# CS420 Midterm 2

Name:	NetID:

Please read the instructions carefully.

- Please check that this booklet has 14 different pages, including this cover sheet.
- This exam is 75 minutes long.
- Please write your name and NetID in the spaces above.
- This is a **closed-book** exam. No calculators, notes, books, slides, electronic devices, cheat sheets, or other aids allowed.
- **No cheating**. Do not share anything with other students. Do not talk to other students. Do not look at another student's exam. Do not expose your exam to easy viewing by other students. Violation of any of these rules will be counted as cheating.
- Read every problem carefully. Don't get stuck on one problem. Move on and come back later.
- There are 11 problems on this exam. The exam will be scored out of 100 points.
- All the sheets in this exam including all scratch paper will be taken back at the end of the exam.
- MPI syntax is provided for your reference in the exam.
- Last page is left for scratch space.
- Good luck!

Problem	Maximum Points	Points obtained
1	12	
2	12	
3	12	
4	4	
5	4	
6	8	
7	9	
8	10	
9	8	
10	10	
11	12	
Total	100	

# Problem 1 (12 Points)

a. True

		r the following statements are necessary.	true	or false. Each question is worth 2 points. No
1.	It is po	ossible that the isoefficiency for	uncti	on cannot be derived for a parallel algorithm.
	a.	True	b.	False
2.	in tota		lgorit	ore basic computations (floating point addition) thm. The reason it can be faster is because a sequential processors.
	a.	True computation, not because pa		False (It's faster because of overlapped processors are faster)
3.		locking communication can hunication with computation.	elp re	educe execution time by overlapping
	a.	True	b.	False
4.	MPI o	ne-sided communication deco	uples	s data movement from process synchronization.
	a.	True	b.	False
5.		ses a distributed memory modele cores that share memory.	lel. T	hus, it cannot be run on a processor with
	a.	True processes each has its own a		False (It can run on such a processor. The MP ss space.)
6.		harm++ program with P object omatically balance load across		d P processors, the runtime system will be able essors.

than P objects to get the benefit of dynamic load balancing)

b. False (Overdecomposition the data into more

## **Problem 2 (12 Points)**

For the following questions, circle the ONE answer that applies. Each question is worth 3 points. No explanations are necessary.

- 1. A program (or the corresponding parallel algorithm) is said to be scalable, in the sense of isoefficiency, if:
  - a. Parallel efficiency on a given number of processors is greater than 50%.
  - b. As you keep on using more processors for solving the same problem instance, the execution time decreases.
  - c. As you increase the number of processors, it is possible to increase the problem size such that you can regain the efficiency.
  - d. The serial fraction decreases with increased number of processors.
- 2. Consider parallel matrix-matrix multiplication operation on square matrices A, B and C of size NxN each (C = A\*B), with the total number of processors P. Which of the following statement is true?
  - a. The sequential computational complexity is  $O(N^2)$ .
  - b. The 3D algorithm needs  $P = N^3$  processors to work.
  - c. In Cannon's algorithm, local submatrix size of each processor is (N/P) x (N/P).
  - d. The Fox algorithm uses more memory than Cannon's algorithm.
- 3. An MPI OpenMP hybrid program is run on a small cluster of 4 nodes. Each node has 8 cores. Which of the following MPI OpenMP distributions can NOT utilize the entire cluster.
  - a. 32 MPI processes with 1 OpenMP thread each.
  - b. 16 MPI processes with 2 OpenMP threads each.
  - c. 2 MPI processes with 16 OpenMP threads each.
  - d. 8 MPI processes with 4 OpenMP threads each.
- 4. A benefit of AMPI over MPI is:
  - a. AMPI automatically parallelizes your application.
  - b. AMPI automatically overlaps communication and computation.
  - c. AMPI automatically selects the right grain size for communication.
  - d. AMPI allows processes to share global variables.

### **Problem 4 (4 Points)**

Define parallel speedup and parallel efficiency in terms of sequential execution time Ts, number of processors P, and parallel execution time Tp. (Write down the expression only.)

```
Parallel speedup = T_s / T_p
Parallel efficiency = T_s / (P * T_p)
```

## **Problem 5 (4 Points)**

For each of the following scenarios, give one MPI call that can be used to perform the necessary operation. The operations are run using P processes and each operation is independent of each other. Only mention the MPI function name, do not give function arguments or explanations. Each part is worth 2 points.

a. Process with rank 0 has a large array of size N which it needs to distribute evenly to all the processes such that each process holds a unique array of size N/P (assume P divides N).

```
MPI Scatter
```

b. Each process has an array of n elements. Process with rank 0 needs to collect these arrays in order to construct a large array such that the total number of elements is P\*n. Also, the array from process i must be placed before the array from process j if i < j.

