ML 2011 Final Project

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In honor of Kobe Bryant

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1 Resources for reproducing this project

The repository containing the raw and cleaned data along with all code required to run the analyses can be found here: https://github.com/joemarlo/ML-NBA.

The original source of the data can be found at these links:

- https://www.kaggle.com/drgilermo/nba-players-stats#player_data.cs
- http://www.espn.com/nba/salaries/_/year/2017
- http://www.espn.com/nba/statistics/rpm/_/year/2017

2 Introduction

2.1 Research question

Are there underlying patterns of groupings between NBA team compensation vs. overall team skill-sets?

2.2 Group member roles

We all collaboratively contributed to the project in all aspects. Specifically, Joe contributed to scraping the player salary, additional player features, and visualizations. Andrew contributed to cleaning the data, hierarchical/K-means models, and post-cluster analysis. Bilal contributed to the hierarchical/K-Means modeling and the write-up. George contributed to the model-based clustering and data transformation.

2.3 Data description

The project is an unsupervised approach to discover underlying patterns or groupings between NBA compensation vs. overall team skill-sets. It uses K-means, hierarchical, and model-based clustering along with other techniques and tools such as principal component analysis, standardizing, scaling, and web-scraping.

The data includes NBA statistics for over 3,000 players, 60+ seasons, and over 50 features per players. The measurement scales are numerical totals and percentages for features such as: points, assists, rebounds, player attributes (height, weight, college attended, etc.). The full dataset represents a time period of 1950-2017, however we are selecting data for the 2016 - 2017 season.

Key feature set:

- MP pg: Minutes played per game
- FG_pg: Field goals made per game
- FGA_pg: Field goal attempts per game
- 3P_pg: 3-point shots made per game
- 3PA_pg 3-points shot attempts per game
- 2P_pg: 2-point shots made per game
- 2PA pg: 2-point shots attempted per game
- FT pg: Free throw shots made per game
- FTA_pg: Free throw shots attempted per game
- TRB_pg: Total rebounds (offensive + defensive) per game
- AST_pg: Total assists per game
- STL pg: Total steals per game
- BLK_pg: Total blocks per game
- PTS pg: Total points made per game

Additional features:

- win_pct: team winning percentage during the regular season (Total wins / total games played)
- Player: First and last name of NBA player
- Team: NBA team player played on. For multiple teams, this is the team the player played on for the most minutes
- Position: NBA position, e.g. C = Center, PF = Power Forward, SG = Shooting Guard, PG = Point Guard
- Salary: Player salary (USD)
- RPM: Real Plus/Minus. Player's average impact in terms of net point differential per 100 offensive and defensive possessions
- VORP: Value Over Replacement Player. Measure to estimate each player's overall contribution to the team

• PER: Player Efficiency Rating. Measures player's overall contributions across different statistics.

2.4 Analysis methods

For this analysis, we applied the following modeling techniques to analyse NBA player data:

- Principal Component Analysis
- Hierarchical Clustering
- K-Means
- Model-Based clustering

2.5 Data exploration and transformation

The data cleaning was done in separate R scripts which can be found within the repo/Data Steps: * Filtered data to the 2016 - 2017 season * Assigned player to one team based on the most minutes he played for, including stats across all teams played for * Scraped player salaries and RPM data from ESPN website, using fuzzy matching on player names to join to the main dataset * Scaled/Transformed data using cube root and standardizing. For model-based clustering, various transformations such as Log + 1, square root, cube root, and Box-Cox were applied. The cube root yielded the best transformation to normalize the data. This was validated using QQ plots. We scaled the data for Hierarchical and K-Means to put all features on an equally weighted basis. For example, minutes played per game vs. blocks per game are on different ranges, so scaling these puts them on a comparable basis.

3 Analysis

3.1 Exploratory data analysis

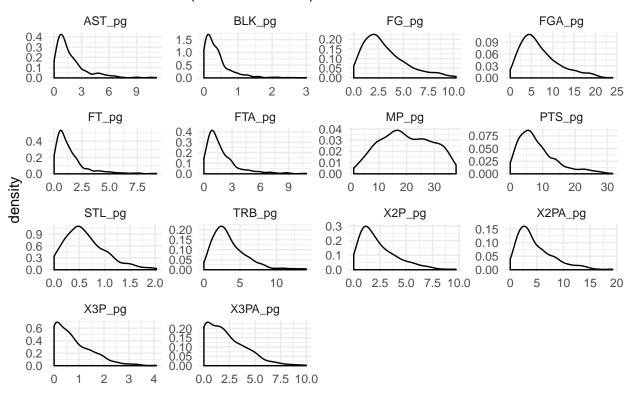
```
library(dendextend)
library(factoextra)
library(GGally)
library(ggfortify)
library(ggrepel)
library(gridExtra)
library(knitr)
library(kableExtra)
library(mclust)
library(NbClust)
library(plyr)
library(rgl)
library(tidyverse)
# set for reproducible results
set.seed(14)
# set theme for ggplot
theme set(theme minimal())
# clear variables
rm(list = ls())
```

We decided to use the 14 features in our analysis (on a per game basis) because they provide a good balance of offensive (e.g Pts, Ast) and defensive stats (e.g. Reb, Blk). This is more likely to provide more balanced groupings between those who are more offensive and those who are better at defense.

