# TopHat: a stylish journey through modular interactive workflows

Tim Steenvoorden

Markus Klinik

Nico Naus

Dutch FP Day, January 11, 2019

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#### Workflows

coordinate collaboration

#### **Interactive**

driven by user input

#### Modular

higher order



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elementary building blocks and concepts





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labeled transition system





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embedding in simply typed  $\lambda$ -calculus (with clearly separated semantics)





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coordinate collaboration

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#### Interactive

driven by user input

labeled transition system

#### Modular

higher order

embedding in simply typed λ-calculus (with clearly separated semantics)

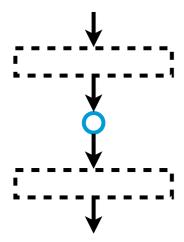


Foundation for formal reasoning and comparison to other frameworks

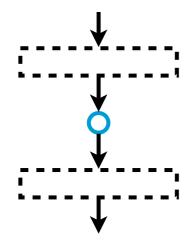


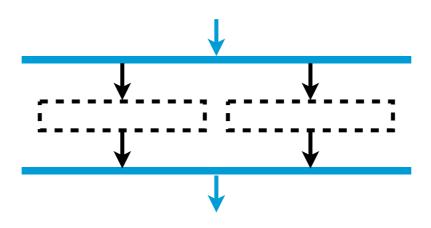






**AFTER EACH OTHER** 

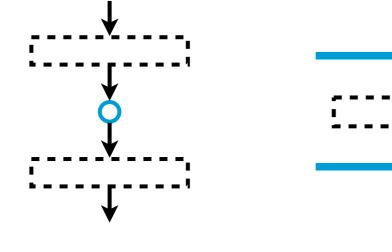


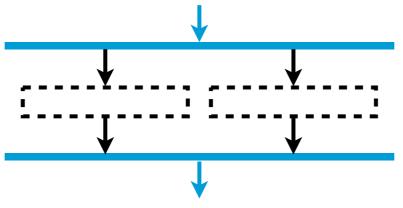


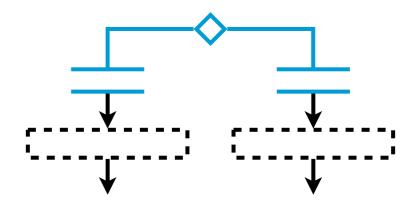
**AFTER EACH OTHER** 

AT THE SAME TIME

**AFTER EACH OTHER** 



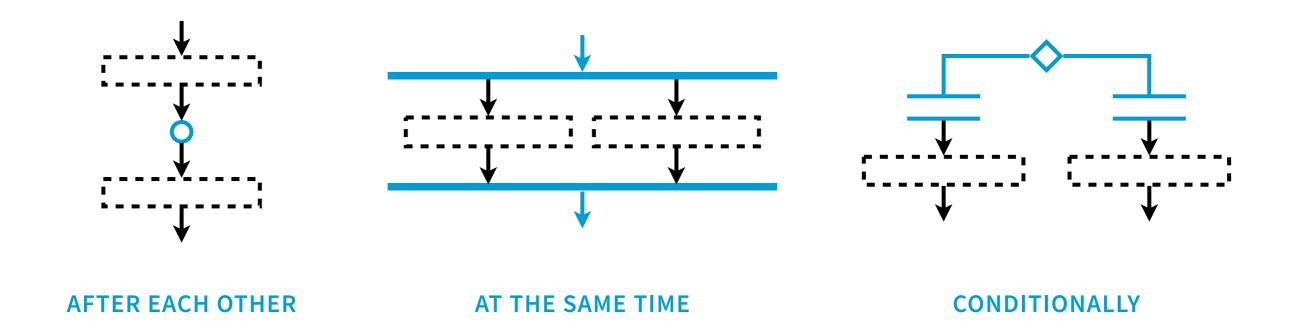




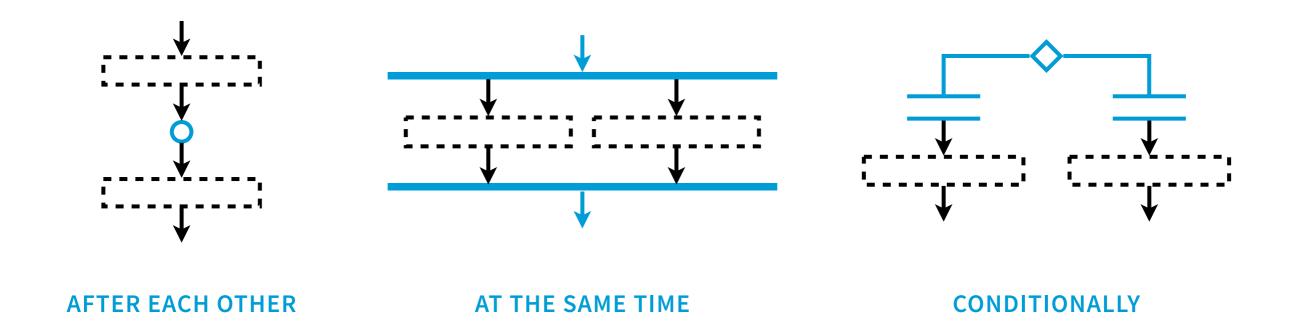
AT '

AT THE SAME TIME

**CONDITIONALLY** 



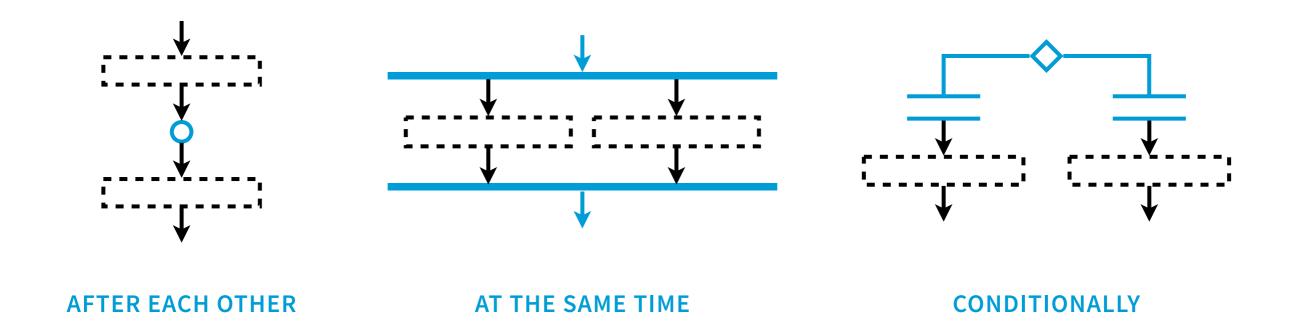
Communication is taken care of!



