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$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

A = Ace of clubs
B = Black Card

$$P(A|B) = \frac{\frac{1}{52}}{\frac{1}{2}} = \frac{2}{52} = \frac{1}{26}, \boxed{A}$$

2. $52 \times 51 \times \dots \times 1$

↓

Possibilities for first card

$$= 52!$$

\boxed{C}

3. $\sum_{n=1,2,4} \sum_{b=1,3} c_{nb} = 1$

$$\sum_{n=1,2,4} (c_n + 3c_n) = 1$$

$$c + 2c + 4c + 3c + 6c + 12c = 1$$

$$c(28) = 1$$

$$c = \frac{1}{28}$$

\boxed{A}

4. $f(x, y) = x^4 - 8x^2 + y^4 - 12y^2$

$$\frac{df}{dx} = 4x^3 - 16x = 0$$

$$4x^3 - 16x = 0$$

$$4x^3 = 16x$$

$$x^2 = 4$$

$$x = \pm 2$$

$$\frac{df}{dy} = 4y^3 - 36y = 0$$

$$4y^3 = 36y$$

$$y^2 = 9$$

$$y = \pm 3$$

$$\frac{d^2 f}{dx^2} = 12x^2 - 16$$

put $x = 2 \Rightarrow \frac{d^2 f}{dx^2} > 0$, local minima

put $x = -2 \Rightarrow \frac{d^2 f}{dx^2} > 0$, local ~~minima~~ ^{minima}

$$\frac{d^2 f}{dy^2} = 12y^2 - 36$$

put $y = 3 \Rightarrow \frac{d^2 f}{dy^2} > 0$, local minima

put $y = -3 \Rightarrow \frac{d^2 f}{dy^2} > 0$, local minima

C

B. $B \in$ Null space if $AB = 0$

$$A = \begin{bmatrix} 2 & 3 & 1 & 4 \\ 1 & 2 & 1 & 3 \\ -1 & 0 & 1 & 1 \end{bmatrix}^T$$

$$AB = \begin{bmatrix} 2 & 3 & 1 & 4 \\ 1 & 2 & 1 & 3 \\ -1 & 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \\ 1 \\ 2 \end{bmatrix} \neq 0$$

for $B = [3, -5, 1, 2]$

$$AB = 0$$

Hence $B = (3, -5, 1, 2)^T$

B

7. $A = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ $b = \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$

$$A = Ab^T = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \begin{bmatrix} 3 & 4 & 5 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & 4 & 5 \\ 6 & 8 & 10 \end{bmatrix}$$

echelon form of $A = \begin{bmatrix} 1 & 4/3 & 5/3 \\ 0 & 0 & 0 \end{bmatrix}$

A has 1 linearly independent vector

So, Rank = 1

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