

EEE 133 Key concepts and Equations

Aj Mesa Jr.

October 8, 2020

1 Diode Models and Circuits

1.1 History of Electronics

1. 1904: John Fleming invented vacuum tubes. First time electron flow is controlled in non-conducting medium
 - (a) if the cathode is heated, some electrons can escape
 - (b) if a voltage is applied (+) on anode (–) on cathode, there will be current
2. 1906: the grid was added to control the current between the anode and cathode
 - (a) vacuum tubes allowed the development of amplifiers, transmitters, receivers, signal processor
3. 1946: the ENIAC computer was completed. it could execute 5000 additions per second
4. 1947: invention of transistor by Shockley, Bardeen, Brattain at the Bell Labs
 - (a) they were point-contact transistors
5. 1948: Schockley invented the BJT. the BJT is monolithic (containted in a single semiconductor crystal)
6. 1958: the first Integrated Circuits (IC) was invented by Jack Kilby of Texas Instruments (non-monolithic)
7. 1959: the first monolithic IC was developed by Robert Noyce at Fairchild Semiconduction
 - (a) uses silicon instead of germanium
 - (b) 2 interconnected BJT transistor
 - (c) SiO_2 insulator, Al interconnection
 - (d) planar IC, 0.06 in diameter
8. Bipolar ICs with BJT devices domidated until early 80s
 - (a) S/M/L Scale Integration : 10, 100, 1000 transistors
9. 1959: MOS ICs started in the 60s after the MOS transistor was developoed at Bell Labs
 - (a) easier to fabricate than bipolar
 - (b) uses less power
 - (c) can fit more transistor in the same silicon area
 - (d) slower than bipolar IC
 - (e) less robust than bipolar IC

10. MOS ICs

- (a) early 70s: MOS technology improved in speed and reliability
- (b) first microprocessor: Intel 4004 (1971)
- (c) emergence of VLSI (>10000 transistors)
- (d) microprocessors evolved into microcontrollers (MCUs) and system on a chip (SOCs)

11. Moore's Law: the transistor density would double every two years

1.2 Piecewise Linear Diode Models

1. 1st Approximation: (when $v_s \gg V_T$)

- (a) Open when $v_D < 0$
- (b) Short when $v_D \geq 0$

2. 2nd Approximation (when above condition not satisfied):

- (a) Open when $v_D < V_T$
- (b) Voltage of V_T when $v_D \geq V_T$

3. 3rd Approximation (2nd with resistor R in series)

- (a) Open when $v_D < V_T$
- (b) Voltage of V_T in series with resistance R when $v_D \geq V_T$

4. To determine diode state:

- (a) Assume it is conducting
- (b) Check direction of current
- (c) If current is from anode to cathode, the assumption is correct and equivalent circuit is valid
- (d) Otherwise, diode should be open

5. Another method:

- (a) Replace diode with open circuit
- (b) Determine the voltage across the diode terminals (+) on anode, (−) on cathode
- (c) If $v_D < \text{the needed threshold}$, assumption is correct
- (d) Otherwise, diode should be replaced with the appropriate model

1.3 Practical Diode Circuits

1. Half Wave Rectifier

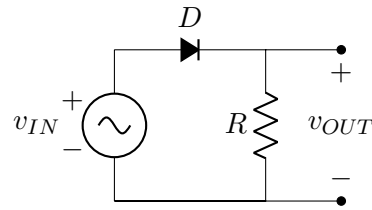


Figure 1: Half Wave Rectifier

(a) When diode is IDEAL:

$$v_{OUT} = \begin{cases} 0, & v_{IN} < 0 \\ v_{IN} & v_{IN} \geq 0 \end{cases}$$

(b) When diode has constant voltage model:

$$v_{OUT} = \begin{cases} 0, & v_{IN} < V_T \\ v_{IN} - V_T & v_{IN} \geq V_T \end{cases}$$

2. Full Wave Rectifier ($v_1 = v_2$)

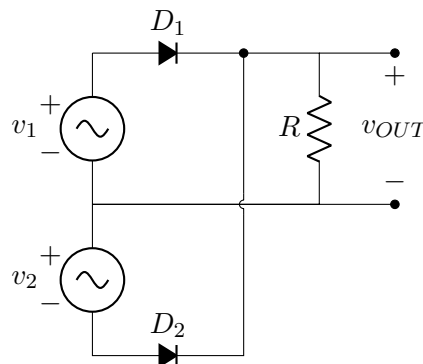


Figure 2: Full Wave Rectifier

(a) When diode is IDEAL:

$$v_{OUT} = |v_{IN}|$$

(b) When diode has constant voltage model:

$$v_{OUT} = \begin{cases} v_1 - V_T, & v_1 > V_T \\ -v_2 - V_T, & v_2 < -V_T \\ 0 & \text{otherwise} \end{cases}$$

