

Causal Inference and Invariance

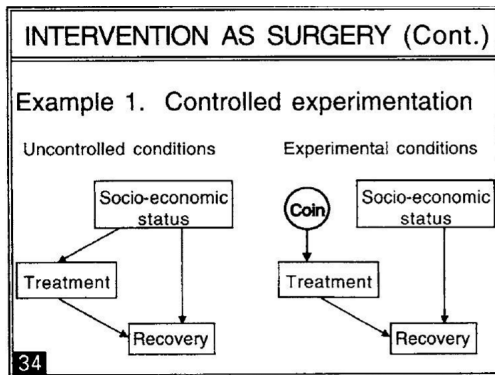
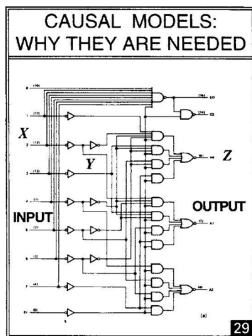
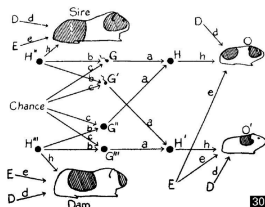
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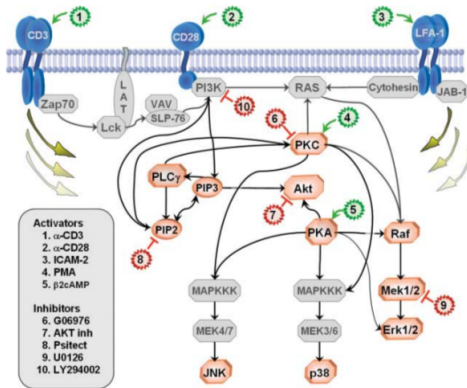
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(Part 1/2)

Understanding nature = cause and effect

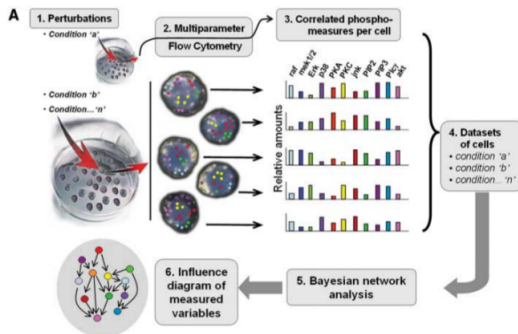


A hot application: systems biology



- In biology: causal relationships due to *chemical interactions*.
- Experimenters *intervene* by injecting *activators* and *inhibitors*.

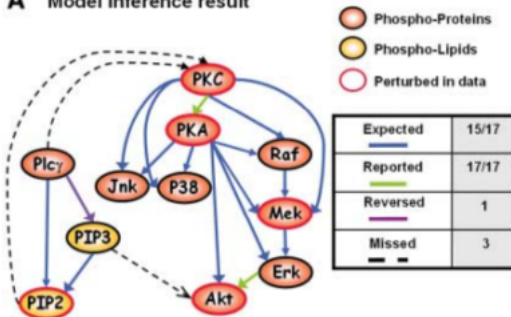
Protein signalling data



- Flow cytometry data from Sachs et al. *Science*, 2005.
- 1 observational data set + 9 interventions (selective activation/inhibition).

Putative causal model

A Model inference result



- Causal inference applied to observational + interventional data.
- Recovered most of the known interactions.

Where does statistics fit into this?

Not just statistics: numerous fields are interested in causal inference.

- *Philosophy*. Starting from Aristotle and still being debated today. What is causality? How do we learn about cause and effect?
- *Computer science*. Can we build an artificial intelligence which reasons like humans? Motivation for Judea Pearl's work.
- *Social science*. What influences an individual's life choices? (Career, political participation, etc.) Can we discover *social mechanisms*?

Statistical applications focus on:

- *Estimating causal effects*. Can we predict a causal effect based on observational or experimental data? E.g. effect of a medical treatment based on clinical trial data? Motivation for potential outcomes approach developed by Rubin, etc.
- *Bayesian networks, structure learning*. Can we model multivariate relationships using a network structure? Networks *can be* given causal interpretation, but causal inference is not the only motivation. Motivation for graphical lasso.

