

# Joint Track Machine Learning

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# Outline

## Aims

Aim 1 - Joint Track Machine Learning

Aim 2 - Correcting Symmetric Implant Ambiguity

## References

## Acknowledgments

I would like to thank the McJunkin Family Charitable Foundation for their generous grant that supports this work.

# The Problem

- By 2030, roughly 3.5 million Total Knee Arthroplasty (TKA) will be performed in the US [15].
- 20% of patients receiving TKA are dissatisfied.
  - Instability, pain, unnatural [14, 17, 18].
- No reliable method of clinically assessing and quantifying joint dynamics.
  - Human supervision
  - Time consuming
  - Specialized equipment



# Our Proposition

Orthopaedic surgeons and clinicians would readily adopt a **practical** and **inexpensive** technology that allows them to **measure** a patient's knee kinematics during **activities of daily living**.

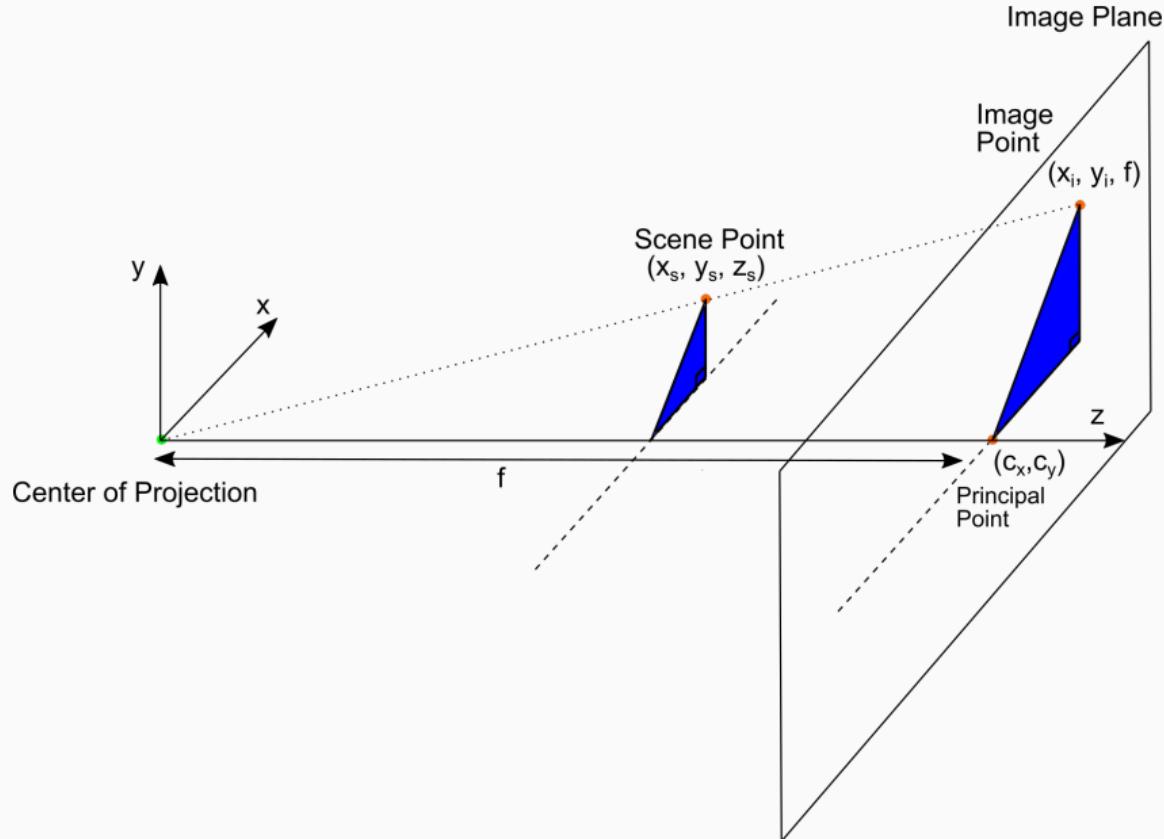


# Constraints

- It must fit within a **standard clinical workflow**
- The technology must utilize equipment **commonly found in hospitals**
- There must not be significant **human supervision** nor interaction to generate an examination report.

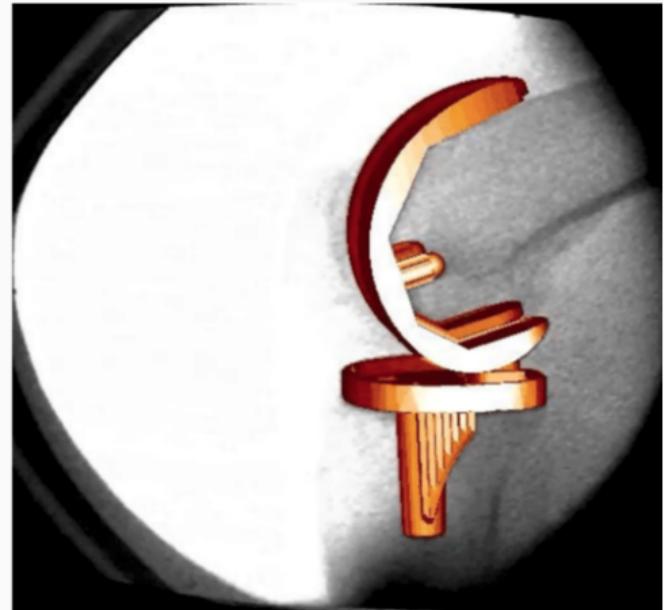


# Background - Projective Geometry



## Background - Model-Image Registration

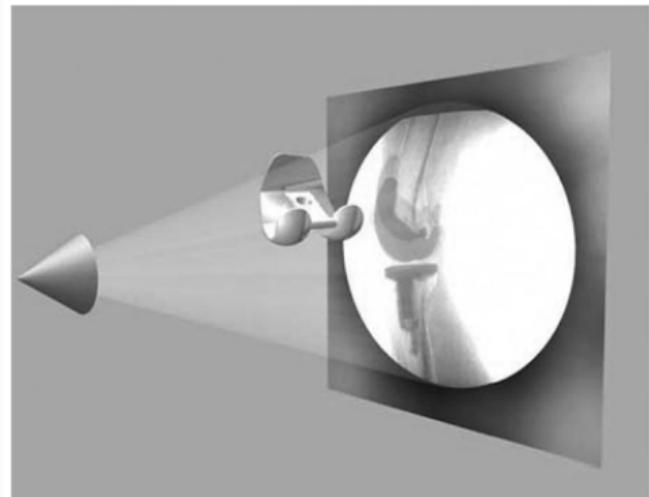
If we know the projective parameters of the fluoroscopy machine, can we tinker with  $T_{implant}^{cam}$  so that our virtual projection matches the fluoroscopic image?



From [11]

## Background - Model-Image Registration

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From [11]

## Historical Overview

Many different approaches have attempted to solve the model-image registration problem.

