

A mixed-dimensional strategy for simulating soil thermal hydrology in low-relief permafrost-affected landscapes

Abstract

Integrated surface/subsurface models for simulating the thermal hydrology of permafrost affected regions in a warming climate have recently become available, but computational demands of those new process-rich simulation tools have thus far limited their applications to one-dimensional or small two-dimensional simulations. We present a mixed-dimensional model structure for efficiently simulating surface/subsurface thermal hydrology in low-relief permafrost regions at watershed scales. The approach solves an operator-split system, sequentially coupling a two-dimensional surface thermal hydrology system with a family of one-dimensional vertical columns, where each column represents a fully coupled surface/subsurface thermal hydrology system without lateral flows. The overland thermal hydrology system with no sources acts to redistribute mass and energy horizontally by updating the column systems before they advance in time. We show that the approach is highly scalable, supports subcycling of different processes, and compares well with the corresponding fully 3D representation at significantly less computational cost. These advances enable state-of-the-art representations of freezing soil physics to be coupled with thermal overland flow and surface energy balance at scales of 100s of meters. Although developed and demonstrated for permafrost thermal hydrology, the mixed-dimensional model structure is applicable to integrated surface/subsurface thermal hydrology in general.

Keywords: Mixed-dimensional model, Permafrost thermal hydrology, Integrated surface/subsurface flow modeling, Arctic

1. Introduction

Approximately 23% of the land surface in the Northern Hemisphere is underlain by continuous permafrost (91-100% frozen area), and another 17% is occupied by discontinuous permafrost (50-90% frozen area) [1, 2]. A massive
5 amount of organic carbon is stored in those regions [3], which are warming at a rate considerably faster than the rest of the planet [4, 5, 6]. As the soils in that region warm, they have the potential to transform from a net sink to a net source of carbon to the atmosphere, which could increase the concentration of carbon in the atmosphere and in turn lead to further increase in the tem-
10 perature [7]. Further, thawing and the resulting degradation of permafrost can cause significant changes in the surface and subsurface thermal hydrology and eventually can substantially alter the Arctic tundra ecosystems [8, 9, 10, 11, 12].

Those potential impacts and feedbacks in the terrestrial Arctic have motivated the development of increasingly sophisticated tools for simulating per-
15 mafrost dynamics in a warming climate. Such simulations can help to better understand the consequences of soil warming and responses of tundra ecosystems to warming trends, and further expose the effects of permafrost degradation on surface and subsurface thermal hydrology. However, simulating permafrost dynamics in a complex and coupled surface/subsurface thermal hydrological en-
20 vironment is a challenging task, especially at larger spatiotemporal scales [13]. A comprehensive review of the modeling efforts of the surface and subsurface can be found in [14]. Early research efforts focused on one-dimensional simulations for fundamental understanding of infiltration in cold climates; see, for exam-
25 ple, [15, 16, 17]. Similar one-dimensional approximations have been adopted as coarse-scale models in global land surface models [18, 19, 20, 12]. Two-dimensional simulations with simplified physics (i.e. saturated conditions, sub-
surface only) have been used for understanding evolution of field-scale ground-
water systems [21, 22], but do not represent key unsaturated zone processes that are needed to understand active layer dynamics and decomposition of soil
30 organic matter. It is worth pointing out that mathematical models with lim-

ited complexity, reduced dimensionality, and relatively coarse spatial resolutions provide some insight into permafrost dynamics but fail to represent important processes such as cryosuction, lateral surface and subsurface flows, and advective heat transfers. Simulations with more mechanistic representations of surface and
35 vadose zone process in three-dimensions are essential to accurately capture the potential impacts of permafrost thawing on the surface and subsurface thermal hydrology and the resulting effects on the carbon cycle.

Two- and three-dimensional models with explicit physics-based representations of ice/liquid/gas partitioning in the vadose zone [23] have only recently
40 started to appear. Painter [2011] developed the three-phase, two-component model MarsFlo which has been used in Mars [25] and Earth permafrost studies [26]. Karra et al. [2014] simplified that subsurface freezing-soil thermal hydrology representation by ignoring gas advection and implemented that Richards-like approximation in the highly parallel PFLOTRAN [?] code. Those com-
45 puter codes are all subsurface-only models; that is, they do not represent surface flows and surface energy balance. Painter et al. 2016 recently introduced the Arctic Terrestrial Simulator, which uses a sophisticated multiphysics management framework [29] to couple the three-dimensional subsurface representation of [27] with a two-dimensional non-isothermal surface flow model, surface energy
50 balance with and without snow, and a simple snow distribution model.

Despite the significant progress in developing integrated surface/subsurface permafrost thermal hydrology models, significant challenges remain in moving to climate-relevant spatiotemporal scales. One of the challenges is that the integrated system is numerically stiff because of the highly dynamic surface sys-
55 tem [28] and the ice-liquid phase transition [30], which often results in relatively small time steps to achieve convergence. Small time steps are not problematic in one-dimensional simulations because a well-designed simulation tool will recover the time step quickly after a convergence failure. However, a small time step becomes problematic in large three-dimensional runs because it becomes
60 increasingly likely that, at any given time, at least one computational cell will be experiencing a phase change and thus a small time step. The other major chal-

lenge is tracking thaw-induced subsidence. Traditional hydrological simulators are mainly designed to conduct three-dimensional simulations, however, deformations in a three-dimensional simulation are not easy to track due to mesh tangling and can be computationally expensive; further, poor mesh quality may
65 raise questions about the accuracy of the results.

To address the aforementioned challenges, we present a mixed-dimensional modeling strategy for process-rich simulations of integrated surface and subsurface thermal hydrology in tundra systems with low topographic gradients.
70 We demonstrate with simulations of polygonal tundra, large and carbon-rich regions of northern Siberia, Alaska, and Canada where soil cracking has led to the formation of subsurface ice wedges that honeycomb the subsurface and tessellate the land surface into polygonal patterns. Rather than solve a fully three-dimensional subsurface system tightly coupled to surface processes as in [28],
75 we take advantage of physical insights gained from fine-scale simulations and approximate the integrated surface/subsurface dynamics with mutually independent 1-D columns, each associated with an ice wedge polygon. The columns are then sequentially coupled to a surface thermal flow system, solving the surface problem in an operator-split manner. This mixed-dimensional modeling
80 approach is motivated by fine-scale simulations at the ice-wedge polygon scale that showed that differences in the thermal conditions among centers, rims and troughs of ice-wedge polygons are largely equilibrated by lateral heat transport during summer such that the system behaves similarly to a one-dimensional system on seasonal time scales. Mixed-dimensional model structures have been
85 used previously in simulations of variably saturated flow at watershed scales, in particular to couple multiple 1-D unsaturated (vadose) zone representations to a two- or three-dimensional saturated zone; for example see [31, 32, 33]. Here we apply the mixed-dimensional model structure to an integrated surface/subsurface flow system including surface and subsurface thermal processes
90 and evaluate the accuracy and computational advantages of the approximation.

