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1 SM0 Theory

Built: 15 March 2020

Parent Theories: ssm1

1.1 Datatypes

command = NP npriv | PR privcmd

npriv = status

output = on | off

privcmd = launch | reset

staff = Alice | Bob | Carol

state = STBY | ACTIVE

1.2 Definitions

[certs_def]

```

⊢ ∀ cmd npriv privcmd.
  certs cmd npriv privcmd =
    [Name Alice controls prop (SOME (NP npriv));
     Name Alice controls prop (SOME (PR privcmd));
     Name Bob controls prop (SOME (NP npriv));
     Name Bob says prop (SOME (PR privcmd)) impf prop NONE]

```

[SM0StateInterp_def]

```

⊢ ∀ state. SM0StateInterp state = TT

```

1.3 Theorems

[Alice_exec_privcmd_justified_thm]

```

⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os) (exec (PR privcmd))
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)
      (Name Alice says prop (SOME (PR privcmd))::ins) s
      outs)
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd) ins
      (NS s (exec (PR privcmd))))
    (Out s (exec (PR privcmd))::outs)) ⇔
  inputOK (Name Alice says prop (SOME (PR privcmd))) ∧
  CFGInterpret (M, Oi, Os)
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)
      (Name Alice says prop (SOME (PR privcmd))::ins) s
      outs) ∧ (M, Oi, Os) sat prop (SOME (PR privcmd))

```

[Alice_justified_privcmd_exec_thm]

$\vdash \forall NS \text{ Out } M \text{ Oi } Os \text{ cmd npriv privcmd ins } s \text{ outs.}$
 $\text{inputOK (Name Alice says prop (SOME (PR privcmd)))} \wedge$
 $\text{CFGInterpret (M, Oi, Os)}$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Alice says prop (SOME (PR privcmd))::ins}) s$
 $\quad \text{outs}) \Rightarrow$
 $\text{TR (M, Oi, Os) (exec (PR privcmd))}$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Alice says prop (SOME (PR privcmd))::ins}) s$
 $\quad \text{outs})$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins}$
 $\quad (NS s (\text{exec (PR privcmd)})))$
 $(\text{Out } s (\text{exec (PR privcmd))::outs}))$

[Alice_privcmd_lemma]

$\vdash \text{CFGInterpret (M, Oi, Os)}$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Alice says prop (SOME (PR privcmd))::ins}) s$
 $\quad \text{outs}) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop (SOME (PR privcmd))}$

[Alice_privcmd_verified_thm]

$\vdash \forall NS \text{ Out } M \text{ Oi } Os.$
 $\text{TR (M, Oi, Os) (exec (PR privcmd))}$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Alice says prop (SOME (PR privcmd))::ins}) s$
 $\quad \text{outs})$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins}$
 $\quad (NS s (\text{exec (PR privcmd)})))$
 $(\text{Out } s (\text{exec (PR privcmd))::outs}) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop (SOME (PR privcmd))}$

[Carol_discard_lemma]

$\vdash \text{TR (M, Oi, Os) discard}$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME cmd)::ins}) s \text{ outs})$
 $(\text{CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins}$
 $\quad (\text{SMOns } s \text{ discard}) (\text{SMOut } s \text{ discard::outs}))$

[Carol_rejected_lemma]

$\vdash \neg \text{inputOK (Name Carol says prop (SOME cmd))}$

[command_distinct_clauses]

$\vdash \forall a' a. \text{NP } a \neq \text{PR } a'$

[command_one_one]

$$\vdash (\forall a \ a'. \text{ (NP } a = \text{NP } a') \iff (a = a')) \wedge \\ \forall a \ a'. \text{ (PR } a = \text{PR } a') \iff (a = a')$$
[inputOK_def]