- Pre-computed projections
- Skin-mounted motion Capture
- Biplane Imaging
- Iterative Projections
- Roentgen Stereophotogrammetry

# Pre-Computed Projections

- Saving space and memory by pre-computing as much as possible.
- Pre-computed distance maps [30, 6].
- Pre-computed shape libraries [7]

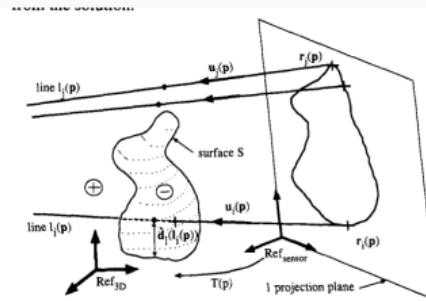
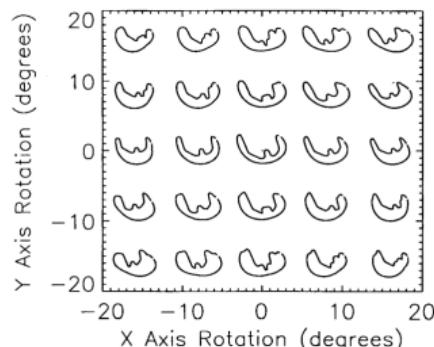


Fig. 2. Projection line to surface distance computation.

From [6]



# Limitations of Pre-Computed Projections

- Requires an accurate contour from the input image in order to perform calculations.
  - Human supervision for isolated contour
  - Inaccuracy with naive edge detection

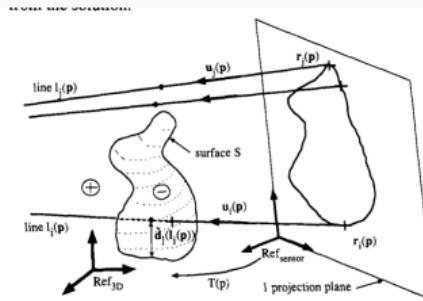
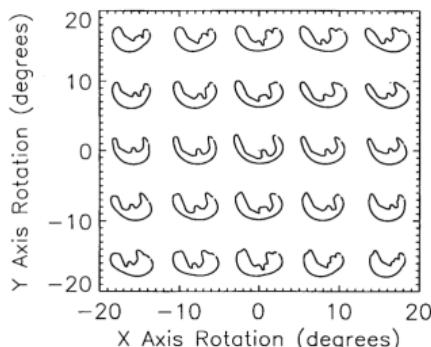
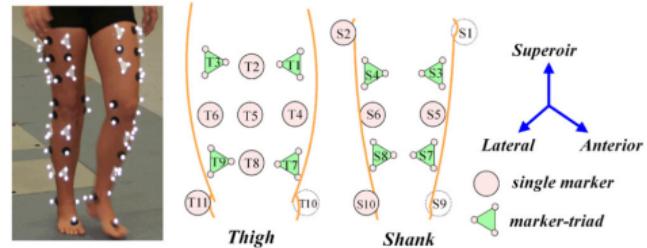


Fig. 2. Projection line to surface distance computation.

From [6]



# Motion Capture (MoCap)

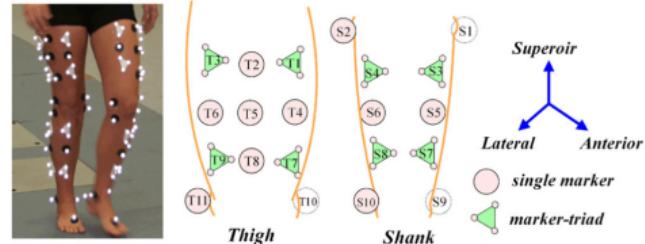


From [16]

- Can measure motion of MoCap beads very accurately.
- Skin-mounted [16, 19, 21].
- Bone pins [5].



# Limitations of Motion Capture



From [16]



Skin Mounted

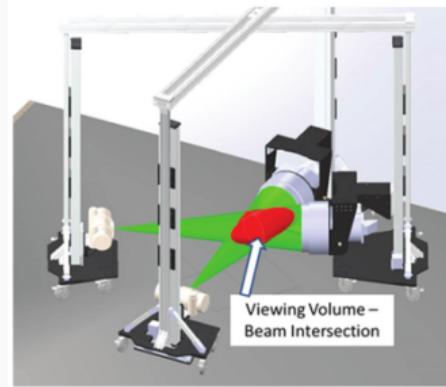
- Doesn't accurately describe underlying skeletal motion with clinical accuracy [16, 19, 21].

Bone Pins

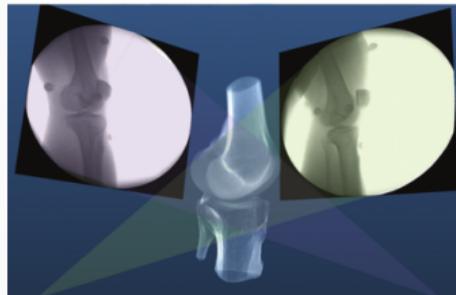
- Any volunteers?

# Biplane Imaging

- Utilizes multiple cameras to resolve 3D position and orientation[20, 27].
  - Highly accurate.
  - Gold Standard.

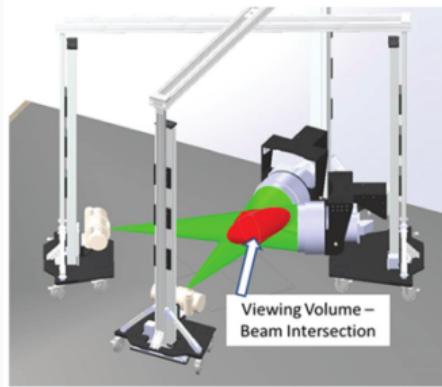


Both from [20]

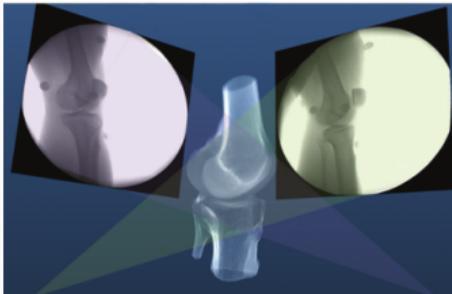


# Limitations of Biplane Imaging

- Not many hospitals have biplane fluoroscopy setups.
- Clinically impractical

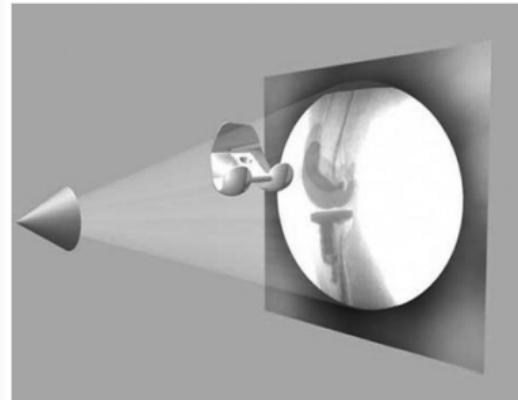


Both from [20]



# Iterative Projections

- Take advantage of modern computational graphics pipelines to quickly perform projection matching.
  - Image/Intensity similarity metrics [11]
  - Feature/Contour similarity metrics [23]



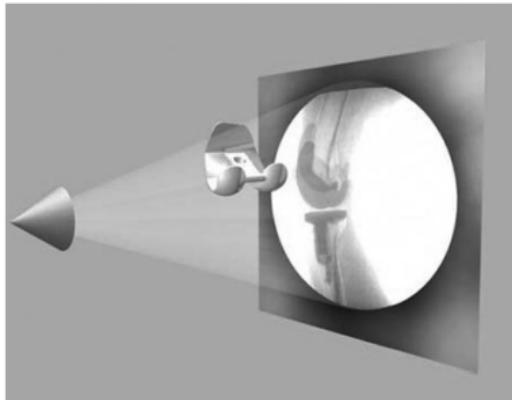
From [11]



From [23]

## Limitations of (historic) Iterative Projection Methods

- Requires human supervision for:
  - Pose initialization
  - Escaping local minima
  - Implant detection
- Chaotic and Noisy objective function



