# Joint Track Machine Learning

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# Outline

# Introduction

# Acknowledgments

I would like to thank the McJunkin Family Charitable Foundation for their generous grant that supports this work.

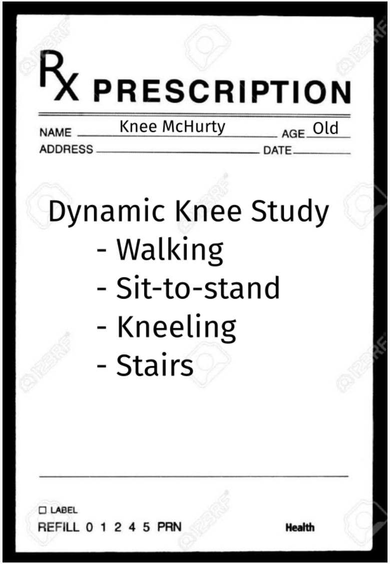
# Motivation

# The Problem

- 20% of patients receiving TKA are dissatisfied.
  - Instability, pain, unnatural [1, 3, 16].
- No reliable method of clinically assessing and quantifying joint dynamics.
  - Too much human supervision, too time consuming

# Our Proposition

Orthopaedic surgeons and clinicians would readily adopt a practical and inexpensive technology that allows them to measure a patient's knee kinematics during activities of daily living.



# Constraints

- It must fit within a standard clinical workflow
- The technology must utilize equipment commonly found in hospitals
- There must not be significant human supervision nor interaction to generate an examination report.

# Background

**Translation**

$$\begin{pmatrix} v'_x \\ v'_y \end{pmatrix} = \begin{pmatrix} v_x \\ v_y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix}$$

$$\rightarrow$$

$$\begin{pmatrix} v'_x \\ v'_y \\ 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} v_x \\ v_y \\ 1 \end{pmatrix}$$

# Rigid Body Transformations

## Rotations

$$R_x = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_x & -s_x \\ 0 & s_x & c_x \end{pmatrix}$$

$$R_y = \begin{pmatrix} s_y & 0 & c_y \\ 0 & 1 & 0 \\ c_y & 0 & -s_y \end{pmatrix}$$

$$R_z = \begin{pmatrix} c_z & -s_z & 0 \\ s_z & c_z & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

**Homogeneous Transformation Matrices**

$$\begin{aligned}\tilde{\vec{v}}' &= \begin{pmatrix} & \mathrm{R}_{3\times3} & & \vec{t}_{3\times1} \\ 0 & 0 & 0 & 1 \end{pmatrix} \tilde{\vec{v}} \\ &= T_B^A \tilde{\vec{v}}\end{aligned}$$

Now we have a notation that allows us to describe arbitrary movement between reference frames.

# Projective Geometry

$$\begin{pmatrix} x_s \\ y_s \\ z_s \\ 1 \end{pmatrix}_i = T_{scene}^{cam} \tilde{\mathrm{p}}_{\mathrm{i}}^{\mathrm{obj}}$$

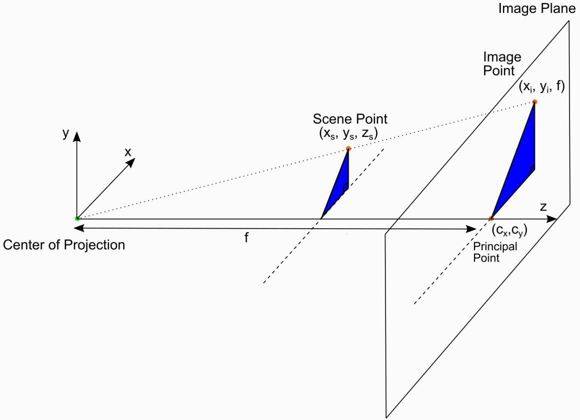
$$\begin{pmatrix} \tilde{x}_{img} \\ \tilde{y}_{img} \\ \tilde{z} \end{pmatrix} = \begin{pmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{pmatrix} \vec{x}_s$$

Where

$$x_{img} = \frac{\tilde{x_{img}}}{\tilde{z}} = \frac{f}{z_s} x_s$$

$$y_{img} = \frac{\tilde{y_{img}}}{\tilde{z}} = \frac{f}{z_s} y_s$$

Note: We are still in the camera's reference frame



# Pixel Coordinates

Convert camera coordinates into image coordinates.

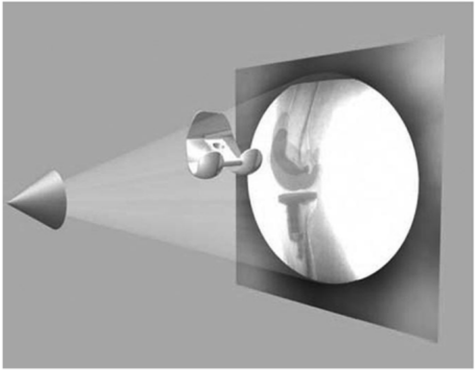
$$p_x = k_x x_{img} + c_x$$
$$p_y = k_y y_{img} + c_y$$

Where

$$k \equiv \text{ Pixel Spacing}$$
$$c \equiv \text{ Image Focal Point}$$

# Model-Image Registration

If we know the projective parameters of the fluoroscopy machine, can we tinker with $T_{implant}^{cam}$ so that our virtual projection matches the fluoroscopic image?



From [14]

# Historical Methods

# Overview

Many different approaches have attempted to solve the model-image registration problem.

