

Determining a Wind Tunnel Calibration Coefficient to Predict the Fluid Velocity and Velocity Profile

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Abstract—This study presents a method of determining airspeed or dynamic pressure when unfavorable pitot static tube conditions are present in addition to characterizing the velocity profile of a given wind tunnel. A pressure transducer is first calibrated using a water manometer to properly measure gauge pressures. The calibrated pressure transducer and Pitot-static probe are used to measure the dynamic and change in static pressure at differing fan speeds in the empty test section. It can be shown from the first law of thermodynamics that the dynamic pressure and the change in static pressure should be proportional. After the experimental data was analyzed, a calibration constant of $K = -0.600 \pm 0.002$ was derived. The Pitot-static probe was then used to measure the dynamic pressure at varying heights in the test section to define the velocity profile. It was found that the velocity profile exhibited signs of uniform flow. This velocity profile pattern was common for the entrance and exit of the test section.

Index Terms—calibration, flow velocity, viscous loss, wind tunnel

I. INTRODUCTION

WIND tunnels have proven to be a valuable tool for predicting the aerodynamic capabilities of objects for over a century [1]. Air is moved through the tunnel and the interactions between the airflow and the object can be used to simulate the actual characteristics of the object in flight. As the velocity of the flowing air can be a major influence on the aerodynamics of the object in the wind tunnel, it is vital to have an accurate understanding of the velocity of the airflow. This can be complicated by the presence of viscous losses and the use of flow conditioning screens which affect the kinetic energy of the fluid. The use of a pitot tube to measure the air velocity would be the simplest choice, but the physical presence of a model in the wind tunnel would disrupt the flow to the pitot tube and cause inaccurate readings.

Using the first law of thermodynamics, a relationship between the dynamic pressure and the static pressure can be established, where q is the dynamic pressure, ΔP is the change in static pressure, ρ is the fluid density, $\dot{Q}_{net,in}$ is the net heat transfer rate, \dot{m} is the mass rate of change, and Δu is the change in fluid velocity (1).

$$q = \Delta P + \frac{\rho \dot{Q}_{net,in}}{\dot{m}} + \rho \Delta u \quad (1)$$

The last two terms, which represent the heat transfer and frictional losses respectively, can be assumed to be proportional to the dynamic pressure by a tunnel calibration coefficient, K (2) [1].

$$q = \Delta P + Kq \quad (2)$$

After rearranging (2), a linear relationship between the dynamic pressure in the test section and the change in the static pressure can be established (3), where m is just an arbitrary constant.

$$q = \frac{1}{1 - K} \Delta P = m \Delta P \quad (3)$$

With this relationship in mind, a calibrated pressure transducer was used to record the dynamic pressure and change in static pressure at various fan speeds. After a linear equation was fitted for the experimental data, the slope of the best-fit line was used to obtain the tunnel calibration coefficient, K . With the tunnel calibration coefficient, the velocity of the fluid could be determined (5) even with the presence of an object in the wind tunnel by knowing the density of the fluid and equating the definition of the dynamic pressure and the linear relationship between pressures accounting for viscous losses (4).

$$q = \frac{\rho V_{\text{flow}}^2}{2} = \frac{1}{1 - K} \Delta P \quad (4)$$

$$V_{\text{flow}} = \sqrt{\frac{2 \Delta P}{\rho(1 - K)}} \quad (5)$$

The first objective of this experiment was to determine the tunnel calibration coefficient of the wind tunnel by measuring the change in static pressure and dynamic pressure inside the test section at various fan speed settings. This would allow future determinations of the velocity of the flow when measurements of the dynamic pressure prove to be impractical due to the presence of models in the test section. The second objective of the experiment was to graph velocity profiles of the flow at the entrance and exit of the test section by establishing a relationship between the dynamic pressure measured by the Pitot-static probe and the velocity of the flow.

II. PROCEDURE

A. Calibrating the Pressure Transducer

Before calibration, the pressure transducer was allowed to warm up and stabilize itself to a zero setting. The ambient pressure was measured, and the humidity and temperature were recorded. After a zero setting was ensured, the heights between the columns of the water manometer were checked for equal height. For positive gauge pressures, a barbed fitting was attached to a valved tee on one leg of the manometer, which was then connected to the port marked "TOTAL" on the pressure transducer. The other port of the pressure transducer, marked "STATIC", was exposed to the ambient environment (Fig. ??).

