

# COS 4807 Assignment 1

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## 1 Abstract

hello

## 2 Introduction

Human attempts to mathematically predict life expectancy is not a new endeavour. Gompertz (1825) introduced an equation to predict life expectancy, which was modified in Makeham (1860) to create the famous Gompertz–Makeham law.

Why use machine learning? find relationships that regression analysis cannot Chen & Asch (2017).

Machine learning is used in medicine Chen & Asch (2017).

life expectancy vs mortality rate?

cohort life expectancy vs period life expectancy (<https://ourworldindata.org/life-expectancy-how-is-it-calculated-and-how-should-it-be-interpreted>)

Rajkomar et al. (2018) Google uses machine learning to predict in hospital medical events for patients.

## 3 Literature Review

Forecasting Mortality in Developed Countries Tableau 2001

### 3.1 Life tables

A life table is a table given for a specific year that contains the probability that a person of a certain age will die in that specific year. Life tables are also called actuarial tables and are used by actuaries in the life insurance industry. Table 1 is an example of a life table taken from Arias (2007).

Seminal work Fergany (1971).

<https://www.mortality.org/> place to find mortality info for developed countries

### 3.2 Used Life Tables

Luy et al. (2019)

### 3.3 ?Grossman?

2017 determinants of health: an economic perspective ???? 1972 The Demand for Health: A Theoretical and Empirical Investigation,

Grossman (2000)

### 3.4 Life expectancy projections

The United Nations use a Bayesian model to predict future life expectancy (Raftery et al. 2014).

Lee Carter method Shang et al. (2011) later extended into the Li-Lee model

Siminal work Lee & Carter (1992)

Bongaarts (2005)

### 3.5 Determinants of life expectancy

#### 3.5.1 Income

The relationship between income and life expectancy has been given a lot of attention in academic circles (Preston 1975, Hu et al. 2015, Chetty et al. 2016, Oeppen 2019).

Preston (1975) was the first to show the relationship between life expectancy and per capita income. His original curve can be seen in Figure 1. As we can see from Figure 1, for low income countries, life expectancy increases rapidly with per capita income. Whereas in high income countries a small increase in per capita income does not have a large effect on life expectancy.

This relationship has also been shown in more recent studies (Chetty et al. 2016, Oeppen 2019). Even though Shkolnikov et al. (2019) found that in Russia the Preston curve is not an accurate predictor of life expectancy. They found that the actual life expectancy should be “substantially higher” when comparing to the Preston curve predicted value.

Studies in first world countries involving mortality rather than life expectancy have also found a relationship with income level (Blakely et al. 2004, Kalwij et al. 2013, von Gaudecker & Scholz 2007).

Just 16% of the increase in life expectancy between 1930s and 1960s could be explained by rising income levels Preston (1975). Which seems to indicate that a countries life expectancy is dependant on more than income levels.

Kalwij (2014)

