



United International University (UIU)
Dept. of Computer Science & Engineering (CSE)
Mid Exam Year: 2021 Trimester: Summer
Course: CSE 2217/CSI 227 Data Structure and Algorithms II,
Total Marks: 20, Time: 1 hour, Upload & Download: 15 min

(Any examinee found adopting unfair means will be expelled from the trimester / program as per UIU disciplinary rules)

There are THREE questions. Answer all of them. Figures in the right-hand margin indicate full marks.

1. a) What does it mean when we say that an algorithm X is asymptotically more efficient than Y? [1]
- b) Prove that divide and conquer method will give maximum sum subarray in $O(n \log n)$ time when $n > 1$ [2]
- c) Suppose you have to choose among two algorithms to solve a problem: [2]
- Algorithm X solves an instance of size n by recursively solving four instances of size $n/2$, and then combining their solutions in time $O(n)$.
 - Algorithm Y solves an instance of size n by recursively solving four instances of size $3n$, and then combining their solutions in time $O(1)$.
- Which one is preferable, and why?
- d) Analyze the time complexity of the following algorithm and express in big-O notation: [2]

```
func eatChips(int bowlOfChips) {  
    Println("Have some chips!")  
    for chips := 0; chips <= bowlOfChips; chips++ {  
        // dip chips  
    }  
    Println("No more chips.")  
}  
  
func pizzaDelivery(int boxesDelivered) {  
    Println("Pizza is here!")  
    for pizzaBox := 0; pizzaBox <= boxesDelivered; pizzaBox++ {  
        // open box
```

```

    for pizza := 0; pizza <= pizzaBox; pizza++ {
        // slice pizza
        for slice := 0; slice <= pizza; slice++ {
            // eat slice of pizza
        }
    }

    Println("Pizza is gone.")
}

```

2. a) Find an optimal solution to the 0/1 knapsack instance of $n = 4$, $W = 5$, $(v_1, v_2, v_3, v_4) = (50, 30, 35, 60)$, and $(w_1, w_2, w_3, w_4) = (2, 2, 1, 3)$. [3+2]
Also find the optimal solution considering the fractional knapsack problem for the same instance.

- b) Consider the following five symbols present in a file along with their frequencies: [2+1]

a	b	c	d	e
3	1	1	3	2

Construct the tree for finding codes from the Huffman encoding algorithm and write the optimal encoding codes for each symbol. **You must show the tree constructed by the algorithm and for each intermediate constructed node mention the creation sequence number.** For example, if you form a node t with a and b at first mention 1 beside the node t and then if form a node s with c and d next mention 2 beside the node s .

3. a) Discuss how the problem of computing the Fibonacci sequence demonstrates overlapping subproblems. Also, discuss how dynamic programming helps optimizing the computation. [2]
- b) How can you detect cycle in a directed graph using DFS? [1]
- c) Maloins are used as coins in the Maliceland for daily transactions. In its monetary system, Maliceland has the following coins available: $\{1, 7, 12, 25\}$. Show an example of an amount where the greedy strategy for the Coin-Change problem does not provide an optimal solution. [2]