

# Introduction To Machine Learning

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# Learning Outcomes

- Be able to analyze learning algorithms using theoretical ideas such as estimation and approximation errors and bias-variance decomposition
- Know the main algorithms for learning, such as decision tree, random forest, and SVM
- Understand some methods for data that is big in number and dimension

# Topics

- How Learning Works + Basic Algorithms
- Estimation Error + Linear SVM
- Approximation Error + Kernel SVM
- Other Theoretical Ideas
- Improving Performance + Random Forest

# Formalizing a Decidable Situation

- It must be fully represented as an object in some **feature space  $X$**
- $X$  is usually a vector space—an object is a vector of  $D$  **features**
- E.g. how to detect free riders in online team games?
  - Use the number of met enemies and the % of explored game space as features
  - A player who met 0 enemies and explored < 5% of the game space is a free rider

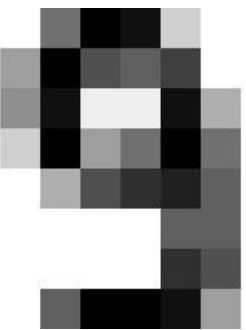
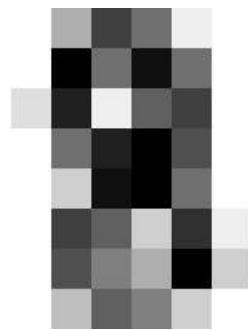
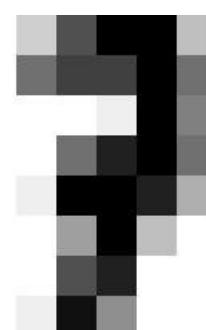
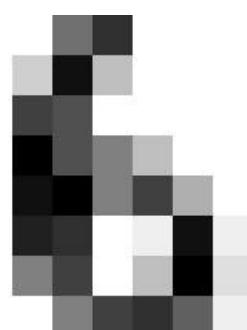
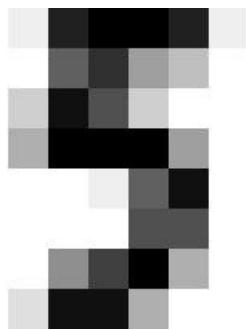
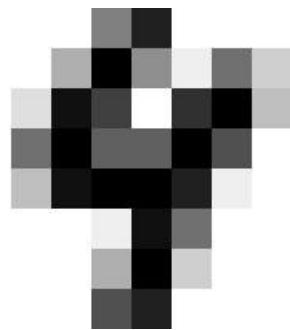
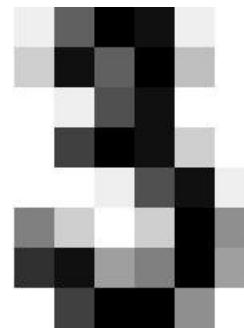
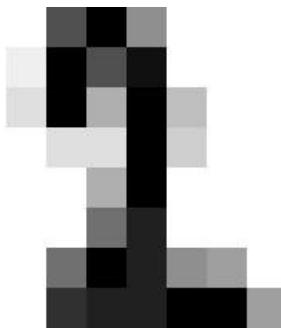
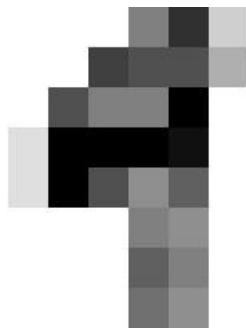
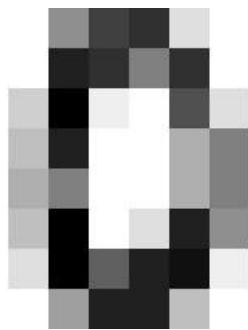
# Automatic Learning

- Nature generates data—can never know the true model
- Want **predictor**  $f$  that decides correctly in specific situations
- So pick a surrogate model and fit it to the data
- The data set  $S = n$  examples  $z_i$
- Data reduces uncertainty in the surrogate model
  - Never know it exactly

# Classification

- $\forall z_i$  have  $x_i$  and **class label**  $y_i \in [0, k - 1]$ .
- A **loss function**  $L_f(z) = L_f(x, y)$  measures error of  $f$  on  $z$ .
  - Binary loss—right decisions have profit 0 and wrong ones cost 1.
- **Risk**  $R_f(P) = E_z[L_f(z)]$  measures generalization error of  $f$ .
  - For binary loss,  $R_f = E[\text{the \% of misclassified } z]$

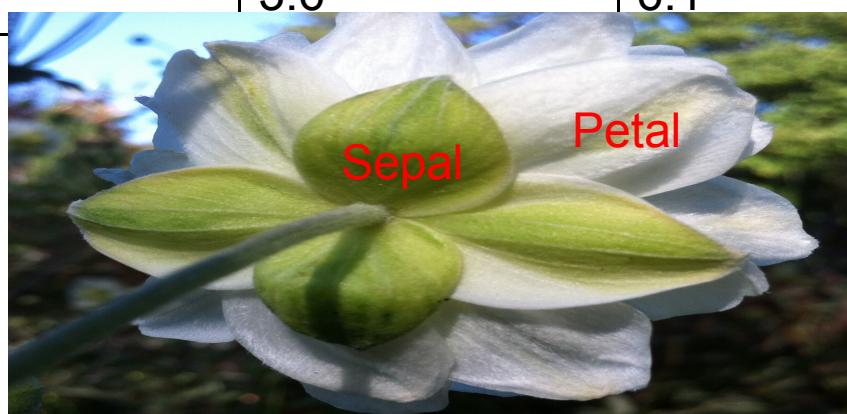
# Digit Data



# Iris Data

- Iris leaf measurements—want to decide what type of iris it is.

Type	Sepal Length	Sepal Width	Petal Length	Petal Width
Setosa	5.1	3.5	1.4	0.2
Setosa	5.4	3.9	1.7	0.4
Versicolor	6.4	3.2	4.5	1.5
Versicolor	5.6	2.9	3.6	1.3
Virginica	6.2	3.4	5.4	2.3
Virginica	7.2	3.6	6.1	2.5

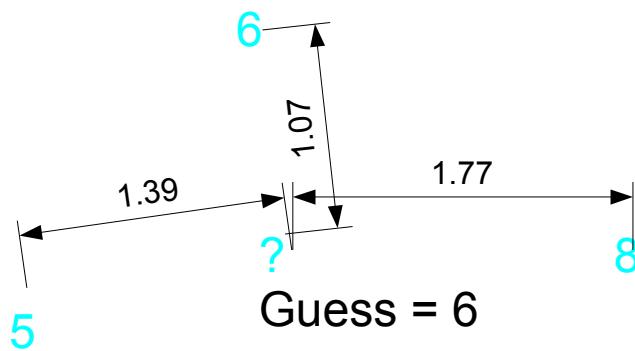


# Data Preparation and Cleaning

- Data may have **missing values**
  - Delete examples or features
- May not be **numerical**
  - Convert each **categorical** value into 0/1 vector, increasing  $D$
- Some algorithms like **normalized scale**
  - $\forall$  feature make range  $[0, 1]$
  - Or mean 0 and variance 1
- Remove useless features like record id
  - Infamous—spot a military tank from sky color

