183          198          207
##  2.030545 -2.033182 -3.142106 -2.675935 -2.747921
```

Above are outliers with respect to the y value AllStarRank.

```
k=9
cooksD = cooks.distance(modely1)
F0.5 = qf(0.5,k+1,n-k-1) ; print(F0.5)
```

```
## [1] 0.9373542
```

```
F0.8 = qf(0.2,k+1,n-k-1); print(F0.8)
```

```
## [1] 0.6151237
```

```
print("Influential:")
```

```
## [1] "Influential:"
```

```
print(cooksD[cooksD>F0.5])
```

```
## named numeric(0)
```

```
print("Potential to be influential:")
```

```
## [1] "Potential to be influential:"
```

```
print(cooksD[cooksD<F0.5 & cooksD>F0.8])
```

```
## named numeric(0)
anova(modely1)

## Analysis of Variance Table
##
## Response: y1
##
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
AGE	1	72.23	72.23	53.8664	5.424e-12	***
GP	1	187.49	187.49	139.8194	< 2.2e-16	***
W	1	55.60	55.60	41.4618	8.902e-10	***
PPG	1	705.79	705.79	526.3494	< 2.2e-16	***
FG.	1	10.02	10.02	7.4734	0.006829	**
REB	1	30.85	30.85	23.0070	3.169e-06	***
AST	1	14.00	14.00	10.4431	0.001442	**
DD2	1	4.61	4.61	3.4355	0.065296	.
Plus.Minus	1	0.41	0.41	0.3062	0.580644	
Residuals	198	265.50	1.34			

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

MSE is 1.34

MSE <- function(y,yhat){
  n=length(y);
  sum((y-yhat)^2)/n;
}

MAPE <- function(y,yhat){
  n=length(y);
  AE = abs(y-yhat);
  sum(AE/y*100)/n;
}

MAD <- function(y,yhat){
  n=length(y)
  sum(abs(y-yhat))/n;
}

yhat=fitted(modely1)
MSE(y1,yhat)

## [1] 1.276448

MAPE(y1,yhat)

## [1] 16.03014

MAD(y1,yhat)

## [1] 0.8710102
```