$$\vdash (\text{inputOK (Name Alice says prop (SOME cmd))} \iff T) \wedge \\ (\text{inputOK (Name Bob says prop (SOME cmd))} \iff T) \wedge \\ (\text{inputOK TT} \iff F) \wedge (\text{inputOK FF} \iff F) \wedge \\ (\text{inputOK (prop } v) \iff F) \wedge (\text{inputOK (notf } v_1) \iff F) \wedge \\ (\text{inputOK (} v_2 \text{ andf } v_3) \iff F) \wedge (\text{inputOK (} v_4 \text{ orf } v_5) \iff F) \wedge \\ (\text{inputOK (} v_6 \text{ impf } v_7) \iff F) \wedge (\text{inputOK (} v_8 \text{ eqf } v_9) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says TT) } \iff F) \wedge (\text{inputOK (} v_{10} \text{ says FF) } \iff F) \wedge \\ (\text{inputOK (Name Carol says prop (SOME } v_{142})) \iff F) \wedge \\ (\text{inputOK (Name } v_{132} \text{ says prop NONE) } \iff F) \wedge \\ (\text{inputOK (} v_{133} \text{ meet } v_{134} \text{ says prop } v_{66}) \iff F) \wedge \\ (\text{inputOK (} v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says notf } v_{67}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says (} v_{68} \text{ andf } v_{69})) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says (} v_{70} \text{ orf } v_{71})) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says (} v_{72} \text{ impf } v_{73})) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says (} v_{74} \text{ eqf } v_{75})) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{76} \text{ says } v_{77}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{80} \text{ controls } v_{81}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says reps } v_{82} \ v_{83} \ v_{84}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{85} \text{ domi } v_{86}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{87} \text{ eqi } v_{88}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{89} \text{ doms } v_{90}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{91} \text{ eqs } v_{92}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{93} \text{ eqn } v_{94}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{95} \text{ lte } v_{96}) \iff F) \wedge \\ (\text{inputOK (} v_{10} \text{ says } v_{97} \text{ lt } v_{98}) \iff F) \wedge \\ (\text{inputOK (} v_{12} \text{ speaks_for } v_{13}) \iff F) \wedge \\ (\text{inputOK (} v_{14} \text{ controls } v_{15}) \iff F) \wedge \\ (\text{inputOK (reps } v_{16} \ v_{17} \ v_{18}) \iff F) \wedge \\ (\text{inputOK (} v_{19} \text{ domi } v_{20}) \iff F) \wedge \\ (\text{inputOK (} v_{21} \text{ eqi } v_{22}) \iff F) \wedge \\ (\text{inputOK (} v_{23} \text{ doms } v_{24}) \iff F) \wedge \\ (\text{inputOK (} v_{25} \text{ eqs } v_{26}) \iff F) \wedge (\text{inputOK (} v_{27} \text{ eqn } v_{28}) \iff F) \wedge \\ (\text{inputOK (} v_{29} \text{ lte } v_{30}) \iff F) \wedge (\text{inputOK (} v_{31} \text{ lt } v_{32}) \iff F)$$
[inputOK_ind]

$$\vdash \forall P. \\ (\forall \text{cmd}. P (\text{Name Alice says prop (SOME cmd)})) \wedge \\ (\forall \text{cmd}. P (\text{Name Bob says prop (SOME cmd)})) \wedge P \text{ TT} \wedge P \text{ FF} \wedge \\ (\forall v. P (\text{prop } v)) \wedge (\forall v_1. P (\text{notf } v_1)) \wedge \\ (\forall v_2 \ v_3. P (v_2 \text{ andf } v_3)) \wedge (\forall v_4 \ v_5. P (v_4 \text{ orf } v_5)) \wedge \\ (\forall v_6 \ v_7. P (v_6 \text{ impf } v_7)) \wedge (\forall v_8 \ v_9. P (v_8 \text{ eqf } v_9)) \wedge$$