# Nearest Neighbor Model

- Need an appropriate distance function for the problem and/or to scale features
  - E.g. Euclidean distance in age-height space doesn't mean much, so scale first
- To train, create an efficient index (usually **vantage point tree**) from the examples
- To predict, return the class of the closest example

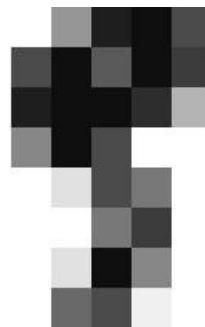


# Evaluating Performance

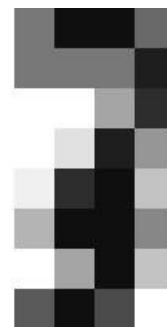
- Estimate  $R_f$  by **empirical risk**  $R_{f,n} = (\sum L_f(z_i))/n$ .
- **Accuracy** =  $1 - R_{f,n}$
- NN gets  $\approx 98\%$  accuracy on the digit data

# Some NN Mistakes on Digit Data

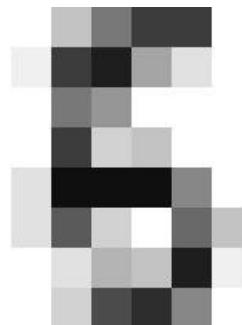
Inferred: 5. Actual: 9



Inferred: 7. Actual: 3



Inferred: 6. Actual: 5



# Is Accuracy Accurate?

- **Hoeffding inequality** for  $L \in [0, 1]$ :
  - Let  $e(p) = \sqrt{\ln(1/p)/(2n)}$
  - Then with probability  $\geq 1 - p$ :
    - Upper bound:  $X \leq m + e$
    - *Lower bound*:  $X \geq m - e$
    - *Confidence interval*:  $X \in m \pm e(p/2)$
- Digits test set has  $n = 1798$ , so with 95% probability have  $0.98 \pm 0.032$
- Works for separate iid test set only

# General Problem

- Can't have 100% accuracy with 100% probability
- Ok for many applications, but not for others
- E.g. data-trained self-driving car can never be perfectly safe

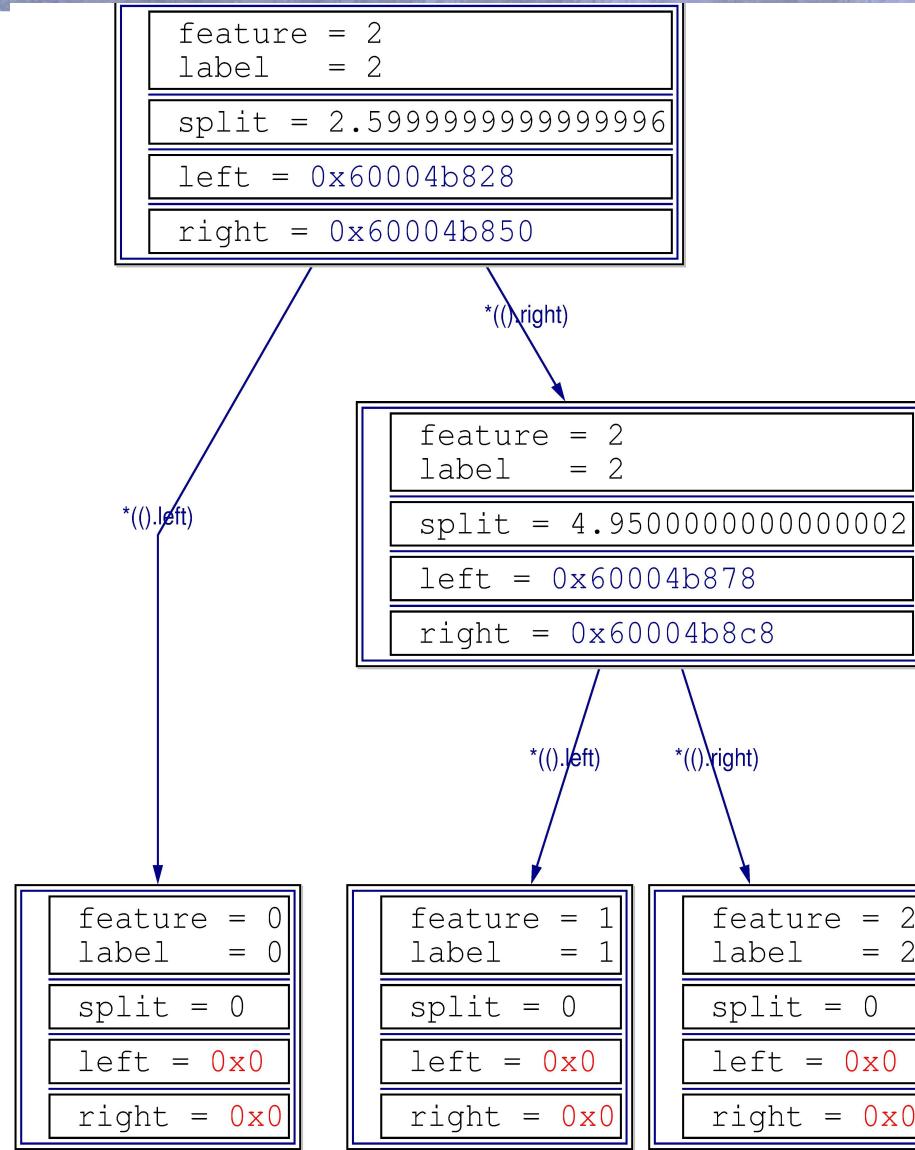
# Problems with NN

- Poor accuracy on most data sets despite good results on digits
- Inefficient
  - $O(n)$  memory
  - Index query needs  $\approx O(n)$  time for large  $D$
- No explanation of decisions
  - E.g. credit denied because you look like a family from 10 years ago who defaulted

# Decision Tree

- Binary tree
- An internal node look at values of a specific feature to decide which branch to take
- A leaf gives the resulting class

# Decision Tree for Iris



# Creating a Decision Tree

- Find best split
- Split data based on it into left and right parts
- Recurse until get a pure node or exceed some depth  $m$  (50?)
- **Prune** to not overfit
- Can explain decisions
- $\approx 87\%$  on Iris and  $\approx 84\%$  on digits

# Picking Split Feature and Value

- For  $S$ , **entropy** of labels =  $\sum H(p_i)$ 
  - $H(p) = -\lg(p)$ , and  $p_i$  = % of examples of class  $i$
- Want a split that minimizes the total entropy after splitting:
  - $\#$  left child examples  $\times$  entropy(left) +  $\#$  right child examples  $\times$  entropy(right)
- I.e. pick a split that gains most information
- Calculate splits incrementally in a linear pass

