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# Title: Trait-dependent diversification in angiosperms

Andrew J. Helmstetter<sup>1,\*</sup>, Rosana Zenil-Ferguson<sup>2</sup>, Hervé Sauquet<sup>3,4</sup>, Hugo de Boer<sup>5</sup>, Sarah P. Otto<sup>6</sup>, Mario Vallejo-Marin<sup>7</sup>, Jürg Schönenberger<sup>8</sup>, Marcos Méndez<sup>9</sup>, Bruce Anderson<sup>10</sup>, John Pannell, Mathilde Dufay, Concetta Burgarella<sup>11</sup>, Jos Käfer<sup>12</sup>, Sylvain Glemin<sup>13</sup>

<sup>1</sup>*Fondation pour la Recherche sur la Biodiversité - Centre for the Synthesis and Analysis of Biodiversity, 34000 Montpellier, France. email: andrew.j.helmstetter@gmail.com*, <sup>2</sup>*School of Life Sciences, University of Hawaii Manoa, Honolulu, HI, 96822, USA. email: roszenil@hawaii.edu*, <sup>3</sup>*National Herbarium of New South Wales, Royal Botanic Gardens and Domain Trust, Sydney, New South Wales, 2000, Australia*, <sup>4</sup>*Evolution and Ecology Research Centre, School of Biological, Earth and Environmental Sciences, University of New South Wales, Sydney, Australia. email: herve.sauquet@gmail.com*, <sup>5</sup>*Natural History Museum, University of Oslo, 0318 Oslo, Norway. email: h.d.boer@nhm.uio.no*, <sup>6</sup>*Department of Zoology, 6270 University Blvd., University of British Columbia, Vancouver BC, V6T 1Z4, Canada. email: otto@zoology.ubc.ca*, <sup>7</sup>*Department of Biological and Environmental Sciences, University of Stirling, Stirling, FK9 4LA, United Kingdom. email: mario.vallejo@stir.ac.uk*, <sup>8</sup>*Department of Botany and Biodiversity Research, University of Vienna, Rennweg 14, 1030 Vienna, Austria. email: juerg.schoenenberger@univie.ac.at*, <sup>9</sup>*Area of Biodiversity and Conservation, Universidad Rey Juan Carlos, 28933 Móstoles (Madrid), Spain. email: marcos.mendez@urjc.es*, <sup>10</sup>*Department of Botany and Zoology, University of Stellenbosch, Private Bag X1, Matieland 7602, South Africa. email: banderso.bruce@gmail.com*, <sup>11</sup>*Department of Organismal Biology, University of Uppsala, Uppsala, 75236, Sweden. email: concetta.burgarella@gmail.com*, <sup>12</sup>*Université de Lyon, Université Lyon 1, CNRS, Laboratoire de Biométrie et Biologie Evolutive UMR 5558, F-69622 Villeurbanne, France. jos.kafer@univ-lyon1.fr*, <sup>13</sup>*CNRS, Ecosystèmes Biodiversité Evolution (Université de Rennes), 35000 Rennes, France. email: sylvain.glemin@univ-rennes1.fr*

**Correspondence:** Andrew J. Helmstetter, FRB-Cesab Institut Bouisson Bertrand, 5, rue de l'École de médecine - 34000 MONTPELLIER. Tel: +33 4 11 28 20 58. Email: andrew.j.helmstetter@gmail.com

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**Data accessibility statement:** The data supporting the results will be archived in an appropriate public repository and the data DOI will be included at the end of the article upon article acceptance.

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## Abstract

Understanding the origins and distribution of species diversity across the tree of life is the central goal in macroevolution and is increasingly recognized as being key to community and functional ecology. ~~The rich variety of ecological and morphological characteristics in nature has inspired many studies to attempt to link~~ traits with species diversification, encouraged by the development of powerful macroevolutionary models and large phylogenies. Angiosperms are a highly diverse group that illustrate how species diversification affects ecosystem functioning, having fundamentally shaped life on earth since the Cretaceous. However, we still know relatively little about the traits that have shaped their diversity. Here, we synthesized data from 152 studies that used state-dependent speciation and extinction (SSE) models to investigate trait-based diversification in angiosperms. Intrinsic traits related to reproduction and morphology were often linked to diversification but a set of universal drivers did not emerge due to widespread inconsistency in results. Dataset properties were closely correlated to SSE model results - trees that were larger, older, or less well-sampled tended to yield trait-dependent outcomes. To aid future work we provide a set of best practices to follow when designing studies and reporting results, and highlight clades and traits that are understudied.

## Introduction

Species diversity is unevenly distributed across the tree of life and while substantial research has investigated why some clades are more diverse than others, many fundamental questions remain unanswered. The causes behind this unevenness can be diverse, from catastrophic mass extinctions that decimate diversity (Raup & Sepkoski, 1982) to key innovations that spur on rapid speciation (Hodges & Arnold, 1995) to ecological factors such as competition that shapes species co-existence (Drury et al., 2016; Rabosky, 2013). A greater understanding of the drivers of species diversification is important because they can have far-reaching consequences that affect the assembly of communities and their phylogenetic structure, the evolution of functional traits that underpin a species' role in its environment, the formation of species interaction networks, and simply how biodiversity has evolved through time (Morlon, 2014). Research aiming to link species characteristics to macroevolutionary dynamics has become extremely popular over the last decade due to the increasing availability of large phylogenetic trees (Jetz et al., 2012; Rabosky et al., 2018; Smith & Brown, 2018; Upham et al., 2019) and the continuing development of a range of statistical models to infer patterns in species diversification and the drivers behind them (Barido-Sottani et al., 2020; Beaulieu & O'Meara, 2016; Maliet et al., 2019; Rabosky & Huang, 2016). The increasing amount of empirical knowledge provides an opportunity to synthesise what we know so far about a wide range of ecologically diverse and species-rich clades to uncover general dynamics about the traits that have driven their diversification.

Species diversification can be linked to traits via state-dependent speciation and extinction (SSE) models. This popular family of models are birth-death processes where the diversification rates (birth is speciation, and death is extinction) are dependent on character states, and where transition rates between states define how state changes occur. The simplest SSE model is the binary-state speciation and extinction (BiSSE) model (Maddison et al., 2007) that takes as input a phylogenetic tree and state values (0 or 1) for each species in the tree. This allows users to uncover whether lineages with one state diversify faster than those with the other. SSE models can also be used to test whether the transition rates between states in one direction (0 to 1) are faster than the other (1 to 0). The original model has been extended in various different ways (Fig. 1) to address different types of macroevolutionary questions. For example, ClaSSE (Goldberg & Igić, 2012) and BiSSE-ness (Magnuson-Ford & Otto, 2012) are extensions of BiSSE that include cladogenetic events (speciation simultaneously associated with change in

state), and GeoSSE (Goldberg et al., 2011) explicitly models how diversification differs among geographic regions. Other developments include models with more than two character states (MuSSE (FitzJohn, 2012)), quantitative traits (QuaSSE (FitzJohn, 2010)) and semi-parametric models (FiSSE (Rabosky & Goldberg, 2017)). Perhaps the most important innovation after the initial wave of SSE models was the introduction of hidden states into SSE models (Beaulieu & O’Meara, 2016; Caetano et al., 2018; Herrera-Alsina et al., 2019) as a solution to various factors increasing the rate of false positives inferred in SSE models including phylogenetic pseudo-replication (Maddison & FitzJohn, 2015) and diversification patterns driven by traits other than the focal one (Rabosky & Goldberg, 2015). The incorporation of hidden states into SSE models allowed diversification rates to be influenced by the focal traits as well as an unobserved trait(s) and provided a new set of more complex null hypotheses (the character independent (CID) models). This allowed users to test how relevant the ~~main trait being studied~~ is to species diversification (Beaulieu & O’Meara, 2016; Caetano et al., 2018) in the context of other factors. Here we focus on synthesizing results from SSE models used to investigate trait-dependent diversification in flowering plants, or angiosperms. There have been more than 150 of such studies, providing an opportunity for an updated perspective on the role different traits have played in angiosperm diversification (Vamosi et al., 2018).