With these features, we will explore the distribution of each future.

```
# load data
nba <- read.csv('Data/season_stats_clean.csv')
# replace NA values in RPM column with Os
nba$RPM[is.na(nba$RPM)] <- 0</pre>
```

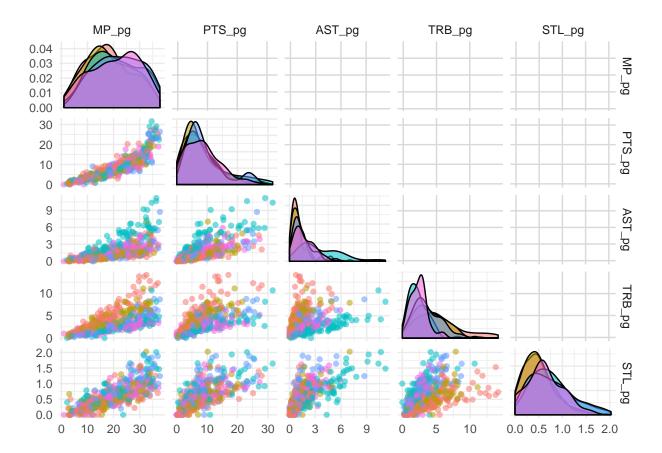
Feature Densities (Untransformed)



We calculate the variance to look at the spread of each feature.

Table 1: Feature Variance

	Variance
MP_pg	82.07
FG_pg	4.67
FGA_pg	20.49
$X3P_pg$	0.57
$X3PA_pg$	3.76
$X2P_pg$	3.23
$X2PA_pg$	11.89
FT_pg	2.04
FTA_pg	2.99
${\rm TRB_pg}$	5.89
AST_pg	3.11
STL_pg	0.17
BLK_pg	0.17
PTS_pg	36.72



We then scaled the data because the ranges of the data can be different. A good example is minutes and blocks per game - most players will have more minutes per game than blocks per game.

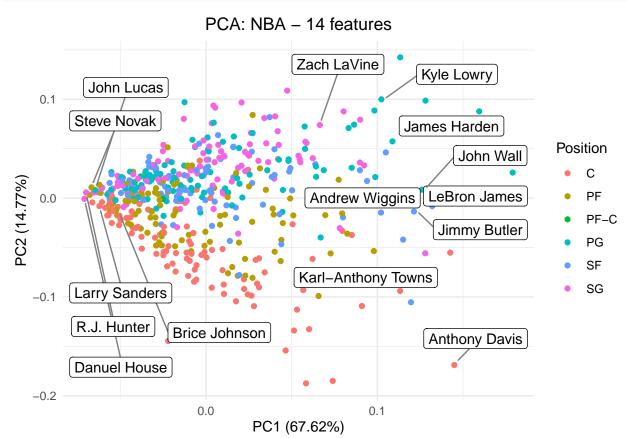
3.2 Principal component analysis

Before running any clustering algorithms, we will perform principal component analysis to determine if there are any inherent groupings among players.

```
nba_feat_sc <- scale(nba_feat)</pre>
# run PCA
nba_pca <- prcomp(nba_feat_sc)</pre>
summary(nba_pca)
## Importance of components:
                                              PC3
                                                      PC4
                                                              PC5
                                                                       PC6
##
                              PC1
                                     PC2
                                                                               PC7
                           3.0767 1.4379 0.88672 0.80819 0.63364 0.52061 0.46651
## Standard deviation
## Proportion of Variance 0.6762 0.1477 0.05616 0.04666 0.02868 0.01936 0.01555
## Cumulative Proportion 0.6762 0.8239 0.88002 0.92667 0.95535 0.97471 0.99026
##
                               PC8
                                       PC9
                                               PC10
                                                       PC11
                                                                 PC12
## Standard deviation
                           0.29741 0.16765 0.10779 0.09065 2.849e-15 2.194e-15
## Proportion of Variance 0.00632 0.00201 0.00083 0.00059 0.000e+00 0.000e+00
## Cumulative Proportion 0.99658 0.99858 0.99941 1.00000 1.000e+00 1.000e+00
##
                                PC14
## Standard deviation
                           1.597e-15
## Proportion of Variance 0.000e+00
## Cumulative Proportion 1.000e+00
# create plot PCA data function
plot_pca <- function(object, frame = FALSE, x = 1, y = 2,
                      data, colour, title, label, leg_title) {
  # plots data in PCA space
  # object = PCA or K-Means object
  # x = which PC for x-axis (1, 2, 3, etc...)
  \# y = \text{which PC for } y - \text{axis } (1, 2, 3, \text{ etc...})
  # object: PCA or K-means object
  # data = underlying data
  p <- autoplot(nba_pca, x = x, y = y, data = nba, colour = colour, frame = frame) +
        ggtitle(title) +
        # center title
        theme(plot.title = element text(hjust = 0.5)) +
        geom_label_repel(aes(label = label),
                         box.padding = 0.35,
                         point.padding = 0.5,
                         segment.color = 'grey50') +
    ## This is supposed to override the autoplot legend title.
    ## Only works when plotting PCA directly. Does not work for HCL and KM objects
    labs(colour = leg_title)
  return(p)
}
```