$$\begin{aligned}
& (\forall v_{10}. P (v_{10} \text{ says TT})) \wedge (\forall v_{10}. P (v_{10} \text{ says FF})) \wedge \\
& (\forall v_{142}. P (\text{Name Carol says prop (SOME } v_{142})) \wedge \\
& (\forall v_{132}. P (\text{Name } v_{132} \text{ says prop NONE})) \wedge \\
& (\forall v_{133} v_{134} v_{66}. P (v_{133} \text{ meet } v_{134} \text{ says prop } v_{66})) \wedge \\
& (\forall v_{135} v_{136} v_{66}. P (v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66})) \wedge \\
& (\forall v_{10} v_{67}. P (v_{10} \text{ says notf } v_{67})) \wedge \\
& (\forall v_{10} v_{68} v_{69}. P (v_{10} \text{ says } (v_{68} \text{ andf } v_{69}))) \wedge \\
& (\forall v_{10} v_{70} v_{71}. P (v_{10} \text{ says } (v_{70} \text{ orf } v_{71}))) \wedge \\
& (\forall v_{10} v_{72} v_{73}. P (v_{10} \text{ says } (v_{72} \text{ impf } v_{73}))) \wedge \\
& (\forall v_{10} v_{74} v_{75}. P (v_{10} \text{ says } (v_{74} \text{ eqf } v_{75}))) \wedge \\
& (\forall v_{10} v_{76} v_{77}. P (v_{10} \text{ says } v_{76} \text{ says } v_{77})) \wedge \\
& (\forall v_{10} v_{78} v_{79}. P (v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79})) \wedge \\
& (\forall v_{10} v_{80} v_{81}. P (v_{10} \text{ says } v_{80} \text{ controls } v_{81})) \wedge \\
& (\forall v_{10} v_{82} v_{83} v_{84}. P (v_{10} \text{ says reps } v_{82} v_{83} v_{84})) \wedge \\
& (\forall v_{10} v_{85} v_{86}. P (v_{10} \text{ says } v_{85} \text{ domi } v_{86})) \wedge \\
& (\forall v_{10} v_{87} v_{88}. P (v_{10} \text{ says } v_{87} \text{ eqi } v_{88})) \wedge \\
& (\forall v_{10} v_{89} v_{90}. P (v_{10} \text{ says } v_{89} \text{ doms } v_{90})) \wedge \\
& (\forall v_{10} v_{91} v_{92}. P (v_{10} \text{ says } v_{91} \text{ eqs } v_{92})) \wedge \\
& (\forall v_{10} v_{93} v_{94}. P (v_{10} \text{ says } v_{93} \text{ eqn } v_{94})) \wedge \\
& (\forall v_{10} v_{95} v_{96}. P (v_{10} \text{ says } v_{95} \text{ lte } v_{96})) \wedge \\
& (\forall v_{10} v_{97} v_{98}. P (v_{10} \text{ says } v_{97} \text{ lt } v_{98})) \wedge \\
& (\forall v_{12} v_{13}. P (v_{12} \text{ speaks_for } v_{13})) \wedge \\
& (\forall v_{14} v_{15}. P (v_{14} \text{ controls } v_{15})) \wedge \\
& (\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge \\
& (\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge \\
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[output_distinct_clauses]

$\vdash \text{on} \neq \text{off}$

[privcmd_distinct_clauses]

$\vdash \text{launch} \neq \text{reset}$

[SMOns_def]

$$\begin{aligned}
& \vdash (\text{SMOns STBY (exec (PR reset))} = \text{STBY}) \wedge \\
& (\text{SMOns STBY (exec (PR launch))} = \text{ACTIVE}) \wedge \\
& (\text{SMOns STBY (exec (NP status))} = \text{STBY}) \wedge \\
& (\text{SMOns ACTIVE (exec (PR reset))} = \text{STBY}) \wedge \\
& (\text{SMOns ACTIVE (exec (PR launch))} = \text{ACTIVE}) \wedge \\
& (\text{SMOns ACTIVE (exec (NP status))} = \text{ACTIVE}) \wedge \\
& (\text{SMOns STBY (trap (PR reset))} = \text{STBY}) \wedge \\
& (\text{SMOns STBY (trap (PR launch))} = \text{STBY}) \wedge \\
& (\text{SMOns STBY (trap (NP status))} = \text{STBY}) \wedge \\
& (\text{SMOns ACTIVE (trap (PR reset))} = \text{ACTIVE}) \wedge
\end{aligned}$$

$(\text{SM0ns ACTIVE (trap (PR launch))} = \text{ACTIVE}) \wedge$
 $(\text{SM0ns ACTIVE (trap (NP status))} = \text{ACTIVE}) \wedge$
 $(\text{SM0ns STBY discard} = \text{STBY}) \wedge (\text{SM0ns ACTIVE discard} = \text{ACTIVE})$

[SM0ns_ind]