Angiosperms are one of the most successful and diverse clades in the tree of life. There are more than 350,000 extant species, the result of a 140 to 270 million year history (Foster et al., 2017; Li et al., 2019; Magallón et al., 2015; Sauquet et al., 2021; Silvestro et al., 2021). Almost all of terrestrial life is linked, directly or indirectly to angiosperms (Benton et al., 2021) and their success makes them an ideal study group for uncovering the intrinsic and extrinsic traits driving their diversification. Previous work has suggested that the origins of angiosperm diversity can neither be tied to major global events nor the evolution of a single key innovation but instead various combinations of traits, environment and ecology acting to stimulate diversification in different groups (Davies et al., 2004; Magallón & Castillo, 2009; Sauquet & Magallón, 2018) creating a landscape of macroevolutionary dynamics that vary substantially across different angiosperm clades (Magallón et al., 2019). One hypothesis ~~about the variation~~ argues that the traits driving the differences in diversification are a range of vegetative and reproductive characteristics, some of which are unique to angiosperms (Stebbins, 1974). In sexual systems, for example, dioecy originated in 900-5000 independent instances (Renner, 2014) but not all of

these led to the same macroevolutionary dynamics (Wang et al., 2021). In some groups, dioecy was associated to increased diversification, in others to decreased diversification, while in still others it seemed to have no effect (Käfer et al., 2014; Sabath et al., 2016). This may depend on interaction with other associated traits (Zenil-Ferguson et al., 2019) although none has been clearly identified (Käfer et al., 2014; Sabath et al., 2016). In the majority of studied traits, we do not know how pervasive such inconsistency is, nor have broad-scale empirical studies of trait-dependent diversification provided a general consensus on which traits are most important for angiosperm diversification.

In this study we bring together the latest empirical knowledge on flowering plant diversification to identify those traits that have been found to repeatedly stimulated diversification in angiosperms and compare their effect in different evolutionary contexts. We also investigate the relationship between the properties of datasets (e.g. tree size and global sampling fraction) and the results of published studies, highlighting how biases in our use of SSE models can affect our conclusions when searching for general trends. Finally, we identify gaps in our current knowledge and provide a set of best practices for diversification result-reporting to enhance our ability to fill these gaps in the future.

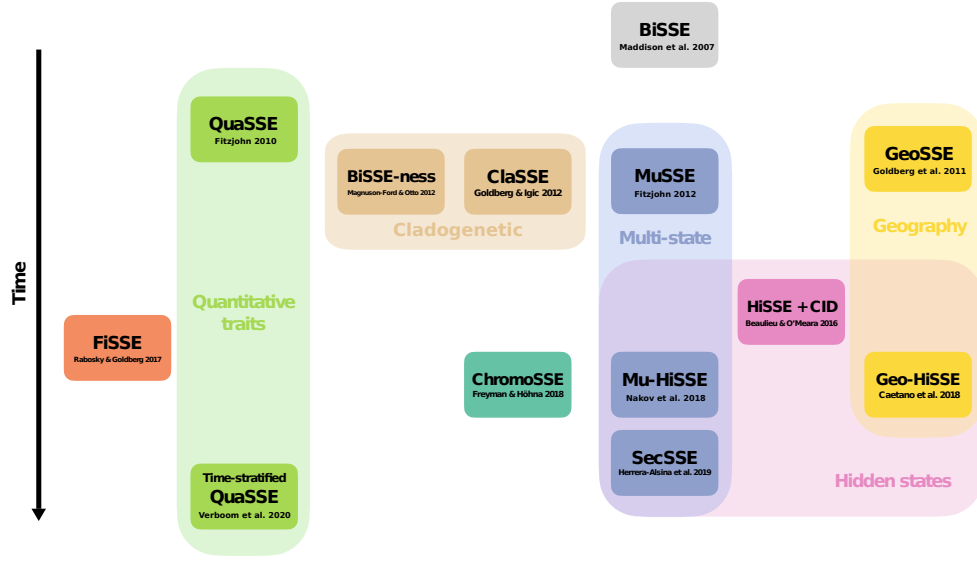


Figure 1: The development of state-dependent speciation and extinction (SSE) models. The original binary-state speciation and extinction model (BiSSE) model (Maddison et al., 2007) is shown at the top of the diagram with all other models depicted below, in the order of their publication. Acronyms are defined as follows; Binary-State Speciation and Extinction–node enhanced state shift (BiSSE-ness)(Magnuson-Ford & Otto, 2012), Cladogenetic and Anagenetic Models of Chromosome Number Evolution (ChromoSSE) (Freyman & Höhna, 2018), Character-Independent Diversification (CID) (Beaulieu & O’Meara, 2016), Cladogenetic State change Speciation and Extinction (ClaSSE) (Goldberg & Igić, 2012), Fast, intuitive State-dependent Speciation-Extinction (FiSSE) (Rabosky & Goldberg, 2017), Geographic State Speciation and Extinction (GeoSSE) (Goldberg et al., 2011), Hidden Geographic State Speciation and Extinction (GeoHiSSE) (Caetano et al., 2018), Hidden State Speciation and Extinction (HiSSE) (Beaulieu & O’Meara, 2016), Multi-State Speciation and Extinction (MuSSE) (FitzJohn, 2012), Multicharacter Hidden State Speciation and Extinction (Mu-HiSSE) (Nakov et al., 2018), Quantitative State Speciation and Extinction (QuaSSE) (FitzJohn, 2010; Verboom et al., 2020), Several examined and concealed states-dependent speciation and extinction (SecSSE) (Herrera-Alsina et al., 2019). Each box shows the name of the model and the associated citation. Models that share similar attributes (e.g. those with hidden states) are colour coded and grouped with boxes. This is not an exhaustive list of SSE models, and does not include, for example models used in epidemiology that allow tips to be sampled at various points in time (Scire et al., 2020).

# Materials & Methods

## Data collection

We collected all published studies that cited SSE methods papers (Beaulieu & O’Meara, 2016; Caetano et al., 2018; FitzJohn, 2010, 2012; Freyman & Höhna, 2018; Goldberg & Igić, 2012; Goldberg et al., 2011; Herrera-Alsina et al., 2019; Maddison et al., 2007; Magnuson-Ford & Otto, 2012; Nakov et al., 2018; Rabosky & Goldberg, 2017; Verboom et al., 2020) using Google Scholar, last accessed 18th May 2021. To facilitate data collection from papers using SSE models, we developed a new R package called ‘papieRmache’ (<https://github.com/ajhelmstetter/papieRmache>). This package has two main purposes (1) to classify papers into different categories based on the frequency of term use in the text and (2) to pull out sections of the main text that contain a keyword or a pair of keywords while highlighting relevant information. We identified the SSE studies on angiosperms by using the keywords ‘angiosperm’, ‘flowering’ and ‘plant’ subsequently validating the subset of papers by hand and removing any studies on groups other than angiosperms. We then collected up to 30 different dataset properties from each paper relating to the trait investigated, the group studied, the phylogenetic tree and the outcome of the SSE model used (see appendix S1 for a detailed explanation of each property). In cases where there was uncertainty in how to interpret or collect data from a study we contacted the authors for their assistance and clarification, where possible.

