Recall one variable function classification of critical criteria for Sti jeg inflection pt. Local wex local min $f_{ii} = 0$ f" < 0 £">0 (2) f'is decreaning E) f'is increasing (2 f is gren word) E) f'is open upword

$$\int_{0}^{\infty} \int_{0}^{\infty} \int_{0$$

SECOND DERIVATIVES TEST Suppose the second partial derivatives of f are continuous on a disk with center (a, b), and suppose that $f_x(a, b) = 0$ and $f_y(a, b) = 0$ [that is, (a, b) is a critical point of f]. Let

$$f(x m) = \chi^2 \sin(y)$$

$$D = D(a, b) = f_{xx}(a, b) f_{yy}(a, b) - [f_{xy}(a, b)]^{2}$$

- (a) If D > 0 and $f_{xx}(a, b) > 0$, then f(a, b) is a local minimum.
- (b) If D > 0 and $f_{xx}(a, b) < 0$, then f(a, b) is a local maximum.
- (c) If D < 0, then f(a, b) is not a local maximum or minimum.

classification of critical points into Local max/min/ 8atolle points

Q classify t = x,+4, critical point = (0,0) $D = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 2 & 0 \\ 0 & 2 \end{vmatrix} = 4 D = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} -2 & 0 \\ 0 & -2 \end{vmatrix} = 4$ D> 0 kfxx > 0

=) (0,0) is a point of back win

critical points of

$$f = -x^2 - y^2$$

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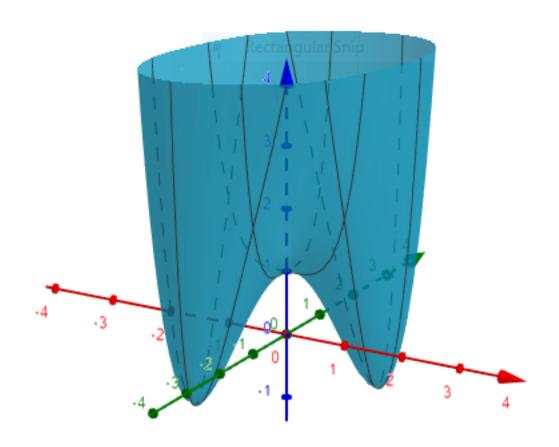
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EXAMPLE 3 Find the local maximum and minimum values and saddle points of

$$f(x, y) = x^4 + y^4 - 4xy + 1.$$



$$f_{x} = 0$$
 $4x^{3} - 4 = 0$
 $4x^{3} - x = 0$
 $4x^{3} - x = 0$

on
$$4 = 0$$

$$44^{3} - 4x = 0$$

$$4 = x^{3}$$

$$(x^{3})^{3} - x = 0$$

$$x^{9} - x = 0$$

$$D = |f_{xx} f_{xy}| = |12x^2 - 4|$$

$$|f_{xy} f_{yy}| = |-4| 12x^2$$

$$x = 0$$

 $x = 0$
 $x = 0$

EXAMPLE 4 Find the shortest distance from the point (1, 0, -2) to the plane x + 2y + z = 4.

EXAMPLE 5 A rectangular box without a lid is to be made from 12 m² of card-board. Find the maximum volume of such a box.

33. Find the points on the cone $z^2 = x^2 + y^2$ that are closest to the point (4, 2, 0).

Find the volume of the largest rectangular box with edges parallel to the axes that can be inscribed in the ellipsoid

$$9x^2 + 36y^2 + 4z^2 = 36$$