

## **United International University (UIU)**

Dept. of Computer Science & Engineering (CSE)

Midterm Exam Total Marks: 30 Fall 2021

Course Code: CSE 2217 Course Title: Algorithms

Time: 1 hour 45 minutes

Any examinee found adopting unfair means will be expelled from the trimester / program as per UIU disciplinary rules.

There are **FOUR** questions. **Answer all of them**. Show full simulation/tabulations wherever necessary. Figures in the right-hand margin indicate full marks.

1. (a) Derive the best-case and the worst-case running-time equations for the following function has common and express those in Big-Oh (O) notation. Also provide the best-case and the worst-case examples of the arrays A and B with n = 4 and m=5 for the function has common.

[2+2]

(b) Derive the exact-cost equation for the running-time of the following function bubble sort and prove that it is in  $O(n^2)$ .

- 2. (a) Determine a good asymptotic upper bound for the following recurrence equation:  $T(n) = 2T(\frac{n}{2}) + O(1)$ , where T(1) = O(1).
  - (b) Consider a modified version of the Merge sort algorithm as follows: [2]

If the array size is less than or equal to 2, then it sorts the array at constant time. Otherwise, it divides the array of size n into 3 subarrays, each with a size of n/3. This division takes  $O(n^2)$  time. Then the algorithm sorts the subarrays recursively, and then merges their solutions at time O(n). Write a recurrence relation for the running-time T(n) of this algorithm.

- 3. (a) Given an array  $A = \{-2, 8, -4, 2, -6, 4\}$ , find the maximum-sum continuous subarray using divide-and-conquer approach. You must show the recursion tree and clearly mention left, right and crossing sum for each tree node.
  - (b) What is the activity selection problem? Is it true that the activity selection problem has one unique optimal solution? [2]

[3]

[3]

- (c) "Data encoded using Huffman coding is uniquely decodable"- is the statement true or false? Justify your answer.
- (d) Information to be transmitted over the internet contains the following characters with their associated frequencies as shown in the following table:

Character	a	е	1	n	0	S	t
Frequency	45	65	13	45	18	22	53

Use Huffman technique to answer the following questions:

- i. Build the Huffman code tree for the message and find the codeword for each character.
- ii. If the data consists of only these characters, what is the total number of bits to be transmitted? What is the percentage saving if the data is sent with 8-bit ASCII values without compression?
- **4. (a)** What is Optimal Substructure property? How Dynamic Programming differs from Divide-and-Conquer problems in terms of subproblems?
  - (b) Suppose, on a cold winter morning, you went to Starbucks to buy a hot chocolate coffee. After paying the bill, the cashier needed to give you a total change of 7 cents. There is a huge supply of 1 cent, 2 cents, and 5 cents coins available in the cashbox. You don't want to carry many coins, so you asked her to return the change using a minimum number of coins. Determine how many coins she should return in this scenario by applying the Dynamic Programming Process?
  - (c) Determine the maximum profit for the 0-1 Knapsack problem given in the following table using Dynamic Programming.

Knapsack Weight: 8 kg

Objects	(1)	(2)	(3)	(4)
Weight (kg)	5	4	6	3
Profit (\$)	11	10	12	9

Also show that **Greedy Strategy** for the 0-1 Knapsack problem fails to achieve the maximum profit for the same objects.