## Trait classification

While some sets of character states were the same among studies (e.g. annual vs perennial; diploid vs polyploid), many of them did not overlap. We classified traits into different categories to facilitate comparisons among different trait types. At the broadest classification these were intrinsic (traits belonging to the species), extrinsic (environmental or geographic traits), interaction (traits related to other species), and combination (multiple traits belonging to different categories that were grouped e.g. species that have both small fruits and are found on islands). To allow for analyses at different grouping levels we developed a trait ontology (Table ??) starting at level one as detailed above and becoming more specific, up to level six.



## Data analysis

To examine the effect of particular traits on diversification we used the trait categories defined above and calculated the proportion of models in which trait-dependent diversification was inferred. In many cases multiple models are run per study, typically to investigate the effect of a single trait across different clades or the effects of different traits on diversification in a single clade. We considered each model separately here with an outcome of 1 (trait-dependent diversification detected) or 0 (no effect of trait detected) recovered per model. We examined patterns at different levels of trait categorization, as well as using only those models with hidden states. Whether or not trait-dependent diversification was detected was typically based on significance in model comparisons and/or posterior distributions of rates among states. However, if significance wasn't inferred or reported, we followed the study narrative and statements made in the text. If model comparisons were conducted and reported, only the best-fitting model was considered, unless other models were explicitly referred to in the study. To facilitate comparison, we mainly consider whether or not a trait has an effect on diversification, irrespective of the direction of the effect (i.e. increase or decrease of diversification), as the direction is only defined at the state level. When both the effect and the absence of an effect of a trait on diversification has been inferred in different studies, we consider these studies "inconsistent".

In models where information was available, net diversification rates (lineages per million years) were extracted for each character state. At a broad scale, relative differences in net diversification rates were calculated as  $(r_{max} - r_{min})/r_{max}$  and were used to represent the magnitude of the effect of a given trait on diversification, while taking into account general variation in diversification rates among clades. Comparisons were then made across trait level 1 and 2 categories. For ease of interpretation, these analyses were restricted to ~~only~~ those models where all net diversification rates were positive. At a more narrow scale, we identified eight ~~cases~~ in which there was enough replication to be able to assess whether one character state had consistently higher net diversification rates than the other(s). We selected this subset of traits by identifying those that had been tested at least five times, in at least two different studies and two different clades.

We also examined the relationship between SSE model inferences and continuous dataset properties; number of tips, root age, number of genetic markers, sampling fraction (here referring to global sampling fraction unless stated otherwise) and tip bias (here calculated as the number

of tips with the most common state divided by the number of tips with rarest state). For each of these we constructed two density plots representing the distributions of values in cases where trait-dependent diversification was, and was not, inferred and compared the overlap between densities. We also fitted generalized additive models (GAM, Hastie and Tibshirani, 2017) to the continuous dataset properties with the SSE model result as a binary response variable (trait-dependent diversification vs no effect). The GAM approach allows linear or non-linear smooth functions to be used for predictor variables, giving greater flexibility in the estimation of relationships between predictors and the dependent variable. When analysing continuous data, all variables were log-transformed (or arcsine in the case of sampling fraction) to conform better to a normal distribution. Initially, we constructed a GAM using all five variables and assigned the mean of the known values to any missing values. We also assessed each variable individually to determine the shape of each relationship when examined in isolation. In all cases we used smoothing functions (cubic regression splines) with  $k = 5$  dimensions for each variable.

## Predicting results based on dataset properties

After collecting information from all studies we found that the dataset properties were sometimes associated with the outcome of the SSE model, that is, whether trait-dependent diversification was inferred or not. We therefore attempted to predict SSE model results (inference of trait-dependent diversification vs no effect) from dataset properties alone, and identify those properties with the largest predictive power. We used all available dataset properties except for highly-specific categorical variables (e.g. trait levels 5-6, clade, family) and those that varied among different states (putative root state, sampling per state, samples per state). We used a machine learning approach, extreme gradient boosting, with the R package ‘xgboost’ (Chen & Guestrin, 2016), a supervised learning approach based on gradient boosting machines. This family of methods uses a labelled dataset (the outcome is known) and an ensemble of weak prediction models (e.g. decision trees) whereby new models are added on to existing models per iteration to minimize error. The xgboost algorithm improves upon other boosting methods with its increased speed and enhanced regularization to minimize overfitting (Chen & Guestrin, 2016). Prior to running our models, categorical variables with more than two categories were converted into binary, dummy variables using one-hot encoding to facilitate model building. We trained models on a random selection of 80% of our dataset and tested them on the other 20%.

After a parameter optimisation step we repeated this process 500 times to produce a range of accuracy values, the percentage of cases where the real outcome matched the classification, to account for stochasticity in the test and training datasets. For each iteration we also recovered the relative importance of each variable, which allowed us to determine which dataset properties had the most influence on the model. Given the inter-dependency of variables across the different decision trees, it is difficult to uncover whether a given property generally leads to trait-dependent diversification or not with xgboost. We avoid interpreting the results in this way, focusing on how accurate prediction can be and the variables that are most important to the model's predictive ability.

## Results

### Traits studied and their effects on diversification

We collated information on trait-based diversification from 152 studies using a total of 629 SSE models to study angiosperm diversification. We found that 124 studies were conducted on a single clade, the rest examined diversification patterns across multiple clades. Variation in ~~breadth of different~~ traits investigated was also observed within studies. In total, 92 studies examined just a single trait level 6 category, while 38 studies looked at diversification patterns in sets of traits that belonged to more than one trait level 1 category (e.g. extrinsic and intrinsic traits). In terms of taxonomic level, SSE models were most often run on focal genera, or families (Fig. ??) and study clades were relatively evenly-distributed across the angiosperm tree of life (Fig. ??). Studies have focused on 36 out of 64 angiosperm orders, and 83 out of 416 families. As expected, diversification interest is generally proportional to the amount of species diversity in different parts of the angiosperm tree of life. There was a clear, positive correlation between the number of species in a clade (family, order) and the number of state-dependent diversification studies applied to the clade (Fig. ??, ??).

At the highest level of classification, intrinsic traits (i.e. those belonging to the plant species itself) were tested more often (295 models or 47% of models run) than extrinsic traits (i.e. those related to the species' habitat and geography, 255 models or 41%). Researchers tended to study intrinsic traits relating to reproduction (e.g. flower morphology, fruit morphology, breeding system), traits related to species' biogeography (biome, geographic region) and vegetative traits (e.g. life form, leaf morphology) and less often physiological characters (e.g. photosynthesis) or those related to interaction (symbiosis, pollination, or dispersal) (Fig. 2). We compared the proportion of trait-dependent diversification outcomes in SSE models at different category levels (see ontology Table ??). In general, intrinsic traits were found to be associated to diversification slightly more often than extrinsic traits (57.3% vs 52.5%). If a trait has been studied more than once we can compare the effect of this trait on diversification in different evolutionary contexts to see if similar trends are found.