The pressure selector was set to the zero position and the pressure display was set as close to "0000" using the "Zero" potentiometer. The valved tee was then opened, and a pressure near the maximum differential pressure of 6 inH₂O was then applied to the manometer by pumping the rubber bulb. Once the manometer neared the maximum differential pressure, the valved tee was closed. The differential pressure on the manometer was obtained by recording the difference in the heights of the columns of water. This difference in height was matched to the pressure transducer's display of the differential pressure by adjusting the "SPAN" potentiometer until an identical differential pressure was displayed. The valve was then opened. Once the manometer was level, the "ZERO" setting was adjusted in the case of the final pressure not being sufficiently close to 0. This process was repeated starting with setting the zero position and ending with final adjustments to the "ZERO" setting. Once no final adjustments were needed, the potentiometer settings were locked.

To verify the full range of pressures, the pressure transducer was additionally calibrated to negative gauge pressures using the same process described before but with the configuration of the STATIC and TOTAL ports reversed. To record potential uncertainties, after each calibration, various pressures were measured. The difference in pressure readings was taken for five pressure measurements between the manometer and the pressure transducer in the positive range and five pressure readings in the negative range.

B. Testing for the Calibration Coefficient

Once the pressure transducer was calibrated, the "STATIC" and "TOTAL" ports had their connections disconnected. The pitot static probe was placed in the middle of the test section lengthwise and height wise. The calibration was performed for the wind tunnel settings of 2.5 Hz to 50 Hz in 2.5 Hz intervals. At each wind tunnel setting the dynamic pressure and the ambient pressure difference were taken using a LABVIEW pressure reading software. To measure the dynamic pressure, the tubes marked stagnation and static pitot tube pressure were connected to the "STATIC" port and "TOTAL" port respectively. To measure the ambient pressure difference, the tube marked test section pressure was connected to the "TOTAL" port, the "STATIC" port was left open to air. The LABVIEW software was first used by selecting the bias input while at 0 Hz. The speed was then increased to 2.5 Hz and the dynamic pressure

and ambient pressure difference were recorded by selecting the save button. The data was collected over 5 seconds with 1000 data points being taken per second. This process was repeated until 50 Hz was reached.

C. Forming the Velocity Profile

The "STATIC" and "TOTAL" ports of the transducer were configured in the same manner as the dynamic pressure. The pitot static probe was brought to the front of the test section and was lowered to its minimum height. The pressure difference was then recorded using the LABVIEW pressure reading software. The data was recorded for 5 seconds with 1000 data points per second. After data was recorded, the height of the pitot static probe was increased by 1.5 in. At every increment the same process of data collection was performed. The pitot static probe was then moved to the back of the test section and then lowered to its minimum height. The distance the pitot static probe traveled was recorded. The same incremental process was performed for the pressure readings of the back of the test section.

III. RESULTS

The ambient pressure, P_{amb} , of the test room was measured using a wall-mounted barometer. The temperature, T , and the relative humidity, ϕ , of the room was measured using a digital thermometer and hygrometer placed next to the test section (Table I). The data for the initial calibration of the pressure transducer was gathered by reading the pressure readout on the transducer and by recording the difference of heights on the water manometer (Table I). These two sets of data were then plotted and fitted with a trendline for an accurate depiction of the relation between the two values (Fig. 1). The data appears to be strongly correlated to a linear regression for both positive and negative pressure ranges. It can be noted that at the origin the trendline does not run through the coordinates (0,0).

TABLE I
ATMOSPHERIC CONDITIONS

Parameter	Value	Uncertainty
P_{amb}	760.11 mmHg	0.02 mmHg
T	22 °C	0.1 °C
ϕ	50%	1%

TABLE II
PRESSURE TRANSDUCER CALIBRATION

P_{man} (inH ₂ O)	Uncertainty in P_{man} (inH ₂ O)	P_{ind} (inH ₂ O)	Uncertainty in P_{ind} (inH ₂ O)
-3.40	0.05	-3.405	0.017
-1.35	0.05	-1.460	0.007
-3.60	0.05	-3.613	0.018
-2.10	0.05	-2.217	0.011
-3.55	0.05	-3.512	0.018
3.05	0.05	3.002	0.015
3.60	0.05	3.586	0.018
4.05	0.05	3.922	0.020
3.65	0.05	3.667	0.018
2.40	0.05	2.370	0.012