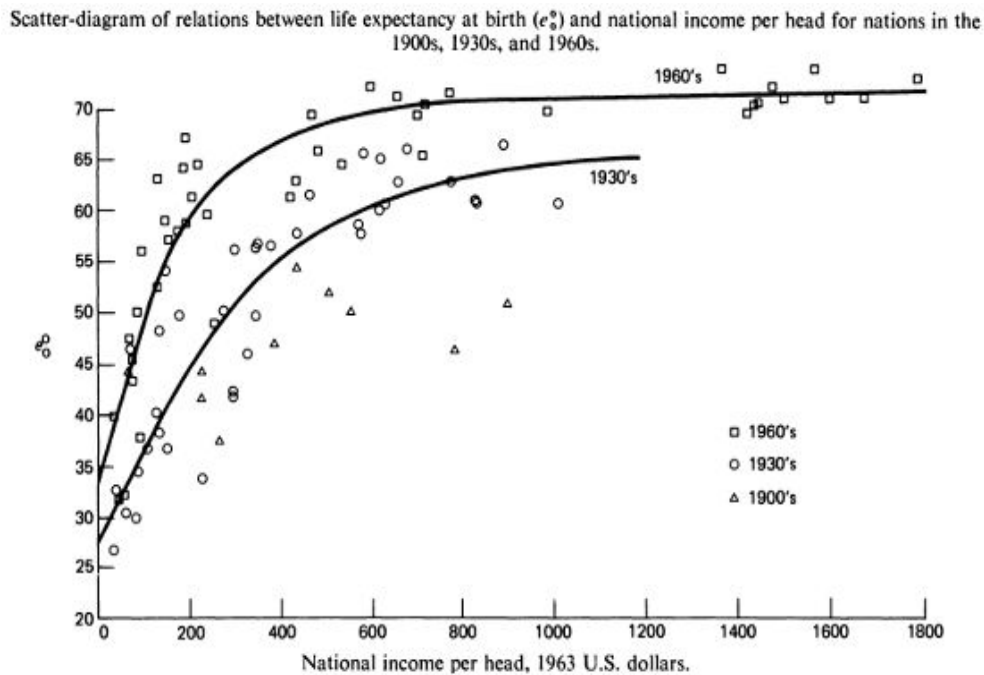


Figure 1: The original Preston curve from Preston (1975)

Oeppen (2019) Very Good!!

Preston (1975) is a seminal work according to Oeppen (2019)

inequality Hu et al. (2015)

Chetty et al. (2016) in the US

income inequality does not affect health of a country Jason Beckfield (2004)

Tarkiainen et al. (2012) (To be downloaded)

### 3.5.2 Education attainment

Kaplan et al. (2015) investigated the relationship between educational attainment and life expectancy in eight states in the United States. They found that even when controlling for variables like income, race, sex and common medical issues like cardiovascular disease, the relationship between educational attainment and life expectancy remains statistically significant.

Luy et al. (2019) studied 3 developed nations, namely the United States, Italy and Denmark. They have also found a strong correlation between education levels and longevity.

But what is the nature of this correlation? According to Deary & Gottfredson (2004) Intelligence Quotient or IQ could explain the association. While Hayward et al. (2015) does not believe in a “causal relationship” but rather that it depends on factors like “time, place, and the social environment”.

In an attempt to find a causal relationship between education and life expectancy, van Kippersluis et al. (2011) investigated the result of the Netherlands increasing the mandatory number of years a child had to attend school to 7 years. It was 6 years previously. van Kippersluis et al. (2011) found a decrease in mortality of 3% for 81 year old males who had the additional year of schooling.

This relationship appears strongest in more developed countries where the life expectancy is already above 60 years (Bulled & Sosis 2010). In these countries, any educational investment leads to greater compensation for the learner than they would get in a less developed country Bulled & Sosis (2010), Handwerker (1986). In addition, Kabir (2008) also studied this relationship, among others, with regards to developing countries and did not find a correlation.

The question remains, which educational indicators should be used when investigating the relationship between education and life expectancy?

Various educational indicators have been used in the literature for comparing to life expectancy. One approach is to use the International Classification of Education (ISCED) system (UNESCO Institute for Statistics 2012). The ISCED 2011 standard consists of 9 levels ranging from ISCED level 0 (Early childhood education) to ISCED level 8 (Doctoral or equivalent level).

Luy et al. (2019) used the United Nations ISCED-97 (consisting of 7 levels) scale to break education attainment down into 3 levels namely Low (None to Lower Secondary), Medium (Upper secondary) and High (Tertiary education). In van Kippersluis et al. (2011) the Dutch SOI system (Standaard Onderwijs Indeling).

Which according to van Kippersluis et al. (2011) is similar to the ISCED system. While in Deboosere et al. (2009) educational attainment was broken into 5 levels also ranging from no education to Tertiary education.

Kaplan et al. (2015) broke educational attainment into 4 levels ranging from less than high school to college graduate.

In the study Bulled & Sosis (2010), the relationship between educational investments and fertility against life expectancy, over 193 countries, was investigated. They used adult literacy and the enrolment ratios for primary, secondary and tertiary schooling.

helping individuals to mobilise health resources Elo & Preston (1996) from Deboosere et al. (2009)

Study in Belgium Deboosere et al. (2009)

Inverse relationship Hoque et al. (2019)

netherlands van Kippersluis et al. (2011)

van Baal et al. (2016)

### **3.5.3 Per capita spending on health**

Shaw et al. (2005) showed that pharmaceutical expenditures shows a positive correlation with life expectancy in OECD countries.

medical spending Cutler et al. (2006)

### **3.5.4 Access to safe drinking water**

### **3.5.5 Infant mortality**

Centers for Disease Control & Prevention (1999)

### **3.5.6 Turmoil**

(Low et al. 2008) p211

## **3.6 The gender gap**

Rochelle et al. (2015)

## **3.7 Unemployment**

unemployment Bonamore et al. (2015) Roelfs et al. (2011) Roelfs et al. (2015)

## **4 Methodology/Procedure**

There are many studies that attempt to extrapolate future life expectancy for countries based on current data. This includes studies for high income countries (Kontis et al. 2017) and low income countries ???cite.