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"We do A and B at the same time, then we continue with C."





#### Communication is taken care of!

"We do A and B at the same time, then we continue with C."

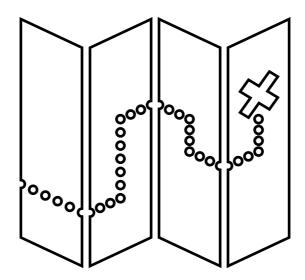


"When I send you M, you can do B and I'll wait for you to send N."





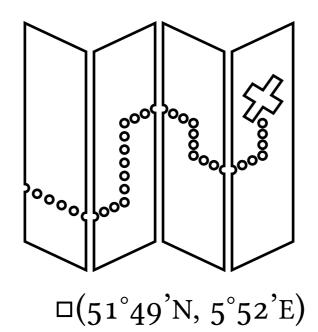






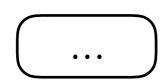
5

□5

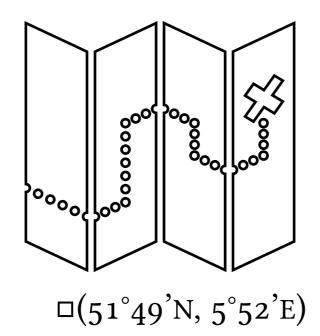




□True

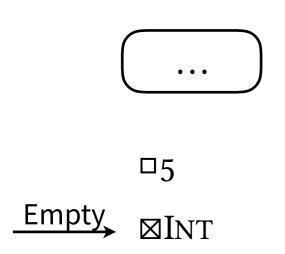