The first 2 principal components explain the majority of the variance in the feature set, we will plot the data in these two dimensions to better assess player similarities.

At first glance, there are differences between players based on overall statistics. For example, LeBron James and James Harden are near each other, indicating star players may be grouped together. There are also similarities based on player position. For example, Centers/Power Forwards such as Anthony Davis and Karl-Anthony Towns are in the bottom of the chart.



3.3 Clustering

3.3.1 Hierarchical clustering

The first method of clustering we will try is hierarchical clustering. The dendrogram can help provide a visual aid in the number of clusters we can start to use.

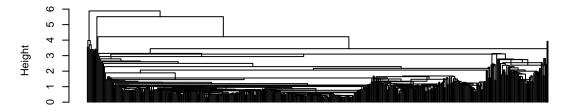
```
# distance matrix for features
nba_dist_sc <- dist(nba_feat_sc, method = 'euclidean')

# try single, centroid, and ward (D2) linkage hier clustering
hcl_single <- hclust(d = nba_dist_sc, method = 'single')
hcl_centroid <- hclust(d = nba_dist_sc, method = 'centroid')
hcl_ward <- hclust(d = nba_dist_sc, method = 'ward.D2')</pre>
```

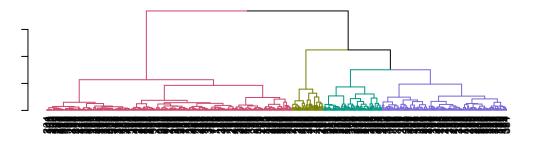
Single Linkage



Centroid Linkage



Ward (D2) Linkage: K = 4



Since the Ward dendrogram seems to be the best among the three, we will look at its distribution for 3 and 4 clusters. We chose these initial groupings because this provides a good start to separate and distinguish between player groups.

```
# add cluster labels to main data
nba$hcl_ward_labs_three <- cutree(hcl_ward, k = 3)
nba$hcl_ward_labs_four <- cutree(hcl_ward, k = 4)

hcl_df_three <- data.frame(table(nba$hcl_ward_labs_three))
hcl_df_four <- data.frame(table(nba$hcl_ward_labs_four))
col_names <- c('Clusters', 'Count')
colnames(hcl_df_three) <- col_names</pre>
```

```
colnames(hcl_df_four) <- col_names
kable(hcl_df_three, caption = 'Three Clusters', format = "markdown")</pre>
```

