

1.  $x_u + x_v = 1$
2. maximize  $\sum x_u$
3. The optimum objective value of the program is always  $\geq \frac{n}{2}$   
The linear program is always feasible, whether or not there exists a valid coloring for the given graph
4. The optimum objective value of the new linear program can be  $< \frac{n}{2}$   
If there is no valid coloring, the new optimization problem is infeasible  
If any feasible solution, the  $x_v$  values for all the vertices  $v$  will be “integral” (i.e., they will be 0 or 1, no fractions)