

Joint Track Machine Learning

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Introduction

Acknowledgments

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Motivation

The Problem

- Joints manifest pain during dynamic activity.
- 20% of patients receiving TKA are dissatisfied.
 - Instability, pain, unnatural [1, 3, 15].
- No reliable method of clinically assessing and quantifying joint dynamics.
 - Too much human supervision, too time consuming



Our Proposition

Orthopaedic surgeons and clinicians would readily adopt a practical and inexpensive technology that allows them to measure a patient's knee kinematics during activities of daily living.

Rx PRESCRIPTION

NAME Knee McHurty AGE Old
ADDRESS _____ DATE _____

Dynamic Knee Study

- Walking
- Sit-to-stand
- Kneeling
- Stairs

☐ LABEL
REFILL 0 1 2 4 5 PRN

Health

Constraints

- It must fit within a standard clinical workflow
- The technology must utilize equipment commonly found in hospitals
- There must not be significant human supervision nor interaction to generate an examination report.



Background

Homogeneous Transformation Matrix

$$T_B^A = \begin{pmatrix} R_B^A & P_{B,origin}^A \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Rotation Matrices

$$R_x = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_x & -s_x \\ 0 & s_x & c_x \end{pmatrix}$$

$$R_y = \begin{pmatrix} s_y & 0 & c_y \\ 0 & 1 & 0 \\ c_y & 0 & -s_y \end{pmatrix}$$

$$R_z = \begin{pmatrix} c_z & -s_z & 0 \\ s_z & c_z & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Translation

$$\begin{pmatrix} v'_x \\ v'_y \end{pmatrix} = \begin{pmatrix} v_x \\ v_y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix}$$

\rightarrow

$$\begin{pmatrix} v'_x \\ v'_y \\ 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} v_x \\ v_y \\ 1 \end{pmatrix}$$

Rotations

$$R_x = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_x & -s_x \\ 0 & s_x & c_x \end{pmatrix}$$

$$R_y = \begin{pmatrix} s_y & 0 & c_y \\ 0 & 1 & 0 \\ c_y & 0 & -s_y \end{pmatrix}$$

$$R_z = \begin{pmatrix} c_z & -s_z & 0 \\ s_z & c_z & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Homogeneous Transformation Matrices

$$\begin{aligned}\vec{v}' &= \begin{pmatrix} R_{3 \times 3} & \vec{t}_{3 \times 1} \\ 0 & 1 \end{pmatrix} \tilde{v} \\ &= T_B^A \tilde{v}\end{aligned}$$

Now we have a notation that allows us to describe arbitrary movement between reference frames.

Projective Geometry

$$\begin{pmatrix} x_s \\ y_s \\ z_s \\ 1 \end{pmatrix}_i = T_{scene}^{cam} \tilde{p}_i^{obj}$$

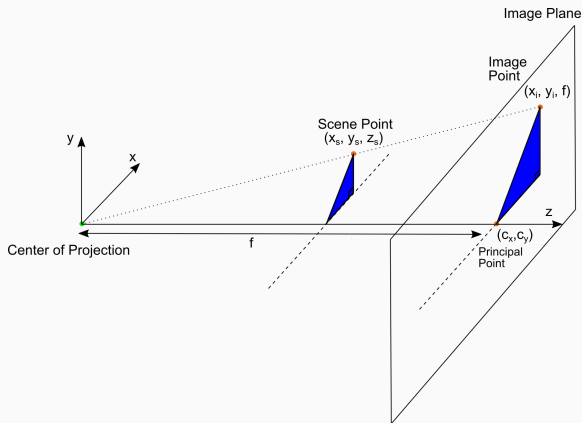
$$\begin{pmatrix} \tilde{x}_{img} \\ \tilde{y}_{img} \\ \tilde{z} \\ 1 \end{pmatrix} = \begin{pmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{pmatrix} \vec{x}_s$$

Where

$$x_{img} = \frac{\tilde{x}_{img}}{\tilde{z}} = \frac{f}{z_s} x_s$$

$$y_{img} = \frac{\tilde{y}_{img}}{\tilde{z}} = \frac{f}{z_s} y_s$$

Note: We are still in the camera's reference frame



Convert camera coordinates into image coordinates.

$$p_x = k_x x_{img} + c_x$$

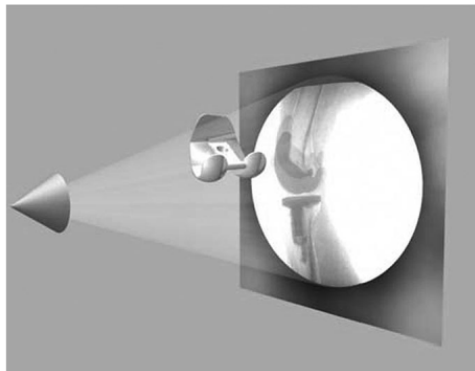
$$p_y = k_y y_{img} + c_y$$

Where

$k \equiv$ Pixel Spacing

$c \equiv$ Image Focal Point

If we know the projective parameters of the fluoroscopy machine, can we tinker with $T_{implant}^{cam}$ so that our virtual projection matches the fluoroscopic image?