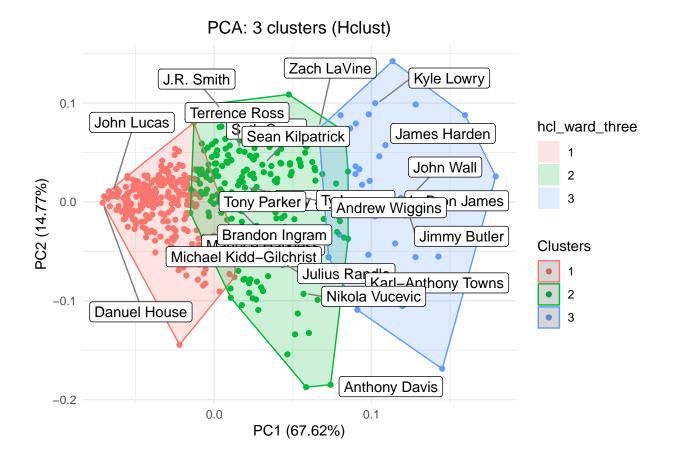
Clusters	Count
1	259
2	194
3	33

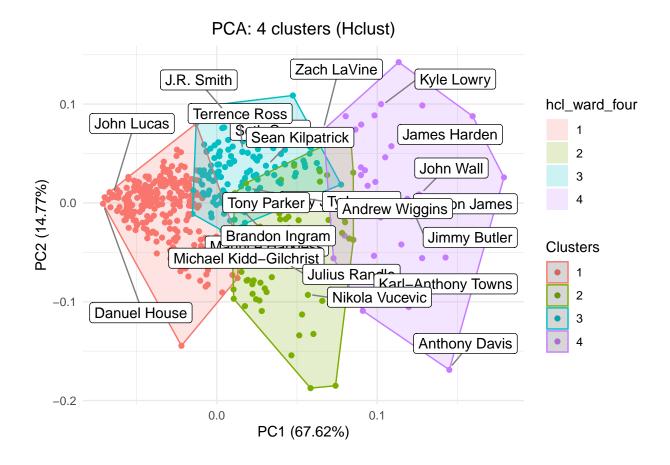
```
kable(hcl_df_four, caption = 'Four Clusters', format = "markdown")
```

Clusters	Count
1	259
2	62
3	132
4	33

Visualizing the clusters in PC space, we see clear separation in the 4-cluster solution vs the 3-cluster method based on apparent skillsets. For example, LeBron James and James Harden (star players) are in one cluster, whereas John Lucas and Danuel House (lower performers) are in the left-most cluster, opposite to the 'star player' cluster on the right. These will be explored further when we look at player statistics by cluster.

```
# add labels to data
nba$hcl_ward_three <- factor(cutree(hcl_ward, k = 3))</pre>
nba$hcl_ward_four <- factor(cutree(hcl_ward, k = 4))</pre>
# player names to include in plot
hcl_labels <- ifelse(nba$MP_pg >= 36 | nba$MP_pg <= 2.5 |
                      (nba$MP_pg >= 28.8 \& nba$MP_pg <= 29) |
                      (nba$MP_pg >= 25 & nba$MP_pg <= 25.2),
                      as.character(nba$Player), '' )
# elements to loop over
hcl_labs <- names(nba %>% select(tail(names(.), 2)))
hcl_ks \leftarrow c(3, 4)
# plot hclust labels superimposed over PCA
for (i in seq_along(hcl_labs)) {
 p <- plot_pca(nba_pca, frame = TRUE,</pre>
                data = nba, colour = hcl_labs[i],
                 title = paste0('PCA: ', hcl_ks[i], ' clusters (Hclust)'),
                 label = hcl_labels,
                leg_title = 'Clusters'
  )
  print(p)
```





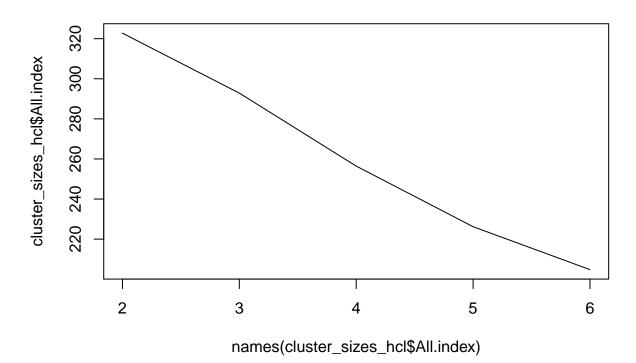
3.3.1.1 Optimize number of clusters

To optimize the number of clusters, we used two index methods: Calinski-Harabasz and Silhouette. These methods measure how well separated clusters are, and how homogeneous data is within each cluster. Both indices yield 2 as the optimal number.

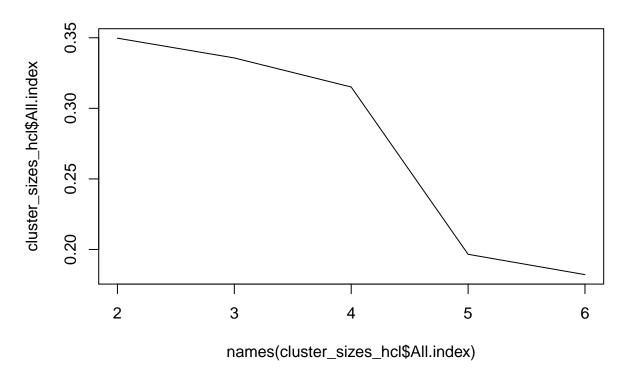
Although the indices say 2 is optimal, these does not provide enough distinction or separation among players. However, the Silhouette index provides 4 as a local maximum. This provides a more practical distinction among players.