Principles of Causal Inference

- These diverse applications of causal inference share a common set of useful principles.
- The *graphical approach* pioneered by Judea Pearl is the best approach for developing causal intuition.

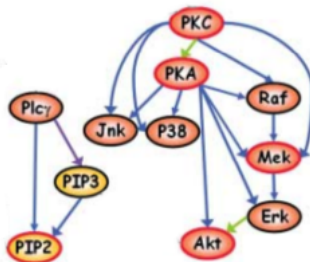
TYPICAL DERIVATION IN CAUSAL CALCULUS

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graph LR
    S((Smoking)) --> T((Tar))
    S((Smoking)) --> C((Cancer))
    T((Tar)) --> C((Cancer))
    
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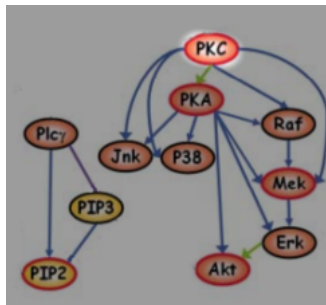
$P(c \mid do\{s\}) = \sum_t P(c \mid do\{s\}, t) P(t \mid do\{s\})$	Probability Axioms
$= \sum_t P(c \mid do\{s\}, do\{t\}) P(t \mid do\{s\})$	Rule 2
$= \sum_t P(c \mid do\{s\}, do\{t\}) P(t \mid s)$	Rule 2
$= \sum_t P(c \mid do\{t\}) P(t \mid s)$	Rule 3
$= \sum_t \sum_{s'} P(c \mid do\{t\}, s') P(s' \mid do\{t\}) P(t \mid s)$	Probability Axioms
$= \sum_{s'} \sum_t P(c \mid t, s') P(s' \mid do\{t\}) P(t \mid s)$	Rule 2
47 $= \sum_{s'} \sum_t P(c \mid t, s') P(s') P(t \mid s)$	Rule 3

Graphs: nodes and vertices



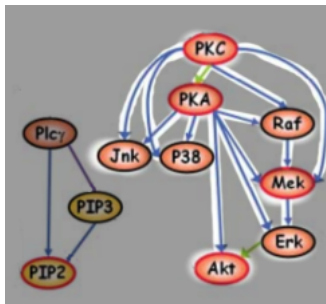
- Each variable in the dataset is given a *node*.
- Arrows indicate which variables *cause* which other variables.
- Undirected or bidirected edges indicate that variables are associated, but neither causes the other.

Causality and experiments



- The *observational distribution* is the joint distribution under the “natural” state of the system.
- One can consider *intervening* on one of the variables in the system. This changes the joint distribution of the system.

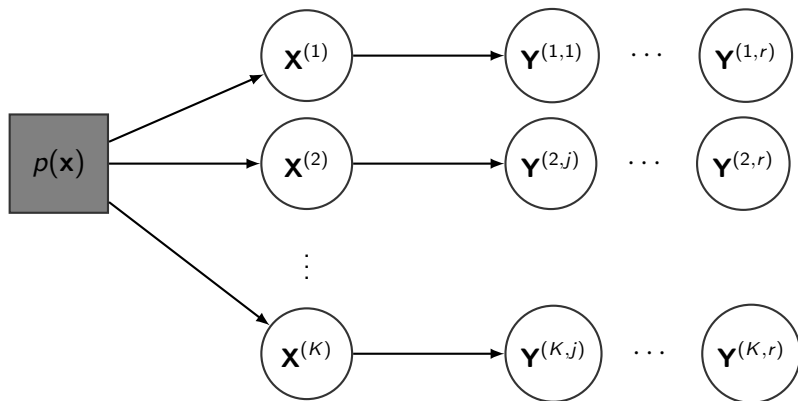
Causality and experiments



- However, not every variable will be affected by the intervention!
- By following the arrows, we determine the set of variables which are affected by the intervention.

Look! A diagram!

Don't put this in the final presentation.



Legend: $K = \{ \text{2}, \text{9}, \text{99}, \text{999} \}$