$\vdash \forall P.$
 $P \text{ STBY (exec (PR reset))} \wedge P \text{ STBY (exec (PR launch))} \wedge$
 $P \text{ STBY (exec (NP status))} \wedge P \text{ ACTIVE (exec (PR reset))} \wedge$
 $P \text{ ACTIVE (exec (PR launch))} \wedge P \text{ ACTIVE (exec (NP status))} \wedge$
 $P \text{ STBY (trap (PR reset))} \wedge P \text{ STBY (trap (PR launch))} \wedge$
 $P \text{ STBY (trap (NP status))} \wedge P \text{ ACTIVE (trap (PR reset))} \wedge$
 $P \text{ ACTIVE (trap (PR launch))} \wedge P \text{ ACTIVE (trap (NP status))} \wedge$
 $P \text{ STBY discard} \wedge P \text{ ACTIVE discard} \Rightarrow$
 $\forall v \ v_1. P \ v \ v_1$

[SM0out_def]

$\vdash (\text{SM0out STBY (exec (PR reset))} = \text{off}) \wedge$
 $(\text{SM0out STBY (exec (PR launch))} = \text{on}) \wedge$
 $(\text{SM0out STBY (exec (NP status))} = \text{off}) \wedge$
 $(\text{SM0out ACTIVE (exec (PR reset))} = \text{off}) \wedge$
 $(\text{SM0out ACTIVE (exec (PR launch))} = \text{on}) \wedge$
 $(\text{SM0out ACTIVE (exec (NP status))} = \text{on}) \wedge$
 $(\text{SM0out STBY (trap (PR reset))} = \text{off}) \wedge$
 $(\text{SM0out STBY (trap (PR launch))} = \text{off}) \wedge$
 $(\text{SM0out STBY (trap (NP status))} = \text{off}) \wedge$
 $(\text{SM0out ACTIVE (trap (PR reset))} = \text{on}) \wedge$
 $(\text{SM0out ACTIVE (trap (PR launch))} = \text{on}) \wedge$
 $(\text{SM0out ACTIVE (trap (NP status))} = \text{on}) \wedge$
 $(\text{SM0out STBY discard} = \text{off}) \wedge (\text{SM0out ACTIVE discard} = \text{on})$

[SM0out_ind]

$\vdash \forall P.$
 $P \text{ STBY (exec (PR reset))} \wedge P \text{ STBY (exec (PR launch))} \wedge$
 $P \text{ STBY (exec (NP status))} \wedge P \text{ ACTIVE (exec (PR reset))} \wedge$
 $P \text{ ACTIVE (exec (PR launch))} \wedge P \text{ ACTIVE (exec (NP status))} \wedge$
 $P \text{ STBY (trap (PR reset))} \wedge P \text{ STBY (trap (PR launch))} \wedge$
 $P \text{ STBY (trap (NP status))} \wedge P \text{ ACTIVE (trap (PR reset))} \wedge$
 $P \text{ ACTIVE (trap (PR launch))} \wedge P \text{ ACTIVE (trap (NP status))} \wedge$
 $P \text{ STBY discard} \wedge P \text{ ACTIVE discard} \Rightarrow$
 $\forall v \ v_1. P \ v \ v_1$

[staff_distinct_clauses]

$\vdash \text{Alice} \neq \text{Bob} \wedge \text{Alice} \neq \text{Carol} \wedge \text{Bob} \neq \text{Carol}$

[state_distinct_clauses]

$\vdash \text{STBY} \neq \text{ACTIVE}$

2 SM0Solutions Theory

Built: 15 March 2020

Parent Theories: SM0

2.1 Definitions

[certs2_def]

```
⊢ ∀ cmd npriv privcmd.  
  certs2 cmd npriv privcmd =  
  [Name Carol controls prop (SOME (NP npriv));  
   Name Carol says prop (SOME (PR privcmd)) impf prop NONE]
```

2.2 Theorems

[Alice_exec_npriv_justified_thm]

```
⊢ ∀ NS Out M Oi Os.  
  TR (M, Oi, Os) (exec (NP npriv))  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)  
     (Name Alice says prop (SOME (NP npriv))::ins) s outs)  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd) ins  
     (NS s (exec (NP npriv))))  
    (Out s (exec (NP npriv))::outs)) ⇔  
  inputOK (Name Alice says prop (SOME (NP npriv))) ∧  
  CFGInterpret (M, Oi, Os)  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)  
     (Name Alice says prop (SOME (NP npriv))::ins) s  
     outs) ∧ (M, Oi, Os) sat prop (SOME (NP npriv))
```