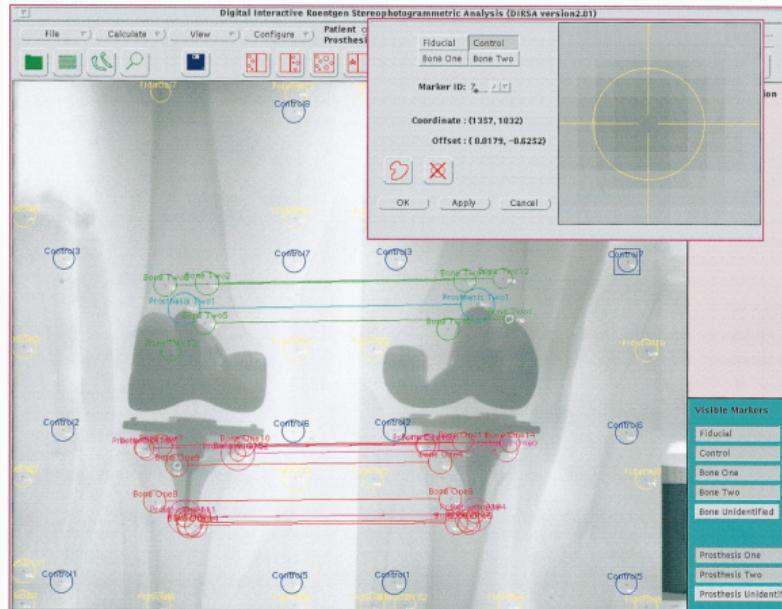
From [11]



From [23]

# Roentgen Stereophotogrammetry (RSA)

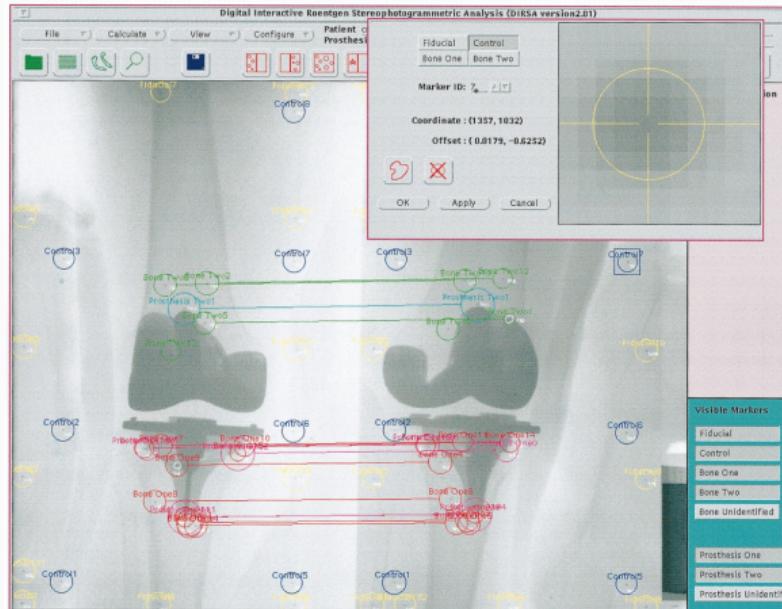
- Uses implanted tantalum beads for motion tracking [10, 4]
- Extremely accurate [12, 13]
- Gold standard Measurement [28]



From [10]

# Limitations of RSA

- Involves additional surgical procedures for inserting tantalum beads.
- Human supervision
- Bi-plane imaging



From [10]

## Aims

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## Aims

**Aim 1:** Joint Track Machine Learning: An Autonomous Method of Measuring Total Knee Arthroplasty Kinematics From Single-Plane X-Ray Images<sup>1</sup>

**Aim 2:** Correcting Symmetric Implant Ambiguity in Measuring Total Knee Arthroplasty Kinematics from Single-Plane Fluoroscopy<sup>2</sup>

**Aim 3:** Some Musings on a “Kinematics Translator” and Synthetic Kinematics Data

**Aim 4:** This will definitely work on shoulders, right?<sup>3</sup>

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<sup>1</sup>Published in the Journal of Arthroplasty [29]

<sup>2</sup>In Revision for Publication in the Journal of Biomechanics

<sup>3</sup>In Review for Publication in the Journal of Computers in Biology and Medicine

## Aims

Aim 1 - Joint Track Machine Learning

Aim 2 - Correcting Symmetric Implant Ambiguity

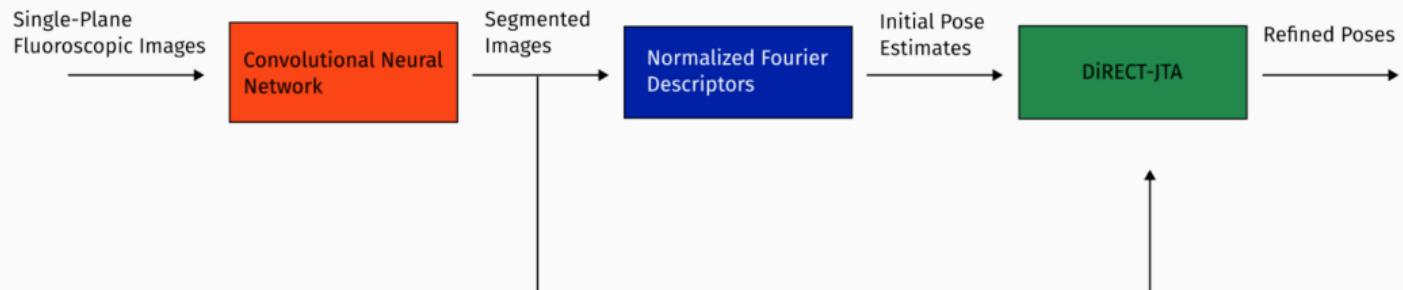
## References

## Goal

Demonstrate the feasibility of a fully autonomous, model-image registration pipeline.

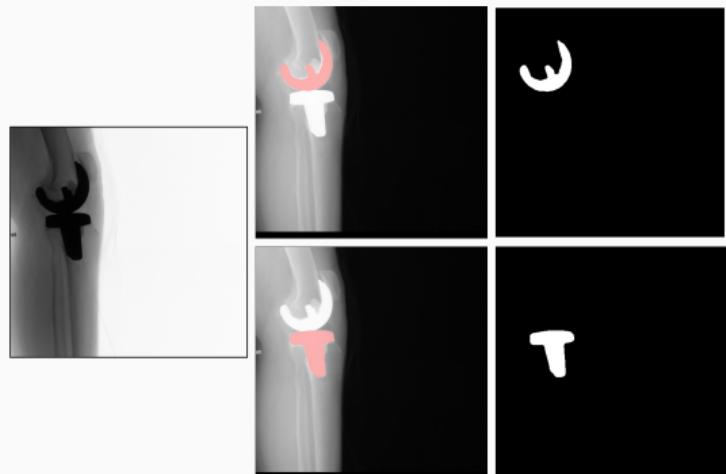
# Method

- Three-tiered approach
  - Convolutional Neural networks (CNN) for autonomous implant detection
  - Normalized Fourier Descriptor shape libraries
  - Robust contour-based global optimization scheme