The paper is organized as follows: Section 2 highlights the Advanced/Arctic Terrestrial Simulator (ATS) and the Arcos multiphysics management frame-

work, within which we implemented our approach. Section 3 presents some fine-scale simulation results and analysis that motivated the approach. In Section 4 we introduce our mixed-dimensional modeling approach, loosely coupled
95 scheme and the ATS refactoring strategy. To illustrate the performance and efficiency of our modeling strategy, in Section 5 we compare our numerical results with the three-dimensional simulations based on strong coupling, and present speedup and scalability of the new technique. Concluding remarks and future
100 research are offered in Section 6.

2. The ATS Software

We implemented our mixed-dimensional modeling strategy in open-source parallel software known as Amanzi-ATS [?] (or simply ATS). Amanzi-ATS is the result of extending the flow and reactive transport simulator Amanzi [34]
105 by adding an advanced multiphysics management system known as Arcos [29]. Arcos is key to managing the complex spatial structures used here. It was originally built to manage couplings among process models (denoted process kernels and abbreviated as PKs), which may be selected at runtime. A PK encapsulates the mathematical representation of a particular physical process
110 or coupled set of processes; PKs are coupled together through Multiprocess Coordinators MPCs. An MPC is regarded as a PK by MPCs at higher levels in the tree, thus allowing complex hierarchical model structures to be built dynamically at runtime. In this work, we used Arcos to coordinate not only process kernels but also subdomains of the larger spatial domain.

115 Amanzi, and by extension ATS, uses the Trilinos [Heroux et al., 2003] framework for parallel infrastructure. An unstructured mesh framework [Garimella et al., 2014] is included for interacting with the computational mesh. General polyhedral meshes are supported. Discretization accuracy is maintained on the potentially distorted grids through the use of the mimetic finite difference
120 (MFD) method [Beirao da Veiga, 2014; Lipnikov et al., 2014]. The backward Euler method is used for time stepping with a Nonlinear Krylov Acceleration

(NKA) method [Calef et al., 2013; Carlson and Miller, 1998] to solve the resulting discretized residual equations.

The initialism ATS may refer to either the Advanced Terrestrial Simulator, which is the general capability, or the Arctic Terrestrial Simulator, which is one particular configuration [28], depending on context. The Arctic Terrestrial Simulator configuration solves strongly coupled surface energy balance, and surface and subsurface thermal hydrology with freeze/thaw dynamics. This work extends the ATS to work with a multicolumn spatial structure.

130 3. Motivation: Results from Fine-scale Simulations

This mixed-dimensional approach is motivated by the results of fine-scale, two-dimensional simulations on vertical cross-sections across ice-wedge polygons at the Barrow Environmental Observatory. The simulations coupled a surface energy balance model with and without snow, snow distribution models, models for thermal overland flow including phase change, and a recently developed three-phase subsurface thermal hydrology model. The soil properties were calibrated against borehole temperature data in a previous study [35]. The simulations were forced with meteorological data for the site. Those simulations used an unstructured mesh that conforms to surface topography derived from lidar measurements. Horizontal mesh resolution is approximately 0.25 m. Vertical resolution is 0.02 cm at the surface and gradually increases with depth. Details on boundary conditions and the spinup process can be found in [28].

Snapshots of ice and liquid saturation indices in cross-section across two ice-wedge polygons are shown in Fig. 1. These snapshots are for October 15, 2013, which is during the fall freeze-up. During this period, the rims of the ice-wedge polygons are significantly colder than the centers and troughs because the thermally insulating snowpack is smaller on the rims. Previous one-dimensional simulations [36] have shown that thermal differences caused by differences in snow depth lead to differences in active layer thickness, the depth of the annual thaw. However, in the two-dimensional simulations shown here, the active layer

thickness shows little variation across the polygon (Fig. 2). Although transient differences in subsurface temperature occur due to differences in snow depth, soil moisture content, and albedo, lateral heat transport is sufficient to equilibrate those differences by the time of maximum thaw. Thus, the active layer thickness, which is a primary control on the annual carbon decomposition rates, is not directly affected by microtopographic position within an ice-wedge polygon in cases where organic matter is relatively uniform. This lack of sensitivity suggests a model structure where the ice-wedge polygon becomes the unit computational cell on the surface.

4. Modeling Approach, Coupling Scheme, and ATS Refactoring Strategy

In this section, we first describe the mixed-dimensional modeling approach then present the operator splitting scheme followed by the refactoring strategy of the ATS.

4.1. Mixed-Dimensional Modeling Approach

Technically, our modeling strategy splits a 3D domain into $2N + 1$ subdomains, where N is the total number of surface elements. The total $2N + 1$ subdomains include N subdomains for 1D subsurface columns (on which flow and energy equations are solved), N subdomains as the surface of those columns (on which the surface energy balance is solved), and one subdomain for the 2D overland system (on which lateral surface flow is solved). To avoid confusion, hereafter the 2D overland system is referred to as surface-star system, and the 1D surface cells will collectively be called surface system. The 1D columns and surface-star system is highlighted in Fig. 3. Arcos represents physics on these domains as a hierarchical PK tree which shows how the processes are coupled on and across these domains, as illustrated in Fig. 4. The PK tree consists of individual conservation equations, strong (globally implicit) couplers, and weak (sequential) couplers highlighted in blue, light cyan, and orange colors, respectively. In our approach, the interaction at the interface between the surface-star