Fig. 1. Indicated Transducer Gauge Pressure vs. Indicated Manometer Gauge Pressure

The data for the dynamic pressure of the wind tunnel and the change in static pressure were gathered using a computer that was connected to the pressure transducer running a LABVIEW.vi program. For each fan speed, 5000 data points over five seconds were gathered and averaged for each pressure measurement (Fig. 2). The relationship between the two pressures at varying speed appears to be linear. The distance between points is also seen to increase between the points plotted. The data points with the smallest magnitude of gauge pressures correspond to the lowest fan speed with all higher fan speeds coming after it sequentially.

Fig. 2. Dynamic Pressure vs. Change in Static Pressure

To measure the velocity profile, the dynamic pressure at each indicated height was averaged from the LABVIEW.vi program. The data was measured every 1.5 in starting at an indicated ruler height of 1.5 in ± 0.05 in. This starting height of 1.5 in corresponded to the lowest possible position that the Pitot-static probe could be positioned (Fig. ??). The horizontal distance between the front and the back of the test section was recorded as 43 in ± 0.05 in (Table T). At the front of the test section, the dynamic pressure was noted to be non-zero at the Pitot-static probe's lowest position. This observation was consistent with the back of the test section which also provided a lower non-zero dynamic pressure reading. After the first height change, the pressure reached a stable value. This value fluctuated in small amounts but did exhibit large changes relative to the initial change. After collecting the data for the velocity profile, the maximum pressure reached at the back end of the test section was reported as being slightly higher than that of the pressure at the front end of the test section (Table T).

TABLE III
PRESSURE TRANSDUCER CALIBRATION

Height (inches)	q_{front} (inH ₂ O)	Uncertainty in q_{front} (inH ₂ O)	q_{back} (inH ₂ O)	Uncertainty in q_{back} (inH ₂ O)
1.5	0.965	0.002	0.636	0.002
3	1.158	0.002	1.191	0.002
4.5	1.158	0.002	1.188	0.002
6	1.153	0.002	1.189	0.002
7.5	1.156	0.002	1.195	0.002
9	1.163	0.002	1.202	0.002
10.5	1.164	0.002	1.225	0.002

IV. DISCUSSION

A. Pressure Transducer Calibration Accuracy

Five calibration points each were taken in the positive and negative pressure differential ranges. The transducer calibration curve (Fig. 1) was plotted to obtain an understanding of how similarly the pressure transducer was outputting gauge pressures when compared to the manometer. With an R^2 value of 0.9996, this indicated that the linear regression matched very well with

the experimental calibration data. One observation is that the slope of the line of best fit (1.005) was very close to unity. This indicated that the span of the pressure transducer matched well with the physical manometer for both the positive and negative range of gauge pressures. Despite best attempts to adjust the zero potentiometer on the pressure transducer to match the resting position of the manometer, the y-intercept of the equation was -0.0373 . This indicated that there may have been some slight systematic bias in the pressure transducer going from the positive to negative ranges as the expected y-intercept was zero. This potential systematic bias was accounted for by taring all additional pressure readings against the ambient pressure reading while the fan was not powered on.

B. Tunnel Calibration Coefficient

During the experiment, the change in static pressure (ΔP) and the dynamic pressure (q) were recorded for 19 different fan speed settings as seen in Table T. A Monte Carlo simulation was run by simulating 10000 data sets of the pressures considering the uncertainty in the pressure readings (Fig.3). A linear regression was fitted to each data set and a statistical analysis of the linear regressions yielded a mean slope (\bar{m}) of 0.6249 ± 0.0006 . Eq. (3) can be manipulated to solve for the tunnel calibration coefficient, K (6). From the value of the mean slope, it was found that for the specific wind tunnel used, the tunnel calibration coefficient was 0.600 ± 0.002 (See Appendix for uncertainty calculation for K).

$$K = 1 - \frac{1}{\bar{m}} \quad (6)$$

Fig. 3. Graphical result from Monte Carlo simulation for linear relationship between the dynamic pressure, q , and the change in static pressure, ΔP .