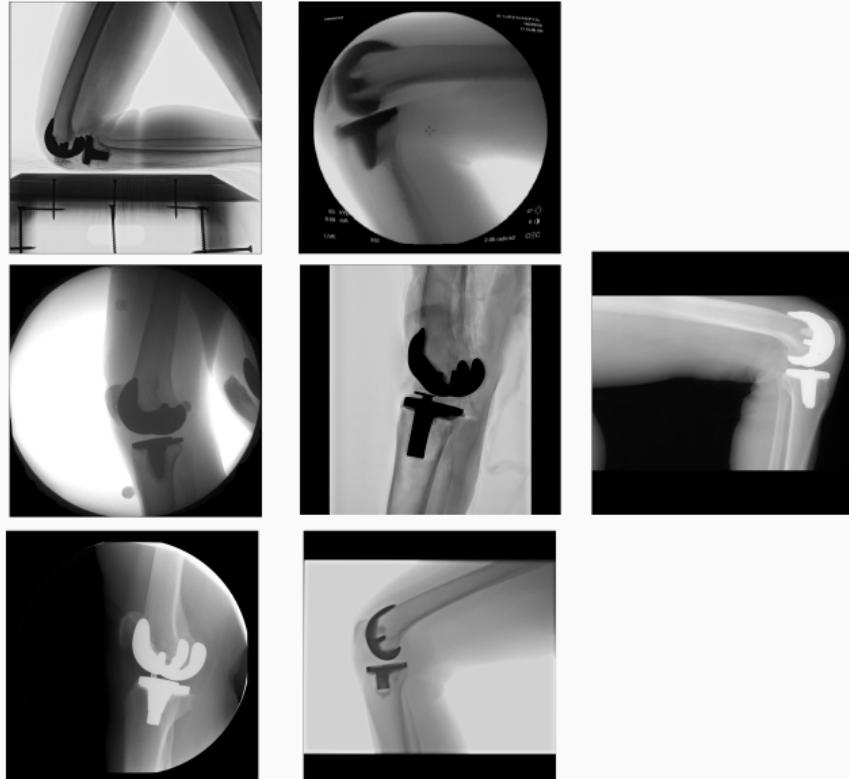
# Autonomous Implant Detection Using Convolutional Neural Networks

- 2 CNNs
  - Femoral and Tibial implants
- High Resolution Network [25]



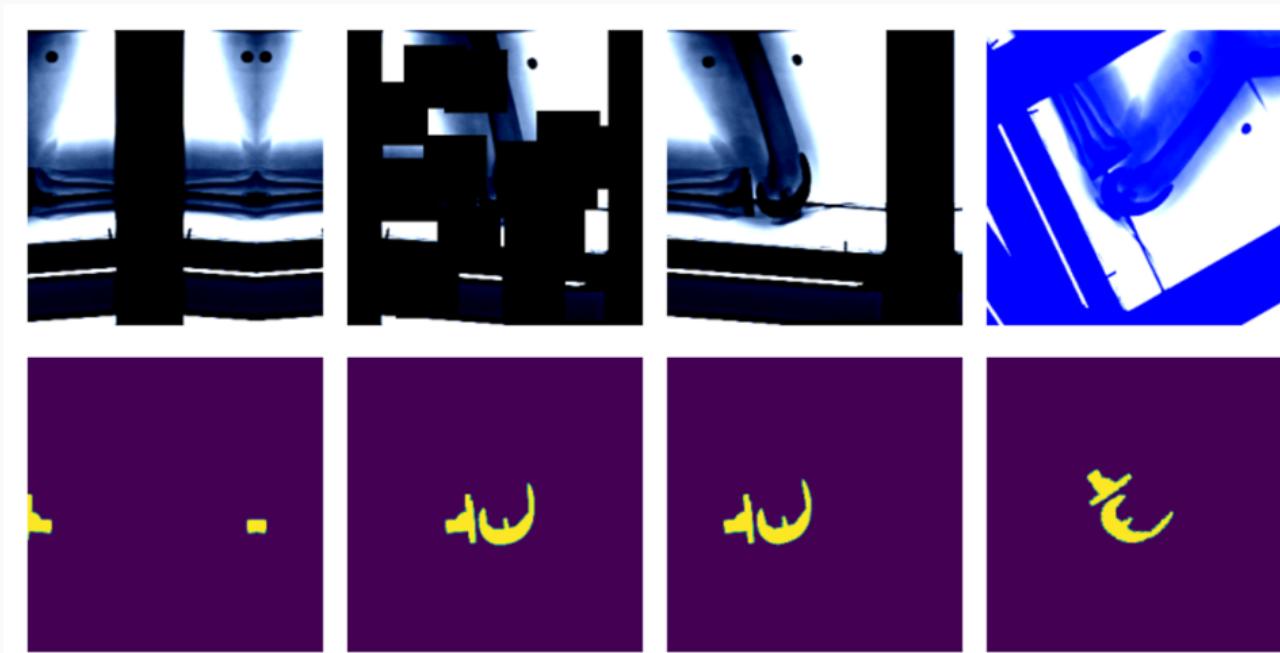
# Neural Network Data

- ~8000 images
  - 7 TKA kinematics studies
    - 71 subjects
    - 7 implant manufacturers
    - 36 distinct implants
    - Squat, lunge, knee, stair ascent



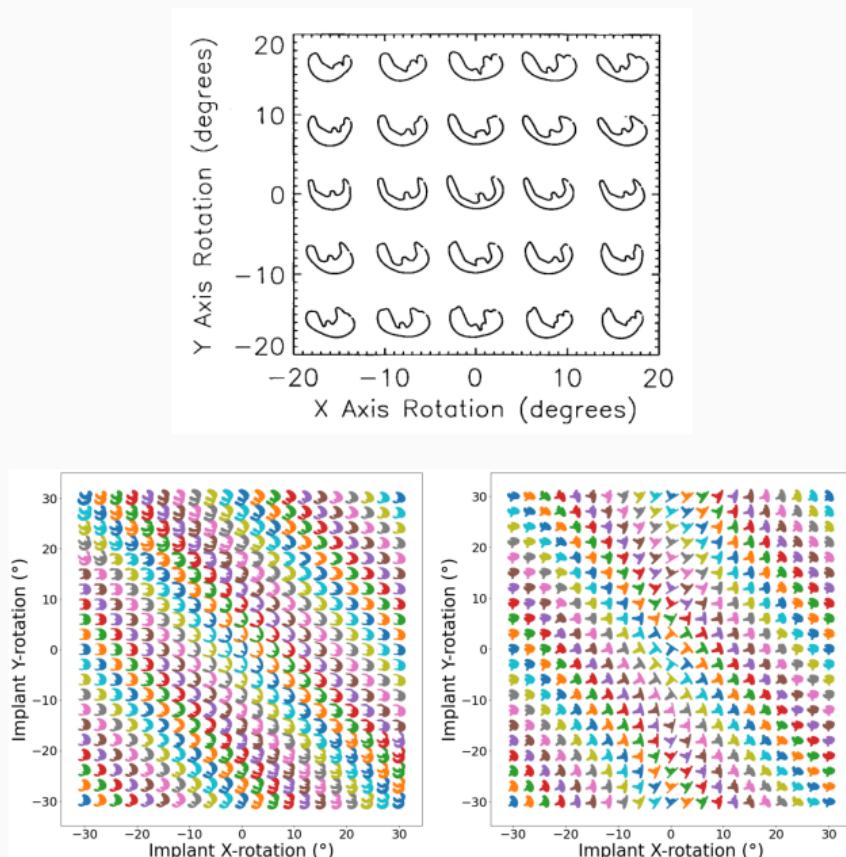
# Neural Network Robustness

- Additional augmentations introduced during training [24].



# Normalized Fourier Descriptor Shape Libraries

- Pose initialization using segmentation output.
- $\pm 30^\circ$  library span at  $3^\circ$  increments.