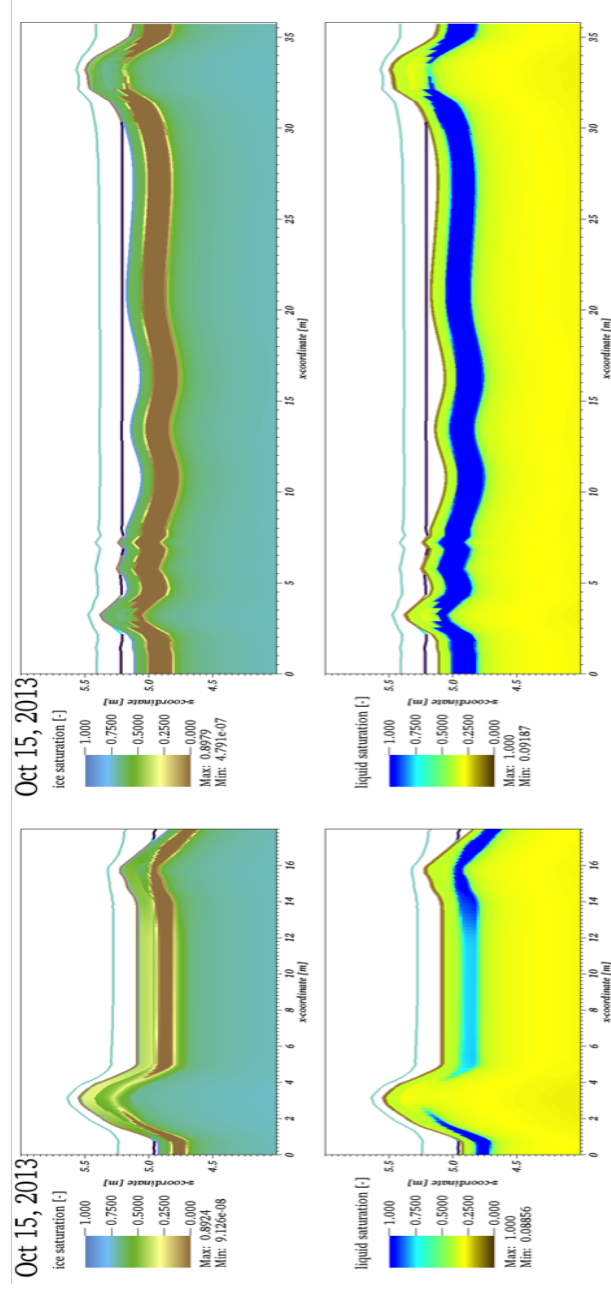


Figure 1: Results from two-dimensional fine-scale modeling. Shown are snapshots of ice saturation index and liquid saturation index in cross-sections across two ice-wedge polygons.

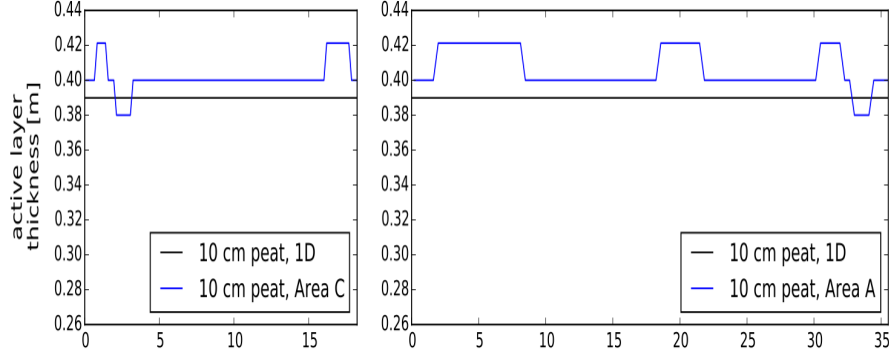


Figure 2: Active layer thickness from fine-scale modeling. Note that the mesh resolution here is 2cm , and the discontinuities reflect jumps between cells of the mesh.

180 and 1D columns happens at the top level weak MPC. The strong MPC (on
the left at the second level) is the surface-star system. The weak MPC at the
second level iterates over all the surface and subsurface subdomains. The PK-I,
 $I = 1, 2, 3, \dots, N$ denote integrated surface (a cell) and subsurface (1D column)
system. The tree attached to the black octagon shape is replicated across all
185 PK-I, $I = 1, 2, 3, \dots, N$.

4.2. Operator Splitting Scheme

The operator splitting scheme for advancing our mixed-dimensional model
is a two-step sequential algorithm. First, we solve the surface-star thermal
hydrology system without any external or exchanged sources and then compute
190 the solution of the one-dimensional columns. Each 1D column is a system of
the subsurface thermal hydrology, surface ponding and energy exchange but no
lateral flow, and surface energy balance. The first step mainly acts as a spatial
distributor of the mass and energy. That is, it distributes the water and energy
across the 2D overland system, and its solution serves as initial condition for
195 the second step. After the update from the first step, we solve the family of
1D columns, and use the output of that half-step to update the surface-star
pressure and temperature for the next iteration in the algorithm. As depicted
in Fig. 5, the top and bottom orange spots represent 2D surface-star system and

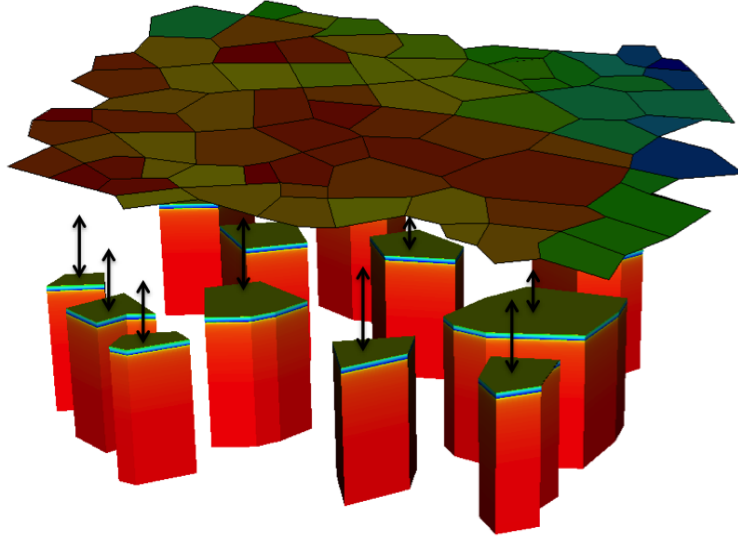


Figure 3: An illustration of the independent 1D subsurface columns coupled to the surface-star system. The surface system (1D cells lying on the top of corresponding columns) are not shown.

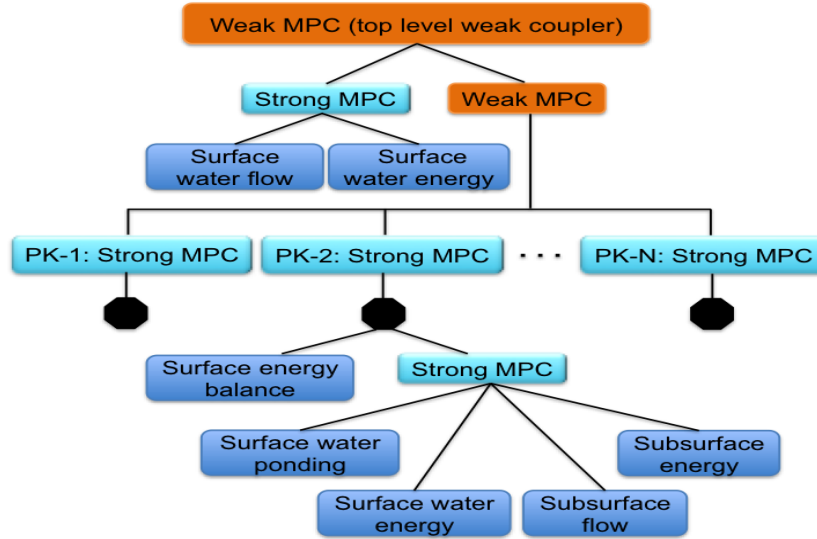


Figure 4: A customized hierarchical structure of the process kernels. Blue blocks highlights independent process models; Light blue blocks strongly coupled independent process kernels; Orange blocks represent weak couplers.