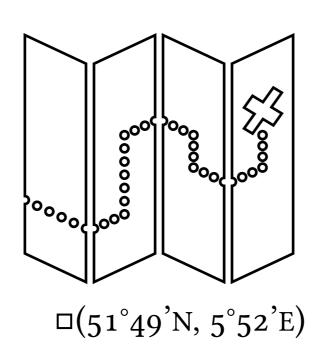
□5
Empty ⊠INT

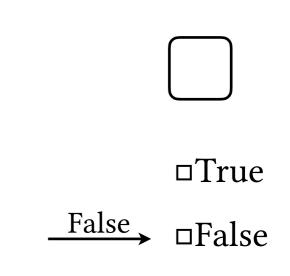


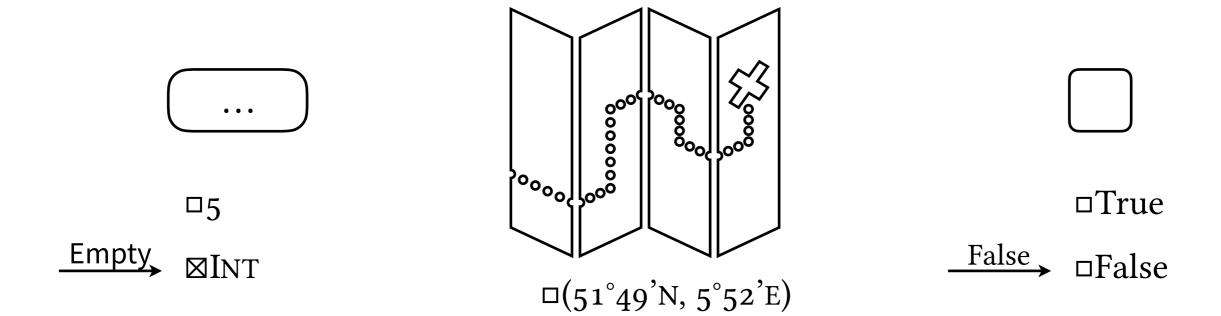


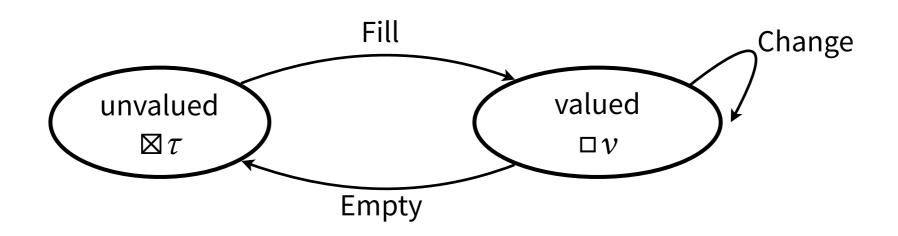
□True

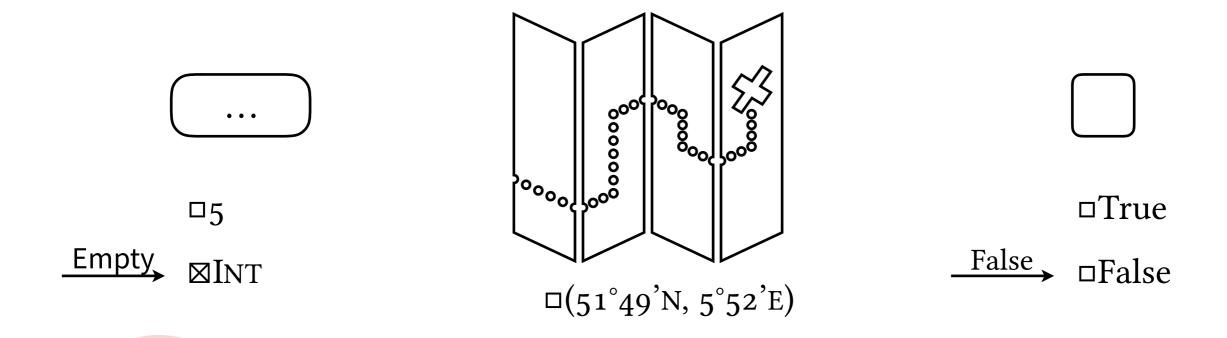




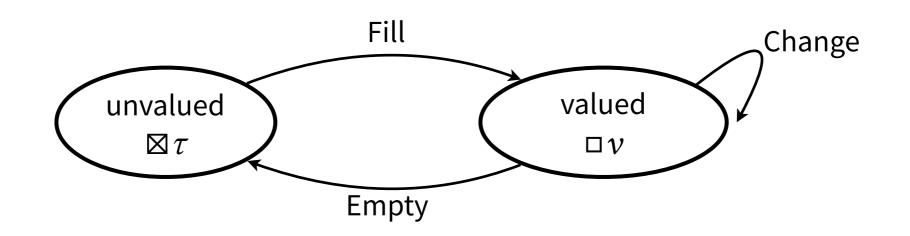


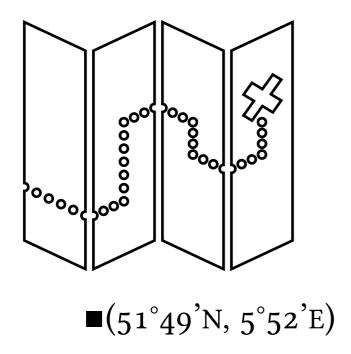


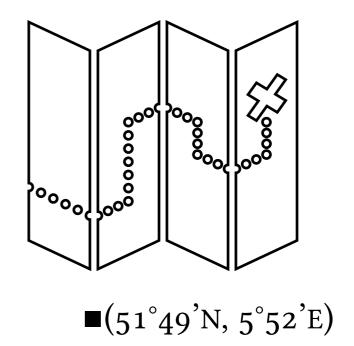


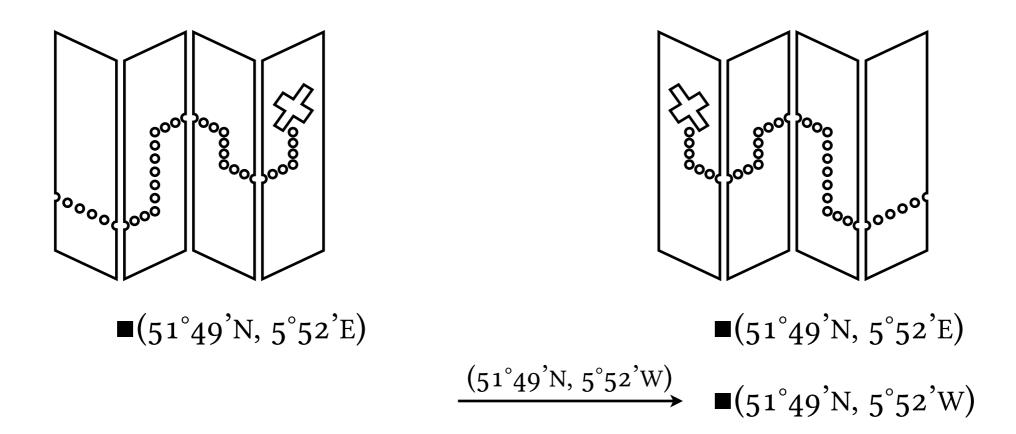


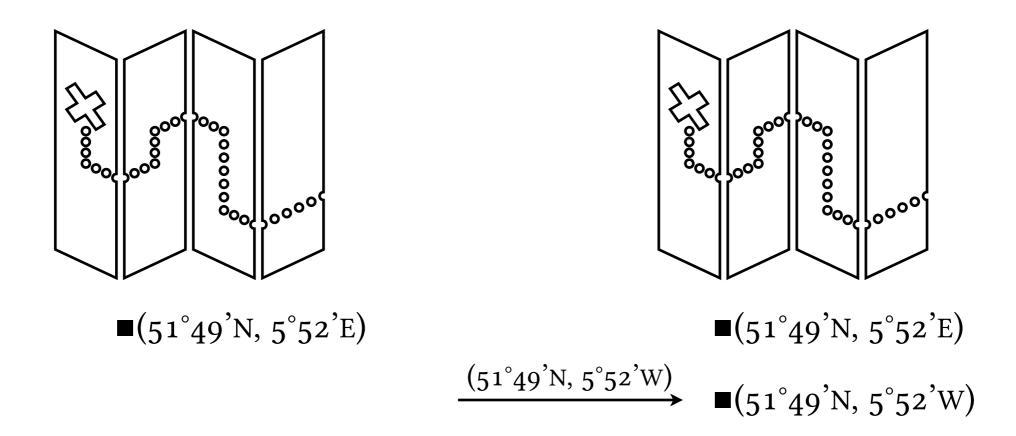
CAPTURE
THE EVER
CHANGING
NATURE OF
WIDGETS