# Sign Test Pruning

- Subtree must be better than its root to not be pruned
- Test idea: given two players, one is better if wins significantly more than  $\frac{1}{2}$  of all games, including draws.
  - Modeled as  $\text{binomial}(\# \text{games}/2, \# \text{ games})$ , can approximate by normal
  - $z \text{ score} = (n\text{Wins} - n\text{Games}/2) / \sqrt{n\text{Games}/4}$
- Significantly better only if  $z$  of best subtree's performance  $> 1 \text{ std}$  (not the usual 2)

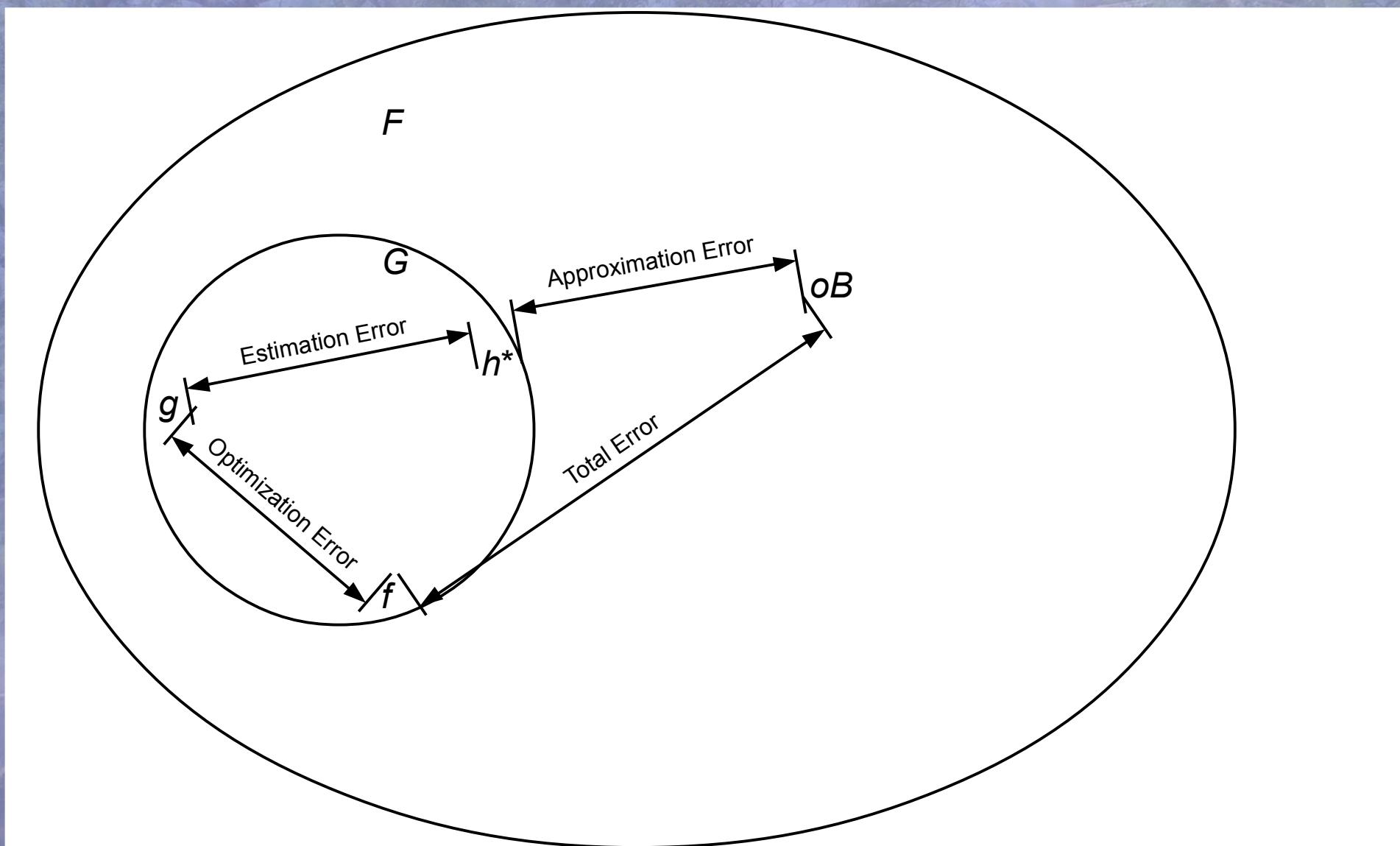
# Topics

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- Other Theoretical Ideas
- Improving Performance + Random Forest

# Is There the Best Model?

- Yes—**optimal Bayes** (oB)
- Assume that know the distribution of  $y|x$
- But still  $R_{\text{oB}}$  need not be 0
  - E.g., if have a coin that comes up heads 90% of the time,  $R_{\text{oB}} = 10\%$  by always predicting heads
- Don't know oB in practice—purely theoretical ideal

# Error Decomposition

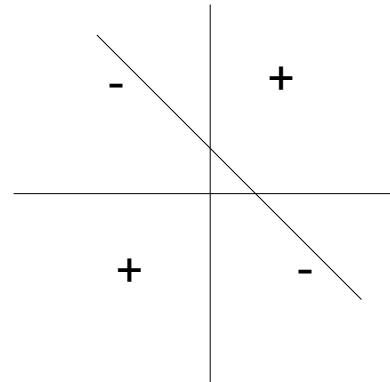
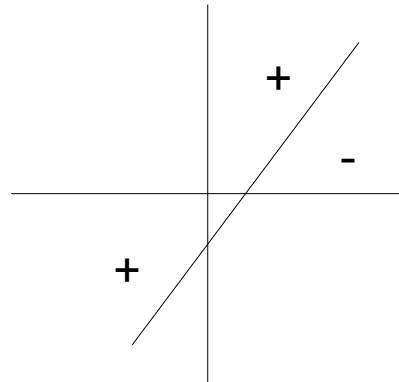


# Error Decomposition

- $R_f \leq$  sum of:
  - **feature informativeness error**  $R_{\text{oB}}$ , due to not having informative features
  - **approximation error**  $\min_{h \in G} R_h - R_{\text{oB}}$ , due to not using the best  $G$
  - **estimation error**  $R_g - \min_{h \in G} R_h$ , for  $g = \operatorname{argmin}_{h \in G} \text{SearchObjective}(h, n)$ , due to not knowing  $X$
  - **optimization error**  $R_f - R_g$ , for  $f = \operatorname{approx} \operatorname{argmin}_{h \in G} \text{SearchObjective}(h, n)$ , due to optimizing approximately

# VC-dimension for Binary Classifiers

- Max  $d$  such that  $\exists d$   $x$  arranged such that  $\forall$  assignment of binary labels to them,  $\exists f \in G$  that can separate them
- E.g. a line can separate any 3 points in 2D, but not 4 points, so for 2D lines  $d = 3$



# Using VC-dimension

- Theorem: with probability  $\geq 1 - p$ ,  $R_f \leq R_{f,n} + \sqrt{2d\ln(en/d)/n} + \sqrt{-\ln(p)/(2n)}$
- Some conclusions:
  - If  $n/d \rightarrow \infty$  as  $n \rightarrow \infty$ ,  $R_{f,n} \rightarrow R_f$
  - For hyperplanes  $d = D + 1$ , so can overfit for  $D \approx n$
  - The bounds are usually loose, but still conceptually useful