1D columns, respectively, and the cyan colors (in the middle) are intermediate
 200 steps for updating surface-star and 1D column systems. For the sake of clarity,
 we will refer to the pressure and temperature fields of the first step as surface-
 star pressure and temperature, while that of the second step will be called as
 subsurface and surface pressures and temperatures.

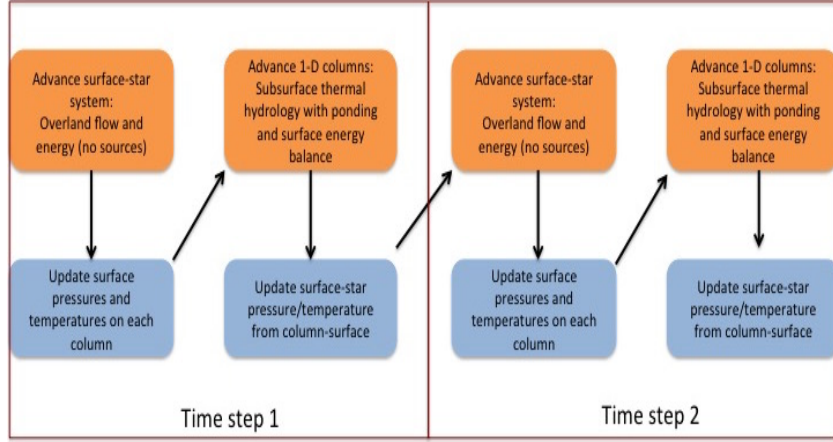


Figure 5: Schematic of the loosely coupled scheme for our mixed-dimensional model. Orange represents advancement of PKs in time; blue shows intermediate steps for initialization of PKs within a single time step.

4.3. ATS Refactoring Strategy

205 The ATS was significantly refactored to accommodate the above customized
 weak MPC. The refactoring allows multiple instances of a given PK, each at-
 tached to a different mesh representing a subdomain of the primary mesh. This
 stateless structure permits each surface and subsurface subdomain to have its
 own domain name, say column_n , surface_column_n , $n = 1, 2, 3, \dots, N$. In fact,
 210 the refactoring strategy prefixes the variables (primary, secondary, and inde-
 pendent) with their corresponding subdomain names (e.g., column_n -pressure,
 column_n -temperature, $n = 1, 2, 3, \dots, N$) – that yields each PK in its most
 general form. These generic PKs now allow to construct any type of customize
 MPC for mixed-dimensional modeling technique.

215 Complexity of the multiphysics PK tree in our modeling strategy could not
 have been achieved without the Arcos framework. Though the complexity in
 the PK tree is evident but additional complications are intended as we include
 more processes (physical, chemical, biological and geological processes) and their
 mutual interactions. All these processes are equally important for an accurate
 220 and reliable long-term projections of permafrost regions. That said, the refac-
 tored ATS is more effective in addressing important challenges in the permafrost
 thawing in warming climate.

5. Results and Discussions

In this section, we present numerical results that highlights the accuracy and
 225 efficiency of our modeling technique. At the development stage, several numeri-
 cal experiments were performed to verify the physical behavior of the refactored
 modules (PKs) of the ATS, code verification details are presented in Appendix
 A. The spinup process (i.e., model’s initialization) has been described in detail
 in [28].

230 5.1. Numerical Results – A Comparative Study

To demonstrate the accuracy of our modeling technique, we compare nu-
 merical results of the mixed-dimensional model against a fully coupled three-
 dimensional simulations that act as a benchmark for our simulations. The do-
 main under consideration has surface elevation varying between 4.14-4.62 m,
 235 is 40 m deep, and enclosed by a rectangle in the horizontal plane 173×160
 m^2 ; see Fig. 6. This domain is a part of the low-gradient polygonal tundra in
 Barrow, Alaska and consist of 75 ice wedge polygons. As highlighted in Fig. 6,
 we select five spots (based on different elevations) to perform a location-based
 comparison of the numerical results of the two schemes.

240 In addition to evaluating the quality of our mixed-dimensional approach
 for the Barrow tundra, we also want to understand when it will give inaccurate
 results. Because our modeling strategy is based on a loosely coupled scheme and

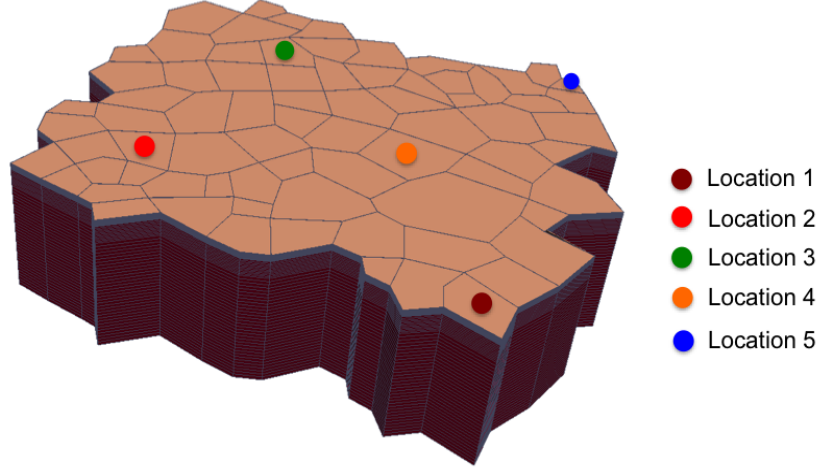


Figure 6: An illustration of the five spatial locations on 75 polygons cluster for location-based comparison of the two schemes. Location 1: Outlet. Location 2: High elevated spot. Location 3-4: Intermediate elevation spots. Location 5: Lowest elevation spot.