# Pose Refinement Using Global Optimization

- Two main features
  - Objective function
  - Optimization routine

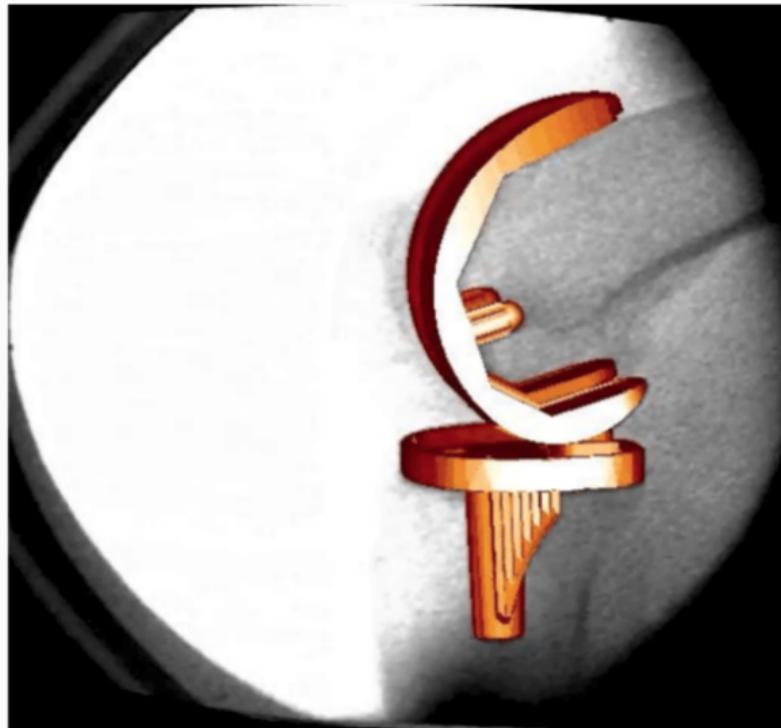
$$\underset{x}{\operatorname{argmin}} \{f(x) : x \in \Omega\}$$

## Contour-based Objective Function

- With accurate projection, contours provide a strong heuristic for orientation.
- Overlapping pixels between CNN segmentation and projected implant.
  - $L_1$  norm has quick parallel computation.

$$J = \sum_{i \in H} \sum_{j \in W} |I_{ij} - P_{ij}| = L_1(I, P)$$

- Sensitive to minor perturbations



# Improving Robustness

- Dilation decreases sensitivity to perturbations.
- Multi-stage optimization can reduce dilation back to original edges.

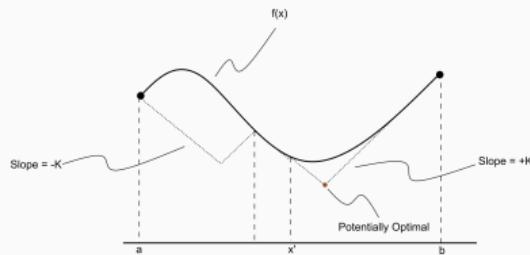
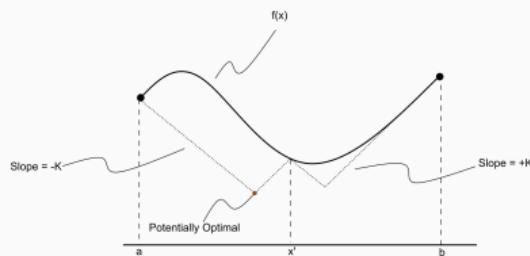
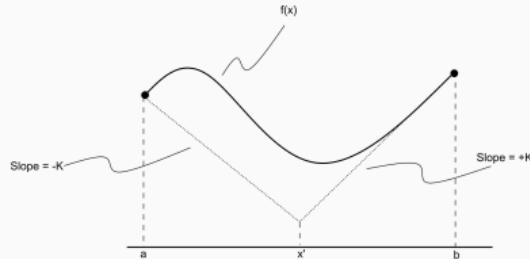


## Optimization Routine

- No analytic form of the objective function exists, it **must** be sampled at points of interest.
  - Black Box Optimization [22, 26]

# Lipschitzian Optimization

- Robust, global, black-box optimization routine if Lipschitz constant ( $K$ ) is known [2].
- Lipschitz constant bounds the rate of change of a function.
- What if you don't know the Lipschitz constant?

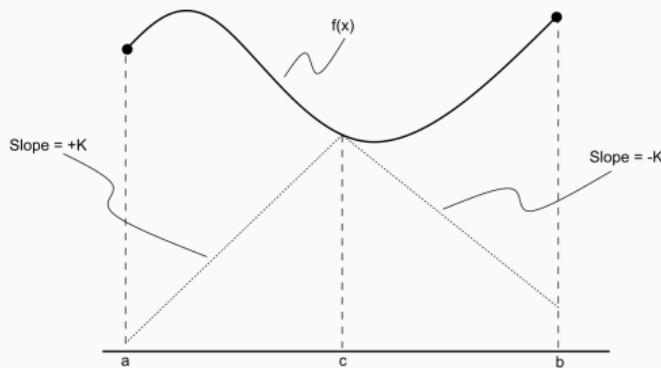


# Lipschitzian Optimization without the Lipschitz Constant

## Lipschitzian Optimization Without the Lipschitz Constant

D. R. JONES,<sup>1</sup> C. D. PERTTUNEN,<sup>2</sup> AND B. E. STUCKMAN<sup>3</sup>

- Sample end-points instead of intersecting lines.
- Potentially optimal regions based on value at center and total size.
  - Trisect potentially optimal regions and re-sample centers



# Trisecting Region

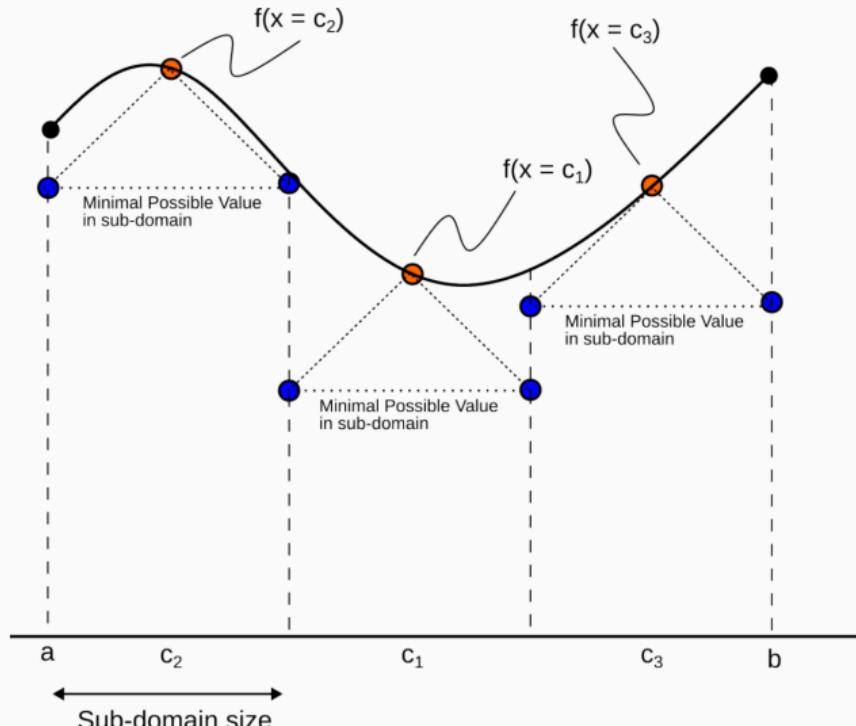
$$\begin{bmatrix} f(x = c_1) & d(c_1) \\ f(x = c_2) & d(c_2) \\ \vdots & \vdots \\ f(x = c_N) & d(c_N) \end{bmatrix}$$

