

# Synthetic controls and general panel data methods

EC420 MSU

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## Difference-in-differences

- Control for unobserved heterogeneity in  $i$  and And for overall time trends in  $t$
- Develop a counterfactual:  $E[Y_0|D = 1]$
- Constructed with *treatment* and *control* groups
- Regression specification to get "*DiD Estimtor*"
- **Parallel trends assumption**

- Past the *parallel trends* assumption
- Synthetic Counterfactual Method (SCM)

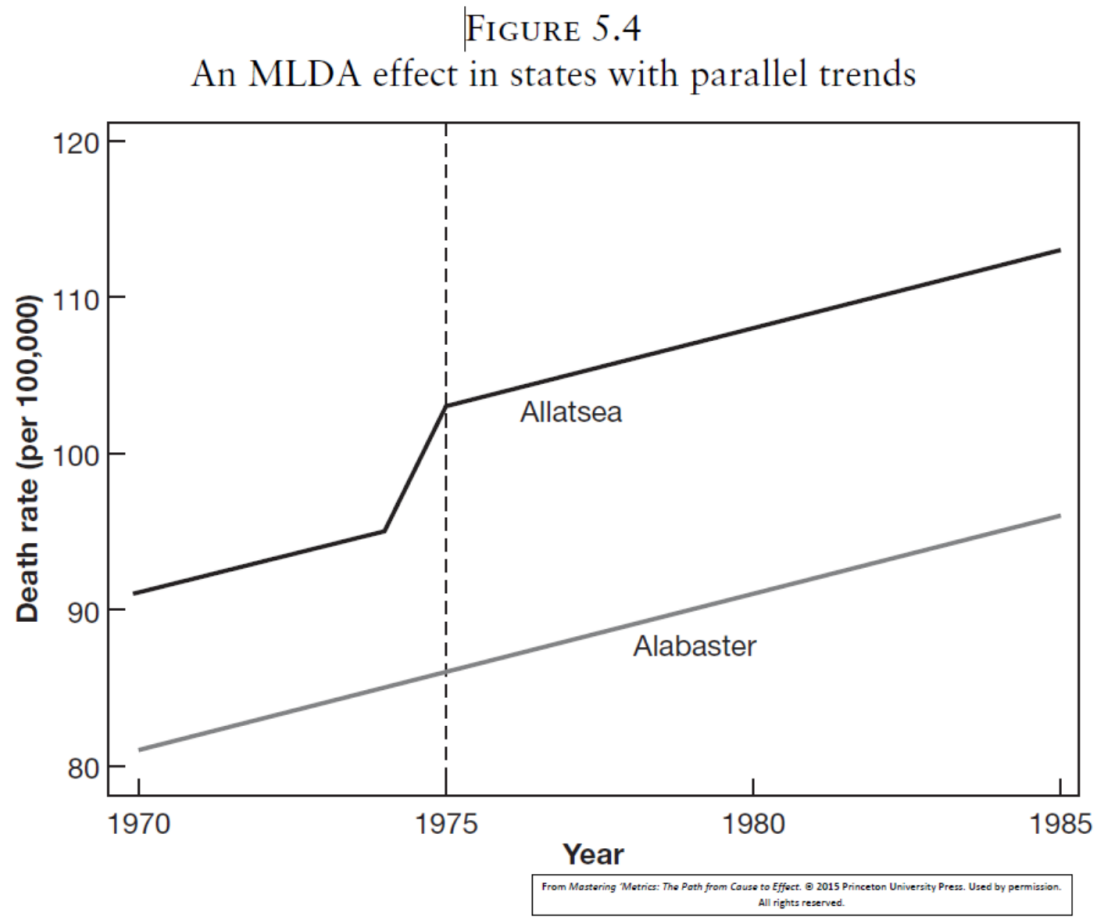
Recall that DiD's *identifying assumption* is that:

In the absence of treatment, the trends in both groups would have been the same.

