

Introduction to Coalgebra 59

Towards Mathematics of States and Observation

The area of coalgebra has emerged within theoretical computer science with a unifying claim: to be the mathematics of computational dynamics. It combines ideas from the theory of dynamical systems and from the theory of state-based computation. Although still in its infancy, it is an active area of research that generates wide interest.

Written by one of the founders of the field, this book acts as the first mature and accessible introduction to coalgebra. It provides clear mathematical explanations with many examples and exercises involving deterministic and non-deterministic automata, transition systems, streams, Markov chains and weighted automata. The theory is expressed in the language of category theory, which provides the right abstraction to make the similarity and duality between algebra and coalgebra explicit and which the reader is introduced to in a hands-on manner. The book will be useful to mathematicians and (theoretical) computer scientists and of interest to mathematical physicists, biologists and economists.

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CAMBRIDGE
UNIVERSITY PRESS

University Printing House, Cambridge CB2 8BS, United Kingdom

One Liberty Plaza, 20th Floor, New York, NY 10006, USA

477 Williamstown Road, Port Melbourne, VIC 3207, Australia

4843/24, 2nd Floor, Ansari Road, Daryaganj, Delhi – 110002, India

79 Anson Road, #06–04/06, Singapore 079906

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www.cambridge.org

Information on this title: www.cambridge.org/9781107177895

10.1017/9781316823187

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First published 2017

Printed in the United Kingdom by Clays, St Ives plc, November 2016

A catalogue record for this publication is available from the British Library.

Library of Congress Cataloging-in-Publication Data

Names: Jacobs, Bart.

Title: Introduction to coalgebra : towards mathematics of states and observation / Bart Jacobs.

Description: Cambridge : Cambridge University Press, [2017] |

Series: Cambridge tracts in theoretical computer science ; 59 |

Includes bibliographical references and indexes.

Identifiers: LCCN 2016023664 | ISBN 9781107177895 (Hardback)

Subjects: LCSH: Associative algebras. | Universal enveloping algebras. | Algebra, Universal.

Classification: LCC QA251.5 .B36 2017 | DDC 512/.46–dc23 LC record available at <https://lcn.loc.gov/2016023664>

ISBN 978-1-107-17789-5 Hardback

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