[Alice_justified_npriv_exec_thm]

```
⊢ ∀ NS Out M Oi Os cmd npriv privcmd ins s outs.  
  inputOK (Name Alice says prop (SOME (NP npriv))) ∧  
  CFGInterpret (M, Oi, Os)  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)  
     (Name Alice says prop (SOME (NP npriv))::ins) s  
     outs) ⇒  
  TR (M, Oi, Os) (exec (NP npriv))  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)  
     (Name Alice says prop (SOME (NP npriv))::ins) s outs)  
    (CFG inputOK SM0StateInterp (certs cmd npriv privcmd) ins  
     (NS s (exec (NP npriv))))  
    (Out s (exec (NP npriv))::outs))
```

[Alice_npriv_lemma]

```
⊢ CFGInterpret (M, Oi, Os)  
  (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)  
   (Name Alice says prop (SOME (NP npriv))::ins) s outs) ⇒  
  (M, Oi, Os) sat prop (SOME (NP npriv))
```


[Alice_npriv_verified_thm]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$
 $\text{TR } (M, Oi, Os) \text{ (exec (NP npriv))}$
 $(\text{CFG inputOK SM0StateInterp (certs cmd npriv privcmd)}$
 $\quad (\text{Name Alice says prop (SOME (NP npriv))::ins) s outs})$
 $(\text{CFG inputOK SM0StateInterp (certs cmd npriv privcmd) ins}$
 $\quad (NS s (\text{exec (NP npriv)})))$
 $(\text{Out s (exec (NP npriv))::outs})) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop (SOME (NP npriv))}$

[Carol_exec_npriv_justified_thm]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$
 $\text{TR } (M, Oi, Os) \text{ (exec (NP npriv))}$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (NP npriv))::ins) s outs})$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad \text{ins } (NS s (\text{exec (NP npriv)})))$
 $(\text{Out s (exec (NP npriv))::outs})) \iff$
 $\text{inputOK2 (Name Carol says prop (SOME (NP npriv))) } \wedge$
 $\text{CFGInterpret } (M, Oi, Os)$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (NP npriv))::ins) s}$
 $\quad \text{outs}) \wedge (M, Oi, Os) \text{ sat prop (SOME (NP npriv))}$

[Carol_justified_npriv_exec_thm]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os \text{ cmd npriv privcmd ins s outs.}$
 $\text{inputOK2 (Name Carol says prop (SOME (NP npriv))) } \wedge$
 $\text{CFGInterpret } (M, Oi, Os)$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (NP npriv))::ins) s}$
 $\quad \text{outs}) \Rightarrow$
 $\text{TR } (M, Oi, Os) \text{ (exec (NP npriv))}$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (NP npriv))::ins) s outs})$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad \text{ins } (NS s (\text{exec (NP npriv)})))$
 $(\text{Out s (exec (NP npriv))::outs}))$

[Carol_justified_privcmd_trap_thm]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os \text{ cmd npriv privcmd ins s outs.}$
 $\text{inputOK2 (Name Carol says prop (SOME (PR privcmd))) } \wedge$
 $\text{CFGInterpret } (M, Oi, Os)$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (PR privcmd))::ins) s}$
 $\quad \text{outs}) \Rightarrow$
 $\text{TR } (M, Oi, Os) \text{ (trap (PR privcmd))}$
 $(\text{CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)}$
 $\quad (\text{Name Carol says prop (SOME (PR privcmd))::ins) s}$

$outs)$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $ins \text{ (NS s (trap (PR privcmd)))}$
 $(Out \text{ s (trap (PR privcmd))::outs}))$

[Carol_npriv_lemma]

$\vdash CFGInterpret \text{ (M, Oi, Os)}$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $(Name \text{ Carol says prop (SOME (NP npriv))::ins) s outs) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop (SOME (NP npriv))}$

[Carol_npriv_verified_thm]

$\vdash \forall NS \text{ Out M Oi Os.}$
 $TR \text{ (M, Oi, Os) (exec (NP npriv))}$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $(Name \text{ Carol says prop (SOME (NP npriv))::ins) s outs)$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $ins \text{ (NS s (exec (NP npriv)))}$
 $(Out \text{ s (exec (NP npriv))::outs})) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop (SOME (NP npriv))}$

[Carol_privcmd_trap_lemma]