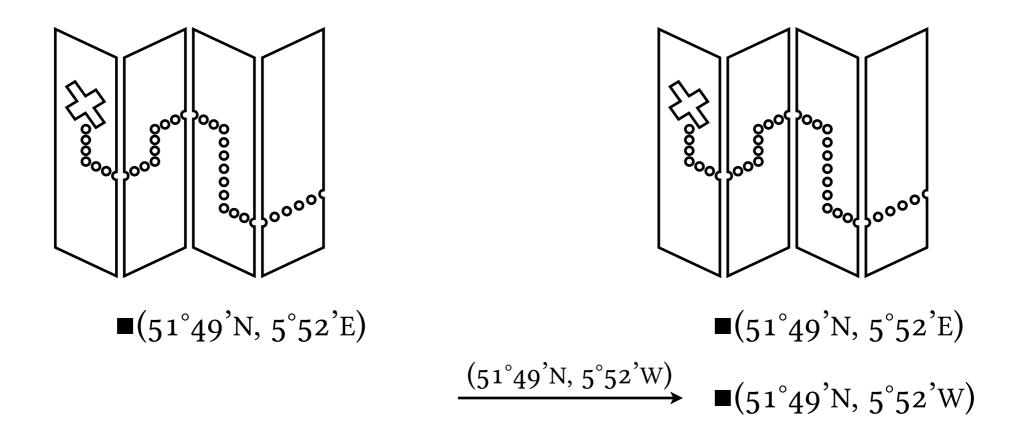


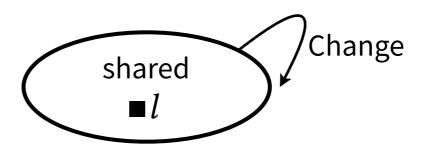


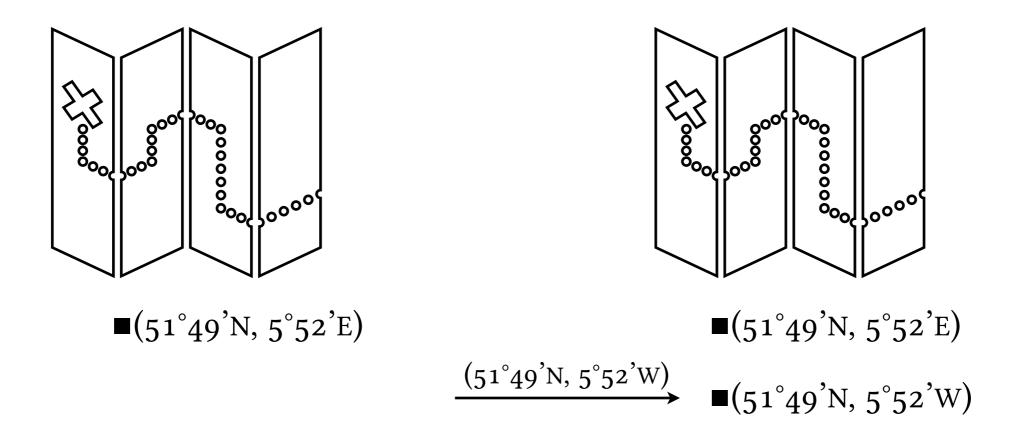


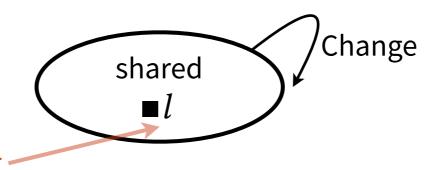






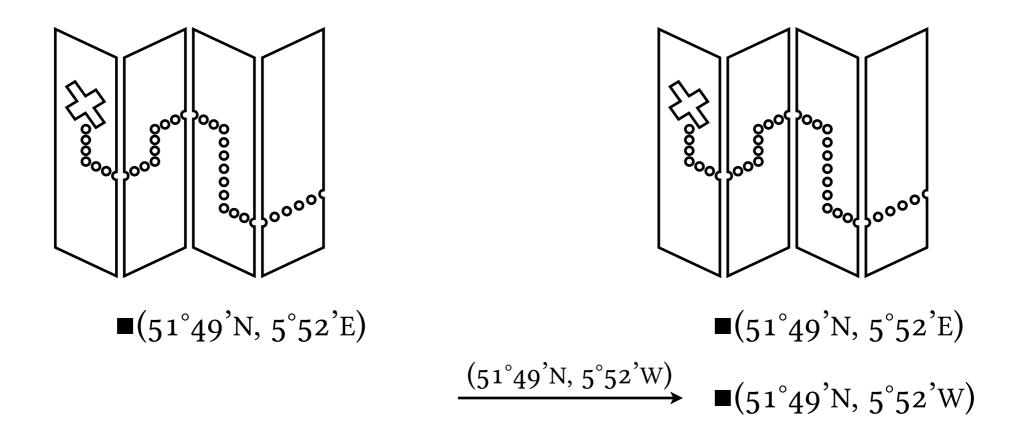


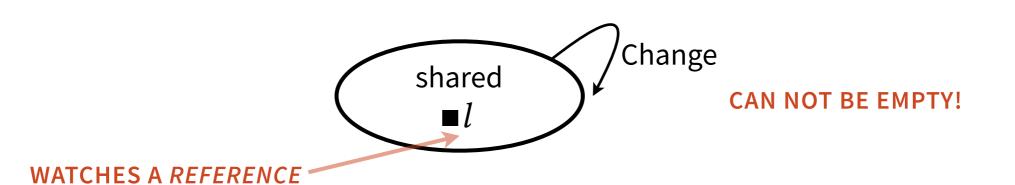




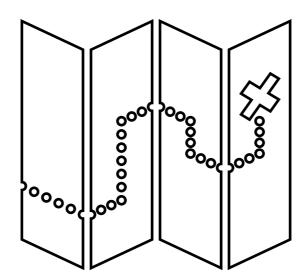
**WATCHES A REFERENCE** 





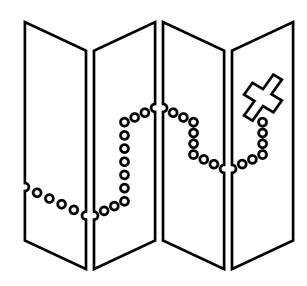








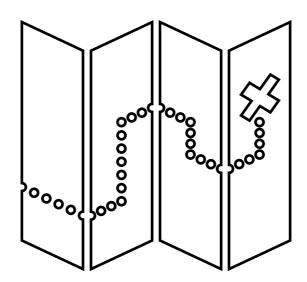






$$\mathcal{V}(\Box \text{True}) = \text{True}$$





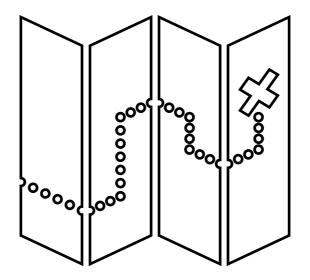
$$\mathcal{V}(\Box(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E}))$$
  
=  $(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E})$ 



$$\mathcal{V}(\Box \text{True}) = \text{True}$$



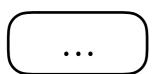
$$\mathcal{V}(\boxtimes Int) = \bot$$



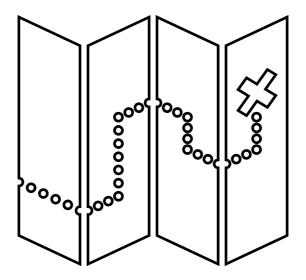
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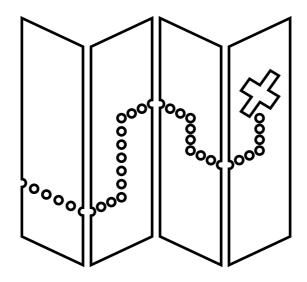


$$\mathcal{V}(\Box \text{True}) = \text{True}$$

 $\mathcal{V}: \mathsf{TASK}\ \tau \longrightarrow \mathsf{MAYBE}\ \tau$ 



$$\mathcal{V}(\boxtimes INT) = \bot$$

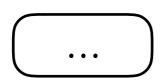


$$\mathcal{V}(\Box(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E}))$$
  
=  $(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E})$ 

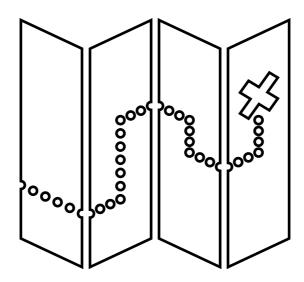


$$\mathcal{V}(\Box \text{True}) = \text{True}$$

value  $\mathcal{V}: \text{TASK } \tau \longrightarrow \text{MAYBE } \tau$ 



$$\mathcal{V}(oxtimes ext{Int}) = ot$$



$$\mathcal{V}(\Box(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E}))$$
  
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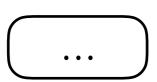