neglects subsurface lateral flow between ice wedge polygons, it should eventually become inaccurate if the topographic relief is sufficiently large. To identify the
 245 range of applicability, we consider three variants of the surface topography. We use the following equation to exaggerate the surface topography,

$$\bar{Z} = \alpha(Z - \mu) + \mu. \quad (1)$$

Here \bar{Z} is the exaggerated elevation, Z is the original elevation with mean μ , and α is the exaggeration parameter. Equation (1) preserves the mean while the standard deviation depends on the value of α and is given in meters by 0.14α .
 250 The coefficient in front of α is the standard deviation of the original elevation Z – in our case Z correspond to the domain shown in Fig. 6. Our three variants correspond to $\alpha = 1, 3$, and 5 . The value $\alpha = 1$ corresponds to the original topography. We expect the model to give promising results for simulating low-gradient polygonal tundra, and believe that the values of α we choose provide
 255 sufficient variation across a domain of 100s of meter. Our numerical experiments confirm a high agreement between the results of the mixed-dimensional model and the 3D model at all selected location for all three α values. Figs. 7 and 8

compare the subsurface water saturations and temperatures, respectively, at locations 1 and 5 and for $\alpha = 1$. The accuracy of our results for the Barrow topography ($\alpha = 1$) is evident. The surface ponded depths and temperatures obtained with the two models are depicted in Fig. 9 and 10, respectively. As expect, our results fit the 3D model's results very well. We see the same level of agreement at the other locations as well, but we are not showing them here. In Fig. 11 we plot the mean annual thaw depth at five locations for the three variants, $\alpha = 1, 3$, and 5. We use the annual mean of the thaw depth rather than the maximum thaw depth (i.e. the active layer thickness) because the mean annual thaw depth depends on both the duration of thaw and maximum thaw depth. Thus it is a direct measure of soil available for decomposition, averaged over the year. Not surprisingly, as the value of α increases the mean annual thaw depth deviates from the results of the 3D model to some extent, but we still see the results of the mixed-dimensional model agree well with to the corresponding benchmark solution. The consistency of our numerical results with the fully coupled 3D simulations confirm the appropriateness of this approximated scheme.

5.2. Speedup Study

We discuss speedup and parallel efficiency for two spatial domains, one with 75 polygons as depicted in Fig. 6 and a larger one consisting of 468 ice-wedge polygons, as shown in Fig 12. The surface ponded depth and temperature during the snowmelt in 2012 are presented in Fig. 13 for the 468 polygon domain. Fully coupled 3D simulations at such a scale are computationally very expensive.

We highlight two aspects of the efficiency of this modeling approach: (i) how the simulation time decreases in comparison with three-dimensional simulations, and (ii) how efficiently it scales with number of processes.

Fig. 14 compares the computational time of the multidimensional strategy versus the three-dimensional solution for the domain consisting of 75 columns. It can be seen that for a fixed number of processors, the computational time decreases by a factor of about four with the multidimensional technique. This

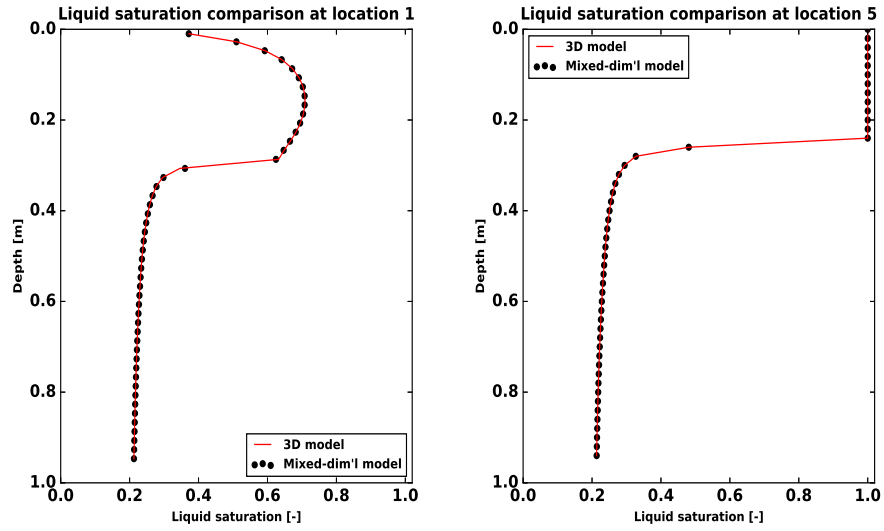


Figure 7: Comparison of the subsurface water saturation at locations 1 and 5 during the summer.

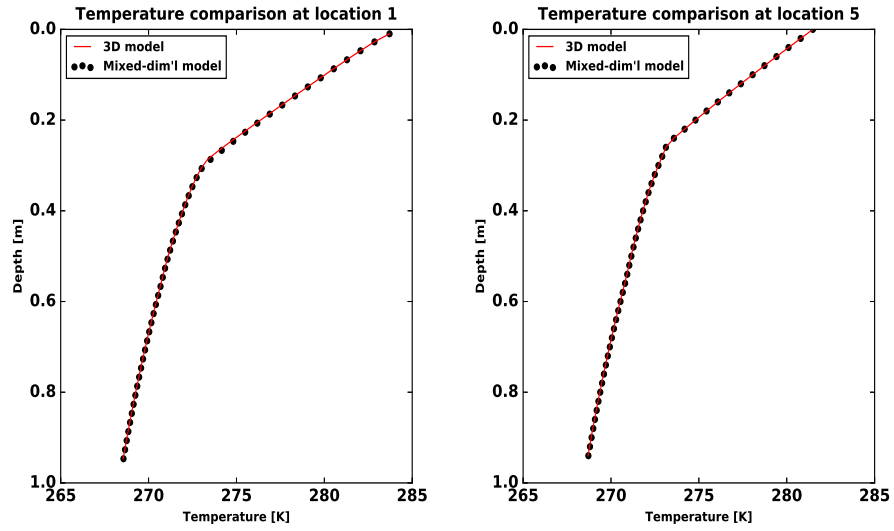


Figure 8: Comparison of subsurface temperature at locations 1 and 5 during the summer.

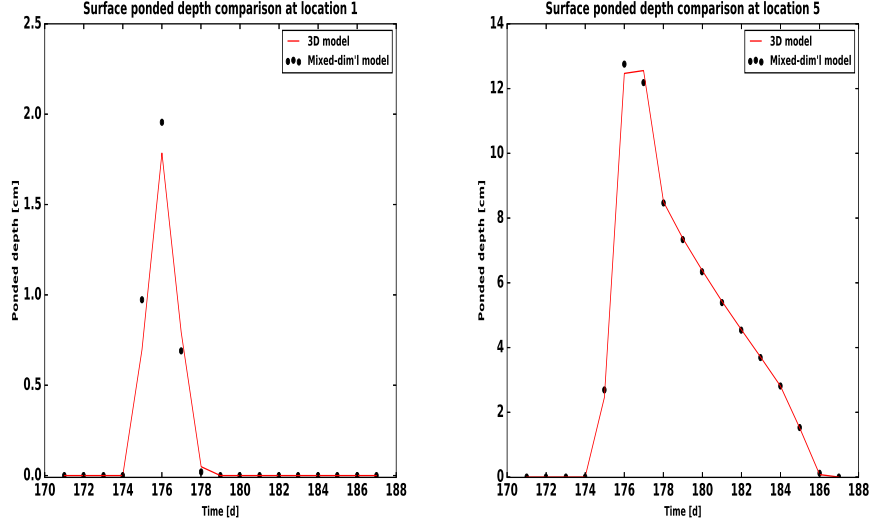


Figure 9: An illustration of the surface ponded depths of the two schemes at locations 1 and 5 when the snow melt starts.