$\vdash CFGInterpret \text{ (M, Oi, Os)}$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $(Name \text{ Carol says prop (SOME (PR privcmd))::ins) s}$
 $outs) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop NONE}$

[Carol_privcmd_trapped_thm]

$\vdash \forall NS \text{ Out M Oi Os.}$
 $TR \text{ (M, Oi, Os) (trap (PR privcmd))}$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $(Name \text{ Carol says prop (SOME (PR privcmd))::ins) s}$
 $outs)$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $ins \text{ (NS s (trap (PR privcmd)))}$
 $(Out \text{ s (trap (PR privcmd))::outs})) \Rightarrow$
 $(M, Oi, Os) \text{ sat prop NONE}$

[Carol_trap_privcmd_justified_thm]

$\vdash \forall NS \text{ Out M Oi Os.}$
 $TR \text{ (M, Oi, Os) (trap (PR privcmd))}$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $(Name \text{ Carol says prop (SOME (PR privcmd))::ins) s}$
 $outs)$
 $(CFG \text{ inputOK2 } SM0StateInterp \text{ (certs2 cmd npriv privcmd)}$
 $ins \text{ (NS s (trap (PR privcmd)))}$
 $(Out \text{ s (trap (PR privcmd))::outs})) \iff$

```

inputOK2 (Name Carol says prop (SOME (PR privcmd))) ∧
CFGInterpret (M, Oi, Os)
  (CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)
    (Name Carol says prop (SOME (PR privcmd))::ins) s
    outs) ∧ (M, Oi, Os) sat prop NONE

```

[inputOK2_def]

```

⊢ (inputOK2 (Name Carol says prop (SOME cmd)) ⇔ T) ∧
(inputOK2 TT ⇔ F) ∧ (inputOK2 FF ⇔ F) ∧
(inputOK2 (prop v) ⇔ F) ∧ (inputOK2 (notf v1) ⇔ F) ∧
(inputOK2 (v2 andf v3) ⇔ F) ∧ (inputOK2 (v4 orf v5) ⇔ F) ∧
(inputOK2 (v6 impf v7) ⇔ F) ∧ (inputOK2 (v8 eqf v9) ⇔ F) ∧
(inputOK2 (v10 says TT) ⇔ F) ∧
(inputOK2 (v10 says FF) ⇔ F) ∧
(inputOK2 (Name Alice says prop (SOME v142)) ⇔ F) ∧
(inputOK2 (Name Bob says prop (SOME v142)) ⇔ F) ∧
(inputOK2 (Name v132 says prop NONE) ⇔ F) ∧
(inputOK2 (v133 meet v134 says prop v66) ⇔ F) ∧
(inputOK2 (v135 quoting v136 says prop v66) ⇔ F) ∧
(inputOK2 (v10 says notf v67) ⇔ F) ∧
(inputOK2 (v10 says (v68 andf v69)) ⇔ F) ∧
(inputOK2 (v10 says (v70 orf v71)) ⇔ F) ∧
(inputOK2 (v10 says (v72 impf v73)) ⇔ F) ∧
(inputOK2 (v10 says (v74 eqf v75)) ⇔ F) ∧
(inputOK2 (v10 says v76 says v77) ⇔ F) ∧
(inputOK2 (v10 says v78 speaks_for v79) ⇔ F) ∧
(inputOK2 (v10 says v80 controls v81) ⇔ F) ∧
(inputOK2 (v10 says reps v82 v83 v84) ⇔ F) ∧
(inputOK2 (v10 says v85 domi v86) ⇔ F) ∧
(inputOK2 (v10 says v87 eqi v88) ⇔ F) ∧
(inputOK2 (v10 says v89 doms v90) ⇔ F) ∧
(inputOK2 (v10 says v91 eqs v92) ⇔ F) ∧
(inputOK2 (v10 says v93 eqn v94) ⇔ F) ∧
(inputOK2 (v10 says v95 lte v96) ⇔ F) ∧
(inputOK2 (v10 says v97 lt v98) ⇔ F) ∧
(inputOK2 (v12 speaks_for v13) ⇔ F) ∧
(inputOK2 (v14 controls v15) ⇔ F) ∧
(inputOK2 (reps v16 v17 v18) ⇔ F) ∧
(inputOK2 (v19 domi v20) ⇔ F) ∧
(inputOK2 (v21 eqi v22) ⇔ F) ∧
(inputOK2 (v23 doms v24) ⇔ F) ∧
(inputOK2 (v25 eqs v26) ⇔ F) ∧
(inputOK2 (v27 eqn v28) ⇔ F) ∧
(inputOK2 (v29 lte v30) ⇔ F) ∧ (inputOK2 (v31 lt v32) ⇔ F)