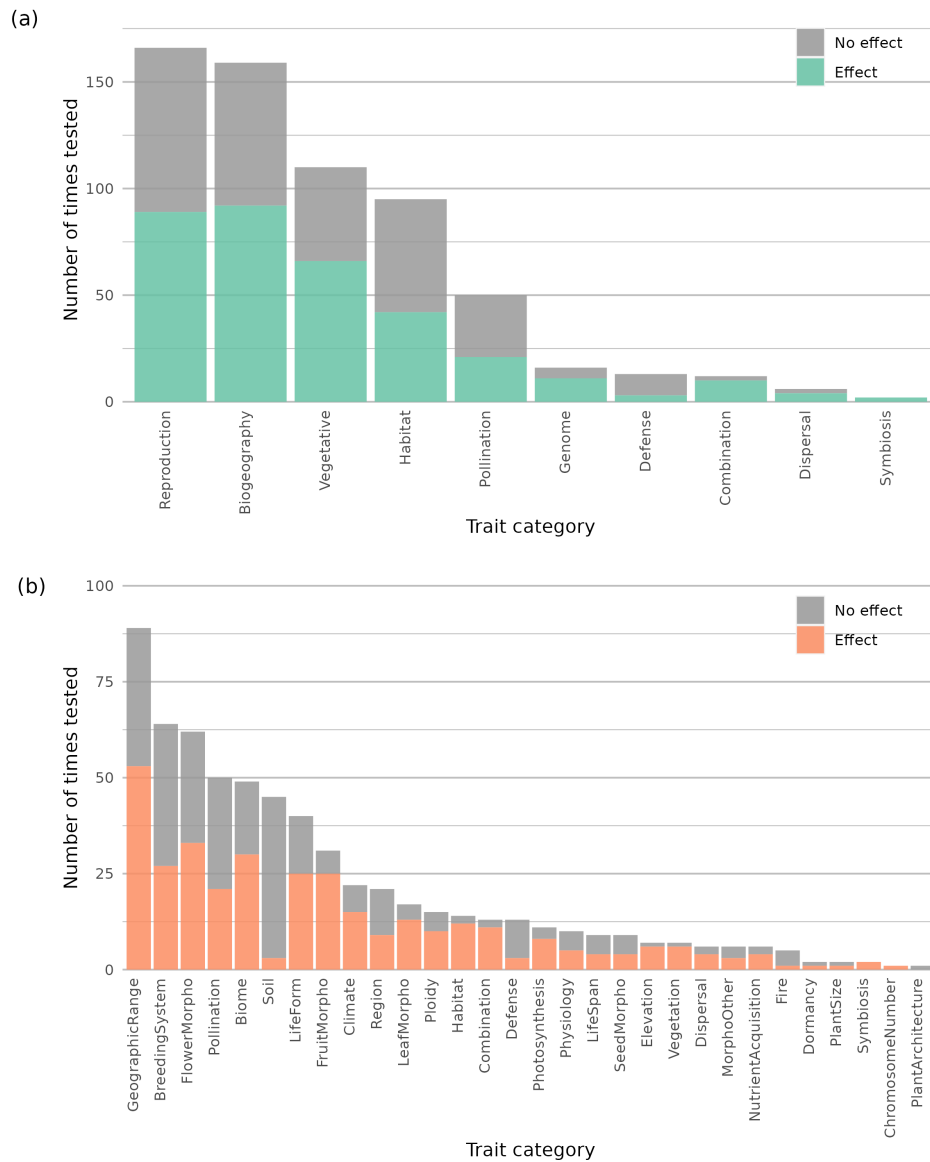



Figure 2: Stacked barplots showing how often particularly trait types were tested with state-dependent speciation and extinction (SSE) models. Bars are coloured to depict how often trait-dependent diversification was detected per trait type. If multiple SSE models were used in a single study they were considered separately i.e. each model contributed one result to the totals for each trait category. Two plots are shown, (a) one with relatively broad trait categories (level 2) and (b) one with more narrow categories (level 4). An ontology depicting how different trait classification levels are connected can be found in Table ??.

Our collation of data showed that results inferred with SSE models were inconsistent at both broad and narrow scales (grey vs coloured portions of bars in Fig. 2). For example, traits such as lifespan (Azani et al., 2019; Drummond et al., 2012; Salariato et al., 2016; Soltis et al., 2013) and ploidy level (Folk & Freudenstein, 2014; Han et al., 2020; Landis et al., 2018; Zenil-Ferguson et al., 2019) yielded different results depending on the angiosperm group studied. Polyploidy has been linked to increased diversification in *Allium* (Han et al., 2020) while ~~Roman-Palacios et al.~~ (Román-Palacios et al., 2019) ~~found that polyploids and diploids diversified at similar rates in Brassicaceae.~~ Among those trait level 2 categories that have been tested using >25 models, vegetative traits yielded trait-dependent diversification at a higher proportion than any other trait type and pollination the lowest proportion (Fig. 2a). We then tested whether results from all models and only those with hidden states (30 studies) differed. We found (Fig. ??) that the proportion of trait-dependent outcomes increased for pollination, remained about the same for reproduction and decreased substantially for biogeography, vegetative and habitat.

Though replication among character states was typically low we found eight ~~of~~ traits that were tested often enough ~~to begin~~ to assess whether there was a consistent effect of one state on diversification and the magnitude of the effect (Fig. ??). In three of these traits (lifespan, sexual system and woodiness) trait-dependent diversification was rarely found while in the remaining traits (epiphytism, biome, ploidy, photosynthesis and self-compatibility) results more often indicated trait-dependent diversification. However, we did find conflict in which states increased in diversification among different models in all traits except epiphyte form and self-incompatibility. Examining the absolute net diversification rates among states of seven traits (sexual system could not be assessed as most rates were not time-calibrated) we found that patterns across clades reflected those detailed above (Fig. ??). Net diversification rates in traits for which there was a low proportion of trait-dependent diversification (e.g. woodiness or lifespan) were generally similar among the different states (Fig. ??). To understand the effect of major trait categories on diversification we plotted the distribution of relative differences in net diversification rates for models belonging to each trait category (Fig. ??). Generally we found that in each trait category there was a wide range of relative differences. For trait level 1 we found rates were generally similar with some indication that interaction traits may have a greater effect on diversification rates than intrinsic or extrinsic traits, but this was not significant (Kruskal-Wallis chi-squared = 0.993, df = 2, p-value = 0.6087). Traits related to the

genome had the largest relative differences but again categories were not significantly different (Kruskal-Wallis chi-squared = 9. , df = 8, p-value = 0.3325).

### **The evolution of SSE model use and methodological innovation**

As SSE models themselves have diversified, the relative frequency of model-use has changed over time. ~~We collated data on the types of SSE model used in each study, and plotted their use by year of publication~~ (Fig. 3). BiSSE has remained popular even as newer more complex models have emerged. Models with multiple states, predominantly MuSSE, have also been commonly used showing that researchers are interested in the effects of more complex traits or trait groups with more than two states. There has also been a consistent focus on using SSE approaches related to geography in models like GeoSSE and GeoHiSSE. When examining the number of studies that use SSE models each year we find a rapid increase since the original BiSSE paper in 2007 until a conspicuous slowdown and slight drop in 2015 (Fig. 3). This appears to coincide with the publication of a number of influential papers that criticised the propensity of SSE methods for false positives (Maddison & FitzJohn, 2015; Rabosky & Goldberg, 2015) and pointed out power limitations (Davis et al., 2013). After this, SSE model use continued with a greater variety of models owing to the development of models with hidden states (Beaulieu & O'Meara, 2016), which have since spread to all aspects of SSE model use (Fig. 1), becoming the dominant set of models by 2019 (Fig. 3).