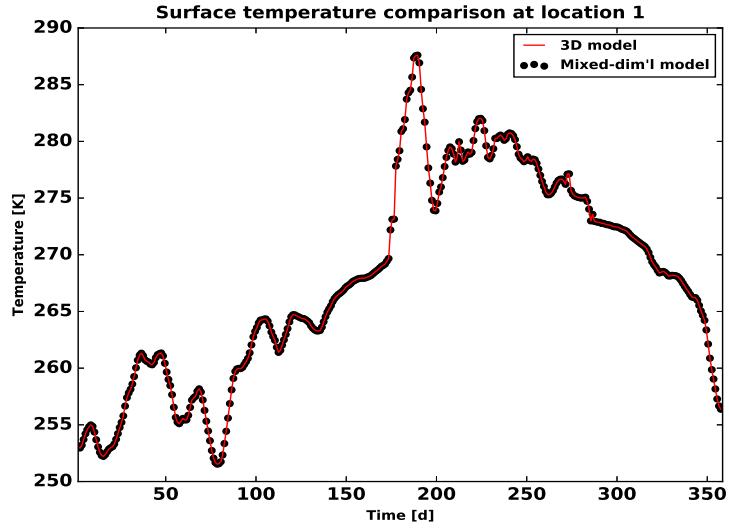


Figure 10: An illustration of the surface temperature of the two schemes at location 1 for the entire year.

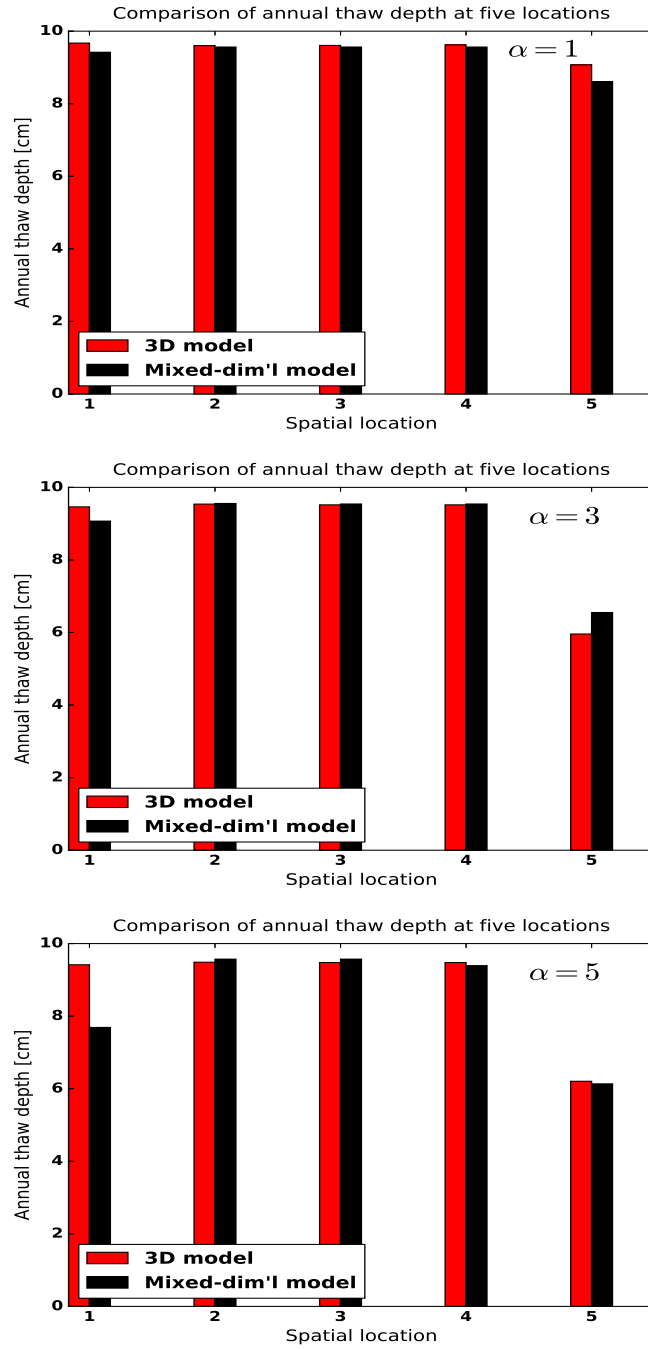


Figure 11: A comparison of the annual thaw depth at the selected locations of the three studies.

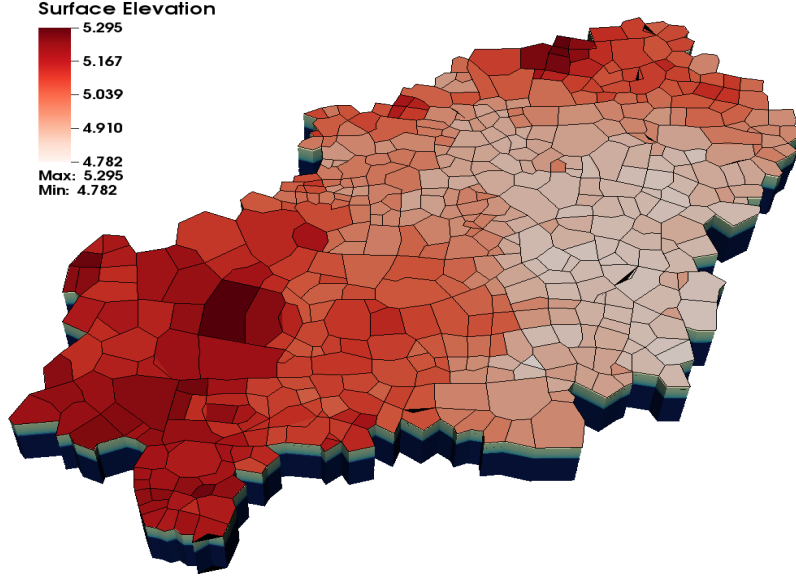


Figure 12: A watershed at Barrow, Alaska.

is a huge computational advantage without sacrificing numerical accuracy.

We show parallel strong scaling for the aforementioned domains in Fig. 15.

Speedup of the smaller domain is significantly less than the linear ideal; this is
 290 caused by communication overhead in the surface-star system. Without consid-
 eration of the surface-star system, the problem is perfectly parallel. To minimize
 communication between the surface-star system and the column systems, the
 surface-star mesh is partitioned so that a column and the coincident mesh cells
 295 on the surface-star system reside on the same processor. If there are too few
 columns per processor, the interprocessor communication for the surface-star
 system becomes the limiting factor despite the lower computational burden for
 the surface-star system compared with the columns. As expected, the scaling is
 better for a larger domain. Scaling is close to linear up to about 16 cores, which
 300 corresponds to about 30 columns per core.