TABLE IV
MONTE-CARLO DATA POINTS

ΔP (inH ₂ O)	Uncertainty in ΔP (inH ₂ O)	q (inH ₂ O)	Uncertainty in q (inH ₂ O)
0.013	0.002	-0.034	0.002
0.091	0.002	-0.005	0.002
0.202	0.002	0.041	0.002
0.339	0.002	0.107	0.002
0.509	0.002	0.193	0.002
0.708	0.002	0.301	0.002
0.938	0.002	0.428	0.003
1.197	0.002	0.579	0.002
1.493	0.002	0.752	0.002
1.816	0.002	0.947	0.002
2.172	0.002	1.170	0.002
2.563	0.002	1.412	0.002
2.984	0.002	1.682	0.002
3.436	0.002	1.972	0.002
3.913	0.002	2.286	0.002
4.417	0.002	2.620	0.002
4.951	0.002	2.981	0.002
5.506	0.002	3.357	0.002

C. Velocity Profile of the Wind Tunnel Test Section

To determine the fluid velocities at each location in the wind tunnel, it was first necessary to determine the density of

the fluid. First, a second-order polynomial was used to find the saturation pressure, P_g , based on the ambient temperature, T (7) [3]. This yielded a saturation pressure of 2641 ± 16 Pa.

$$P_g = 4.94(T - 273.15)^2 + 66.3(T - 273.15) + 1489 \quad (7)$$

Then, an equation that accounted for the relative humidity in the room was used to determine the fluid density, ρ , where P_{amb} was the ambient pressure in the room, ϕ was the relative humidity, R_{air} was the specific gas constant for air, and R_{vapor} was the specific gas constant for the water vapor in the air (8) [3]. This gave a fluid density of 1.191 ± 0.004 kg/m³.

$$\rho = \frac{P_{\text{amb}}}{R_{\text{air}}T} + \frac{\phi}{100} \frac{P_g}{T} \left(\frac{1}{R_{\text{vapor}}} - \frac{1}{R_{\text{air}}} \right) \quad (8)$$

The velocity of the air at a specific point, V_{flow} , could then be determined by using the definition of dynamic pressure (9) [1]. Table III summarizes the derived flow velocity for the different positions that the pitot tube was placed in the test section of the wind tunnel while figure 4 shows the general shape of the velocity profile found at the front and back of the test section of the wind tunnel.

$$V_{\text{flow}} = \sqrt{\frac{2q}{\rho}} \quad (9)$$

TABLE V
VELOCITY PROFILE

Vertical Position of Pitot Tube in Test Section (in)	Front of Test Section		Back of Test Section	
	V_{front} (m/s)	μV_{front} (m/s)	V_{back} (m/s)	μV_{back} (m/s)
0.0	20.10	0.04	16.31	0.04
1.5	22.01	0.04	22.32	0.04
3.0	22.01	0.04	22.30	0.04
4.5	21.96	0.04	22.30	0.04
6.0	22.00	0.04	22.36	0.04
7.5	22.05	0.04	22.43	0.04
9.0	22.06	0.04	22.63	0.04

Fig. 4. Velocity Profile at the front and back of the test section

Fig. 4 shows that the air exhibited approximately uniform flow as expected. The air is moving slower at the walls which indicates the presence of viscous forces at the walls of the test section as predicted [1]. Classic aerodynamic theory indicates that the velocity at the wall should be zero. The deviation between the experimental results and theory likely stems from the diameter of the Pitot tube creating an offset and preventing a true reading at the bottom wall of the test section. It should be noted that due to the geometry of the Pitot-Static probe, a reading at the top wall of the test section could not be obtained. One observation that can be made from Fig. 4 is that the velocities at the back of the test section were generally higher than the at the front. This difference could have been due to heat addition from the ambient environment to the air inside

the wind tunnel causing it to speed up. It was observed that the temperature of the ambient environment had gradually increased over the duration of the experiment. This heat addition could be attributed to the presence of people in the wind tunnel laboratory and the operation of the wind tunnels themselves adding heat to the flow in the test section.