Where

$f(x = c_i) \equiv$  Sampled function value

$d(c_i) \equiv$  Sub-domain size

for  $i \in [1, N]$



## Another Iteration

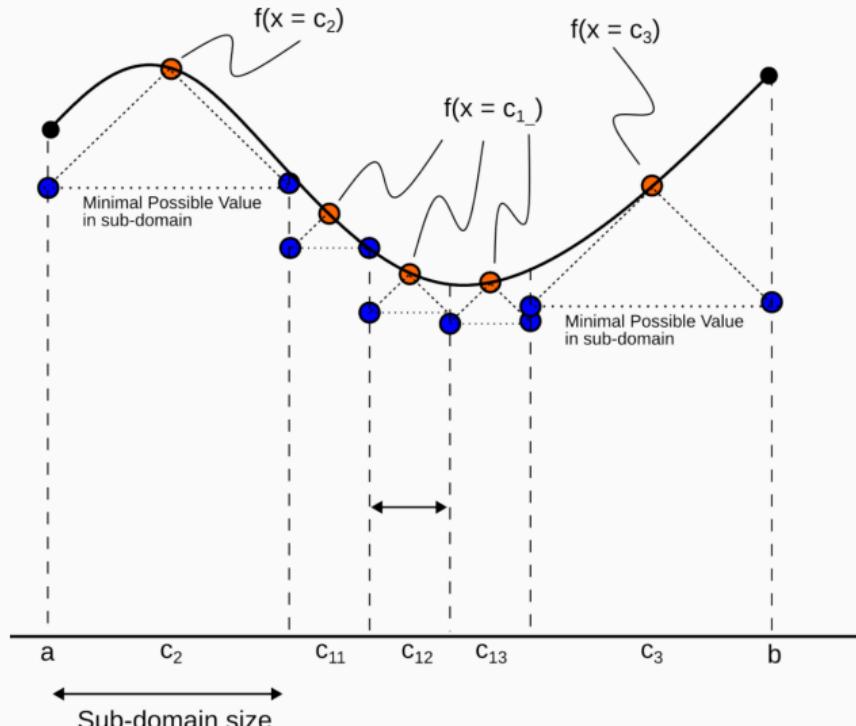
$$\begin{bmatrix} f(x = c_1) & d(c_1) \\ f(x = c_2) & d(c_2) \\ \vdots & \vdots \\ f(x = c_N) & d(c_N) \end{bmatrix}$$

Where

$f(x = c_i) \equiv$  Sampled function value

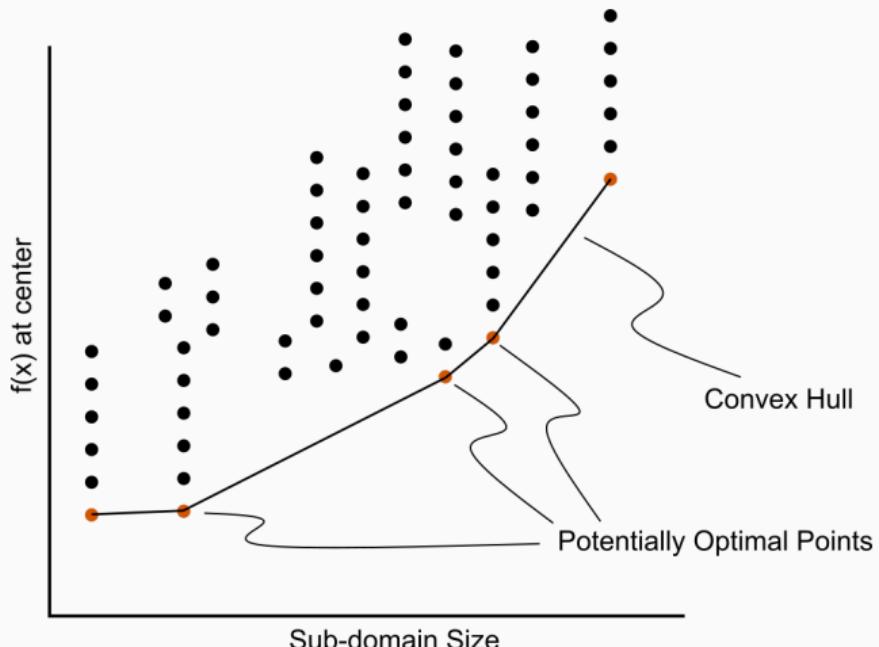
$d(c_i) \equiv$  Sub-domain size

for  $i \in [1, N]$



## Determining Potentially Optimal Regions

- Convex hull [1, 3, 9, 8] of region size vs. center value



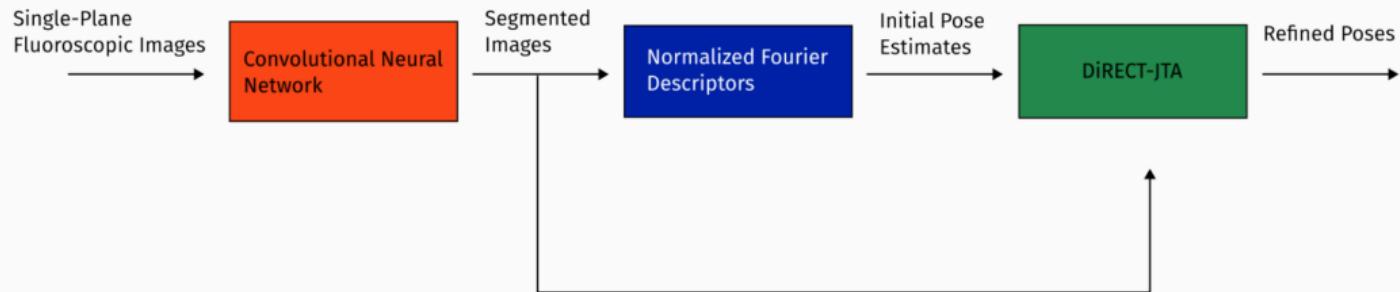
# DiRECT for Joint Track Machine Learning

- Search region is along all 6 degrees of freedom.
  - Normalize to  $[0, 1]$ .
- Three stages, each with decreasing levels of dilation.
  - Iteration budget for each stage.

