Missouri University of Science & Technology

**CS 2500: Algorithms (Sec: 102) Spring 2023** 

**Homework 2: Sorting** 

**Instructor:** Sid Nadendla **Due:** *March 3. 2023* 

#### **Workflow of Heapsort and Quicksort** Problem 1.

25 points

Department of Computer Science

Demonstrate HEAP-SORT and QUICK-SORT iterations for both the following arrays: (i)  $A_1 = \{2, 6, 4, 3, 1, 5\}$ , and (ii)  $A_2 = \{1, 5, 2, 3, 0, 2, 2, 1, 4, 5\}$ .

#### Problem 2. **Empirical Analysis of Heapsort and Quicksort** 25 points

Implement HEAP-SORT (Page 170 with supporting functions in Pages 165, 167, all in CLRS) and QUICK-SORT (Page 183, CLRS) in Python, and validate its average run-time performance (similar to Problem 2 in Homework 1).

### Problem 3. **Modified Quicksort**

25 points

Traditional quicksort routine chooses a pivot q such that  $A[p:q-1] \leq A[q] \leq A[q+1,r]$ . Instead, present an analysis when the quicksort algorithm partitions the array A[p:r] into three parts using two pivots  $q_1$  and  $q_2$  such that  $A[p:q_1-1] \le A[q_1] = \cdots = A[q_2] \le A[q_2+1:r]$ . (Hint: Assume that the entries in A are picked from  $\{1, \dots, m\}$ , where m < n.)

### Problem 4. **Sort by Frequency**

25 points

Write a program in Python that sorts all the integer entries in an input array A of size n according to the decreasing frequency of occurrence. If the frequency of two numbers is the same, then sort them in the increasing order of value. Assume that  $A[j] \in \{0, 1, \dots, k\}$  for all  $j = 1, \dots, n$ , and let  $k \ll n$  to allow enough number of repetitions.

(Hint: You can find frequencies using COUNTING-SORT).

**Example:** Let A =  $\{3, 5, 2, 1, 0, 1, 2, 3, 4, 2, 0, 3, 4, 2, 1\}$ . Note that n = 15 and k = 5. Let f(i)denote the frequency of occurrence of a number i in A. Then, we have

$$f(0) = 2,$$
  $f(3) = 3,$   
 $f(1) = 3,$   $f(4) = 2,$   
 $f(2) = 4,$   $f(5) = 1.$ 

$$f(1) = 3, f(4) = 2,$$

$$f(2) = 4, f(5) = 1$$

Then, the output should look like:  $B = \{2, 2, 2, 2, 1, 1, 1, 3, 3, 3, 0, 0, 4, 4, 5\}.$ 

Lecture 2: Sorting 2

## Problem 5.

# Extra credit (5 points)

# You are strongly encouraged to solve this problem.

Selection-Sort(A) sorts the input array A by first finding the  $j^{th}$  smallest element in A and swapping it with the element in A[j], in the order  $j=1,\,j=2,\,\cdots,\,j=n-1$ . Write pseudocode for Selection-Sort, and find the best-case and worst-case running times of Selection-Sort in  $\Theta$ -notation.