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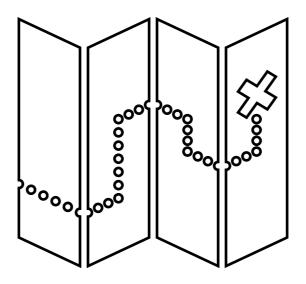
#### SOME TASKS DO NOT HAVE A VALUE

value

 $\mathcal{V}: \mathsf{TASK} \ au \longrightarrow \mathsf{MAYBE} \ au$ 



$$\mathcal{V}(\boxtimes Int) = \bot$$



$$\mathcal{V}(\Box(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E}))$$
  
=  $(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E})$ 



$$\mathcal{V}(\Box \text{True}) = \text{True}$$

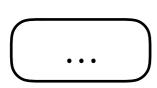
#### SOME TASKS DO NOT HAVE A VALUE

value

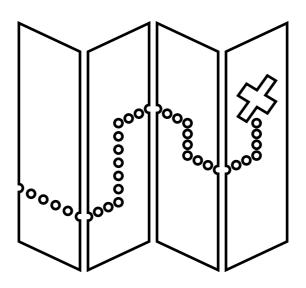
 $\mathcal{V}: \mathsf{TASK}\ \tau \longrightarrow \mathsf{MAYBE}\ \tau$ 

user interface  $\mathcal{U}: \text{TASK } \tau \to \text{HTML}$  (or  $\mathcal{U}: \text{TASK } \tau \to \text{STRING}$  or  $\mathcal{U}: \text{TASK } \tau \to ...$ )

#### **Observations**



$$\mathcal{V}(\boxtimes INT) = \bot$$



$$\mathcal{V}(\Box(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E}))$$
  
=  $(51^{\circ}49'\text{N}, 5^{\circ}52'\text{E})$ 



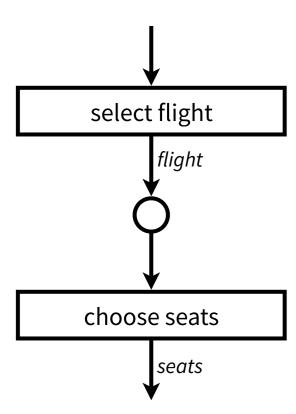
$$\mathcal{V}(\Box \text{True}) = \text{True}$$

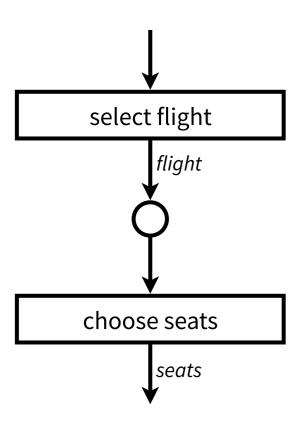
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value  $\mathcal{V}: \text{TASK } \tau \longrightarrow \text{MAYBE } \tau$ 

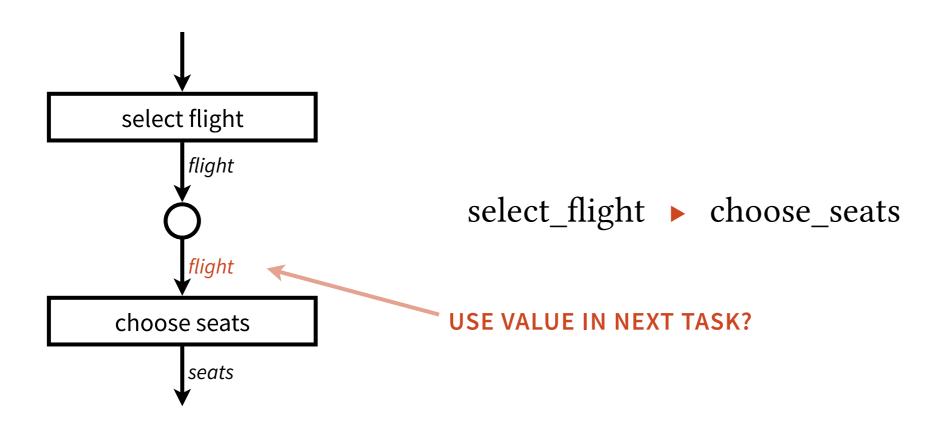
user interface  $\mathcal{U}: \text{Task } \tau \to \text{Html}$  (or  $\mathcal{U}: \text{Task } \tau \to \text{String}$  or  $\mathcal{U}: \text{Task } \tau \to ...$ )

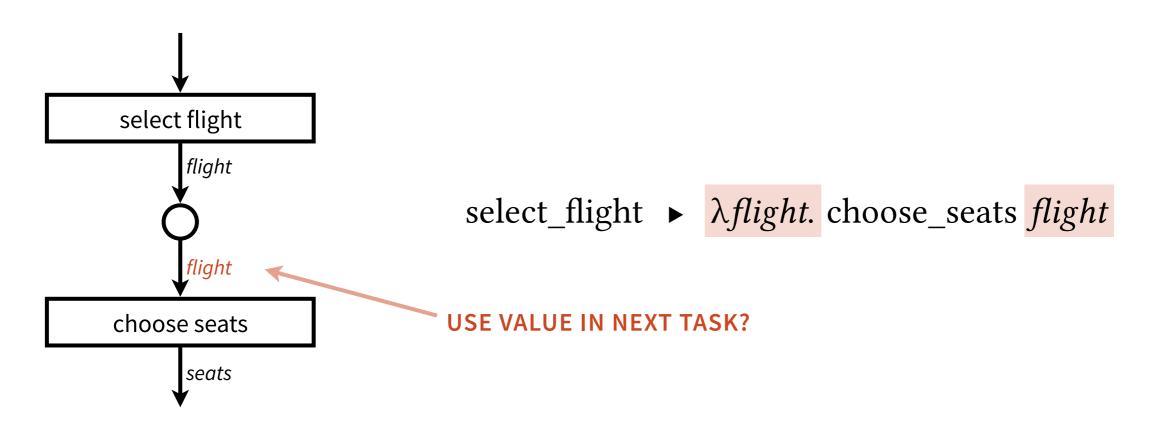
possible inputs  $\mathcal{J}$ : Task  $\tau \to \text{List Input}$ 