# Using VC-dimension

- For  $k = 2$ :
  - VC-dimension of a tree is the number of leaves
    - Getting a tree with  $d$  leaves means that with 95% probability have complexity term  $\approx \sqrt{d \ln(2\epsilon n/d)/n} + \sqrt{1.5/n}$
  - Justifies pruning—give up training accuracy to reduce complexity and overall risk
  - Try to restrict parameters to make  $d$  smaller, e.g. for sin functions VC-dimension =  $\infty$

# General Estimation Error Control

- For some  $G$  have a **finite sample** estimator of  $R_f$ , such as the VC-dimension-based one
- I.e.  $\forall f \in G |R_f - R_{f,n}| \leq B(n, f, p)$  with probability  $\geq 1 - p$ , such that  $\forall \epsilon > 0$  and  $p > 0$ ,  $\exists n(\epsilon, f, p)$  such that  $B \leq \epsilon$  (**PAC** property)
- If  $B$  is the same  $\forall f$ ,  $G$  has **uniform convergence**
  - $B(n, f, p) = B(n, C(G), p)$ , where  $C$  measures of  $G$ 's **capacity to overfit**
- Won't overfit much no matter what  $f$  pick from  $G$

# General Estimation Error Control

- Heuristic C is the number of parameters to be estimated
- E.g. given  $n$  credit card and phone numbers, can construct a polynomial that predicts card number from phone number
  - Doesn't work if restrict the degree of polynomial to a constant  $< n$
- Restricting  $G$  prevents estimation error by excluding  $f$  capable of accurately modeling noise in  $S$

# Empirical Risk Minimization

- Use  $R_{f,n}$  as search objective to fit model on training data
- If  $G$  has uniform convergence,  $B$  is the same  $\forall f \in G$ , so the found one will have a finite sample estimation error bound
- Problem:
  - Need small  $C$  or very large  $n$  to get small  $B$
  - So only useful only for some parametric models such as linear regression, and not for decision tree

# Structural Risk Minimization

- For  $G$  with a finite sample estimator, use search objective =  $R_{f,n} + B(n, f, p)$
- Look at simpler models first
- Stop when for the best found  $f$  and all  $h$  not yet considered  $R_{f,n} + B(n, f, p) \leq B(n, h, p)$
- The solution will have a finite sample bound
- E.g., to prune a decision tree greedily fold least accurate leaf pair while the SRM objective improves

# Occam Risk Minimization

- Let  $G = \cup H_i$  and assume  $H_i$  consists of a single hypothesis  $h$ , and for corresponding  $w_i \in [0, 1]$  let  $\sum w_i \leq 1$
- Then  $R_f \leq R_{f,n} + \sqrt{(\ln(1/w_i) + \ln(2/p))/(2n)}$  with probability  $\geq 1 - p$  (by Hoeffding and Bonferroni)
- Let every  $h$  be represented in binary using some code, such as gamma, and  $w_i = 2^{-|h|}$
- $f = \operatorname{argmin}_{h \in G} (R_{h,n} + \sqrt{(|h| \ln(2) + \ln(2/p))/(2n)})$

# ORM for Decision Tree

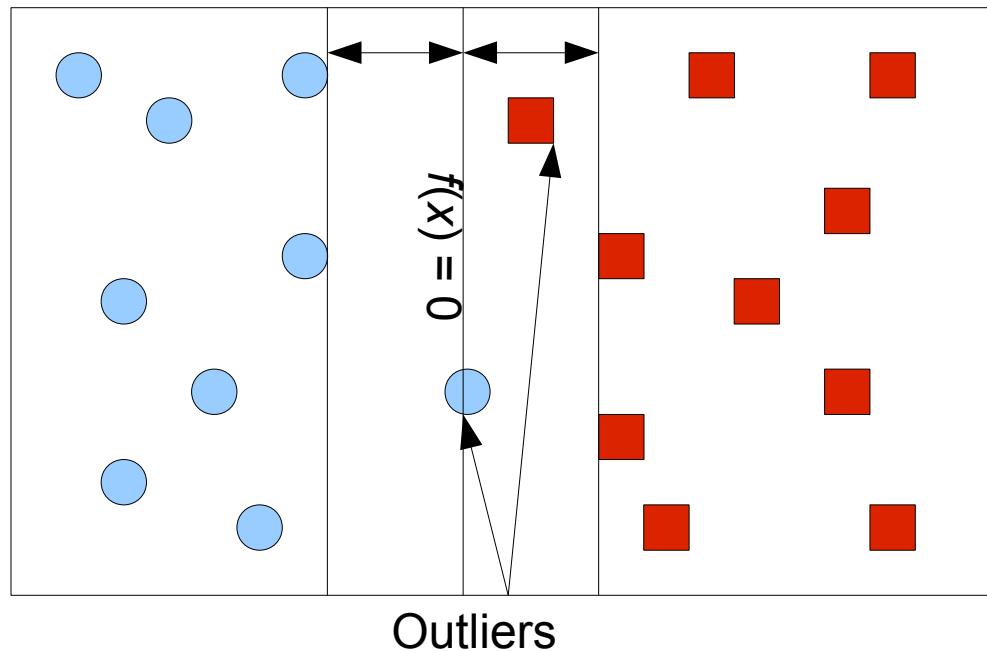
- Structure—2 bits per node, i.e. using DFS to write node, then 1 bit for left child, and 1 bit for the right
- Feature id needs  $\lceil \lg(D) \rceil$  bits, and label  $\lceil \lg(k) \rceil$
- Split point—scale data into  $[0, 1]$ , and represent to precision 0.001, so  $\approx 10$  bits
- With  $m/2$  internal nodes and  $m/2 + 1$  leaves,  $|h| \approx m(10 + \lg(kD)/2)$
- With  $p = 0.05$ , complexity term =  $\sqrt{(|h| \ln(2) + \ln(40))/n}$

# ORM

- Very general—applies  $\forall$  task with bounded  $L$ , not just classification with  $k = 2$ , and it's usually easy to define and search a suitable  $G$
- **Occam razor**—don't make things more complex than needed
- Seems like the ultimate induction principle, but complexity bounds are very loose
  - Hoeffding okay; Bonferroni very loose
- Mostly of conceptual value in practice, but don't increase complexity without need