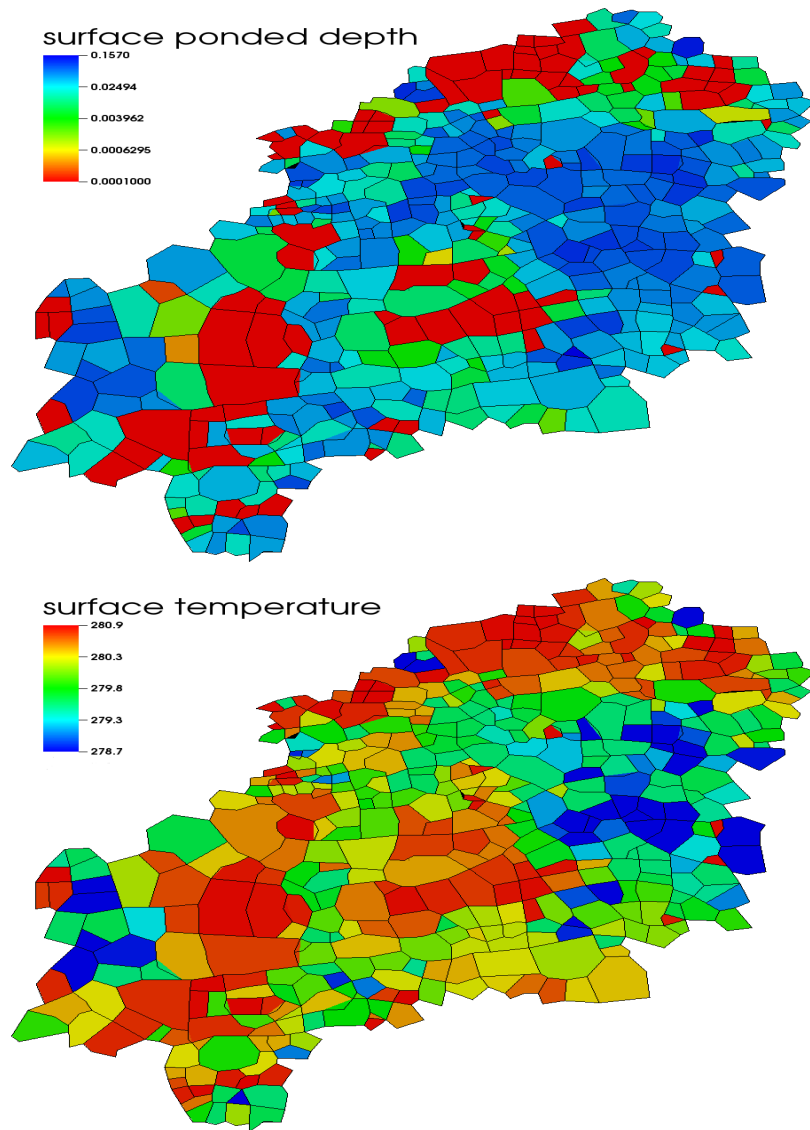


Figure 13: Simulation results of the mixed-dimensional model. Showing the surface ponded depth and temperature during the snowmelt of 2012.

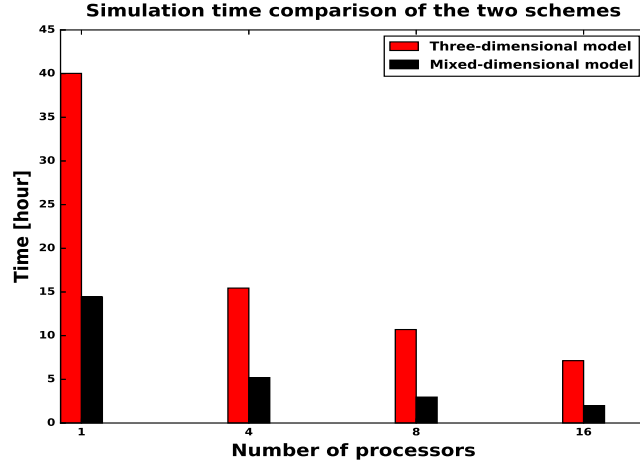


Figure 14: A comparison of the computational time taken by the mixed-dimensional and 3D models.

5.3. Subcycling Process Kernels

One advantage of sequentially coupling different PKs, as opposed to a fully coupled approach, is that sequential coupling makes subcycling possible. With subcycling, individual PKs take their own time step rather than a global time step. The independently evolving PKs are then synchronized on a larger time step. The idea is to assign a suitable local time-step to each subdomain rather than one single global time-step. It is a very convenient approach for simulating permafrost type regions because a relatively small time step may be required when a cell is going through a phase change. Without subcycling, a timestep failure or small timestep caused by phase change in a single cell results in a small global time step. With subcycling, the effects of that phase transition are limited to a single column. Our mixed-dimensional modeling approach efficiently allows subcycling PKs because we discretize subsurface as independent columns/subdomains. Thus, the subdomains can advance in time with their preferred time-steps until they hit the synchronized time. Fig. 16 displays percentage reduction in the simulation time for the domains consisting of 21, 75, and 468 polygons. With the increase in the number of subsurface columns the

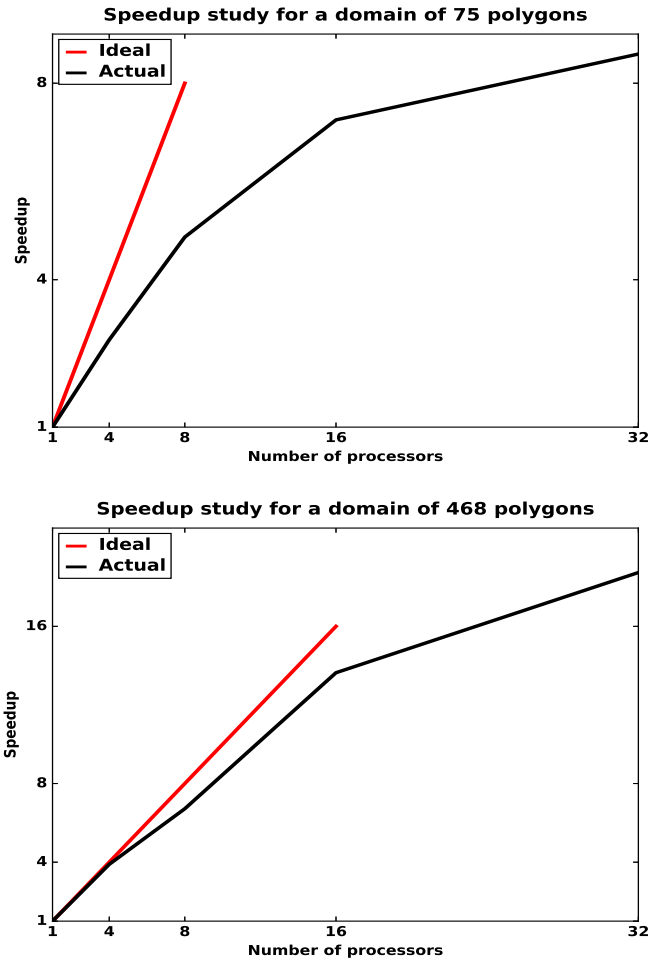


Figure 15: An illustration of the speedup study of a simulation with 75-polygon cluster (top) and 468 polygons barrow watershed (bottom).

computational time decreases, and we see up to 40% reduction in the computational time in comparison with simulations without subcycling. The choice of the synchronization time is crucial, and requires further optimization, which will be studied in future work.