This study will attempt to create a model that can predict life expectancy for a country based on various socio-economic conditions in the country.

segment data into groups where each group has the same amount of data points???

Unlike Shaw et al. (2005), this study will not take into account the age distribution of each country.

As for HDI from Bulled & Sosis (2010) Adult literacy rate

primary secondary and tertiary enrolment ratios

GDP per Capita (Purchasing power parity )

“National datasets must be regarded with some level of caution as data gaps and issues of inconsistency and incoherence remain owing to differences in the effectiveness of infrastructure, political agendas, and additional factors, such as internal conflicts” Bulled & Sosis (2010)

The impact of finishing secondary school is different before vs after the second world war Deboosere et al. (2009)

## 4.1 Choice of dataset

## 4.2 Regression

## 4.3 k-Nearest Neighbour

## 4.4 Support Vector Machines

## 4.5 Cross-validation

# 5 Analysis

# 6 Conclusion

# 7 Recommendations

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## Appendices

Table 1: Life table for the total population: United States, 2003  
(Arias 2007)

	Probability of dying between ages $x$ to $x+1$	Number surviving to age $x$	Number dying between ages $x$ to $x+1$	Person-years lived between ages $x$ to $x+1$	Total number of person-years lived above age $x$	Expectation of life at age $x$
Age	$q(x)$	$l(x)$	$d(x)$	$L(x)$	$T(x)$	$e(x)$
0-1	0.006865	100,000	687	99,394	7,743,016	77.4
1-2	0.000469	99,313	47	99,290	7,643,622	77.0
2-3	0.000337	99,267	33	99,250	7,544,332	76.0
3-4	0.000254	99,233	25	99,221	7,445,082	75.0
4-5	0.000194	99,208	19	99,199	7,345,861	74.0
5-6	0.000177	99,189	18	99,180	7,246,663	73.1
6-7	0.000160	99,171	16	99,163	7,147,482	72.1
7-8	0.000147	99,156	15	99,148	7,048,319	71.1
8-9	0.000132	99,141	13	99,134	6,949,171	70.1
9-10	0.000117	99,128	12	99,122	6,850,036	69.1
10-11	0.000109	99,116	11	99,111	6,750,914	68.1
11-12	0.000118	99,105	12	99,100	6,651,803	67.1
12-13	0.000157	99,094	16	99,086	6,552,704	66.1
13-14	0.000233	99,078	23	99,067	6,453,618	65.1
14-15	0.000339	99,055	34	99,038	6,354,551	64.2
15-16	0.000460	99,022	46	98,999	6,255,513	63.2
16-17	0.000577	98,976	57	98,947	6,156,514	62.2