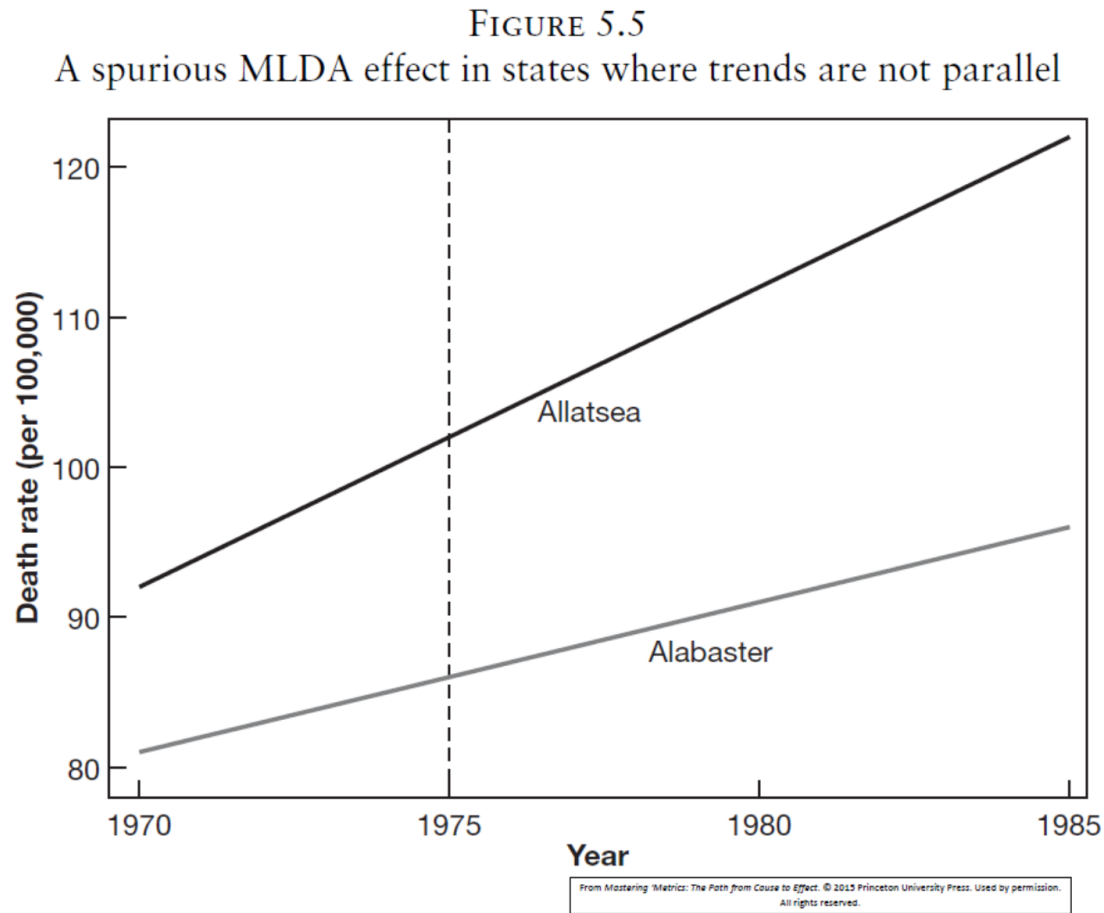
And recall that we can't directly test this

- We can look at pre-treatment trends
- But we would need to see the actual  $E[Y_0|D = 1]$  in order to ensure that it follows the same trend as  $E[Y_0|D = 0]$ , the untreated group.

We saw examples where that seemed like a pretty safe assumption:



And some where it didn't necessarily hold



What are we really after?

- We want a good  $E[Y_0|D = 1]$ , the counterfactual for the treated group.

DiD gets us this by making that link between  
 $E[Y_0|D = 0]$  and  $E[Y_0|D = 1]$

So what if we are a little more flexible on how that link is made...?

Let's start with a DiD specification, but with  $i$  individual fixed effects:

$$y_{it} = \beta_0 + \phi_i + \beta_2 POST_t + \beta_3 TREAT_i * POST_t + u_{it}$$

Our assumption here is that, once we condition on the  $\phi_i$  - that is, once we let each  $i$  have its own intercept, the *trends* are going to be the same.

But what drives those trends...? What moves all  $i$  together? And what if there were things that moved, say, 1/2 of the  $i$ 's?



Let's say we're looking at city-level unemployment rates over different cities across the US

We want to know the effect of worker safety regulations on unemployment.

Let's pretend there is one observed thing and *one unobserved thing* that drives the trends:

- **Observed:** national unemployment rate.
- **Unobserved:** Price of canned tomatoes.

*Why price of canned tomatoes?*

- Some  $i$  have tomato processing facilities in them, and some don't!
- We don't observe this.
- Treatment may be correlated (tomato processing is particularly dangerous for workers?)

## Would you agree that:

- If the price of tomatoes is very high, there will likely be more employment in tomato-processing facilities?
- And thus, unemployment would be lower (better) in those cities with tomato-processing facilities?