(c) This requires a transformer with center-tapped secondary ($n_1 : n_2 = 1 : 2$)

3. Full Wave Bridge Rectifier

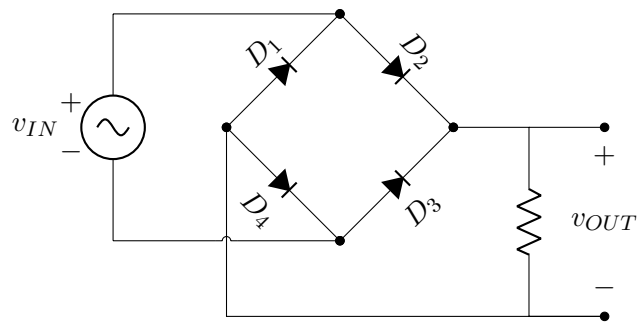


Figure 3: Full Wave Bridge Rectifier

(a) When diode is IDEAL:

$$v_{OUT} = |v_{IN}|$$

(b) When diode has constant voltage model:

$$v_{OUT} = \begin{cases} v_1 - 2V_T, & v_1 > 2V_T \\ -v_2 - 2V_T, & v_2 < -2V_T \\ 0 & \text{otherwise} \end{cases}$$

4. Positive Clipper

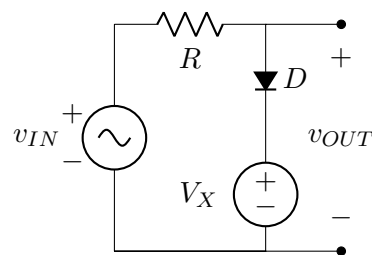


Figure 4: Positive Clipper

$$(a) \ v_{OUT} = \begin{cases} V_X + V_T, & v_{IN} - V_X > V_T \\ v_{IN}, & v_{IN} - V_X < V_T \end{cases}$$

5. Negative Clipper

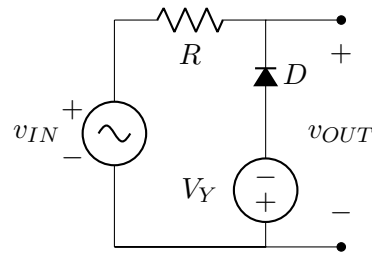


Figure 5: Negative Clipper

$$(a) v_{OUT} = \begin{cases} -(V_Y + V_T), & -V_Y - v_{IN} > V_T \\ v_{IN}, & -V_Y - v_{IN} < V_T \end{cases}$$

6. The positive and negative clippers can be combined

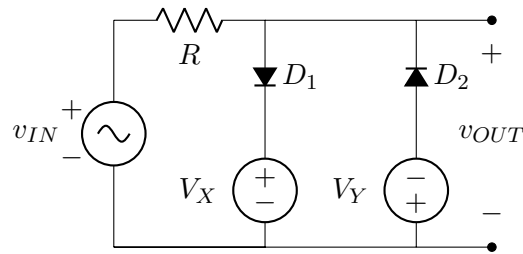


Figure 6: Positive and Negative Clipper

$$(a) v_{OUT} = \begin{cases} V_X + V_T, & v_{IN} - V_X > V_T \\ -(V_Y + V_T), & -V_Y - v_{IN} > V_T \\ v_{IN}, & \text{otherwise} \end{cases}$$

7. Peak Detector

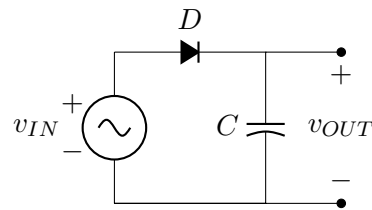


Figure 7: Peak Detector

(a) Let the time t_1 be the first time the input reaches its maximum value V_P and t_0 be the time to reach V_T

(b) When diode is IDEAL:

$$v_{OUT} = \begin{cases} v_{IN}, & t < t_1 \\ V_P, & t \geq t_1 \end{cases}$$

(c) When diode has constant voltage model:

$$v_{OUT} = \begin{cases} 0, & 0 \leq t < t_0 \\ v_{IN} - V_T, & t_0 \leq t < t_1 \\ V_P - V_T & t_1 \leq t \end{cases}$$