# Linear SVM

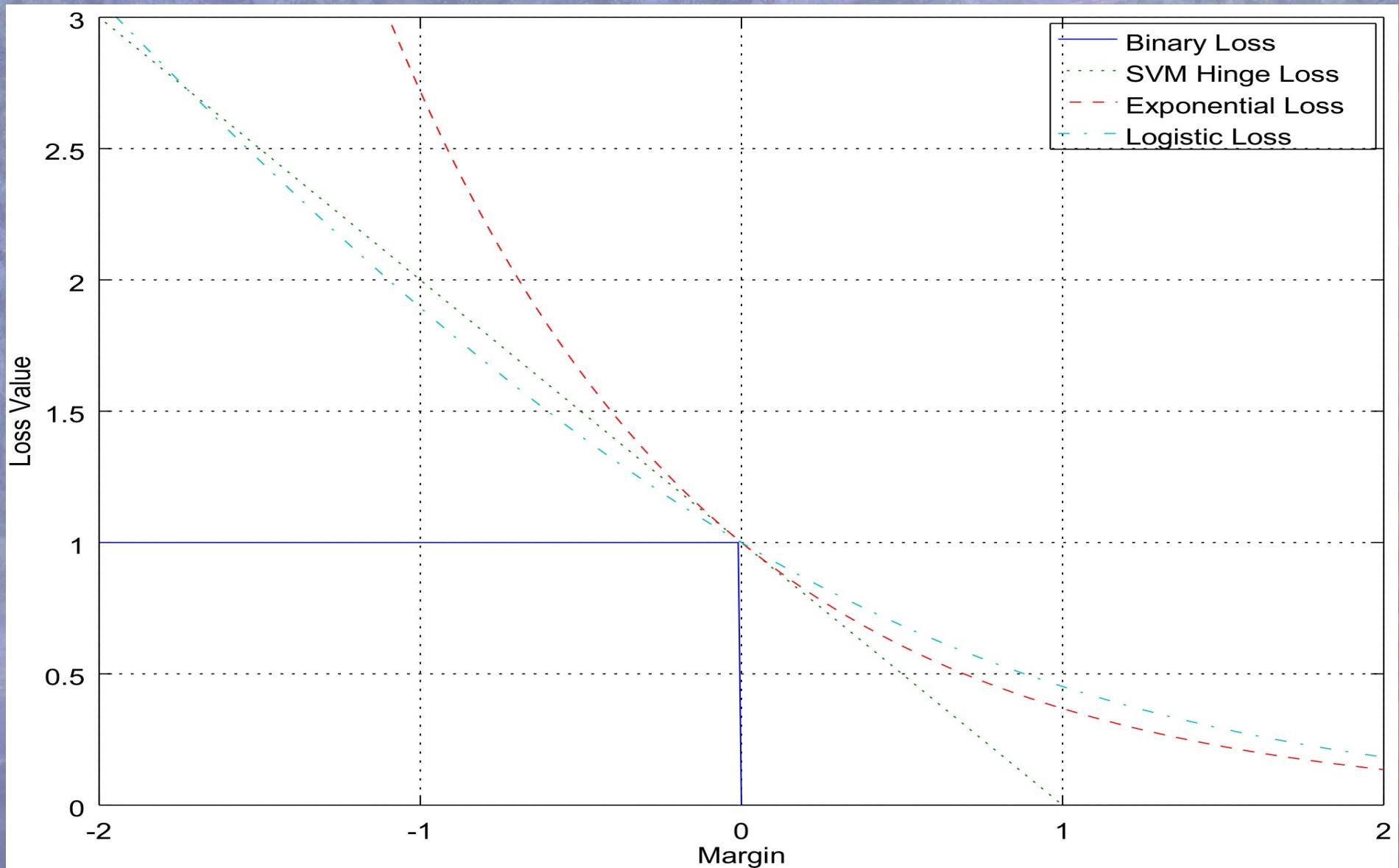
- Given two classes, compute a linear separator  $f(x) = wx + b$  with **maximum margins**
- Put a linear penalty on outsize-of-margin examples—similar to SRM



# Margin

- Distance of patches of examples of a particular class to the partition boundaries
- When walking in a minefield, walk between mines and not close to any of them
- The larger the margin, the more certain is the partition
- A very complex  $f$  can have small margins
  - Much smaller risk bounds than from complexity bounds

# Hinge Loss



# Linear SVM

$$\min \frac{1}{2}w^2 + C\sum e_i \text{ subject to } //\text{margin} + \sum \text{bounds}$$

$$y_i f(x_i) \geq 1 - e_i \quad //\text{loss} + 1 \leq \text{bound}$$

$$e_i \geq 0$$

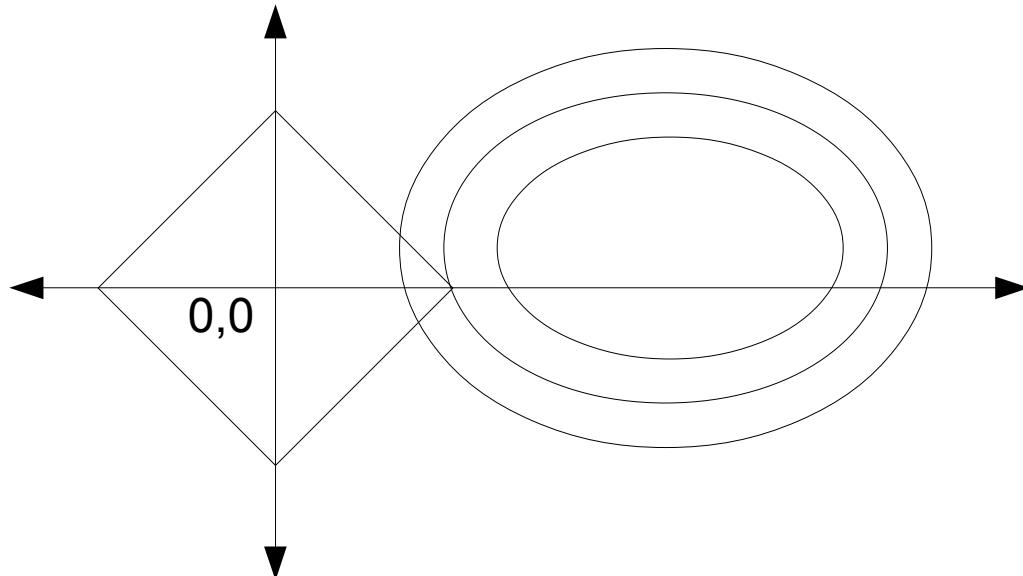
- Constant  $C > 0$  defines trade-off between margin size and accuracy
- Can bound  $d$  as a function of margin and radius of the data's enclosing hypersphere

# Linear SVM and Sparsity

- Most useful for large  $n$  and  $D$ , so use  **$L_1$  weight size penalty** instead
- Solve equivalent unconstrained problem  
$$\min \frac{1}{2} \|w\|^2 + \sum \max(0, 1 - y_i f(x_i))$$
 with  $\lambda = 1/C$
- This is convex nondifferentiable optimization problem
- $L_1$  penalty leads to a **sparse solution**, with many  $w_i = 0$

# SVM Sparsity

- In the equivalent constrained problem, the feasible region contains cusps that correspond to some variables = 0
- One of them is likely to attain the best feasible level set:

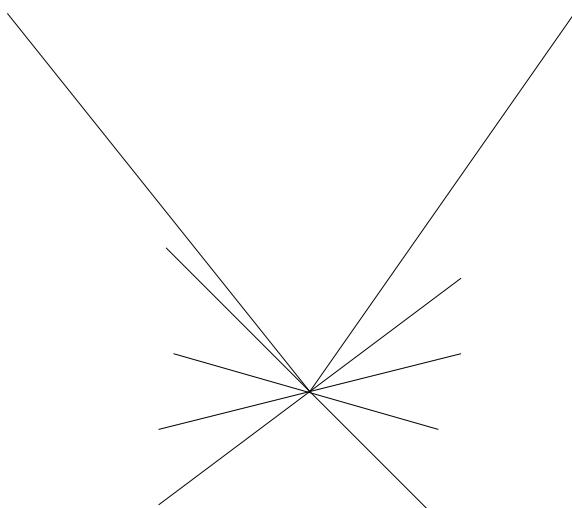


# Solving—Stochastic Gradient Descent

- Starting from any initial solution, take a step of some size  $s$  into the  $-\text{direction}$  of  $\mathbb{E}[\text{gradient}]$
- Repeat until converge, adjusting  $s$
- **Robbins-Munro conditions**—for a convex problem SGD converges if:
  - $\sum_{0 \leq i \leq \infty} s_i = \infty$  —must be able to walk far enough
  - $\sum_{0 \leq i \leq \infty} s_i^2 < \infty$  —can't diverge

# Subgradients

- Linear SVM objective not differentiable—no gradients, so use subgradients
- In 2D, a subgradient is any tangent line to the cusp
- Slow  $O(1/\sqrt{n})$  convergence, but good for generalization



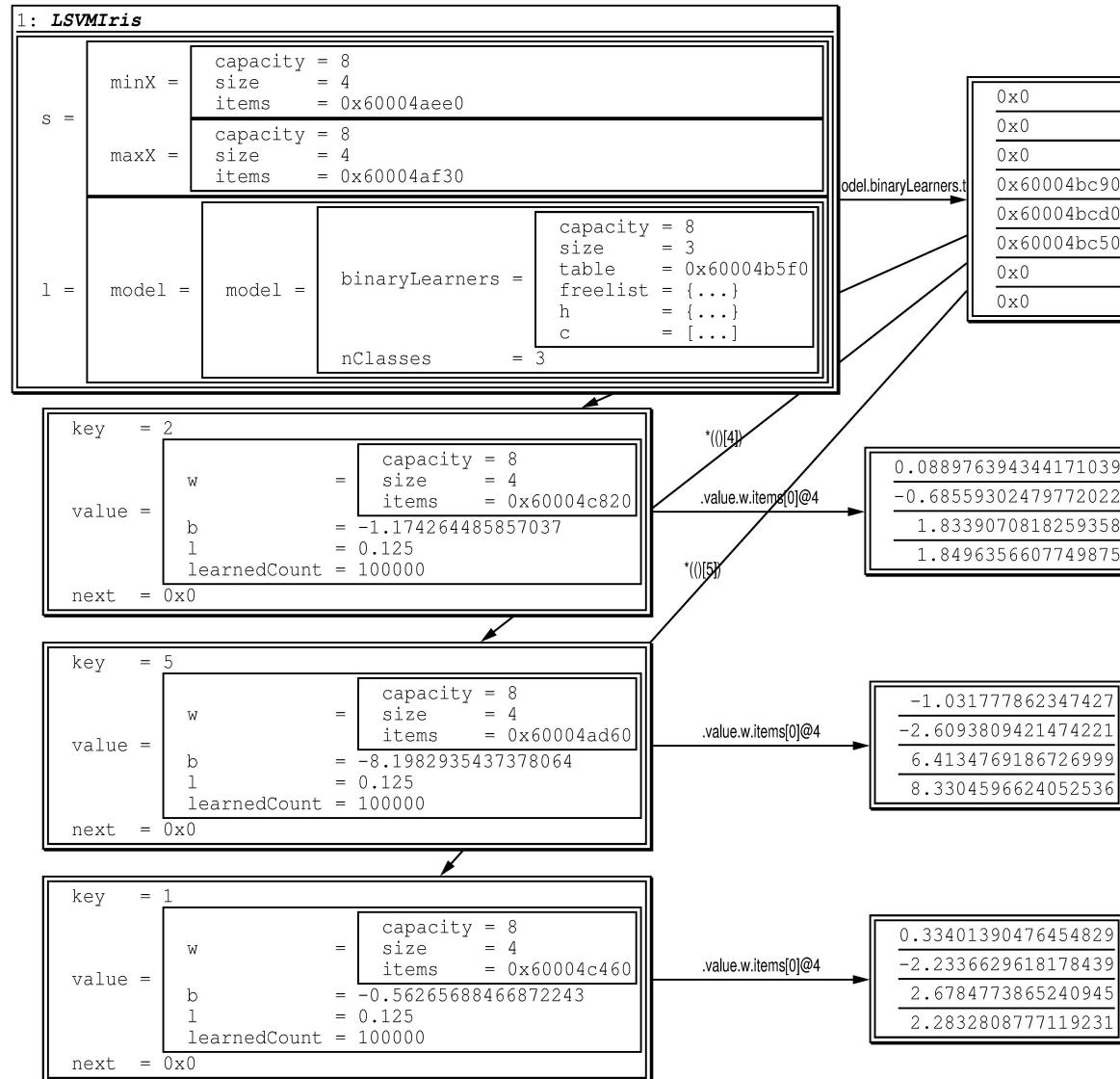
# Solving Linear SVM with SGD

- Need expression whose expected value is a subgradient of the function, calculated from a single example
- For a given  $l$ , start with 0's and update:
  - $\forall 0 \leq j \leq D, w_{ij} := s_i(w_{ij} > 0 ? 1 : -1)l - n(y_i f(x_i) > 1 ? 0 : y_i x_i))$
  - $b += s_i(y_i f(x_i) > 1 ? 0 : y_i)$
- To be disk-friendly, make  $\lceil 10^5/n \rceil$  passes over the data instead of using random examples

# Linear SVM for Many Classes

- Break up a multiclass problem into two-class problems using **one vs one** (OVO) decomposition
  - For  $k$  classes, train  $O(k^2)$  learners for all combinations of binary classifiers
  - For prediction, choose the class with the most votes
- Some good properties – simplicity, asymptotic efficiency for a superlinear binary learner  $A$ , and the lowest approximation error among alternatives

# Linear SVM for Iris



# Tuning Parameters

- How to pick  $\gamma$  for linear SVM?
- Theoretical—use SRM or equivalent, but problem with loose bounds
  - N/A here; ORM suggestion 0 bad
- Old-fashioned—have a statistician look at the problem and figure out the answer by common sense—costly, slow, and doesn't scale
- Practical—use **cross-validation**, works well almost always

# Cross-validation for Estimating Performance

- Partition the data into  $k$  equal subsets
- $k$  times train  $A$  on  $k - 1$  subsets and test on the remaining one
- Return average risk as performance estimate