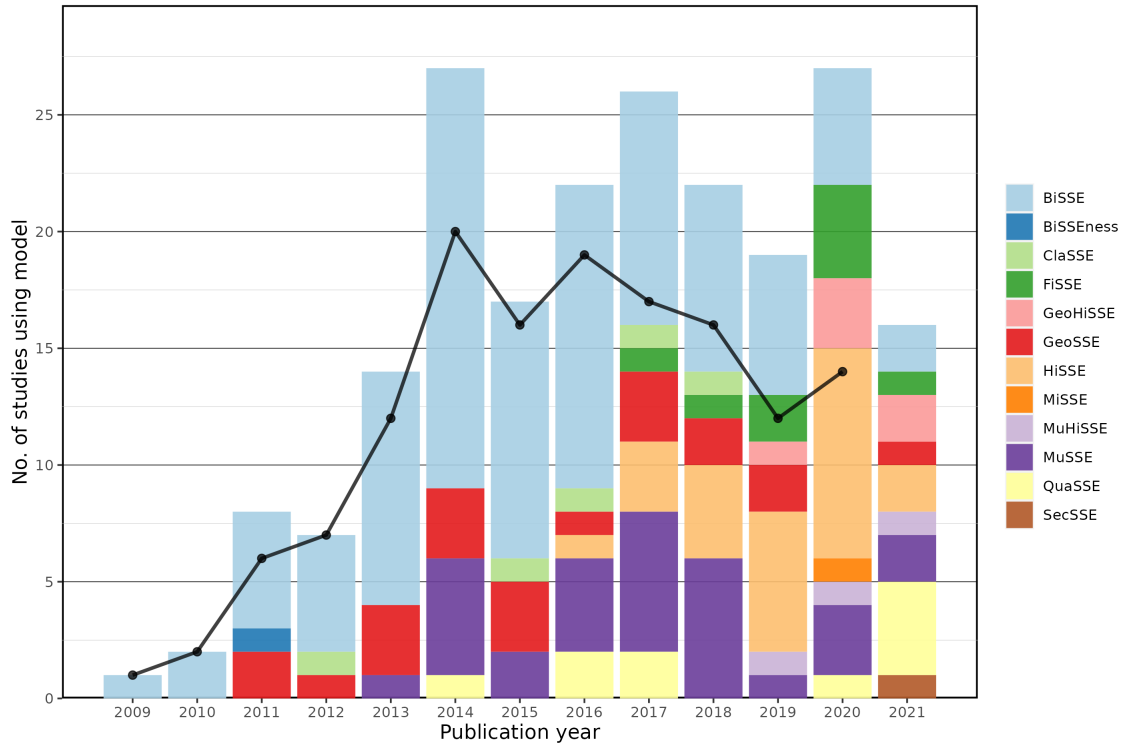


Figure 3: A stacked barplot showing the change in state-dependent speciation and extinction (SSE) models used on angiosperm clades over time. Each bar indicates the number of unique SSE model types per study totaled over the publication year. Bars are coloured according to the proportion of each SSE model type published in that year (see legend on the right of the plot). If multiple of the same type of SSE model are used in a single study this is only counted once (e.g. if BiSSE was used four times in a study published in 2012 this contributes an increase of one to the BiSSE portion of the 2012 bar). The black line shows the total number of studies using SSE models on angiosperms per year. Note that studies published after May 2021 were not included, so this year is incomplete.





## Theoretical recommendations vs empirical practices

The input data for macroevolutionary studies have grown in size and quality, in parallel with the innovations in the SSE models. For example, we found evidence that over time, trees used with SSE models have gradually grown larger (Fig. ??). The number of tips in a tree is important for robustness of SSE model results and guidelines for adequate power were put forward by Davis et al. (2013) who suggested that results from models using trees with fewer than 300 tips should be treated with caution. But how have such recommendations shaped SSE model use? We examined sizes of trees used before and after guidelines were published, across all SSE models. The proportion of models run on trees with fewer than 300 tips was initially very high (94% of 139 total models) in studies published up until 2013. It then decreased to 57% (277 of 482) models in studies published from 2014 onwards. Despite this reduction, more than 60 models were run on trees with fewer than 50 tips after Davis et al. was published in 2013. Tip ratio bias recommendations were also made by Davis et al. (2013) who cast doubt on inferences made when the rarest state occurs in less than 10% of the taxa. Prior to 2014, 83% of SSE models (55 of 66) had suitable tip ratios and this figure remained similar (87%, 313 of 360) for the studies that came after. Global sampling fraction is the proportion of known species that are present in the tree. If the sampling fraction is low it can drastically affect diversification rate estimation (Sun et al., 2020). After introducing the possibility to account for incomplete sampling in SSE models, Fitzjohn et al. (FitzJohn et al., 2009) found that a sampling fraction of 25% was adequate for capturing diversity dynamics. All 10 models published in 2009 and earlier had sampling fractions greater or equal to 25% compared to 60% of 606 models after its publication. This trend (Fig. ??) probably reflects easing of assumptions on complete species sampling, but also indicates that high levels of incomplete sampling are common in recent literature.

## The importance of dataset properties

The recommendations outlined above are largely based on simulations and theory but SSE models are known to behave differently between simulated and empirical trees (Rabosky & Goldberg, 2015). So what happens to results of SSE models when dataset properties vary in practice? We examined the relationship between tree size and whether or not trait dependent diversification was inferred, regardless of the trait investigated. We found that, in general, trait-

dependent diversification was detected less often when trees had smaller numbers of tips (Fig. 4a, ??a). Tree size and root age are closely linked because trees with larger numbers of tips are generally older (Fig. ??). Indeed, we found that ~~when~~ trait-dependent diversification was detected, ~~it also tended to be~~ when trees with an older root age were used (Fig. 4b, ??b). Regardless of their size or age, trees that more accurately represent the true phylogeny of a group will allow us to more reliably estimate its diversification history. ~~We used information on the total number of molecular markers (nuclear + plastid + mitochondrial) as a proxy for tree quality.~~ We found a difference in the distributions indicating that models with trait-dependent outcomes usually had better quality trees than those that did not (Fig. 4c, ??c).

Using a small proportion of known, extant species will typically reduce our ability to reliably detect differences in diversification rate (Chang  et al., 2020; FitzJohn et al., 2009), but modern macroevolutionary models can now account for missing species in a variety of ways (FitzJohn et al., 2009; Rabosky, 2014). ~~In the set of angiosperm studies we use here,~~ sampling fraction ranges from <0.1% to complete (100%) sampling. ~~We found a striking pattern, showing that~~ those models that used trees in which sampling fraction was low generally yielded trait-dependent diversification, particularly when sampling was less than 40% (Fig. 4d, Fig. ??). Conversely, high sampling fraction was more often associated with a lack of trait-dependent diversification. Given that the inference of trait-dependent diversification varies with tree size (Fig. 4a), we wondered whether there may also be a relationship between sampling fraction and tree size. However, ~~upon examination~~ we found only a weak, negative ~~trend where~~ trees with more tips ~~had slightly lower~~ sampling fractions (Fig. ??). We then looked at the relationship between sampling fraction and the number of species in the study clade of interest and found a steeper negative relationship (Fig. ??) meaning that the larger the clade of interest is, the less well-sampled it tends to be. Datasets of small clades with low sampling fraction are generally missing (as they should not be studied) and large clades with high sampling are currently very rare, causing points in the bottom left and top right of figure ?? to be missing. These negative trends remain similar regardless of whether trait-dependent diversification is inferred or not. Another ie that has been repeatedly brought up in simulation studies is the potential effect of inflated tip bias (Davis et al., 2013; Maddison et al., 2007). Tip bias increases when there is a higher frequency of one state than the others across the tips of the tree. Upon examining the data used with SSE models we found substantial overlap between densities (Fig. 4e) except for

extreme values of tip bias where SSE models tended to find no effect of the trait studied (Fig. ??e). To assess the importance of these properties together we fit a GAM including all five continuous variables (Fig. ??) and found that all variables except age of tree were significant when predicting SSE model outcome ( $\Delta AIC = 0.239$ , see Table ?? for full details).