Stage	Budget [Iterations]	Search Range [mm,deg]	Dilation (pixels)
“Tree”	~20,000	$\pm 45$	5
“Branch”	~20,000	$\pm 25$	3
“Leaf”	~10,000	$\pm 100$ ( $z_{trans}$ ) / $\pm 3$ (else)	1

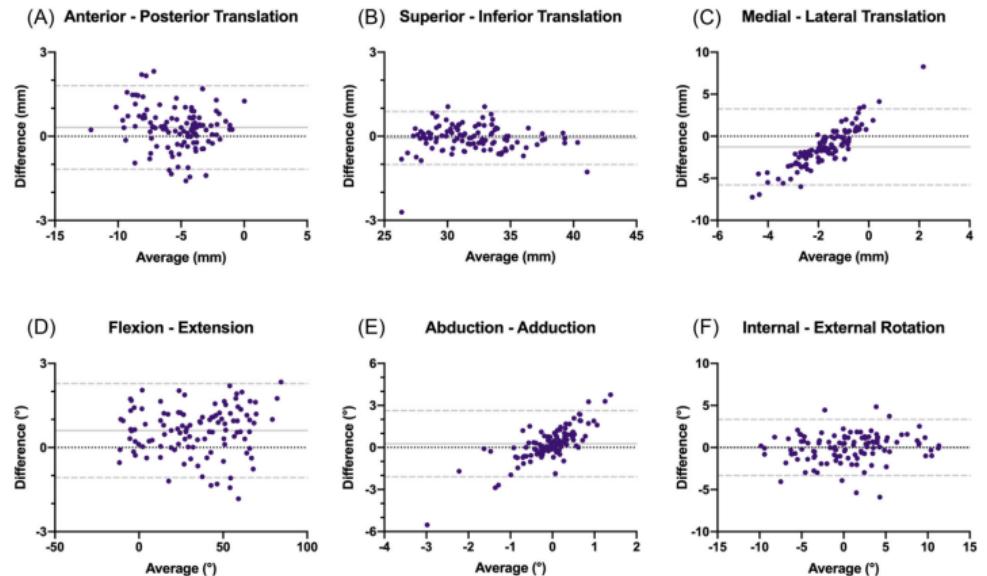
# Testing Performance

Now that we have our refined poses, how well does out system perform?



# Validation

- Independent research group using Model-Based RSA.
- Determine the level of concordance between the two measurement systems
  - Bland-Altman Plots
- Achieved clinically acceptable accuracy [28, 29].
- Highly repeatable



## Awards

The work presented in this aim won the HAP Paul Award for Best Paper from the International Society for Technology in Arthroplasty's 2022 Annual Meeting.



## Aims

Aim 1 - Joint Track Machine Learning

Aim 2 - Correcting Symmetric Implant Ambiguity

## References

## Goal

- The goal of this aim is to validate and test methods that can overcome single-plane limitations for model-image registration.
  - Out-of-plane (OOP) Translation
  - Symmetry Traps

## Translation

- Depth perception is lost when using a single camera.
- Utilize a virtual “spring” to constrain relative OOP translation between implant components.

$$J = \alpha L_1(I, P) + \beta ML(Fem, Tib)$$

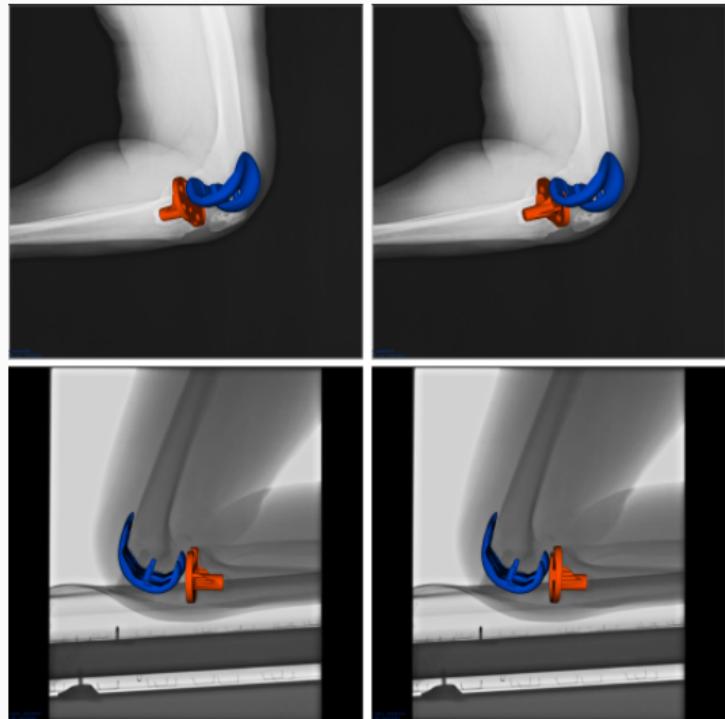
Where

$ML \equiv$  Relative mediolateral translation

# Symmetry Traps

With a symmetric tibial implant, the contour is not always a perfect heuristic for true pose. Human operators typically utilize relative varus-valgus to determine correct pose.

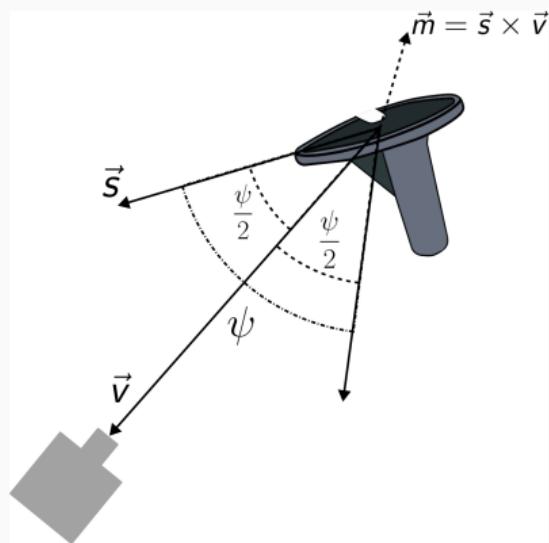
Found “ambiguous zone” within  $3^\circ$  of pure lateral pose with high propensity for symmetry traps [29].



## Solving the Symmetric Pose

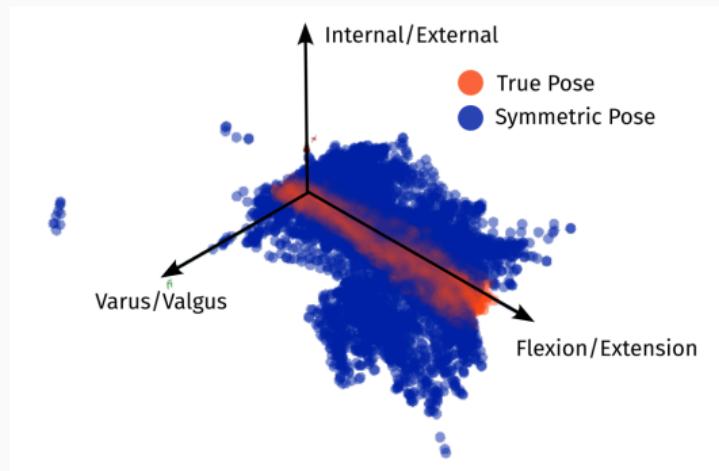
Algorithm devised to “flip” pose into symmetric counterpart.

1. Determine viewing ray from camera to implant centroid, denote  $\vec{v}$ , normalize.
2. Denote symmetric-plane normal vector  $\vec{s}$ , normalize.
3. Measure relative “off-lateral” orientation of implant,  $\cos(\theta) = \frac{\vec{v} \cdot \vec{s}}{||\vec{v}|| ||\vec{s}||}$
4. Apply body-centered rotation to implant about  $\vec{m} = \vec{s} \times \vec{v}$  by  $\psi = 2\theta$ .



## Methods - Training Set

- “Symmetric” poses for each of the 12,000 frames were calculated using the “flipper” algorithm, yielding ~24,000 total training samples. The input for each sample was  $[\theta_{F/E}, \theta_{V/V}, \theta_{I/E}, \psi]$ , and the output was one of {True, Symmetric}



The training data plotted with each axis representing an anatomical rotation (origin not to scale).

Using `scikit-learn`, we implemented the following classification algorithms:

- K-Nearest-Neighbors, Support Vector Machines, Stacked Generalization, Voting Classifier

## Methods - Fixing “Symmetry Traps”

For an input image sequence, we perform the following:

1. Each pose and its symmetric counterpart are fed into the machine learning classifier
  - 1.1 If the outputs are different, take the pose labeled “true” as the correct pose.
  - 1.2 If the outputs are the same, (i.e. both a pose and its symmetric counterpart return “true”), label image “ambiguous”
2. For all images that are NOT ambiguous, construct a cubic spline through the three rotation measurements.
3. For all images that are labeled “ambiguous”, determine which of the two poses is closer to the spline, and take that as the “correct” pose.