Methods: Calinski-Harabasz index and Silhouette

Calinski-Harabasz index: HCL



Silhouette index: HCL



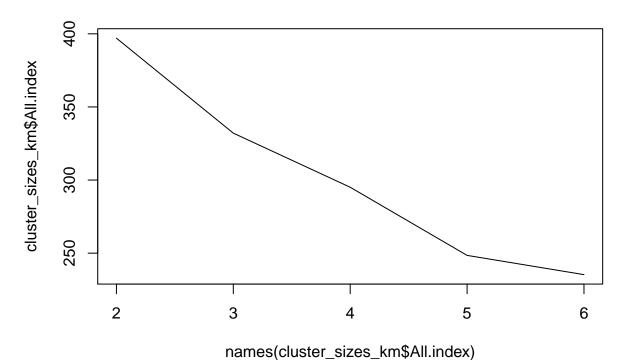
3.3.2 K-Means

3.3.2.1 Optimize number of clusters

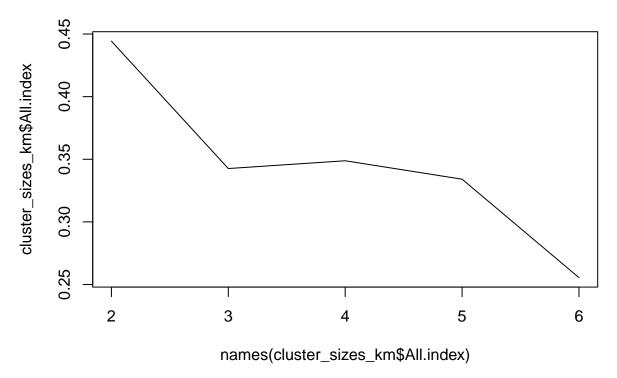
Similar to the optimization for hierarchical, we found similar results for K-Means. We decided with the 4-cluster solution based on the Silhouette index (local maximum.)

Method: Calinski-Harabasz index

Calinski-Harabasz index: K-Means



Silhouette index: K-Means



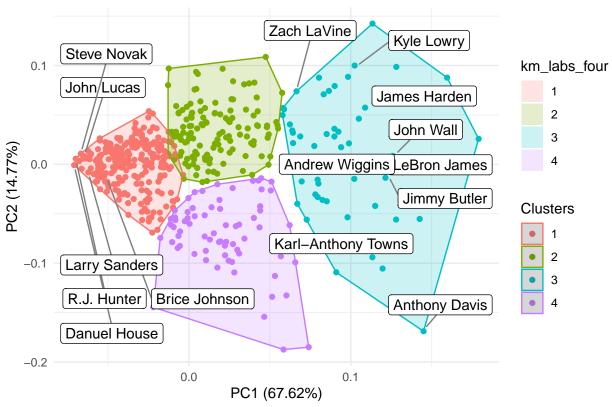
3.3.2.2 K-means clustering with four groups

Compared to the hierarchical solution presented earlier, there is cleaner separation in the K-Means plot. We will see how these clusters are separated by inspecting features within each group.

Table 4: K-Means Player Distribution

Clusters	Count
1	236
2	130
3	51
4	69





One explanation for the imbalanced number of players across clusters is that player skillset level is inherently imbalanced. This imbalance is reflected in the univariate plots, where most densities were positively skewed. This suggests that there a few players whose statistics significantly exceed those of the average player. This is also reflected in the average statistics by cluster shown below.

Table 5: Average Stats by Cluster

km_labs_four	MP_pg	PTS_pg	TRB_pg	AST_pg	BLK_pg	STL_pg	VORP	PER	RPM
1	12.25	3.95	2.13	0.88	0.24	0.35	-0.07	10.19	-1.95
2	25.62	10.31	3.48	2.52	0.29	0.82	0.50	12.75	-0.86
3	33.86	21.82	5.72	4.73	0.62	1.16	3.19	21.29	2.51
4	24.97	10.30	7.01	1.64	0.95	0.79	1.27	17.10	0.37

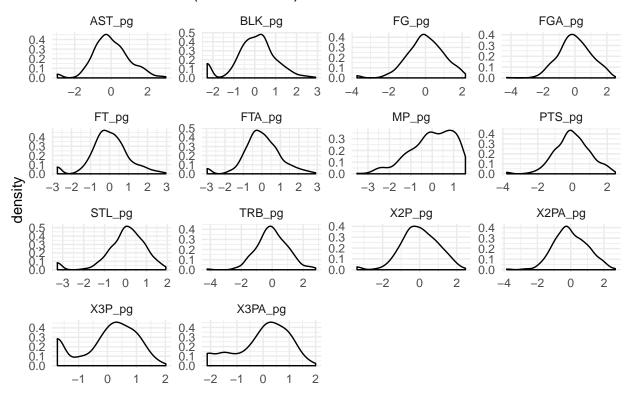
```
kable_styling(latex_options = c("striped", "scale_down"))
```

3.3.3 Model-based clustering

To test alternative approaches to Hierarchical and K-Means clustering, we will perform model-based clustering. Prior to modeling, we will transform the data using the cube root. This normalizes the data, which is a key assumption in model-based clustering. We tested other transformations such as the square root, Box-Cox, and $\log + 1$. Of these, The cube root yielded the best transformation for model-based clustering.

```
# transform features
nba_feat_cr <- (nba_feat) ^ (1/3)
# scale transformed features
nba_feat_cr_sc <- scale(nba_feat_cr)</pre>
```