## And would you agree that:

- If our treatment is somehow correlated with the presence of tomato-processing facilities, we could be in trouble with our "parallel trends" assumption?
- Treatment may be endogenous (more worker safety rules when more dangerous employment)
- The effect may just be confounded by changes in tomato prices

## What would "tomato prices" do as a confounder?

- If tomato prices go up, **some**  $i$ 's (the ones with unobserved tomato processing facilities) will have lower unemployment
- So the *parallel trends* assumption is broken:
  - In the absence of treatment, a tomato-processing city would **not** follow the same trend as an untreated non-tomato-processing city.

## A "factor loading" model:

- Let  $\lambda_i^{tomato} = 1$  (has tomato facility)
- Let  $p_t^{tomato}$  be the national price of tomatos.

$$y_{it} = \beta_0 + \beta_1(\lambda_i^{tomato} * p_t^{tomato}) + \beta_2 D_{it} + \phi_i + \delta_t + u_{it}$$

This is just a model of unemployment  $y$  as a function of  $i$  specific traits,  $t$  specific trends in national unemployment rates, and *the effect of tomato prices on unemployment in tomato-processing cities*.

If  $\lambda_i^{tomato} = 0$ , then price of tomatos has no effect. If  $\lambda_i^{tomato} = 1$ , then the price of tomatos does have an effect ( $\beta_1$ ).

A "factor loading" model:

$$y_{it} = \beta_0 + \beta_1(\lambda_i^{tomato} * p_t^{tomato}) + \beta_2 D_{it} + \phi_i + \delta_t + u_{it}$$

Parallel trends will not hold between a  $\lambda_i^{tomato} = 1$  city and a  $\lambda_i^{tomato} = 0$  city.

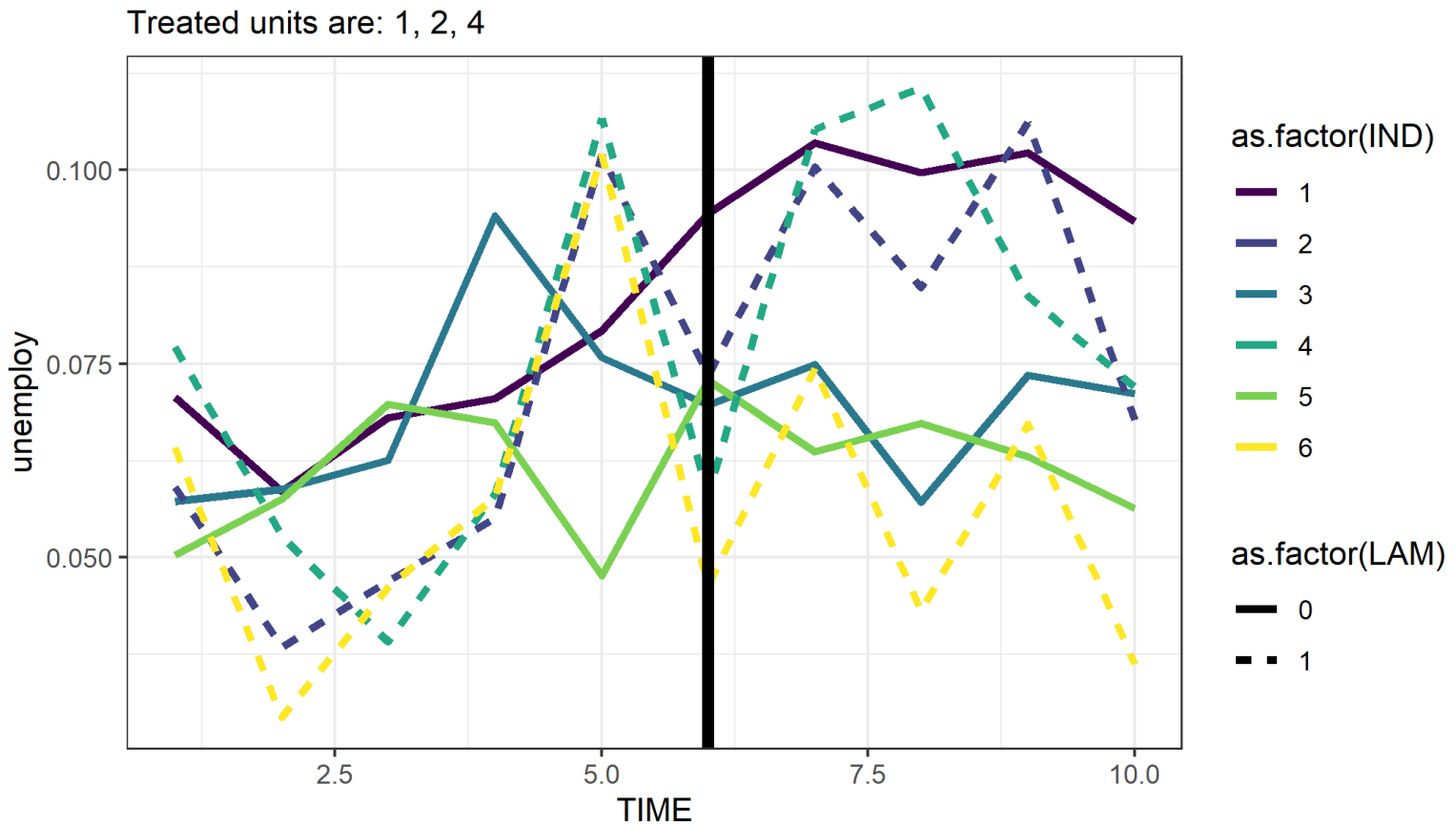
If we observed  $\lambda_i^{tomato}$ , we'd be fine

