Wk 11 Exercises

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9.3.1 (section 9.3.4)

Table 1: Figure 9.8: A utility matrix for exercises

	$\mid a \mid$	b	c	d	e	f	g	h
A	4	5		5	1		3	2
В		3	4	3	1	2	1	
\mathbf{C}	2		1	3		2 4	5	3

Figure 9.8 is a utility matrix, representing the ratings, on a 1-5 star scale, of eight items, a through h, by three users A, B, and C. Compute the following from the data of this matrix.

```
# Utility Matrix #
df \leftarrow data.frame(a = c(4, NA, 2),
              b = c(5, 3, NA),
               c = c(NA, 4, 1),
               d = c(5, 3, 3),
               e = c(1, 1, NA),
               f = c(NA, 2, 4),
               g = c(3, 1, 5),
               h = c(2, NA, 3))
rownames(df) <- c("A", "B", "C")
cn <- colnames(df)</pre>
# User Combinations #
user.pairs <- as.data.frame(t(combn(rownames(df), 2)))</pre>
colnames(user.pairs) <- c("User1", "User2")</pre>
```

9.3.1 (a)

Treating the utility matrix as boolean, compute the Jaccard distance between each pair of users.

```
library(knitr)
# Jaccard Distance #
# Distance function
jaccard.dist <- function(v1, v2) {</pre>
 1 - length(intersect(v1, v2)) / length(union(v1, v2))
# Return boolean to determine set membership
inset <- function(j) {!is.na(j) & as.logical(j)}</pre>
# Apply distance function
jd <- user.pairs</pre>
jd["Jaccard.Distance"] <-</pre>
  apply(user.pairs, 1, function(i) {
    s1 <- cn[sapply(df[i[1], ], inset)]</pre>
    s2 <- cn[sapply(df[i[2], ], inset)]</pre>
    jaccard.dist(s1, s2)
})
# Format output
kable(jd, digits=2)
```

User1	User2	Jaccard.Distance
A	В	0.5
A	\mathbf{C}	0.5
В	\mathbf{C}	0.5

9.3.1 (b)

Repeat part (a), but use the cosine distance.

```
# Cosine Distance #
# ----- #
*** Note: using the cosine distance as defined on **#
#** page 95 of mining massive datasets **#
# Distance function
len <- function(v) { sqrt(sum(v**2)) }</pre>
cosine.dist <- function(v1, v2) {</pre>
 v1[is.na(v1)] <- 0
 v2[is.na(v2)] <- 0
 acos((as.numeric(v1) %*% as.numeric(v2))
      / (len(v1) * len(v2))) * 180/pi
}
# Apply distance function
cd <- user.pairs</pre>
cd["Cosine.Distance"] <-</pre>
 apply(user.pairs, 1, function(i) {
   cosine.dist(df[i[1], ], df[i[2], ])
})
# Format output
kable(cd, digits=2)
```

User1	User2	Cosine.Distance
A	В	53.06
A	\mathbf{C}	52.05
В	\mathbf{C}	59.08

9.3.1 (c)

Treat ratings of 3, 4, and 5 as 1 and 1, 2, and blank as 0. Compute the Jaccard Distance between each pair of users.

```
# Transform Data
binrating <- function(i) {ifelse(i %in% c(3, 4, 5), TRUE, FALSE)}

# Apply distance function
jd.c <- user.pairs
jd.c["Jaccard.Distance"] <-
apply(user.pairs, 1, function(i) {
    s1 <- cn[sapply(df[i[1], ], binrating)]
    s2 <- cn[sapply(df[i[2], ], binrating)]
    jaccard.dist(s1, s2)
})

# Format output
kable(jd.c, digits=2)</pre>
```

User1	User2	Jaccard.Distance
A	В	0.60
A	\mathbf{C}	0.67
В	\mathbf{C}	0.83

9.3.1 (d)

Repeat Part (c), but use the cosine distance.

```
# Apply distance function
cd.d <- user.pairs
cd.d["Cosine.Distance"] <-
    apply(user.pairs, 1, function(i) {
    v1 <- binrating(df[i[1], ])
    v2 <- binrating(df[i[2], ])
    cosine.dist(v1, v2)
    })

# Format output
kable(cd.d, digits=2)</pre>
```

User1	User2	Cosine.Distance
A	В	54.74
A	\mathbf{C}	60.00
В	\mathbf{C}	73.22

9.3.1 (e)

Normalize the matrix by subtracting from each non blank entry the average value for its user.

```
df.normalized <- t(apply(df, 1, function(i) {
   i - mean(i, na.rm=TRUE)
}))
kable(df.normalized, digits=2)</pre>
```

	a	b	c	d	e	f	g	h
A	0.67	1.67	NA	1.67	-2.33	NA	-0.33	-1.33
В	NA	0.67	1.67	0.67	-1.33	-0.33	-1.33	NA
\mathbf{C}	-1.00	NA	-2.00	0.00	NA	1.00	2.00	0.00

9.3.1 (f)

Using the normalized matrix from Part (e), compute the cosine distance between each pair of users.

```
df.normalized[is.na(df.normalized)] <- 0

# Apply distance function
cd.f <- user.pairs
cd.f["Cosine.Distance"] <-
    apply(user.pairs, 1, function(i) {
    v1 <- df.normalized[i[1], ]
    v2 <- df.normalized[i[2], ]
    cosine.dist(v1, v2)
})

# Format output
kable(cd.f, digits=2)</pre>
```

User1	User2	Cosine.Distance
A	В	54.25
A	\mathbf{C}	96.63
В	\mathbf{C}	137.70