# Results - ML Classification

Table 1: Machine Learning Classifier Performance						
Classifier	Tuned Hyperparameters	Test Set	Accuracy (%)	Sensitivity (%)	Specificity (%)	F1-Score
Support Vector Machines (Radial Basis Function)	C = 1000	Internal External	92.1 <b>94.2</b>	94.8 97.1	89.7 91.6	0.92 <b>0.94</b>
Support Vector Machine (Polynomial Kernel)	C = 1000 Polynomial Degree = 2	Internal External	87.7 92.1	92.5 96.6	83.8 88.4	0.87 0.92
K-Nearest-Neighbors	Neighbors = 4 Distance Metric = Minkowski Weights = 'distance'	Internal External	93.1 90.9	94.0 93.6	92.3 88.6	0.93 0.91
AdaBoost	Num. Estimators = 200 Learning Rate = 1 Estimator = Decision Tree	Internal External	88.8 92.9	91.1 <b>97.2</b>	86.7 89.2	0.88 0.93
Histogram Gradient Boosting	Learning Rate = 0.1 Max Iterations = 100 Max Depth = None	Internal External	93.1 93.2	95.0 96.7	91.4 90.3	0.93 0.93
Bagging Estimators	Num. Estimators = 500	Internal External	93.3 93.8	94.3 96.0	92.4 <b>91.9</b>	0.93 0.94
Stacked Generalization	Estimator = Logistic Regression Cross Validation = 'prefit'	Internal External	<b>94.3</b> 92.9	94.8 94.9	<b>93.8</b> 91.0	<b>0.94</b> 0.93
Majority Voting Classifier	N/A	Internal External	92.6 93.3	<b>95.9</b> 96.9	89.9 90.3	0.92 0.93

## Results - Fixing “Symmetry Traps”

- Accuracy: 91.9%
- Sensitivity: 0.674
- Specificity: 0.940

We also measured the distribution of  $\psi$  for correct and incorrect frames.

- Average  $\psi_{correct} = 16.6^\circ$ .
- Average  $\psi_{incorrect} = 7.12^\circ$ .

## Results - Stratified $\psi$ Correction Performance

**Table 2:** Stratified  $\psi$  Test Set Stacked Generalization Classification Performance

Psi Range	Sample Size	Accuracy (%)	Sensitivity (%)	Specificity (%)	F1-Score
0 – 5°	488	71.0	71.4	70.7	0.69
5 – 10°	1132	88.2	90.5	86.0	0.88
10 – 15°	1224	93.0	92.8	93.2	0.93
15 – 20°	1107	96.1	97.0	95.3	0.96
> 20°	3568	98.3	98.3	98.2	0.98

## Discussion

- Reliable post-processing method to overcome pernicious issue (30 years in the making!)
- Suggests an imaging setup for measuring kinematics slightly off-oblique to escape “ambiguous zone”

## Presentations

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- [1] S. Banks, A. J. Jensen, and P. Flood, *In Regione Caecorum Rex Est Luscus - Towards Routine Clinical Examinations of Joint Kinematics*, Oslo, Norway, 2019.
- [2] P. Flood, A. Jensen, and S. Banks, *Towards Practical Clinical Examination of 3D Joint Kinematics Using Machine Learning*, Podium, Toronto, Ontario, 2019.
- [3] A. Jensen, Y. Dai, and A. Gardner, *Impact of Sagittal Resection Variability on Implant Fit during Partial Knee Arthroplasty*, Podium, Phoenix, AZ, Feb. 2020.

## Presentations ii

- [4] A. Jensen, Y. Dai, A. Gardner, *et al.*, *Comparison of Clinical and Computational Implant Fit Analysis in Partial Knee Arthroplasty*, Podium, Phoenix, AZ, Feb. 2020.
- [5] A. Jensen, P. Flood, L. Palm, and S. Banks, *Towards Routine Clinical Examination of 3D Joint Kinematics*, Korea, 2020.
- [6] Y. Dai, D. Wentz, A. Jensen, and B. Martin, *Impact of Fixation Components on Primary Stability of Cementless TKA during Walking*, Podium, Online, Feb. 2021.
- [7] Y. Dai, D. Wentz, A. Jensen, and B. Martin, *Comparative Analysis of Fixation Structure Design on the Primary Stability of Cementless TKA during Walking*, Podium, Online, Feb. 2021.

## Presentations iii

- [8] A. Jensen, P. Flood, L. Palm, and S. Banks, *Accuracy of an autonomous method for extracting joint kinematics from single-plane fluoroscopy*, Oslo, Norway, 2021.
- [9] A. J. Jensen, P. Flood, L. Palm, W. Burton, P. Rullkoetter, and S. Banks, *An Autonomous Method for Extracting 3D Knee Replacement Kinematics from Dynamic Single Plane Fluoroscopic Images*, Online, 2021.
- [10] J. Griffith, A. Jensen, S. Banks, and K. Allen, *Automated Segmentation and Grading of Rodent Knee OA Histology using Convolutional Neural Networks*, Poster, Tampa, FL, Feb. 2022.
- [11] A. Jensen, L. Palm, and S. Banks, *Autonomous Measurement of 3D TKA Kinematics from Dynamic Single-Plane Fluoroscopic Images*, Podium, Tampa, FL, Feb. 2022.

- [12] A. Jensen, *Deep Learning for Image Processing in Orthopaedics*, Virtual Scientific Session, Online, Jan. 2023.

## Publications

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- [1] W. Burton, A. Jensen, C. A. Myers, *et al.*, “Automatic tracking of healthy joint kinematics from stereo-radiography sequences.,” *Computers in Biology and Medicine*, 2021. DOI: 10.1016/j.combiomed.2021.104945.
- [2] A. Jensen, P. Flood, L. Palm-Vlasak, W. Burton, P. Rullkoetter, and S. Banks, “Joint Track Machine Learning: An autonomous method for measuring 6DOF TKA kinematics from single-plane x-ray images,” *arXiv:2205.00057 [q-bio]*, Apr. 2022. arXiv: 2205.00057 [q-bio]. (visited on 05/03/2022).

## Publications ii

- [3] J. S. Broberg, J. Chen, A. Jensen, S. A. Banks, and M. G. Teeter, “**Validation of a machine learning technique for segmentation and pose estimation in single plane fluoroscopy**,” *Journal of Orthopaedic Research*, Feb. 2023, ISSN: 0736-0266, 1554-527X. DOI: 10.1002/jor.25518. (visited on 02/13/2023).

## Timeline

Date(s)	Event
2015-2019	Mech. Eng. B.S, Magna Cum Laude, UF
April 2019 - April 2020	Internship at Exactech
April 2020	Started in Miller Lab
August 2020	Officially Started PhD at UF
November 2021	Best Presentation Award at ISTA: Emerging Technologies
April 2022	Submitted JTML for HAP Paul Award
September 2022	HAP Paul Award at ISTA 2022
June 2023	Single-plane limitations paper submitted
July 2023	Est. IRB Approval
August 2023	v1.0 JTAT
December 2023 ~ May 2024	Patient Data Fully Collected (Aims 3/4)
August 2024	Papers for Aims 3/4 Submitted
December 2024 - April 2025	Est. Graduation

Thank you!

Thanks for listening!!

## References

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