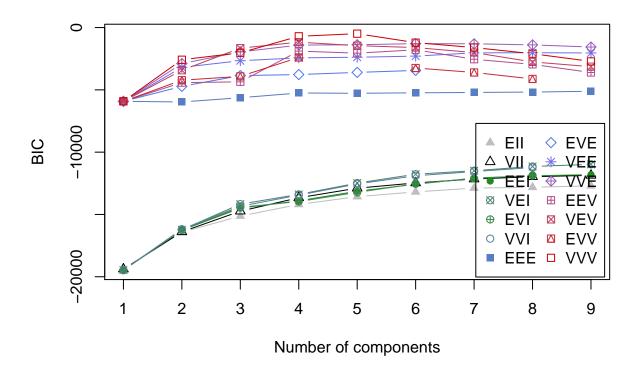
Feature Densities (Transformed)



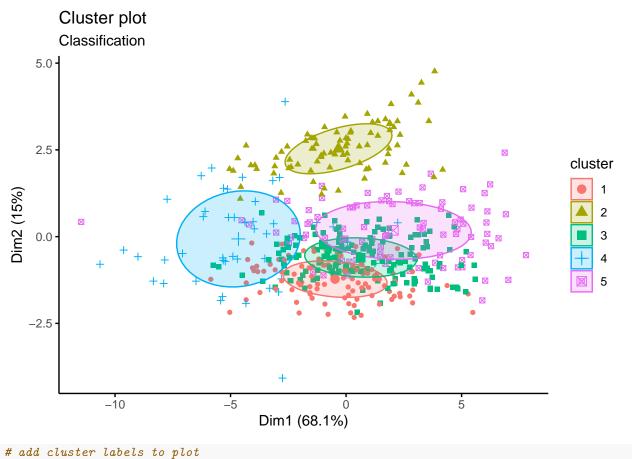
The model-based clustering produced a five-cluster solution based on the BIC. Compared to the previous methods, model-based clustering tended to group players by moreseo by style of play. On the other hand,

K-Means and Hierarchical appear to cluster on overall skillsets across statistics. The clusters also align more with the original PCA plot by position. This type of clustering suggests emphasis on style of play, e.g. better rebounders/blockers, better passers, scorers, etc.

```
# run model
player_clust.mcl <- Mclust(nba_feat_cr_sc)</pre>
summary(player_clust.mcl)
## Gaussian finite mixture model fitted by EM algorithm
##
##
## Mclust VVV (ellipsoidal, varying volume, shape, and orientation) model with 5
##
   components:
##
                                  BIC
    log-likelihood
                                            ICL
##
                     n df
          1607.448 486 599 -490.6436 -505.4606
##
##
## Clustering table:
##
     1
         2
             3
                 4
                     5
## 106 84 160 45 91
plot(player_clust.mcl, what = "BIC")
```



```
# plot results
fviz_mclust(player_clust.mcl, "classification", geom = "point")
```



nba\$mcl_labs <- player_clust.mcl\$classification

3.3.4 Compare methods between clusters

3

5 118

0 33

##

##

Between HCL and KM, the maximum possible agreement between clusters is 87% (424 / 486). Between HCL and MCL, the maximum possible agreement between clusters is 30% (148 / 486). Between KM and MCL, the maximum possible agreement between clusters is 41% (201 / 486).

Based on the analysis, MCL tends to group players by position, whereas HCL and KM tend to cluster based on overall player statistics. This conclusion was reached based on inspecting distributions of player positions across the clustering methods. Because we are looking at player statistics and team compensation, the model-based clustering is not an ideal fit for this purpose.

```
# run crosstabs between cluster methods
xtab hcl km <- xtabs(~nba$hcl ward four + nba$km labs four)
xtab_hcl_mcl <- xtabs(~nba$hcl_ward_labs_four + nba$mcl_labs)</pre>
xtab_km_mcl <- xtabs(~nba$km_labs_four + nba$mcl_labs)</pre>
xtab hcl km
##
                     nba$km labs four
## nba$hcl_ward_four
##
                                 0
                                    24
                                    42
##
                    2
                             8
                                12
```

3

0

6

xtab_hcl_mcl ## nba\$mcl_labs ## nba\$hcl_ward_labs_four 1 2 3 5 ## 1 55 60 75 41 28 ## 24 12 1 25 3 18 ## 0 63 3 48 ## 3 0 10 0 20 xtab_km_mcl