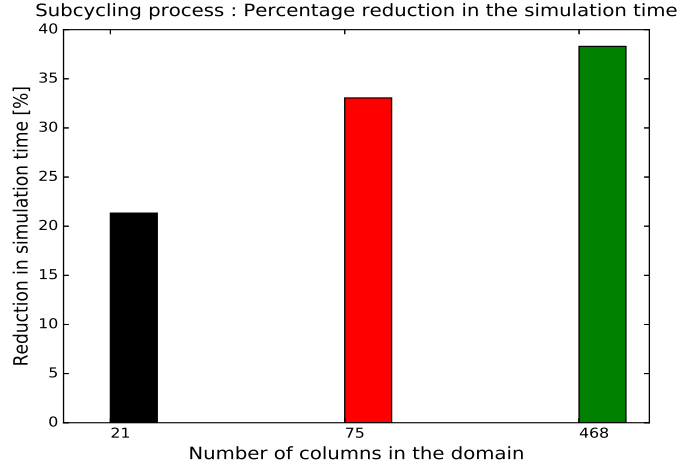


Figure 16: (Subcycling PKs) Percentage reduction in the computational time for the domains consisting of 21, 75 and 468 polygons.

6. Conclusions and Future Work

We present a mixed-dimensional modeling approach that is based on discretizing the subsurface as independent columns that are indirectly coupled through a two-dimensional surface system. This approach was motivated by fine-scale simulations of permafrost regions. This is the first demonstration of state-of-the-art representation of freezing soil physics coupled to overland thermal flow and surface energy balance at scales of 100s of meters.

An operator splitting algorithm is used to advance our mixed-dimensional model. First, we solve a two-dimensional surface thermal hydrology system that spatially distributes mass and energy, and initializes the system of the second step. The second step solves a family of independent one-dimensional columns, where each represents an integrated system of the subsurface, surface ponding

and surface energy balance. That step updates the 2D surface system of the
335 first step for the next iteration.

We compared our numerical results to the conventional scheme of a fully 3D
subsurface that is strongly coupled to a surface system to demonstrate the effi-
ciency and accuracy of our modeling approach. The fully coupled results act as
a benchmark for our scheme. Numerical results show our scheme closely approx-
340 imates the fully coupled system but is significantly more efficient. The scheme
also allows for subcycling of individual subdomains, which further improves the
numerical efficiency.

This work is part of a larger effort to provide process-rich, watershed-scale
simulations capability for permafrost regions. A next step would be to incorpo-
345 rate a subgrid model to represent the effects of variations of topography below
our discretization unit of the ice wedge polygon. Another future direction is
to represent thaw-induced subsidence. Thawing of permafrost and melting of
massive subsurface ice can cause differential subsidence, leading to dynamic
microtopography (low-centered polygons can transform to high-centered poly-
350 gons) [37, 38], substantial changes in hydrology and soil moisture, and altered
drainage networks, thus potentially transforming a dry region to a wetland
ecosystem [39, 40]. This modeling strategy is designed to tractably represent
thaw-induced subsidence. Representing subsidence in one dimension is signif-
icantly easier than a fully three-dimensional representation because mesh tan-
355 gling and other mesh quality issues arise in a fully three-dimensional dynamic
mesh but are avoided in one dimension. Indeed, simulations of thaw-induced
subsidence on a single one-dimensional integrated surface/subsurface system has
already been demonstrated [13]; the work described here will allow the same
techniques to be used at scale with many columns coupled to an overland flow
360 system. Lastly, refactoring ATS not only supports subdomain modeling tech-
niques but is also potentially useful future extensions. We can efficiently imple-
ment and independently test many process representations (physical, chemical,
biological and geological processes) as PKs and let them interact through MPCs.

Although we mainly focus on simulating the thermal hydrology of degrad-

365 ing permafrost, elements of the work presented here have greater applicability.
 A hybrid spatial structure mixing one-dimensional representations of the va-
 dose zone with two-dimensional representations of the saturated zone and over-
 land flow system are important approximations in watershed modeling. This
 operator-split scheme of Fig. 5 is broadly applicable to those systems and to
 370 integrated surface/subsurface simulations, in general. This mixed-dimensional
 representation may be used as an alternative to a fully coupled system or as a
 way of accelerating the time-consuming task of spinup. In addition, this work
 demonstrates the advantages of Arcos or other multiphysics management frame-
 works in greatly simplifies the process of building models with hybrid spatial
 375 structure.

Appendix A. Numerical Experiments – Code Verification

We have performed a series of tests at the development stage for code verifica-
 tion, and compared our results against numerical solution of three-dimensional
 model. The 3D results serve as a benchmark for our scheme. In 3D models
 380 the surface and subsurface systems are strongly coupled and solved implicitly.
 Since our model required major refactoring of the ATS, so individual pieces of
 the code were deeply tested before integration – they are listed below:

- Problem Test 1 (Subsurface Flow): We consider multiple subsurface columns
 with flat top surface – each column is an independent domain. Put water
 385 table below the surface, infiltrates and fills the subsurface columns.
- Problem Test 2 (Surface and Subsurface Flow only): This is an extension
 of the Test 1. We put water table below the surface. Water infiltrates and
 fill subsurface columns prior to surface ponding.
- Problem Test 3 (Subsurface Thermal Hydrology): We add energy equation
 390 to Test 1. Initially, establish water table close to the surface, and start
 freezing from below. The frozen subsurface columns are thawed from the
 top.

- Problem Test 4 (Surface and Subsurface Thermal Hydrology): In this test, we incorporate surface thermal hydrology into Test 3. A warm rain precipitation thaws the subsurface columns, saturate them and afterwards water ponds on the surface.
- Problem Test 5 (Surface Energy Balance, Surface and Subsurface Thermal Hydrology): A fully integrated surface and subsurface processes test. We introduce an energy balance equation to Test 4. An initially established ice table below the surface has been thawed by warm rain, incoming-short radiation and air temperature.

Due to symmetry in the domains of above numerical tests, that is, the subsurface columns are copies of each other and surface is flat, we get identical results and compare very well with its corresponding three-dimensional simulation results. Passing all the above tests conclude refactoring of the ATS a success. In the preceding discussion, we consider general polyhedra due to the polygonal structure of the Arctic landscape.

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