From [13]

Historical Methods

Many different approaches have attempted to solve the model-image registration problem.

- Pre-computed projections
- Skin-mounted motion Capture
- Biplane Imaging
- Iterative Projections

Pre-Computed Projections

- Saving space and memory by pre-computing as much as possible.
- Pre-computed distance maps [17, 11].
- Pre-computed shape libraries [2]

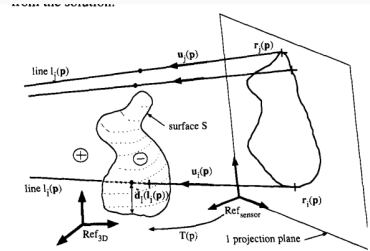
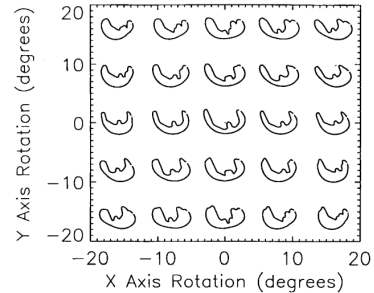


Fig. 2. Projection line to surface distance computation.

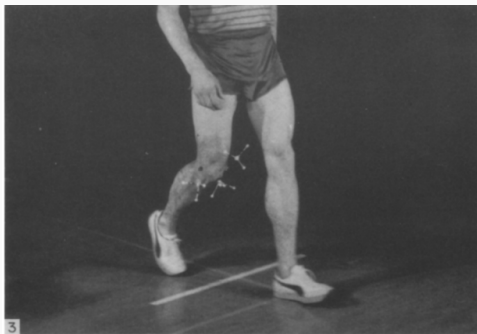
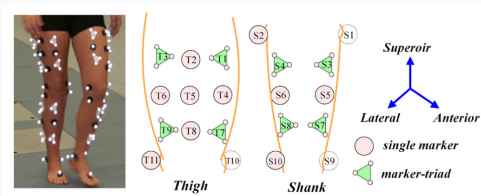


Limitations of Pre-Computed Projections

- Requires an accurate contour from the input image in order to perform calculations.
 - Human supervision vs. inaccuracy.

Motion Capture (MoCap)

- Can measure motion of MoCap beads very accurately.
- Skin-mounted [6, 9, 12].
- Bone pins [10] (any volunteers?).



Limitations of Motion Capture

Skin Mounted

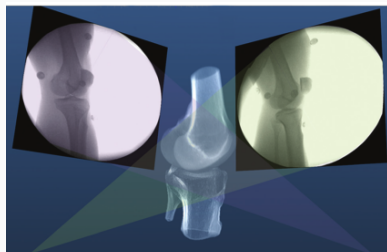
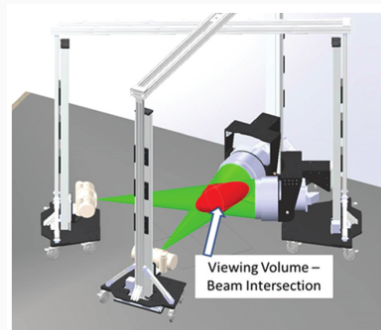
- Doesn't accurately describe underlying skeletal motion with clinical accuracy [6, 9, 12].

Bone Pins

- Bone Pins
- Need I say more?

Biplane Imaging

- Utilizes multiple cameras to resolve 3D position and orientation[7, 5].
 - Highly accurate.
 - Gold Standard.

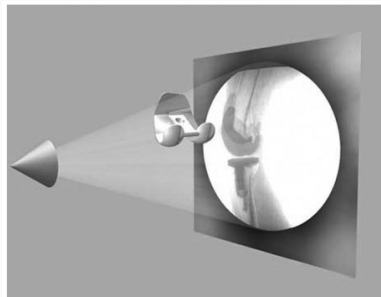


Limitations of Biplane Imaging

- Not many hospitals have biplane fluoroscopy setups.
- Clinically impractical

Iterative Projections

- Take advantage of modern computational graphics pipelines to quickly perform projection matching.
- Image/Intensity similarity metrics [13]
- Feature/Contour similarity metrics



Limitations of (historic) Iterative Projection Methods

- Requires human supervision for:
 - Pose initialization
 - Escaping local minima
 - Implant detection
- Chaotic and Noisy objective function

Model-based Roentgen Stereophotogrammetry (MBRSA)

- Uses implanted tantalum beads for motion tracking [16]
- Extremely accurate [8, 14]
- Gold standard Measurement [4]
- Involves additional surgical procedures for inserting tantalum beads
- Human supervision
- Typically requires bi-plane imaging.

Aims

Aims 1/2

Joint Track Machine

Learning and Overcoming

Single-Plane Limitations

Aim 3/4

Pilot Trials and

Standardized Kinematics

Exam

Aim 5

Joint Track Auto Toolkit

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