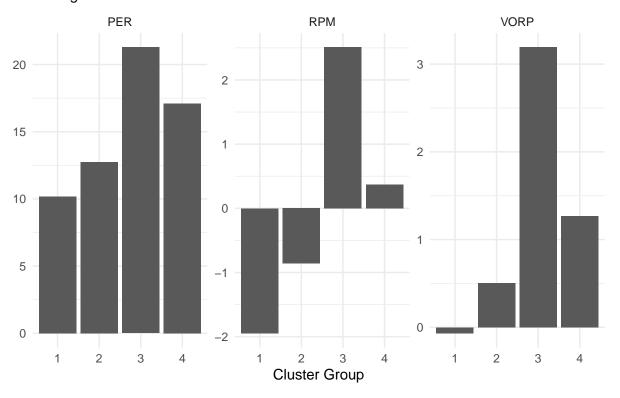
##	nba\$mcl_labs							
##	nba\$km_labs_four	1	2	3	4	5		
##	1	52	40	74	41	29		
##	2	51	0	63	2	14		
##	3	3	0	16	0	32		
##	4	0	44	7	2	16		

3.4 Final cluster selection

K-Means (4 clusters) was the optimal solution. Comparing the HCL and KM cluster plots (per above) reveals the K-Means produces clearer separation of players based on overall skillsets.

We validated this by comparing the clusters against advanced statistics. PER, VORP, and RPM are advanced statistics commonly used to assess general player performance. None of these statistics were used in the cluster modeling.

Overall Player Performance by Cluster Average Advanced Statistics



4 Conclusion

4.1 Post-cluster analysis

We will now look at different statistics and demographics to assess cluster membership and draw insights.

There is potential to update salaries based on player tiers. For example, Chandler Parsons was paid 22M but is considered a low performer, and is paid more than star players such as Steph Curry (12M) and Kawhi Leonard (17.6M). This shows that salary is not necessarily strongly correlated with player performance.

4.1.1 Clusters vs. player salaries

PER vs. Salary

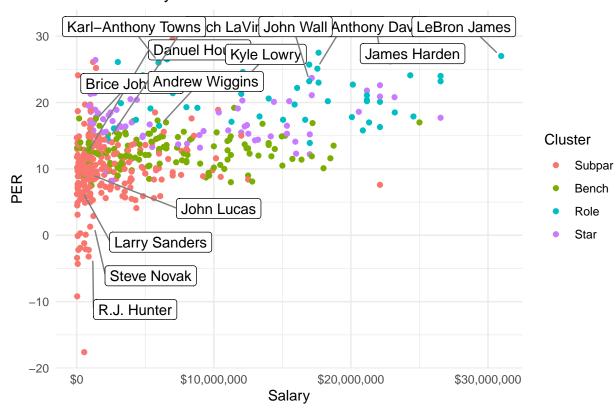


Table 6: Highest Paid Players: Subpar

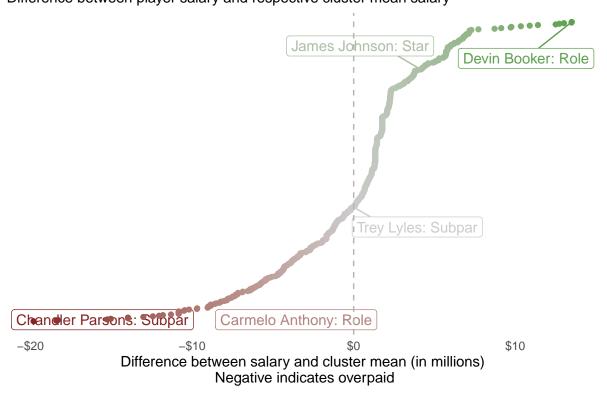
Player	G	MP_pg	Tm	Salary	PER	km_labs_opt_names
Chandler Parsons	34	19.85	MEM	22,116,750	7.6	Subpar
Miles Plumlee	45	10.76	MIL	12,500,000	8.4	Subpar
Amir Johnson	80	20.10	BOS	12,000,000	15.0	Subpar
Mirza Teletovic	70	16.19	MIL	10,500,000	8.8	Subpar
Al Jefferson	66	14.11	IND	10,314,532	18.9	Subpar
Alec Burks	42	15.55	UTA	10,154,495	11.6	Subpar

Table 7: Lowest Paid Players: Star Players

Player	G	MP_pg	Tm	Salary	PER	km_labs_opt_names
Alan Williams	47	15.06	РНО	874,636	19.5	Star
JaMychal Green	77	27.29	MEM	980,431	13.5	Star
Terrence Jones	54	23.52	NOP	980,431	16.1	Star
Edy Tavares	2	14.00	CLE	1,000,000	21.3	Star
Richaun Holmes	57	20.93	PHI	1,025,831	18.6	Star
Ivica Zubac	38	16.03	LAL	1,034,956	17.0	Star

The chart below indicates how much a player is overpaid or underpaid with respect to their cluster average salary. For example, Chandler Parsons was paid 22M vs. the cluster salary average (~2M), indicating he was overpaid. It is important to note that there are players who may have been injured, so their statistics may not be commensurate to their salaries.