MPI Gather

## **Problem 6 (8 Points)**

This problem is about your ability to read and understand MPI program. Consider the following MPI code snippet. Assume all variables are suitably initialized. An in-order tree has been constructed out of all the P processes in the communicator such that integer variables parent, leftchild and rightchild hold the ranks of parent, left child and right child in the tree representation. The value is -1 if no such process exists. [This is similar to the tree construction in MP3.]

```
leftval = rightval = 0;
if (leftchild !=-1)
  MPI Recv(&leftval, 1, MPI DOUBLE, leftchild, 0,
                    MPI COMM WORLD, MPI STATUS IGNORE);
if (rightchild !=-1)
  MPI Recv(&rightval, 1, MPI DOUBLE, rightchild, 0,
                    MPI COMM WORLD, MPI STATUS IGNORE);
val = leftval + rightval + myval;
if (parent !=-1) {
  MPI Send(&val, 1, MPI DOUBLE, parent, 0, MPI COMM WORLD);
   MPI Recv(&val, 1, MPI DOUBLE, parent, 1, MPI COMM WORLD,
                   MPI STATUS IGNORE);
if (leftchild !=-1)
  MPI Send(&val, 1, MPI DOUBLE, leftchild, 1,
                  MPI COMM WORLD);
if (rightchild !=-1)
   MPI Send(&val, 1, MPI DOUBLE, rightchild, 1,
                  MPI COMM WORLD);
```

- a. Each process had a different myval before the code snippet. Describe what the final value of the variable val will be for each process when the code snippet is run. Each process holds the sum of all myval in the variable val when the code snippet is run.
- b. Rewrite the above code snippet with one MPI collective call such that the variable val holds the same value as in the code snippet. Supply not only the function name but also the complete argument list.

```
MPI_Allreduce(&myval, &val, 1, MPI_DOUBLE, MPI_SUM, MPI_COMM_WORLD);
```

# **Problem 7 (9 Points)**

Prefix sum: for a given array of 6 elements, suppose you have 6 processors and each holds a single element. Manually perform recursive doubling algorithm and write down the values being held by each processor in each step.

Rank	P0	P1	P2	Р3	P4	P5
Initial value	-2	3	1	9	-2	0
After 1st step	-2	1	4	10	7	-2
After 2nd step	-2	1	2	11	11	8
After 3rd step	-2	1	2	11	9	9

### **Problem 8 (10 Points)**

In this problem you are asked to design a parallel algorithm for dot-product computation. Given two vector arrays  $\mathbf{A}$  and  $\mathbf{B}$ , both have N scalar elements. Assume you have a distributed memory system of p processors, and n >> p. For simplicity, assume n is divisible by p, and each processor initially gets a consecutive chunk of size n/p from both vectors  $\mathbf{A}$  and  $\mathbf{B}$  and the location is aligned properly for the computation.

$$\mathbf{A} \cdot \mathbf{B} = \sum_{i=1}^{n} A_i B_i = A_1 B_1 + A_2 B_2 + \dots + A_n B_n$$

Image source: Wikipedia. Ai and Bi are scalar elements of the vector arrays

a. Briefly sketch a parallel algorithm that computes dot product  $\mathbf{x} = \mathbf{A} \cdot \mathbf{B}$ . (x is a scalar) At the end of the computation, all processors hold the final result of the dot product in a scalar variable x. You don't have to write the actual program but only have to describe conceptually the computation and communication that have to happen in different steps.

### Steps:

- (1) Perform dot product computation on the locally owned partial vector and store the result in a scalar variable y
- (2) Perform parallel allreduce operation (tree reduction or recursive doubling) on y and store the result in x
- b. Analyze the computation cost and communication cost of your algorithm. Derive the isoefficiency function.

The cost for step (1) is n/p multiplications and (n/p - 1) additions.

The cost for step (2) with tree reduction or recursive doubling is (ts\*logp) for communications, and (logp) additions

Comm-to-comp ratio = k1(n/p) / k2(logp) = k3 (k1, k2, k3 are constants) Total work W = k4\*n

k1((W/k4)/p) / k2(logp) = k3W = O(plogp)

 $*O(p^2)$  is acceptable if the per-process communication cost for all reduce operation is assumed to be O(p)

## **Problem 9 (8 Points)**

The following code snippets are used in an MPI OpenMP hybrid program with MPI\_THREAD\_MULTIPLE. For each of these snippets, mention if the code is correct or not. Give a brief explanation. Assume the variables are initialized properly.

```
#pragma omp parallel
{
    tid = omp_get_thread_num();
    if (tid == 0)
        MPI_Bcast(&N, 1, MPI_INT, 0, comm);
    else if (tid == 1)
        MPI_Allreduce(&n, &s, 1, MPI_DOUBLE, MPI_SUM, comm);
}
```

### Explanation:

Incorrect. Both the collective calls Bcast and Allreduce are performed on the same communicator which is not allowed by MPI.

b. Assume nb is a neighbor rank that has been correctly initialized.

```
#pragma omp parallel
{
    tid = omp_get_thread_num();
    if (tid == 0)
        MPI_Send(&n, 1, MPI_INT, nb, 0, comm);
    else if (tid == 1)
        MPI_Recv(&m, 1, MPI_INT, nb, 0, comm, &status);
}
```

### Explanation:

Correct. MPI allows concurrent point-to-point communication over the same communicator in MPI\_THREAD\_MULTIPLE.