- Pre-computed projections
- Skin-mounted motion Capture
- Biplane Imaging
- Iterative Projections
- Model-based Roentgen Stereophotogrammetry

# Pre-Computed Projections

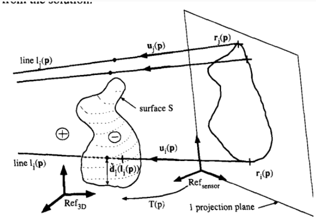
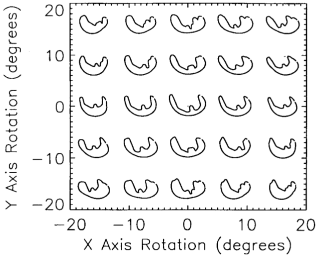


Fig. 2. Projection line to surface distance computation.

From [12]

- Saving space and memory by pre-computing as much as possible.
- Pre-computed distance maps [19, 12].
- Pre-computed shape libraries [2]

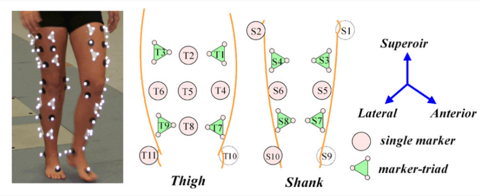



From [2]

# Limitations of Pre-Computed Projections

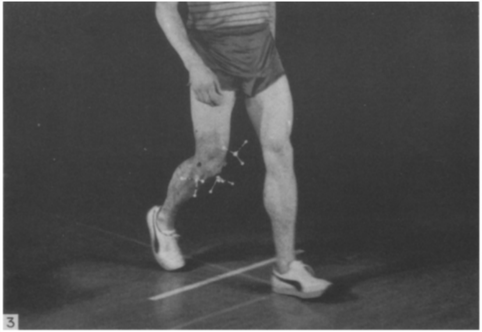
- Requires an accurate contour from the input image in order to perform calculations.
    - Human supervision vs. inaccuracy.

# Motion Capture (MoCap)




From [7]

- Can measure motion of MoCap beads very accurately.
- Skin-mounted [7, 10, 13].
- Bone pins [11] (any volunteers?).




From [11]

# Limitations of Motion Capture

Skin Mounted

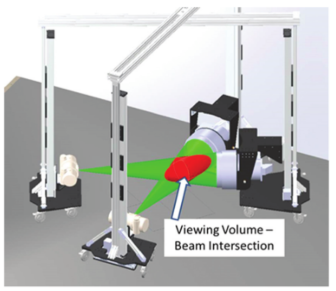
- Doesn't accurately describe underlying skeletal motion with clinical accuracy [7, 10, 13].

Bone Pins

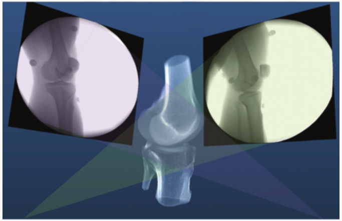
- Bone Pins
- Need I say more?

# Biplane Imaging

- Utilizes multiple cameras to resolve 3D position and orientation[8, 5].
    - Highly accurate.
    - Gold Standard.




Both from [8]

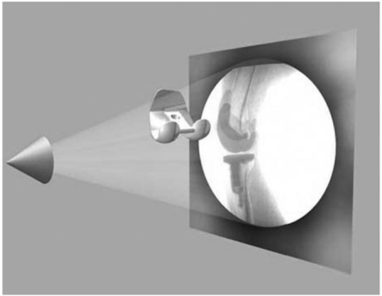


# Limitations of Biplane Imaging

- Not many hospitals have biplane fluoroscopy setups.
- Clinically impractical

# Iterative Projections

- Take advantage of modern computational graphics pipelines to quickly perform projection matching.
  - Image/Intensity similarity metrics [14]
  - Feature/Contour similarity metrics [6]



From [14]

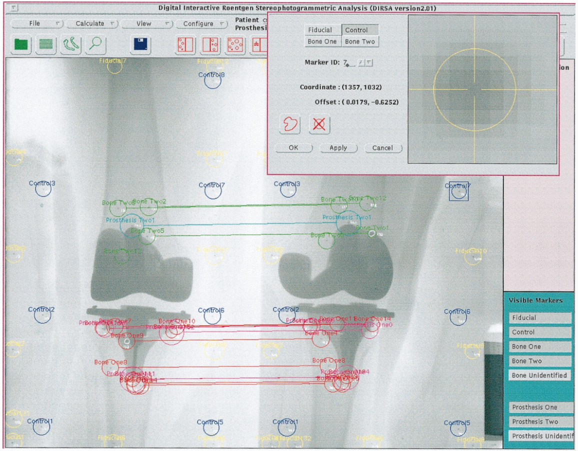
From [6]

# Limitations of (historic) Iterative Projection Methods

- Requires human supervision for:
  - Pose initialization
  - Escaping local minima
  - Implant detection
- Chaotic and Noisy objective function

# Model-based Roentgen Stereophotogrammetry (MBRSA)

- Uses implanted tantalum beads for motion tracking [18, 17]
- Extremely accurate [9, 15]
- Gold standard Measurement [4]




From [18]

# Limitations of MBRSA

- Involves additional surgical procedures for inserting tantalum beads
- Human supervision
- Typically requires bi-plane imaging.

# Aims

# Aims

**Aims 1/2**
Joint Track Machine Learning and Overcoming Single-Plane Limitations

**Aim 3/4**
Pilot Trials and Standardized Kinematics Exam

**Aim 5**
Joint Track Auto Toolkit

# References

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