```

[inputOK2_ind]

```

⊢ ∀ P.
  (∀ cmd. P (Name Carol says prop (SOME cmd))) ∧ P TT ∧ P FF ∧
  (∀ v. P (prop v)) ∧ (∀ v1. P (notf v1)) ∧

```

$$\begin{aligned}
& (\forall v_2 v_3. P (v_2 \text{ andf } v_3)) \wedge (\forall v_4 v_5. P (v_4 \text{ orf } v_5)) \wedge \\
& (\forall v_6 v_7. P (v_6 \text{ impf } v_7)) \wedge (\forall v_8 v_9. P (v_8 \text{ eqf } v_9)) \wedge \\
& (\forall v_{10}. P (v_{10} \text{ says TT})) \wedge (\forall v_{10}. P (v_{10} \text{ says FF})) \wedge \\
& (\forall v_{142}. P (\text{Name Alice says prop (SOME } v_{142})) \wedge \\
& (\forall v_{142}. P (\text{Name Bob says prop (SOME } v_{142})) \wedge \\
& (\forall v_{132}. P (\text{Name } v_{132} \text{ says prop NONE})) \wedge \\
& (\forall v_{133} v_{134} v_{66}. P (v_{133} \text{ meet } v_{134} \text{ says prop } v_{66})) \wedge \\
& (\forall v_{135} v_{136} v_{66}. P (v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66})) \wedge \\
& (\forall v_{10} v_{67}. P (v_{10} \text{ says notf } v_{67})) \wedge \\
& (\forall v_{10} v_{68} v_{69}. P (v_{10} \text{ says } (v_{68} \text{ andf } v_{69}))) \wedge \\
& (\forall v_{10} v_{70} v_{71}. P (v_{10} \text{ says } (v_{70} \text{ orf } v_{71}))) \wedge \\
& (\forall v_{10} v_{72} v_{73}. P (v_{10} \text{ says } (v_{72} \text{ impf } v_{73}))) \wedge \\
& (\forall v_{10} v_{74} v_{75}. P (v_{10} \text{ says } (v_{74} \text{ eqf } v_{75}))) \wedge \\
& (\forall v_{10} v_{76} v_{77}. P (v_{10} \text{ says } v_{76} \text{ says } v_{77})) \wedge \\
& (\forall v_{10} v_{78} v_{79}. P (v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79})) \wedge \\
& (\forall v_{10} v_{80} v_{81}. P (v_{10} \text{ says } v_{80} \text{ controls } v_{81})) \wedge \\
& (\forall v_{10} v_{82} v_{83} v_{84}. P (v_{10} \text{ says reps } v_{82} v_{83} v_{84})) \wedge \\
& (\forall v_{10} v_{85} v_{86}. P (v_{10} \text{ says } v_{85} \text{ domi } v_{86})) \wedge \\
& (\forall v_{10} v_{87} v_{88}. P (v_{10} \text{ says } v_{87} \text{ eqi } v_{88})) \wedge \\
& (\forall v_{10} v_{89} v_{90}. P (v_{10} \text{ says } v_{89} \text{ doms } v_{90})) \wedge \\
& (\forall v_{10} v_{91} v_{92}. P (v_{10} \text{ says } v_{91} \text{ eqs } v_{92})) \wedge \\
& (\forall v_{10} v_{93} v_{94}. P (v_{10} \text{ says } v_{93} \text{ eqn } v_{94})) \wedge \\
& (\forall v_{10} v_{95} v_{96}. P (v_{10} \text{ says } v_{95} \text{ lte } v_{96})) \wedge \\
& (\forall v_{10} v_{97} v_{98}. P (v_{10} \text{ says } v_{97} \text{ lt } v_{98})) \wedge \\
& (\forall v_{12} v_{13}. P (v_{12} \text{ speaks_for } v_{13})) \wedge \\
& (\forall v_{14} v_{15}. P (v_{14} \text{ controls } v_{15})) \wedge \\
& (\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge \\
& (\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge \\
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

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