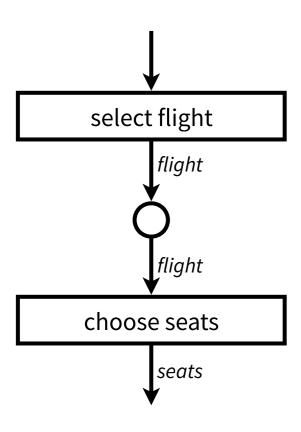




select\_flight > choose\_seats

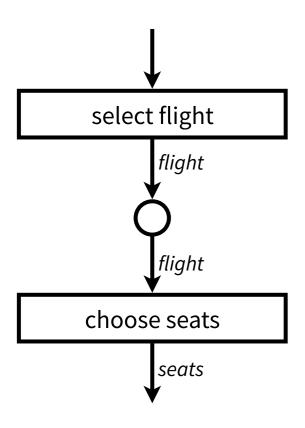






select\_flight ► \(\lambda flight\). choose\_seats \(flight\)

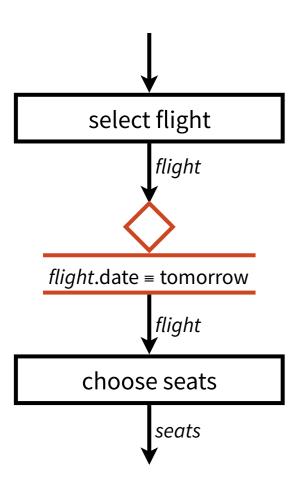
WHEN TO PROCEED TO THE NEXT TASK?



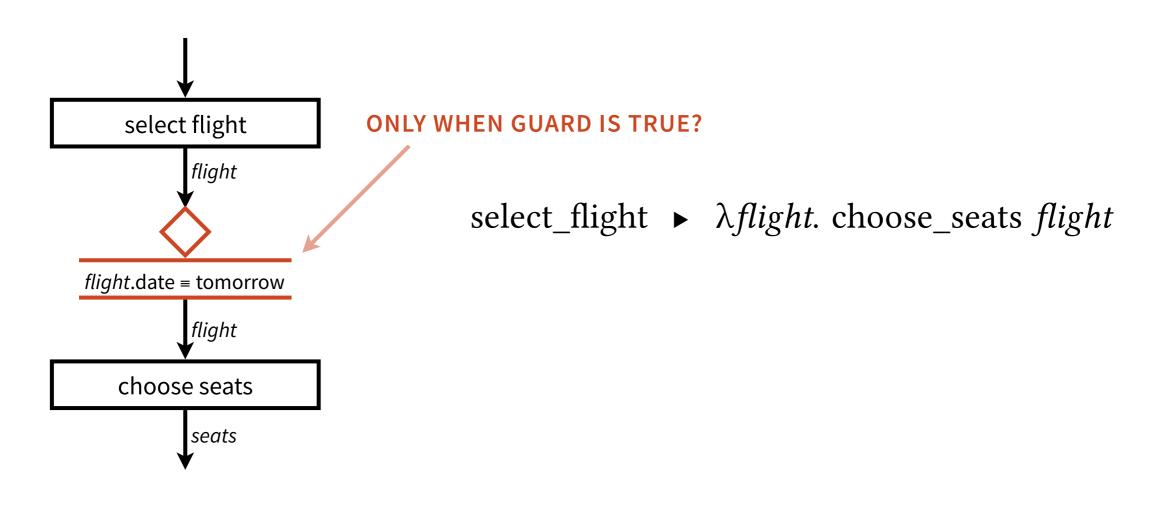
select\_flight ► \(\lambda flight\). choose\_seats \(flight\)

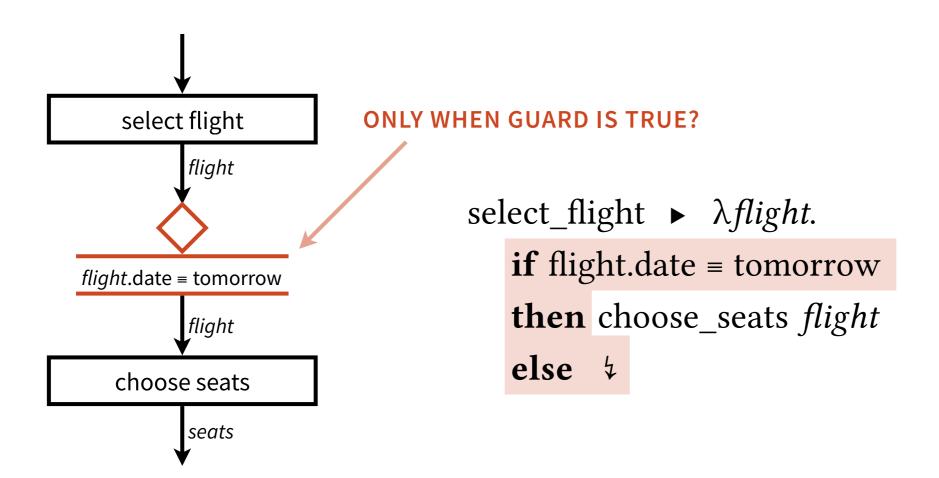
WHEN TO PROCEED TO THE NEXT TASK?