We would just control for it (include it in our  $X$ 's)

But...we don't.

## The Synthetic Counterfactual does its best to account for these unobserved factors

- Even without observing tomato processing facilities or the price of tomatoes, we **would** expect that pre-treatment unemployment in tomato processing cities **would look like other tomato processing cities**.
- That is, since the tomato processing cities are subject to the same price of tomatoes, then all of them will be a little higher on unemployment when tomato prices are low.
- The Synthetic Counterfactual Method looks for similarity in the pre-treatment trend and develops the counterfactual for  $i$  using all  $j$ 's that have similar pre-treatment "paths".



The intuition is that parallel trends assumption is best met by choosing a control pool that...follows parallel trends!

All the SCM does is find the controls that

- Are not treated
- But have similar pre-treatment trends

Since it's straightforward to have parallel trends for **one** treatment unit and some selection of potential controls, the SCM only handles one single treatment unit

- Great for comparative policy analysis
- Some methods for combining results from many SCM's



## Implementation

- Usually with a pre-packaged routine in R - `synth`
- Requires panel data

User specifies:

- **One** treatment unit
- **Many** potential control units (untreated)
- A treatment start time

The Synthetic is estimated by finding weights  $w$  that are used to combine all of the un-treated units in the control group.

## Implementation

- R makes a guess at  $w$ , weights on each of the control units
  - Let's say the guess is that the weights are  $(.5, .5, 0, \dots, 0)$
  - That is, the first two untreated  $i$ 's are weighted at .5 and .5, the rest are 0.
- The pre-treatment "synthetic" outcome at any pre-treatment time  $t$  is:
  - $y_t^{synth} = .5 \times y_{1,t} + .5 \times y_{2,t} + 0 \times y_{3,t} + \dots$

## Implementation con't.

- The distance between  $y_t^{synth}$  and  $y_t^{actual}$  is checked. Much like OLS, synth sums the squared difference:
  - $(y_t^{synth} - y_t^{actual})^2 + (y_{t-1}^{synth} - y_{t-1}^{actual})^2 + \dots$  over the pre-treatment period
  - Obviously, post-treatment, we think there will be a difference. Comparing pre-treatment lets us match up tomato-processing cities!
- R *guesses* at the weights over and over again until the smallest squared sum of errors is found. Observed covariates can be included as well.
- Those weights define the Synthetic Counterfactual in both the pre-treatment period *and* in the post-treatment.

If we get a very good match between  $y_t^{synth}$  and  $y_t^{actual}$  for all  $t$  in the pre-treatment, we would naturally think we have controlled for the unobserved factors (the tomato plants, etc.).

- If we have controlled for these confounders, *even the unobserved ones*, then we can claim that treatment is "as good as exogenous".

- $(Y_{0it}, Y_{1it}) \perp D$

- Thus, the difference between  $Y_t^{synth}$  and  $Y_t^{actual}$  **in the post-treatment periods** is the *ATE*

- $E[Y_0|D = 1] = E[Y_0^{synth}]$ , and the latter is observed.

Let's pull up the Kirkpatrick and Benneer paper and look at the synth implementation there.

We'll focus on the intuition of the method - how do we claim that we are identifying a *causal* effect of PACE?