

1. (a) Remove $\{uv\}$ from the graph ($O(1)$)
 (b) Run $DFS(u)$ ($O(n + m)$)
 (c) If $isReachable[v]$ is true, there is a cycle using $\{uv\}$ ($O(1)$)
2. (a) Run $BFS(u)$ ($O(n + M)$)
 (b) For all $v \in V$, check if $dist[v] \leq r$. ($O(n)$)
3. (a) For any vertex $u \in V$, run $BFS(u)$. ($O(n + m)$)
 (b) For every vertex v , if $dist[v]$ is even, put u in set A ; otherwise, put it in set B . ($O(n)$)
 (c) For every vertex v , check if all of its neighbors are in the opposite set. If not, the partition is impossible. ($O(n + m)$)