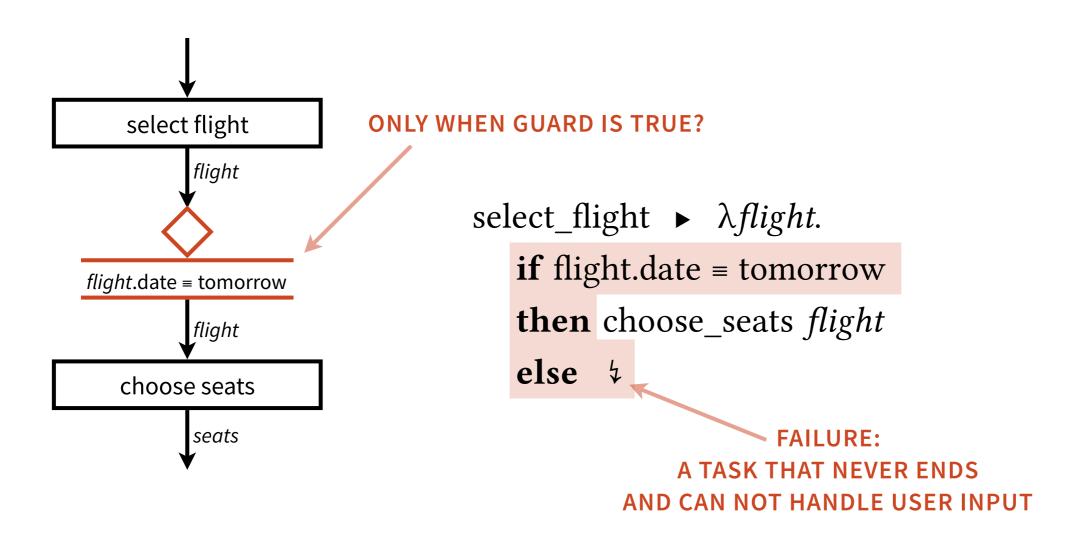
$$\Rightarrow \mathcal{V}(\text{select\_flight}) = v$$

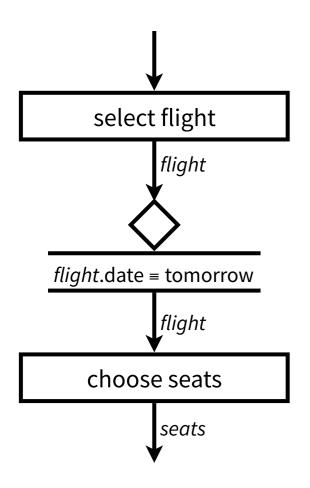


select\_flight ► \(\lambda flight\). choose\_seats \(flight\)



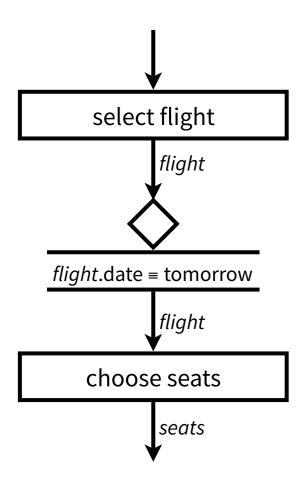






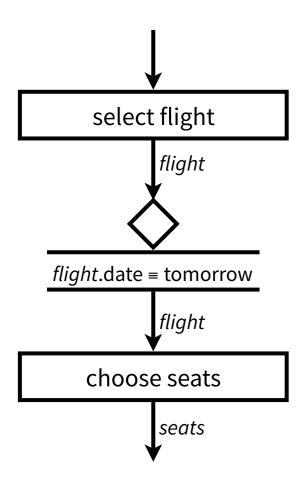
#### WHEN TO PROCEED TO THE NEXT TASK?

$$\Rightarrow \mathcal{V}(\text{select\_flight}) = v$$



#### WHEN TO PROCEED TO THE NEXT TASK?

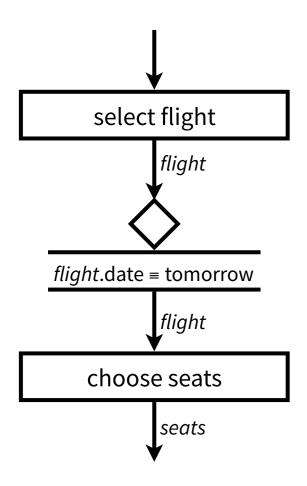
$$\Rightarrow \mathcal{V}(\text{select\_flight}) = v$$
and ...  $(v) \downarrow t$  where  $t \neq 4$ 



#### WHEN TO PROCEED TO THE NEXT TASK?

$$\Rightarrow \mathcal{V}(\text{select\_flight}) = v$$
  
and ...  $(v) \downarrow t \text{ where } t \neq 4$ 

**USING HOST LANGUAGE SEMANTICS!** 



#### WHEN TO PROCEED TO THE NEXT TASK?

$$\Rightarrow \mathcal{V}(\text{select\_flight}) = v$$



**USING HOST LANGUAGE SEMANTICS!** 



#### Take a λ-calculus...

```
Expressions
e :=
                                          - abstraction, application
        \lambda x : \tau . \ e \mid \ e_1 \ e_2
        x \mid c \mid e_1 \star e_2
                                          - variable, constant, operation
        if e_1 then e_2 else e_3 \mid \langle \rangle
                                          - branch, unit
        \langle e_1, e_2 \rangle | fst e | snd e
                                          - pair, projections
                                          - references, location
        ref e \mid !e \mid e_1 := e_2 \mid l
                                          – pretask
                                          Constants
c ::=
        B \mid I \mid S
                                          - boolean, integer, string
```

#### Take a λ-calculus...

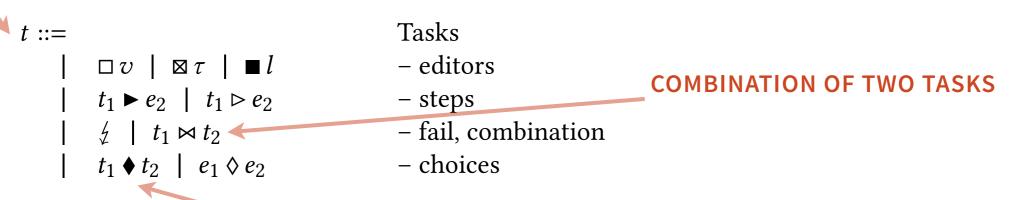
#### ...embed a workflow language

#### Take a λ-calculus...

#### ...embed a workflow language

#### Take a λ-calculus...

## ...embed a workflow language



**CHOICE BETWEEN TWO TASKS** 



Two layers ⇒ two semantics

Two layers ⇒ two semantics

 $e \downarrow v$  standard big step semantics

Two layers ⇒ two semantics

$$e\downarrow v$$
 standard big step semantics

$$p \rightarrow t$$
 SPECIAL TASK SEMANTICS

Two layers ⇒ two semantics



**MAKES USE OF** 

$$p \rightarrow t$$
 SPECIAL TASK SEMANTICS

Two layers ⇒ two semantics

$$e\downarrow v$$
 standard big step semantics

MAKES USE OF

$$p \rightarrow t$$

 $p \rightarrow t$  Special task semantics

S-ThenStay
$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = \bot$$

S-ThenFail
$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = v_{1} \land \mathcal{F}(t_{2}, s'')$$