## Problem 10 (10 Points)

Consider a program that takes 20 hours to execute with no checkpoint mechanism. If a fault occurs, the program is restarted from the beginning, and this process is repeated till the complete program runs without any fault.

a. (2 point) The program starts running at T = 0 and the system fails once at T = 14 hrs. What is the total time required to run the program?

The program runs for 14 hrs and fails. It restarts and runs for 20 hrs. Total time is 34 hrs.

b. (3 points) Now assume a checkpoint mechanism has been introduced to the program which creates a checkpoint after 2 hours of program execution. Each dump takes 15 minutes and a restart, if required, takes 30 minutes. How long does the program take now, if there are no faults.

Since program dumps every 2 hours and there need not be a dump at the end of execution, there are 9 dumps in total. This takes 2 hrs 15 minutes. Total time of execution is 22 hrs and 15 minutes

c. (5 points) Now, assume the same checkpoint mechanism as in part b and give the time taken to run the program if the program begins at T = 0, and system fails at T = 14 hrs (as in part a).

The program runs for 14 hrs and fails. At this point, 12 hrs of actual computation and 6 dumps would have been performed, which finished at 13 hrs and 30 minutes. The last 30 minutes of work would go waste. A restart of 30 minutes is performed to restart at the end of 12 hr mark. The remaining 8 hrs of work and 3 dumps are performed to finish the program. This takes 14 + 0.5 + 8 + 0.75 = 23 hrs and 15 minutes.

## **Problem 11 (12 Points)**

Consider matrix vector multiplication with an N x N matrix A and an N x 1 vector X. To perform this operation in parallel,  $P^2$  processes arranged in a P x P grid are used. The matrix A is divided into N/P x N/P blocks and assigned to the processes. The vector X is divided into P chunks of N/P elements and the chunks are assigned to the diagonal processes such that process (i, i) has the i<sup>th</sup> portion. The result vector B = A X is also divided and allotted similar to X, that is, at the end of the computation, the diagonal processes must hold corresponding portions of final B. The following illustration explains this partition for P = 3.

### Matrix A:

Process (0, 0)	Process (0, 1)	Process (0, 2)
Process (1, 0)	Process (1, 1)	Process (1, 2)
Process (2, 0)	Process (2, 1)	Process (2, 2)

#### Vectors X and B

Process (0, 0)
Process (1, 1)
Process (2, 2)

Write an MPI program which performs this multiplication. Assume the function initialize initializes the arrays A, B, X and the variable n provided the row and column numbers. The variables X and B will be null if the process does not hold that array. The setup and initialization has been done for you. Complete the program by filling the gaps. Assume n = N/P.

```
int main(int argc, char **argv) {
  int n, P, rank, row, col;
  double **A, *X, *B;
  MPI_Comm comm2D, comm_row, comm_col;
  int dimsize[2], periodic[2], mycoords[2];

MPI_Init(&argc, &argv);
  MPI_Comm_size(MPI_COMM_WORLD, &P);
  MPI_Comm_rank(MPI_COMM_WORLD, &rank);
  P = sqrt(P);
  dimsize[0]=dimsize[1] = P;
  periodic[0] = periodic[1] = 0;
  MPI_Cart_create(MPI_COMM_WORLD, 2, dimsize, periodic, 0,&comm2D);
  MPI_Cart_coords(comm2D, myrank, 2, mycoords);
```

Sample Exam with solutions

```
row = mycoords[0]; col = mycoords[1];
 MPI_Comm_split(comm2D, row, col, &comm_row);
 MPI Comm split(comm2D, col, row, &comm col);
 // Initializes the arrays and n
 Initialize(&A, &X, &B, &n, row, col);
// Insert declarations here
double *tempB;
int i, j;
 // Perform matrix vector multiplication
// Broadcast X in column
if(row != col)
 X = (double*) malloc (n * sizeof(double));
MPI Bcast(X, n, MPI DOUBLE, col, comm col);
tempB = (double*) malloc (n * sizeof(double));
// Multiply locally
for (i = 0; i < n; i++) {
 for(j = 0; j < n; j++) {
   tempB[i] += A[i][j] * X[j];
// Reduce B across row
MPI Reduce(tempB, B, n, MPI DOUBLE, MPI SUM, row, comm row);
 MPI Finalize();
```

Sample Exam with solutions