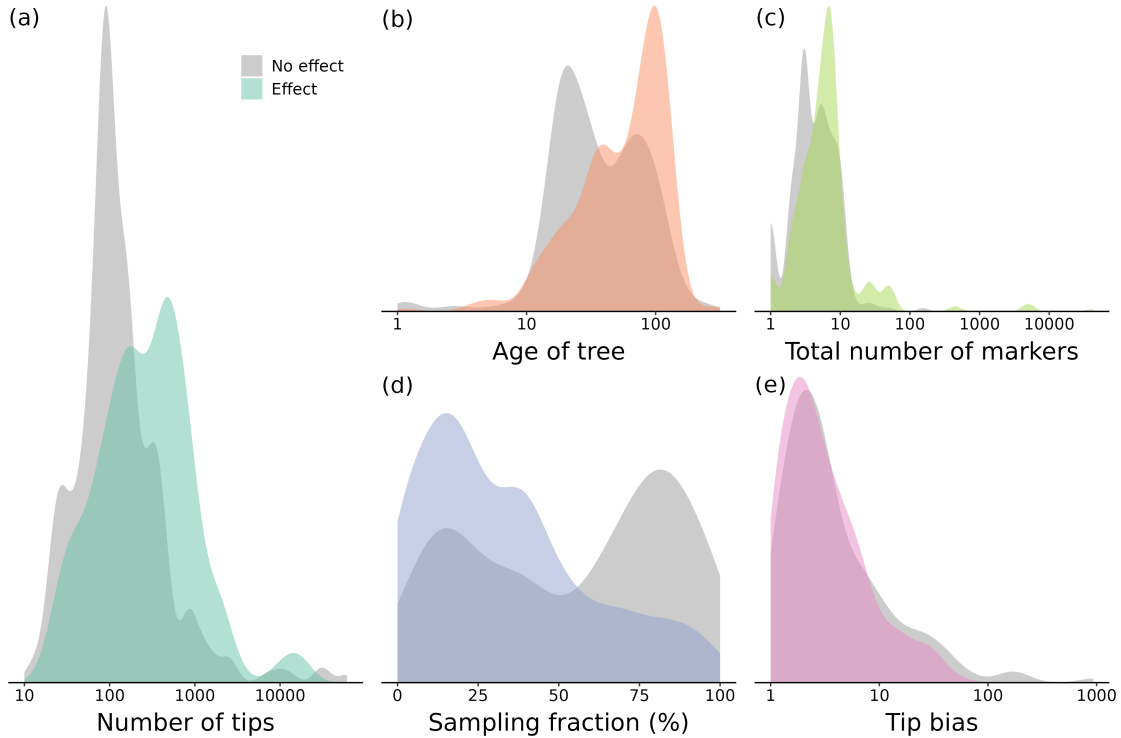



Figure 4: A set of densities depicting the distribution of values for five dataset properties in SSE models that infer trait dependent diversification (coloured densities) and those that do not (grey densities). The dataset properties shown are (a) number of tips in the phylogenetic tree used with the SSE model (data taken from  $n = 621$  models), (b) the age of the tree used with the SSE model ( $n = 523$ ), (c) the total number of genetic markers (nuclear + plastid + mitochondrial) used to infer the phylogenetic tree used with the SSE model ( $n = 615$ ), (d) the global sampling fraction ( $n = 616$ ) and (e) the tip bias, here calculated as the largest tip frequency divided by the smallest ( $n = 429$ ).

## How predictable is the inference of trait-dependent diversification?

Empirical ts in angiosperms clearly exhibit strong relationships between various dataset properties and whether trait-dependent diversification is inferred by the SSE model. If we had comprehensive information about the input data, including the dataset properties investigated above but also information about taxonomy and traits, could we predict whether trait-dependent diversification would be inferred? Using a machine learning approach, extreme gradient boosting (Chen & Guestrin, 2016), we were able to correctly predict, with approximately 72% accuracy (60-80%, Fig. ??), whether SSE models would infer trait-dependent diversification. The most important factors ~~in the gradient boosting models we constructed~~ were the information-dense, continuous variables (Fig. 5) further reinforcing earlier observations about their potential influence on SSE model outcomes (Fig. 4, ??, Table ??). Generally, categorical variables played a smaller but still important role. Studying the association between fruit morphology and diversification, using the HiSSE model and working in Poales were all influential in the model's predictive ability (Fig. 5).

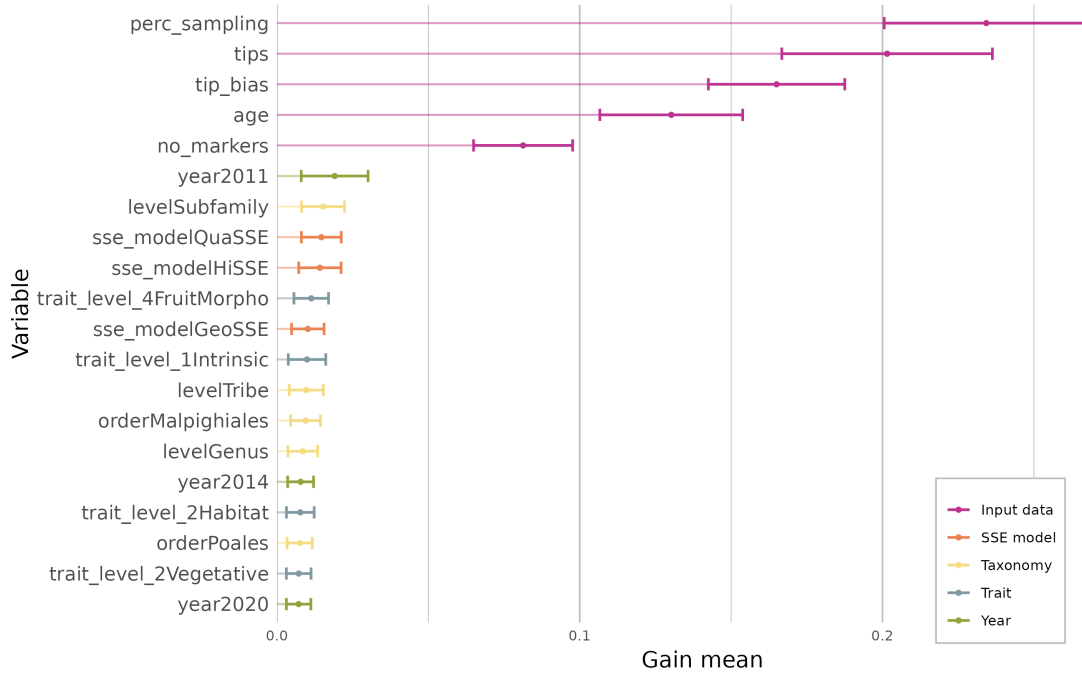


Figure 5: A horizontal barplot showing the relative influence of the 20 most important features included in the xgboost model used to predict the outcomes of SSE models, whether or not trait-dependent diversification is inferred, using input data properties and other characteristics of each study. Points are the mean gain values calculated from the 500 iterations that were run. Error bars represent one standard deviation around the mean. Bars are coloured based on the type of variable they represent.