8. Peak Detector with Load Resistor (Ideal Diode)

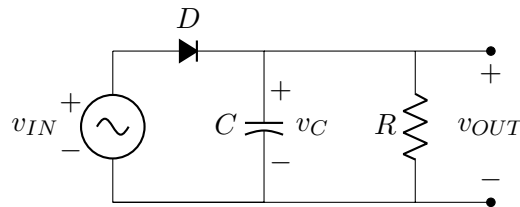


Figure 8: Peak Detector with load resistor

(a) Let the time t_1 be the first time the input reaches its maximum value V_P and the period be T . When the capacitor voltage decays, let time t_2 be when $v_C = v_{IN}$ again

$$(b) v_{OUT} = \begin{cases} v_{IN}, & t < t_1 \\ V_P \exp\left(-\frac{t}{RC}\right), & t_1 \leq t < t_2 \\ v_{IN}, & t_2 \leq t < t_1 + T \\ V_P \exp\left(-\frac{t}{RC}\right), & t_1 + T \leq t < t_2 + T \\ \vdots \end{cases}$$

9. Negative Clamper (ideal diode)

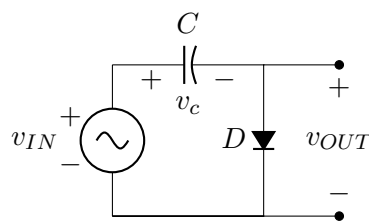


Figure 9: Negative Clamper

(a) Let the time t_1 be the first time the input reaches its maximum value V_P

(b) This is similar to the peak detector, only that $v_{OUT} = v_{IN} - v_C$ where v_C follows the characteristic of the peak detector

$$(c) v_C = \begin{cases} v_{IN}, & t < t_1 \\ V_P, & t_1 \leq t \end{cases}$$

$$(d) v_{OUT} = \begin{cases} 0, & t < t_1 \\ v_{IN} - V_P, & t \geq t_1 \end{cases}$$

10. Positive Clamper (ideal diode)

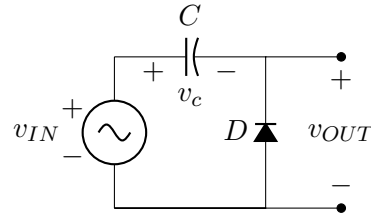


Figure 10: Positive Clamper

(a) Let the period be T

$$(b) v_C = \begin{cases} 0, & 0 \leq t < T/2 \\ v_{IN}, & T/2 \leq t < 3T/4 \\ -V_P, & 3T/4 \leq t \end{cases}$$

$$(c) v_{OUT} = \begin{cases} v_{IN}, & 0 \leq t < T/2 \\ 0, & T/2 \leq t < 3T/4 \\ v_{IN} + V_P, & 3T/4 \leq t \end{cases}$$

1.4 Exponential Diode Model

1. Shockley's Diode Equation

$$i_D = I_S \left[\exp \left(\frac{v_D}{\eta V_T} \right) - 1 \right] \quad (1)$$

(a) v_D : diode voltage with positive at anode

(b) i_D : diode current from anode to cathode

(c) I_S : reverse saturation current due to minority carriers. $10^{-15} \text{A} < I_s < 10^{-9} \text{A}$

(d) η : ideality factor, $1 < \eta < 2$; close to 1 for well fabricated diodes

(e) V_T : thermal voltage, $V_T = \frac{kT_K}{e} \approx \frac{T_K}{11600}$

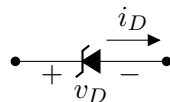
2. for typical operating voltages (forward biased): $\exp \left(\frac{v_D}{\eta V_T} \right) \gg 1 \Rightarrow i_D \approx I_S \exp \left(\frac{v_D}{\eta V_T} \right)$

3. for typical reverse bias voltages, $\exp \left(\frac{v_D}{\eta V_T} \right) \ll 1 \Rightarrow i_D \approx -I_S$

1.5 Small Signal Model

1. $v_D = V_D + v_d$
2. $i_D = I_D + i_d$. I_D is calculated using large signal analysis
3. if the amplitude of v_d is very small, the diode characteristic equation is approximately a line with conductance $g_d = \frac{\partial i_D}{\partial v_D} = \frac{I_S}{\eta V_T} \exp\left(\frac{v_D}{\eta V_T}\right) \approx \frac{I_D}{\eta V_T} \implies r_d = \frac{\eta V_T}{I_D}$

1.6 Zener Diode



1. has 3 modes of operations:

Operation	Condition	Equivalent
Forward-biased	$v_D \leq V_T$	$v_D = -V_T$
Non-conducting	$-V_T < v_D < V_Z$	open circuit
Zener region	$v_D \geq V_Z$	$v_D = V_Z$

2 PN Junction and BJT Operation

3 BJTs as Amplifiers

4 MOSFETs as Amplifiers

5 Small Signal Analysis of Transistor Amplifiers

6 Amplifier Frequency Response