

United International University

School of Science and Engineering

Mid Assessment Trimester: Summer-2020 Course Title: Probability and Statistics Course Code: Stat 205 Marks: 20 Time: 1 Hour

There are 3 questions. Answer question no. 1 and any one from 2 and 3.

- 1. a) During a visit to a doctor's chamber, the probability of having neither medical test not [3] a referral to a specialist is 19%. Of those coming to that chamber, the probability of having a medical test is 37% and the probability of having referral is 54%. What is the probability of having both medical test and referral?
 - b) Bowl *A* contains 7 red and 5 white chips, and bowl *B* contains 9 white and 6 red [3] chips. A chip is drawn at random from bowl *B* and transferred to bowl *A*. Find the probability of then drawing a same color chip from bowl *A*.
 - c) Bean seeds from supplier A have germination rate 76% and those from supplier B [4] have germination rate 87%. A seed-packaging company purchases 53% from supplier A and remaining from supplier B and mixes these seeds together.
 - (i) If a seed germinates find the probability that it has been provided by supplier A.
 - (ii) If a seed does not germinate find the probability that it has been provided by supplier B.
- 2. a) Let a chip be taken at random from a bowl that contains *seven* white chips, *four* red [6] chips, and *one* blue chip. Let the random variable X = 1 if the outcome is a *red chip*, let X = 4 if the outcome is a *white chip*, and let X = 7 if the outcome is a *blue chip*.
 - (i) Find the pmf of X.
 - (ii) Draw a *line graph* and *probability histogram* for this *pmf*.
 - (iii) Find the mean and variance of X.
 - **b)** The life **X** (in years) of a voltage regulator of a car has the **pdf**;

$$f(x) = \frac{3x^2}{9^3}e^{-(\frac{x}{9})^3}; \quad x > 0$$

[4]

- (i) What is the probability that this regulator will last at least 9 years?
- (ii) Find the 37th percentile of f(x).

- 3. a) Show that the mgf of a random variable X is $M(t) = \frac{e^{2t}}{(e^t 2)^2}$. Hence, find the mean [4] and $standard\ deviation$ of the corresponding probability distribution.
 - **b)** Flaws in a certain type of drapery material appear on the average of *two* in **175** square [3] feet. If we assume a Poisson distribution, find the probability of at most *one* flaw appearing in **250** square feet.
 - c) It is claimed that 21% of the people in a certain region are infected by severe virus [3] attack. Suppose 15 people are selected at random. Let *X* equal to the number of people infected by the virus. Assuming independence, how *X* is distributed. Find the probability that (i) at least 3 people are infected, (ii) exactly 12 people are infected.

Formulae:

$$Pmf/pdf$$

$$Hypergeometric$$

$$f(x) = \frac{N_{1}_{C_x} N_{2}_{C_{n-x}}}{N_{C_n}}; \quad N = N_1 + N_2, \qquad x = 1, 2, \dots n$$

$$Geometric$$

$$f(x) = q^{x-1}p; \quad x = 0, 1, 2, \dots$$

$$f(x) = n_{C_x}p^xq^{n-x}; \quad x = 0, 1, 2, \dots n$$

$$f(x) = \frac{\lambda^x e^{-\lambda}}{x!}; \quad x = 0, 1, 2, \dots n$$

$$f(x) = \frac{1}{b-a}; \quad a \le x \le b$$

$$Exponential$$

$$f(x) = \frac{1}{b-a}; \quad a \le x \le b$$

$$f(x) = \frac{1}{b-a}; \quad 0 \le x < \infty$$

$$f(x) = \frac{1}{a}e^{-\frac{x}{\theta}}; \quad 0 \le x < \infty$$

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