17-18	0.000684	98,919	68	98,885	6,057,566	61.2
18-19	0.000769	98,851	76	98,813	5,958,681	60.3
19-20	0.000832	98,775	82	98,734	5,859,868	59.3
20-21	0.000894	98,693	88	98,649	5,761,134	58.4
21-22	0.000954	98,605	94	98,558	5,662,485	57.4
22-23	0.000990	98,511	98	98,462	5,563,928	56.5
23-24	0.000997	98,413	98	98,364	5,465,466	55.5
24-25	0.000982	98,315	97	98,267	5,367,101	54.6
25-26	0.000960	98,219	94	98,171	5,268,835	53.6
26-27	0.000942	98,124	92	98,078	5,170,663	52.7
27-28	0.000936	98,032	92	97,986	5,072,585	51.7
28-29	0.000947	97,940	93	97,894	4,974,599	50.8
29-30	0.000974	97,847	95	97,800	4,876,705	49.8
30-31	0.001008	97,752	98	97,703	4,778,906	48.9
31-32	0.001046	97,654	102	97,603	4,681,203	47.9
32-33	0.001097	97,551	107	97,498	4,583,600	47.0
33-34	0.001162	97,444	113	97,388	4,486,102	46.0
34-35	0.001244	97,331	121	97,271	4,388,715	45.1
35-36	0.001336	97,210	130	97,145	4,291,444	44.1
36-37	0.001441	97,080	140	97,010	4,194,299	43.2
37-38	0.001567	96,940	152	96,864	4,097,289	42.3
38-39	0.001714	96,788	166	96,705	4,000,424	41.3
39-40	0.001874	96,623	181	96,532	3,903,719	40.4
40-41	0.002038	96,442	197	96,343	3,807,187	39.5
41-42	0.002207	96,245	212	96,139	3,710,844	38.6
42-43	0.002389	96,033	229	95,918	3,614,705	37.6
43-44	0.002593	95,803	248	95,679	3,518,787	36.7
44-45	0.002819	95,555	269	95,420	3,423,108	35.8
45-46	0.003064	95,285	292	95,139	3,327,688	34.9
46-47	0.003322	94,993	316	94,836	3,232,548	34.0
47-48	0.003589	94,678	340	94,508	3,137,713	33.1
48-49	0.003863	94,338	364	94,156	3,043,205	32.3
49-50	0.004148	93,974	390	93,779	2,949,049	31.4
50-51	0.004458	93,584	417	93,375	2,855,270	30.5
51-52	0.004800	93,167	447	92,943	2,761,895	29.6
52-53	0.005165	92,719	479	92,480	2,668,952	28.8
53-54	0.005554	92,241	512	91,984	2,576,472	27.9
54-55	0.005971	91,728	548	91,454	2,484,487	27.1
55-56	0.006423	91,181	586	90,888	2,393,033	26.2
56-57	0.006925	90,595	627	90,281	2,302,145	25.4
57-58	0.007496	89,968	674	89,630	2,211,864	24.6
58-59	0.008160	89,293	729	88,929	2,122,234	23.8
59-60	0.008927	88,565	791	88,169	2,033,305	23.0
60-61	0.009827	87,774	863	87,343	1,945,136	22.2
61-62	0.010831	86,911	941	86,441	1,857,793	21.4
62-63	0.011872	85,970	1021	85,460	1,771,352	20.6
63-64	0.012891	84,949	1095	84,402	1,685,892	19.8
64-65	0.013908	83,854	1166	83,271	1,601,490	19.1
65-66	0.015003	82,688	1241	82,068	1,518,219	18.4
66-67	0.016267	81,448	1325	80,785	1,436,151	17.6
67-68	0.017699	80,123	1418	79,414	1,355,366	16.9
68-69	0.019320	78,705	1521	77,944	1,275,953	16.2
69-70	0.021108	77,184	1629	76,369	1,198,008	15.5
70-71	0.022950	75,555	1734	74,688	1,121,639	14.8
71-72	0.024904	73,821	1838	72,902	1,046,951	14.2
72-73	0.027151	71,982	1954	71,005	974,050	13.5
73-74	0.029784	70,028	2086	68,985	903,044	12.9
74-75	0.032753	67,942	2225	66,830	834,059	12.3
75-76	0.035831	65,717	2355	64,540	767,230	11.7
76-77	0.038987	63,362	2470	62,127	702,690	11.1

77-78	0.042503	60,892	2588	59,598	640,563	10.5
78-79	0.046557	58,304	2714	56,947	580,965	10.0
79-80	0.051200	55,589	2846	54,166	524,019	9.4
80-81	0.056335	52,743	2971	51,258	469,853	8.9
81-82	0.061837	49,772	3078	48,233	418,595	8.4
82-83	0.067856	46,694	3168	45,110	370,362	7.9
83-84	0.074504	43,526	3243	41,904	325,252	7.5
84-85	0.081975	40,283	3302	38,632	283,348	7.0
85-86	0.089682	36,981	3317	35,322	244,716	6.6
86-87	0.098031	33,664	3300	32,014	209,394	6.2
87-88	0.107059	30,364	3251	28,739	177,380	5.8
88-89	0.116804	27,113	3167	25,530	148,641	5.5
89-90	0.127300	23,946	3048	22,422	123,111	5.1
90-91	0.138581	20,898	2896	19,450	100,689	4.8
91-92	0.150676	18,002	2712	16,646	81,239	4.5
92-93	0.163611	15,289	2502	14,039	64,594	4.2
93-94	0.177408	12,788	2269	11,654	50,555	4.0
94-95	0.192080	10,519	2021	9,509	38,901	3.7
95-96	0.207636	8,499	1765	7,616	29,392	3.5
96-97	0.224075	6,734	1509	5,980	21,776	3.2
97-98	0.241387	5,225	1261	4,594	15,796	3.0
98-99	0.259552	3,964	1029	3,449	11,202	2.8
99-100	0.278539	2,935	818	2,526	7,752	2.6
100+	1.00000	2,118	2118	5,226	5,226	2.5