S-ThenCont
$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = v_{1} \land \mathcal{F}(t_{2}, s'')$$

$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{2}, s'''} \mathcal{V}(t_{1}', s') = v_{1} \land \neg \mathcal{F}(t_{2}, s'')$$

$$e \downarrow v$$
 standard big step semantics

$$p \rightarrow t$$
 SPECIAL TASK SEMANTICS

But interaction... ⇒ additional layer

S-ThenStay 
$$\frac{t_{1},s \rightsquigarrow t_{1}',s'}{t_{1} \blacktriangleright e_{2},s \rightsquigarrow t_{1}' \blacktriangleright e_{2},s'} \mathcal{V}(t_{1}',s') = \bot$$
S-ThenFail 
$$\frac{t_{1},s \rightsquigarrow t_{1}',s'}{t_{1} \blacktriangleright e_{2},s \rightsquigarrow t_{1}' \blacktriangleright e_{2},s'} \mathcal{V}(t_{1}',s') = v_{1} \land \mathcal{F}(t_{2},s'')$$
S-ThenCont 
$$\frac{t_{1},s \rightsquigarrow t_{1}',s'}{t_{1} \blacktriangleright e_{2},s \rightsquigarrow t_{2}',s''} \mathcal{V}(t_{1}',s') = v_{1} \land \neg \mathcal{F}(t_{2},s'')$$

$$e \downarrow \nu$$
 standard big step semantics

$$p \rightarrow t$$
 Special task semantics

But interaction... ⇒ additional layer

$$t \stackrel{i}{\longrightarrow} t'$$
 HANDLING OF USER INPUT

S-ThenStay
$$\frac{t_{1}, s \rightsquigarrow t'_{1}, s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t'_{1} \blacktriangleright e_{2}, s'} \mathcal{V}(t'_{1}, s') = \bot$$
S-ThenFail
$$\frac{t_{1}, s \rightsquigarrow t'_{1}, s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t'_{1} \blacktriangleright e_{2}, s'} \mathcal{V}(t'_{1}, s') = v_{1} \land \mathcal{F}(t_{2}, s'')$$
S-ThenCont
$$\frac{t_{1}, s \rightsquigarrow t'_{1}, s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t'_{2}, s''} \mathcal{V}(t'_{1}, s') = v_{1} \land \neg \mathcal{F}(t_{2}, s'')$$

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$$e \downarrow v$$
 standard big step semantics

$$p \rightarrow t$$
 Special task semantics

But interaction... ⇒ additional layer

$$t \stackrel{i}{\longrightarrow} t'$$
 HANDLING OF USER INPUT

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$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = \bot$$

S-ThenFail
$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = v_{1} \land \mathcal{F}(t_{2}, s'')$$

S-ThenCont
$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{1}' \blacktriangleright e_{2}, s'} \mathcal{V}(t_{1}', s') = v_{1} \land \mathcal{F}(t_{2}, s'')$$

$$\frac{t_{1}, s \rightsquigarrow t_{1}', s'}{t_{1} \blacktriangleright e_{2}, s \rightsquigarrow t_{2}, s'''} \mathcal{V}(t_{1}', s') = v_{1} \land \neg \mathcal{F}(t_{2}, s'')$$





#### Language + Formal semantics



#### Language + Formal semantics

**Tasks** 

- editors

- choices

Proved progress & preservation



#### Language + Formal semantics

**Tasks** 

- editors

- choices

Proved progress & preservation

Implemented in Idris



#### Language + Formal semantics

#### Still to do...

- Task equality
- Pre- and postconditions
- Symbolic execution



#### Language + Formal semantics

#### Still to do...

- Task equality
- Pre- and postconditions
- Symbolic execution

**IDEAS APPRECIATED!** 



# **Summary**



Language & formal semantics



Proved progress & preservation

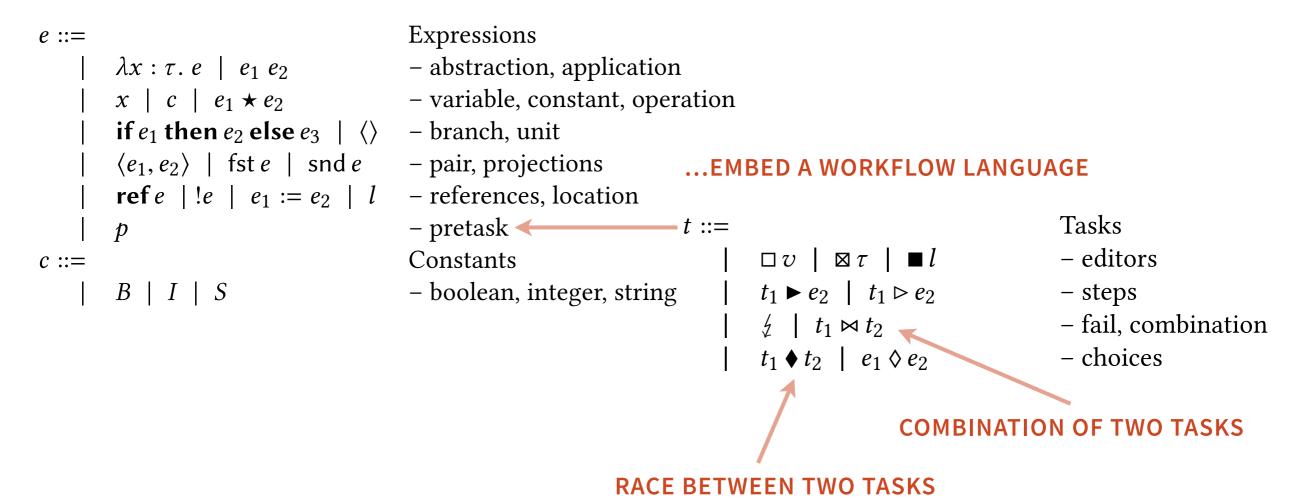


Implemented in Idris



Essence of task oriented programming

#### TAKE A Λ-CALCULUS...





- Language for modular interactive workflows
- Essence of task oriented programming
- Formal semantics
- Proved progress & preservation
- Implemented in Idris

# **Tasks**