Fold	Data Use				
1	Train	Train	Train	Train	Test
2	Train	Train	Train	Test	Train
3	Train	Train	Test	Train	Train
4	Train	Test	Train	Train	Train
5	Test	Train	Train	Train	Train

# Cross-Validation

- Can't estimate variance of the risk estimate
- The estimate is usually very good for picking parameters, but not for predicting the risk of A
- Sources of variance:
  - A itself may be randomized
  - Using different data or its order can give different answer—**stratification helps**
  - Fold results are dependent because training data overlaps

# Picking Continuous Parameters

- Cross-validation works for discrete sets
- **Grid search**—from very small min to very large max, step by a factor of 4
  - Min and max need domain knowledge, but conservative generic choices can do well
- Usually the method of choice, feasible for  $\leq 3$  parameters
- For more no clearly good method, but **random search** shows some promise

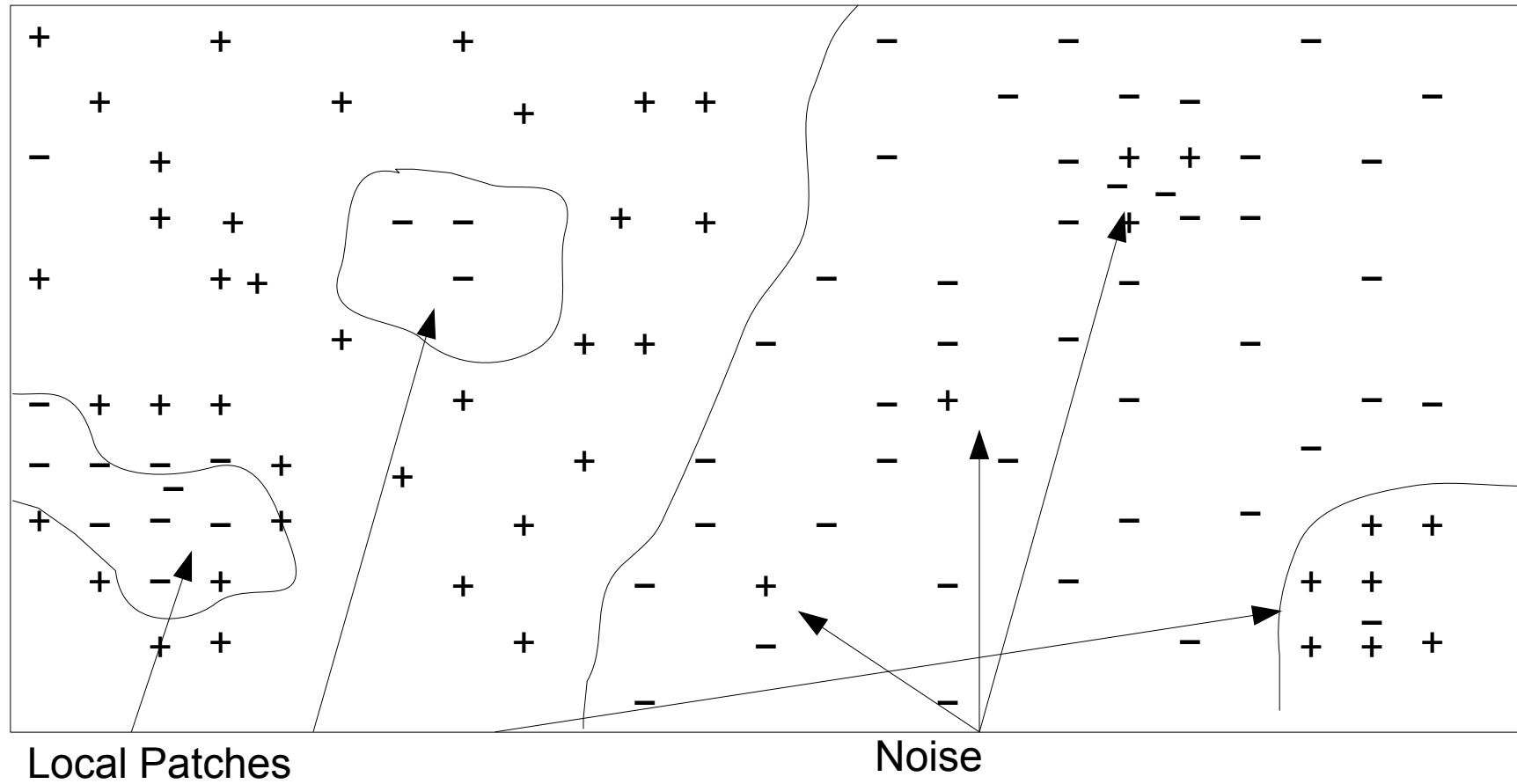
# Big Data

- Large  $n$ , sometimes  $D$ , **that's it**
- Need scalable  $A$ —linear SVM will do
- More data than is needed for good estimation error control – can do a single SGD pass
- **Incremental SGD**—go through examples in a disk-friendly way
- May want to randomly permute—reduces to sorting, which is I/O-fast
- Lots of research on parallelizable and online  $A$

# Topics

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# Approximation Error



# Approximation Error

- For many problems no fixed  $G$  can represent the oB partition
- The latter for a particular problem may be **arbitrarily complex**
- So need arbitrarily many examples to express
- Some examples seem to be **outliers** because it can be hard to distinguish **label noise** (some  $y_i$  are wrong) from valid information
- **Local patches** of  $X$  can have different behavior

# Approximation Error

- At best can approximate the oB partition using something like Stone-Weierstrass theorem
- So usually pick most expressive  $G$  where have satisfactory control of estimation error
- Unlike for estimation error, don't have general finite sample bounds, only asymptotic ones

# Kernels—Improve Linear SVM

- Allow efficiently adding features that are combinations of other features
  - More-complex-than-linear separation—reduce approximation error
- Done by some feature-mapping function  $F$
- A must only use a dot product
  - For linear SVM,  $wx$  becomes  $F(w)F(x) = K(w, x)$
  - $K$  is a **kernel function**, computable directly

# Kernels

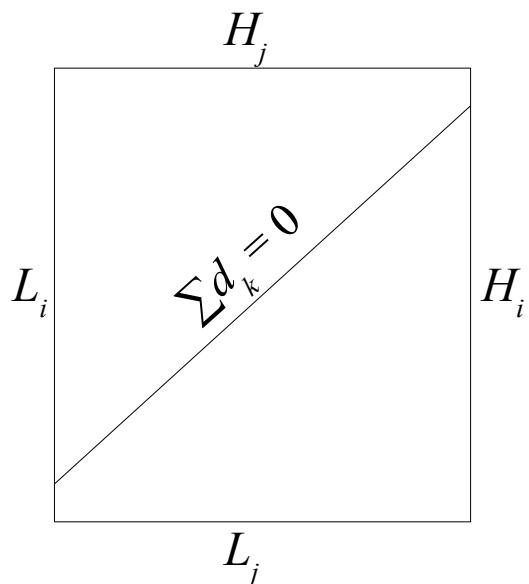
- **Gaussian kernel** is useful for numeric vector  $X$ 
  - $K(x_1, x_2) = \exp(-\|x_1 - x_2\|/\sigma)$ ;  $\sigma$  is width parameter
- Intuitively,  $K$  measures similarity
- Valid iff the all-example  $n \times n$  matrix  $M$  such that  $M[i, j] = K_{ij}$  is **symmetric and positive definite**
- Applies to non-vector data, e.g. can use edit distance between strings to construct  $K$