## Discussion

### Major drivers of angiosperm diversification remain unknown

Angiosperms are by far the most species-rich division of plants, so understanding how this diversity arose is one of the key questions in plant macroevolution (Crepet & Niklas, 2009; Onstein, 2019; Sauquet & Magallón, 2018).

Previous work has proposed that diversity in different angiosperm groups may have been shaped by various combinations of ecology, traits and environment (Davies et al., 2004; de Queiroz, 2002; Donoghue, 2005; Donoghue & Sanderson, 2015; Hernández-Hernández & Wiens, 2020; Magallón & Castillo, 2009). Under the assumption that current studies represent an unbiased view of diversification, we found that their results support this proposal. That is, the factors driving angiosperm diversification are more complex than a set of universal drivers, which did not emerge from our literature survey. When we compared studies investigating the same trait types we found that that conclusions generally differed with some indicating that the trait does have an effect on diversification and others concluding there is no effect. We note that the inconsistency observed might reflect real trends in the data, or be due to dataset properties (lack of power, model mis-specification). In the following, we will first discuss the biological conclusions of our study, before addressing dataset and model issues.

Our analyses and results centered around how traits (e.g. pollination) rather than the character states of these traits (e.g. bee vs bird pollination) affect diversification. After grouping traits into several levels of categories (Table ??), we found that some types of traits were more important to angiosperm diversification than others. ~~Given the nature of ‘flowering plants’ it may come as no surprise that traits related to variation in their defining structure, flowers,~~ are among the most investigated and influential (Fig. 2b). Indeed, the flower contains the organs needed for sexual reproduction, making it central to the biology, ecology and evolution of angiosperms, and flower characteristics certainly have a large role in determining differences in diversification (Vamosi et al., 2018). In particular, reproductive systems are highly variable in angiosperms (Barrett, 2013) and are again thought to be closely linked to their success (Barrett et al., 1996). Results from SSE models lend some support to this idea - for example, ~~trait-dependent diversification was commonly inferred when mating system traits were investigated~~ (Fig. ??). Even so, we found that in most cases, breeding system (the higher level trait

classification including all aspects of mating and sexual systems) did not yield trait-dependent diversification, due to inconsistency in the effect of sexual system. Vegetative traits (those related to the growth, physiology and non-floral morphology of the plant) and other intrinsic traits including those related to photosynthesis and the genome have received less attention than floral traits (Fig. 2). However, contrary to our expectations, they were more consistently associated with trait-dependent diversification than reproductive traits.

Unfortunately we could say little about which state was advantageous for a given trait because a lack of overlap among states across the 152 studies. Nevertheless we were able to examine how particular states affected diversification in eight traits (Fig. ??). Five of these demonstrated how different states of the same trait (e.g. woody and herbaceous species) can increase diversification in different groups (Fig. ??) meaning that only three showed consistent patterns where one state was associated with elevated diversification rates (epiphytism, non-C3 photosynthesis and self-incompatibility). However it is difficult to say whether these are ‘universal drivers’ as they have only been investigated a handful of times (eight or fewer) in a relatively small proportion of angiosperm species.

~~Even though we have outlined~~ some general patterns in those traits that are more often influencing angiosperm diversification, the overarching trend is that the effect of a trait on diversification depends on where one is looking in the tree of life. Therefore, the main question remains open: what drives differences in diversification among angiosperms? ~~This question has been posed many times, and~~ the fact that it still motivates a wide variety of studies suggests that it’s the complex interplay between trait evolution, biotic interactions and geography that matters. Indeed, geography (range size, biome) has been identified many times as an important factor (Hernández-Hernández & Wiens, 2020; Vamosi et al., 2018), but it is unclear whether this is a cause or a consequence of differences in diversification. Others have suggested that it is not the presence or absence of a trait that determines the evolutionary success of a clade, but rather the capacity to change (Onstein, 2019; Ricklefs & Renner, 1994). This may provide an explanation for the widespread inconsistency observed here, but again, trait diversity could be both a cause and a consequence of species richness. Furthermore, the choice of clades and traits, as well as the quality of the input data, also influence whether or not differences in diversification are detected, and therefore our conclusions.

## Evolutionary scale and context need careful consideration

Users of models of trait-based diversification face an important challenge - choosing the context in which to conduct analyses. In the simplest scenario, where a trait only evolved once in the study clade, it is impossible to separate correlation from causation (Maddison & FitzJohn, 2015) and thus this type of context should be avoided. At the intermediate scale a trait may have evolved multiple times in closely related species, but there is now a problem akin to phylogenetic pseudoreplication of lineage-specific factors (Read & Nee, 1995). The evolutionary context (i.e. species' genomes, morphology, ecology, or external environments) of closely-related clades is much more similar than distantly-related ones. So, repeated associations between states and rates might not be as independent as we might assume. Broadening the phylogenetic scope of the analysis, by way of either a larger tree, or multiple trees in a meta-analytic framework (Sabath et al., 2016) can help to avoid pseudo-replication.

However, the increased complexity and heterogeneity of processes acting at large phylogenetic scales may also open the door to other issues relating to the heterogeneity of the tree, ~~such as shifts in molecular clock rates (Shafir et al., 2020), that will make it difficult to SSE models to accurately estimate diversification rates. This heterogeneity may also be behind why larger, older trees more commonly yield trait-dependent diversification (Fig. 4).~~ Trees with many taxa are more likely to contain a range of branching patterns where lineage accumulation is faster in some parts of the tree than in others. In older clades there has been more time for macroevolutionary processes to have an impact on the trees we infer and the traits we observe today. ~~However,~~ this would also make them more susceptible to false-positive errors that could over-inflate the number of times trait-dependent diversification is detected (Rabosky & Goldberg, 2015). Indeed, one of the major criticisms of early SSE models was the propensity to infer false positives due to model inadequacy: the models were based on the assumption that only the trait of interest would influence diversification, so any kind of heterogeneity would lead to the rejection of the null hypothesis (Maddison & FitzJohn, 2015; Rabosky & Goldberg, 2015). This could be a potential explanation for the inconsistency of the effects of traits across clades - it may be that false positives caused by lineage-specific factors correlated with the shared focal trait are driving the disparate patterns. Models with hidden states go some way towards alleviating this issue as they can account for lineage-specific factors. When only considering results from models with hidden states we found that the proportion of trait-dependent diversification changed substantially for



some traits—though inconsistency was still common (Figs. 2,??) though more studies using hidden states are needed to uncover robust, general trends. While hidden states certainly are an improvement, models like HiSSE assume that these states are categorical and have constant transition rates, which very likely doesn't capture all sources of heterogeneity; there has yet to be a study that assesses the model adequacy of HiSSE, as has been done for BiSSE (Rabosky & Goldberg, 2015).