V. CONCLUSION

For the first part of the experiment, the value of the tunnel calibration coefficient was found to be -0.600 ± 0.002 . The determination of the tunnel calibration coefficient will allow future experiments to determine the velocity of the flow without the use of a Pitot-static probe in the test-section. A simple measurement of the change in static pressure between the ambient environment and the test section can be interpolated with the tunnel calibration coefficient to obtain a corresponding dynamic pressure from which the flow velocity can be calculated. For the second part of the experiment, the velocity profiles at the entrance and exit of the test section exhibited signs of uniform flow as expected. The observation that the flow velocities at the exit were slightly greater than those at the entrance indicated the presence of an external factor that was adding kinetic energy to the flow. If this experiment were to be repeated, additional mitigations, like thermal insulation, could be put into place to ensure steady adiabatic conditions that would help to reduce any systematic biases in the results.

APPENDIX A: UNCERTAINTY CALCULATION

TABLE VI
SUMMARY OF MEASUREMENT UNCERTAINTIES

Parameter	Symbol	Justification	Uncertainty
Transducer Calibration	μP_{ind}	Manual	0.5% P_{ind}
Manometer Reading	μP_{man}	Half of interval	0.05 inH ₂ O
Temperature	μT	Digital	0.1 °C
Humidity	$\mu \phi$	Digital	1%
Ambient Pressure	μP_{amb}	Barometer	0.02 mm
Dynamic Pressure	μq	95% Conf. Int.	Variable, ~ 0.002 inH ₂ O
Static Pressure Difference	$\mu \Delta P$	95% Conf. Int.	Variable, ~ 0.002 inH ₂ O
Tunnel Calibration Slope	μm	Monte Carlo	0.0006
Tunnel Calibration Coefficient	μK	RSS	0.002
Saturation Pressure	μP_g	RSS	16 Pa
Density	$\mu \rho$	RSS	0.004 kg/m ³
Flow Velocity	μV_{flow}	RSS	Variable, ~ 0.04 m/s

The uncertainty for the Dynamic Pressure (q) and the Static Pressure Difference (ΔP) was obtained using a 95% confidence interval with a normal distribution. A normal distribution was used instead of a student's t -distribution as the sample size of 5000 was deemed sufficiently large that the sample distribution approach the normal distribution due to the central limit theorem [2]. A z value of 1.96 was used for the calculation of the 95% confidence interval [2]. The margin of error then

served as the uncertainty, where μX is the margin of error for an arbitrary measurement, S_x is the sample standard deviation, and n is the number of samples (10). For both pressure readings, the margin of error, after rounding to the nearest thousandth, was consistently 0.002 except for one specific sample of the dynamic pressure ($q_i = 0.428$ inH₂O at the 20 Hz fan setting) where it was 0.003.

$$\mu X = z \frac{S_x}{\sqrt{n}} \quad (10)$$

The uncertainty for the tunnel calibration coefficient (K) can be calculated using the RSS method, where m is the tunnel calibration slope obtained from the line of best fit of the dynamic Pressure vs. static pressure difference plot (Fig. 2) (11).

$$\mu K = \left[\left(\mu m \frac{\partial K}{\partial m} \right)^2 \right]^{1/2} = -\frac{\mu m}{m^2} \quad (11)$$

The uncertainty for the saturation pressure (P_g) can be calculated using the RSS method, where T is the ambient temperature (12).

$$\mu P_g = \left[\left(\mu T \frac{\partial P_g}{\partial T} \right)^2 \right]^{1/2} \quad (12)$$

The uncertainty for the fluid density (ρ) can be calculated using the RSS method, where P is the ambient pressure, T is the ambient temperature, ϕ is the relative humidity, and P_g is the saturation pressure (13).

$$\mu \rho = \left[\left(\mu P \frac{\partial \rho}{\partial P} \right)^2 + \left(\mu T \frac{\partial \rho}{\partial T} \right)^2 + \left(\mu \phi \frac{\partial \rho}{\partial \phi} \right)^2 + \left(\mu P_g \frac{\partial \rho}{\partial P_g} \right)^2 \right]^{1/2} \quad (13)$$

The uncertainty for the velocity of the fluid (V_{flow}) can be calculated using the RSS method, where q is the dynamic pressure and ρ is the fluid density (14). The uncertainty, while technically a distinct value for each value of the fluid velocity, was consistently ± 0.04 m/s when rounded to the nearest hundredth.

$$\mu V_{\text{flow}} = \left[\left(\mu q \frac{\partial V_{\text{flow}}}{\partial q} \right)^2 + \left(\mu \rho \frac{\partial V_{\text{flow}}}{\partial \rho} \right)^2 \right]^{1/2} \quad (14)$$

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