# Kernel SVM

- Replace dot product by kernel, in case of Gaussian add  $\sigma$
- Can't represent  $w$  explicitly, so solve the **dual**:
  - $\max \sum y_i d_i - \frac{1}{2} \sum d_i d_j K_{ij}$  subject to
  - $L_i \leq d_i \leq H_i$
  - $\sum d_i = 0$
  - $[L_i, H_i] = [0, C]$  if  $y_i = 1$  and  $[-C, 0]$  otherwise
- **Support vectors** are  $x_i$  for which  $|d_i^*| > 0$
- Given optimal  $d_i^*$ ,  $f(x) = \sum d_i^* K(x_i, x) + b$

# Solving Kernel SVM

- **Quadratic programming problem**, but black-box solvers are too slow and need  $M$  in memory
- **SMO** idea—until convergence greedily pick two variables and optimize on the line in the box:



# Kernel SVM Results

- Good:
  - Can approximate any continuous boundary with Gaussian kernel
  - Similar error bound as for linear SVM
  - One of the best black-box A
- Bad:
  - Performance isn't perfect
  - SMO is still slow
  - Need  $O(n)$  memory for support vectors

# Topics

- How Learning Works + Basic Algorithms
- Estimation Error + Linear SVM
- Approximation Error + Kernel SVM
- Other Theoretical Ideas
- Improving Performance + Random Forest

# Universal Consistency

- $A$  is **consistent** for a problem if  $R_{f(A, n)} \rightarrow R_{\text{oB}}$  as  $n \rightarrow \infty$
- **Universally consistent** if it's consistent  $\forall$  problem
- Intuitively, estimation and approximation errors  $\rightarrow 0$
- $k\text{NN}$ —takes the majority label of  $k$  neighbors
  - Universally consistent if  $k \rightarrow \infty$  and  $k/n \rightarrow 0$
  - E.g.  $k = \ln(n)$  works
- SVM too, with technical conditions
  - E.g. parameter optimization must not fail

# No Free Lunch—Popular Version

- $\exists$  problems where finite training data is harmful and not helpful, so that over all problems no  $A$  wins
  - Doesn't contradict universal consistency, which is asymptotic
  - Over all problems, learning is impossible
  - $A$  that win on some problems, must lose on others

# Interpretations of NFL

- **Pessimism**—solve only nice problems, use as much domain knowledge as possible, and don't trust performance comparisons
- **Optimism**—NFL is nonsense because nobody wants to solve problems where training data is harmful.
- **Realism(?)**—different problems favor different assumptions
  - E.g. digits are well-linearly-separable, but other data isn't

# NFL—Devroye Version

- $\forall A$  that uses  $n$  examples for learning  $f$  and  $\epsilon > 0$ ,  $\exists$  a problem with  $R_{\text{oB}} = 0$  such that  $R_f \geq \frac{1}{2} + \epsilon$
- Some problems need arbitrarily many examples
  - No finite sample approximation error control
- No  $A$  is best in all cases because for one that is bad for some problem another may do well
  - But some can be best in most practical cases

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# Bias-variance Decomposition

- **Bias**—preference for certain functional relationships over others due to prior knowledge
  - Unlike approximation error, takes into account all decisions
  - E.g. optimization error in using local search
- **Variance** – producing different  $f$  from different random  $S$  of same size due to not being able to estimate parameters exactly
  - Unlike estimation error, takes part of optimization error and other randomness in decisions into account

# Quantifying Bias and Variance

- Let  $p$  be a random predictor variable and its **optimal combination**  $C(p) = \operatorname{argmin}_m E_p[L(p, m)]$ —combine samples to minimize loss
- E.g.  $C$  = the majority for binary  $L$
- $\text{oB}(x) = C(y|x)$  because generate arbitrarily many samples from  $y|x$  and combine them
- **Main predictor**  $M(x) = C(f_s(x))$ 
  - E.g., randomly sample  $S$  of size  $n$  many times, train decision tree on each, and combine them

# Quantifying Bias and Variance

- **Bias( $x$ )** =  $L(oB(x), M(x))$  – the main predictor performance relative to  $oB$
- **Variance( $x$ )** =  $E_s[L(f_s(x), M(x))]$  – cost of performance difference from the main predictor
- **Noise( $x$ )** =  $E_s[L(oB(x), y(x))]$  – can't avoid noise, i.e.  $E_x[\text{noise}(x)] = R_{oB}$
- $\forall x$  and metric  $L$ ,  $L(x, y) \leq \text{noise}(x) + \text{bias}(x) + \text{variance}(x)$

# Measuring Bias and Variance

- **Bagging** simulates the main predictor using bootstrap:
- $T$  times for some  $T$  such as 300
  - Create a resample of  $S$  of size  $n$
  - Train  $A$  on it to get  $f$
- To predict given  $x$ , form the main predictor out of all  $f$  and return its answer
- Use **out-of-bag** risk estimates—run the bagged predictor on  $S$ , and for an example combine only the base  $f$  in training which it wasn't used

# Measuring Bias and Variance

- Don't know oB, so use loss of the main predictor as bias + noise
- A with high enough variance is **unstable**
- Decision tree is **unbiased** and unstable
  - Bagged tree is a very good predictor
  - Pruning increases bias and reduces variance
- NN too
  - $k > 1$  increases bias and reduces variance

# Random Forest

- Improves bagged decision tree:
  - Decorrelate the trees as much as possible to reduce bias, combination will take care of the extra variance
- When building a tree from a resample, at every split randomly select and consider only  $\sqrt{D}$  features
- No pruning, but should still cap depth

# Random Forest

- Top performance in many domains in terms of risk
- Fast, easily parallelizable
- Out-of-bag estimate removes need for cross-validation
  - Use more trees (1000 will do) for an accurate estimate
- No parameters to tune
  - The default number of trees and considered features work well

# What Really Controls Estimation Error?

- Randomization ensembles don't overfit more as  $T \rightarrow \infty$
- Intuitively, some finite number of base learners create a concentration that quickly converges to the set of solutions with similar generalization error
- E.g. majority vote for classification converges to fixed class probabilities
- Simplicity vs stability vs multiple testing—stability seems to win, but unsolved

# Conclusions

- Generally random forest is best, and kernel SVM 2<sup>nd</sup>
- Deep network best for some tasks, but not an effective black box yet
- Machine learning far from solved—thousands of researchers still working on many problems
- Focus on data preparation
- Go for insight—decision tree and linear SVM first
- Best of random forest and kernel SVM next

# References

- Kedyk, D. (2016). *Commodity Algorithms and Data Structures in C++: Simple and Useful.* 2<sup>nd</sup> Edition. CreateSpace.