## Best practices for SSE model use and result reporting


Though a number of recommendations have been made on the requirements for accurate inference with SSE models, most empirical studies do not meet them. When using strict thresholds (25% taxon sampling, 300 tips and minor tip state frequency of 10%) we find that just 20 studies contain models that meet all criteria. The apparent relationship between sampling fraction and inference of trait-dependent diversification (Fig 4) might suggest that studies with low sampling fraction are leading to more false positives. If we assume that better sampled trees yield more accurate estimates of diversification rates (Chang et al., 2020; FitzJohn et al., 2009) then we should take caution when interpreting results from trees with lower sampling fraction, particularly when trait-dependent diversification is inferred. However, publication bias may also be playing a role. If no trait-dependent diversification is detected in a poorly sampled clade this may be attributed to a lack of power that ultimately prevents publication, thereby inflating the number of studies with low sampling that detect trait-dependent diversification. Regardless, simulation studies should be undertaken to investigate the influence of sampling fraction on SSE models and whether false positives occur more often when sampling fraction is low.


In most studies, some of the information we consider crucial for the interpretation of the results was lacking, or it was difficult to access. Collecting data for many properties (e.g. samples per state) required us to count from figures or extract statistics from archived raw data, which were not always freely available.

For example, we were unable to extract and use the number of independent origins of each character state. Robust estimates of associations between traits and diversification rates necessitate multiple independent origins (but not too many (Rabosky & Goldberg, 2015)) and corresponding rate changes (FitzJohn et al., 2009), so an idea of this value per study, inferred using ancestral state reconstructions, would be useful for interpretation of the robustness of

results. This could be done by combining stochastic mapping of traits with an SSE model (Freyman & Höhna, 2019), though this is generally not available for SSE approaches. Likewise, diversification and transition rates were often not reported in an easily-accessible and standardized manner, or in some cases, not at all. These should be reported, and if possible, with confidence metrics around rate estimates e.g. Bayesian credible intervals.

Louca & Pennell (~~Louca & Pennell~~, 2020a) recently pointed out how diversification rate estimation can be susceptible to issues of unidentifiability.

Though  models are not directly implicated (Helmstetter et al., 2021), one potential way to help ‘future proof’ analyses from unidentifiability caused by overfitting would be to avoid reporting and assessing speciation and extinction rates separately, focusing instead on compound parameters such as net diversification rate ( $\lambda - \mu$ ), turnover rate ( $\lambda + \mu$ ) and extinction fraction ( $\mu/\lambda$ ) that are typically used in more recent SSE models (e.g. HiSSE). To encourage standardized result reporting we propose an initial set of characteristics that should be made available in all future studies using SSE models (Supplementary Data 1).

~~As we argue above,~~ evolutionary context appears to be important for understanding trait-dependent diversification. ~~So~~ how to best choose a trait  clade to study? In terms of choosing a clade, it is first important to adhere, as best as possible, to the recommendations for using SSE models e.g. avoid clades much smaller than 300 taxa and focus on those that are well sampled (>25%). Trait choice can be helped by preliminary knowledge of the phylogenetic tree and ancestral state reconstruction, which could be used to ensure that the derived state(s) arose multiple times and that the ratio among different states is not extreme (<10:1). If recommendations cannot be followed, because of natural limitations in clade size, for example, these should be stated clearly as caveats.

Working at a much larger scale, e.g. angiosperm-level analyses, is certainly appealing but creates a range of issues related to confounding factors that current models will find difficult to disentangle. To better learn about the factors that influence angiosperm diversity we therefore suggest a focus on intermediate-sized clades i.e. large genera, families or tractable orders. However, if these clades are well-sampled they would approach the limit of our current computational feasibility (but see Louca and Pennell, 2020b). Working with many smaller clades may therefore be more feasible in the near future and also yield important insights via the comparison of diversification patterns among many different groups (e.g. Sabath et al., 2016), which we think is an

acceptable tradeoff for reduced power in standalone analyses. Examining the effect of the same trait in multiple clades would allow researchers to account for the unique and shared aspects of their biology (e.g. through the use of hidden states or trait combinations), and then to combine results (Rabosky & Goldberg, 2015) to uncover general patterns.

## Knowledge gaps and future avenues

Our review allowed us to identify groups that are understudied and therefore good focal points for future research to gain more well-rounded picture of angiosperm macroevolutionary dynamics. One of the most obvious is Asteraceae, species-rich yet subject to relatively few trait-based diversification studies (Fig. ??), or Alismatales, an order that has more than 4,500 species (Fig. ??) but just a single study on their trait-based diversification (Canal et al., 2019). In addition, some families with more than 1,000 species, such as Phyllanthaceae or Orobanchaceae have yet to be studied in this way.

High-quality phylogenetic trees are not the only ingredient for SSE studies; trait data also need to be available. We highlight traits related to lifespan, dispersal and symbiosis as ripe avenues for future work that have potential to unearth important patterns in trait-dependent diversification. However, apart from a few traits such as geographical range or climatic preferences, gathering high-quality data for large numbers of species is a time-consuming activity. We encourage the integration of trait data generated from SSE studies (and others) into large, global trait databases such as eFLOWER (Sauquet et al., 2017), TRY (Kattge et al., 2020) or more focused databases e.g. AusTraits (Falster et al., 2021). These will act as important resources as researchers consider several traits in tandem when testing for context-dependent effects of traits, or when disentangling the traits hiding in the hidden-state approaches.

By definition, macroevolutionary models try to capture the result of many aggregated small-scale processes in a few high-level parameters. Just consider speciation, which is an instantaneous split of one branch into two in most macroevolutionary models, although in reality there might be a wide range of different dynamics depending on environmental heterogeneity, biotic interactions, and intrinsic traits (e.g. breeding systems, genomic incompatibilities) (Coyne et al., 2004). Thus, if a trait is predicted to affect speciation and extinction it is through various ecological and genetic processes that can also be put to the test. For example, Park et al. 2018 compared sister species with contrasted mating systems (selfing vs. outcrossing) and showed that niche breadth

tended to decline over time in selfing lineages, in agreement with the dead-end scenario proposed for this trait and detected in macroevolutionary analyses (Goldberg & Igić, 2012; Höhna et al., 2019). Additionally, we can identify traits that have an effect on ecological and genetic mechanisms that control speciation and extinction, such as traits affecting coexistence and niche partitioning (Adler et al., 2013) (e.g. specific leaf area or seed mass), genetic differentiation between populations or species (Gamba & Muchhala, 2020) (e.g. pollination mode, mating system, growth form) or those associated with commonness and rarity (Murray et al., 2002) (e.g. seed production). Such traits could be ideal candidates for macroevolutionary studies exploring their effect on diversification and provide *a priori* hypotheses.

## Conclusions

When bringing together the last 12 years of study on trait-dependent diversification in angiosperms, it is the inconsistent effects of traits that stand out, rather than the importance of a particular set of universal drivers. This points towards an important role for the evolutionary context of a clade in determining how a particular trait affects diversification. Furthermore, the nature of the data itself, relating to factors such as how well-sampled or large a clade is, was shown to have a greater influence on practical SSE model use than previously thought. The guidelines we set out in this review will help to improve how we use trait-dependent models and our template for reporting results will facilitate future synthesis as SSE models continue to be used and developed. We have only touched the surface of what we can learn about trait-dependent diversification in angiosperms. Will results from novel studies change the trends we observe here? Given the production of new datasets that meet recommendations for robust inference, future methodological developments enabling studies at wider scopes and the potential for new discoveries in understudied traits and clades, we think it is certainly possible. Though our study focused on angiosperms the conclusions we draw about consistency, context dependence and SSE model use will apply to studies of trait-dependent diversification across the entire tree of life.

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## Supplementary Material

Code associated with this manuscript is available from <http://github.com/ajhelmstetter/ss> eReview. PapieRmache can be found at <http://github.com/ajhelmstetter/papieRmache>.

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