Finding Over/underpaid players based on cluster membership Difference between player salary and respective cluster mean salary

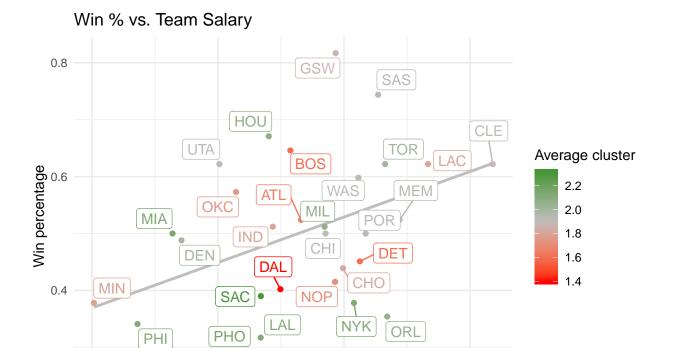


4.1.2 Team compensation and performance vs. clusters

Tm	team_salary	win_pct	avg_clust
SAC	86,799,609	0.39	2.31
PHO	78,930,157	0.29	2.17
MIA	72,782,449	0.50	2.14
NYK	$101,\!570,\!502$	0.38	2.12
LAL	86,775,415	0.32	2.12
PHI	$67,\!225,\!712$	0.34	2.11
HOU	88,062,247	0.67	2.07
MIL	96,913,241	0.51	2.06
ORL	106,849,160	0.35	2.06
DEN	$74,\!208,\!517$	0.49	2.00
TOR	106,521,470	0.62	2.00
MEM	108,808,118	0.52	1.94
SAS	105,410,231	0.74	1.94
CHI	97,064,073	0.50	1.93
UTA	80,223,193	0.62	1.93
WAS	102,276,673	0.60	1.93
POR	103,439,444	0.50	1.93
CLE	123,591,014	0.62	1.88
GSW	98,681,493	0.82	1.87
СНО	$99,\!830,\!531$	0.44	1.82
IND	88,698,690	0.51	1.80
LAC	113,327,068	0.62	1.80
BRK	75,102,568	0.24	1.79
MIN	$60,\!311,\!572$	0.38	1.79
OKC	82,858,524	0.57	1.75
NOP	98,573,436	0.42	1.71
ATL	93,172,774	0.52	1.65
BOS	$91,\!484,\!921$	0.65	1.60
DET	$102,\!503,\!259$	0.45	1.60
DAL	89,904,500	0.40	1.40

Although a team can have better players on average clusters, there are many variables at play here. A team can be better on average but poor management or coaching can affect a team's overall performance, e.g. NYK. Interestingly, GSW did not have the highest average cluster rating, because their bench is not very strong. This speaks to the strong influence that starter players can have on team performance. Another interesting note is that teams can play well even if they do not have many all-stars or a strong overall team, e.g BOS. This could be driven by great coaching and team chemistry. It is important to note that items such as injuries could greatly influence win %, even if players have high ratings.

Although there is a correlation between overall team salary and win %, it is interesting that average player rating does not necessarily align with overall win %.



BRK •

\$80,000,000

\$60,000,000

```
# Inspect some teams
teams sample <- c('NYK', 'GSW', 'BOS')</pre>
teams_sample_list <- list(rep(NA, length = length(teams_sample)))</pre>
for (i in seq_along(teams_sample)) {
  teams_sample_list[[i]] <- nba %>%
    filter(Tm == teams_sample[i]) %>%
    arrange(desc(km_labs_four)) %>%
    select(Player, PER, cl_label)
}
# change index to see different teams
team index <- 2
team_sample <- data.frame(teams_sample_list[team_index])</pre>
colnames(team_sample) <- c('Player', 'PER', 'Cluster')</pre>
teams_sample_list[[2]] %>%
  kable(booktabs = TRUE) %>%
  kable_styling(latex_options = c("striped"))
```

\$100,000,000

Team salary

\$120,000,000

Player	PER	km_labs_opt_names
Draymond Green	16.5	Star
Zaza Pachulia	16.1	Star
Stephen Curry	24.6	Role
Kevin Durant	27.6	Role
Klay Thompson	17.4	Role
Andre Iguodala	14.4	Bench
Ian Clark	13.1	Subpar
Damian Jones	5.3	Subpar
Shaun Livingston	10.1	Subpar
Kevon Looney	13.4	Subpar
James Michael	13.0	Subpar
Patrick McCaw	8.6	Subpar
JaVale McGee	25.2	Subpar
Anderson Varejao	9.4	Subpar
David West	16.6	Subpar

4.2 Final thoughts