

# Data Mining

## Lab - 6

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# Dimensionality Reduction using NumPy

### What is Data Reduction?

Data reduction refers to the process of reducing the amount of data that needs to be processed and stored, while preserving the essential patterns in the data.

### Why do we reduce data?

- To reduce computational cost.
- To remove noise and redundant features.
- To improve model performance and training time.
- To visualize high-dimensional data in 2D or 3D.

Common data reduction techniques include:

- Principal Component Analysis (PCA)
- Feature selection
- Sampling

### What is Principal Component Analysis (PCA)?

PCA is a **dimensionality reduction technique** that transforms a dataset into a new coordinate system. It identifies the **directions (principal components)** where the variance of the data is maximized.

### Key Concepts:

- **Principal Components:** New features (linear combinations of original features) capturing most variance.
- **Eigenvectors & Eigenvalues:** Used to compute these principal directions.
- **Covariance Matrix:** Measures how features vary with each other.

PCA helps in **visualizing high-dimensional data**, **noise reduction**, and **speeding up algorithms**.

### NumPy Functions Summary for PCA

Function	Purpose
<code>np.mean(X, axis=0)</code>	Compute mean of each column (feature-wise mean).
<code>X - np.mean(X, axis=0)</code>	Centering the data (zero mean).
<code>np.cov(X, rowvar=False)</code>	Compute covariance matrix for features.
<code>np.linalg.eigh(cov_mat)</code>	Get eigenvalues and eigenvectors (for symmetric matrices).
<code>np.argsort(values)[::-1]</code>	Sort values in descending order.
<code>np.dot(X, eigenvectors)</code>	Project original data onto new axes.

```
In [8]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

# Step 1: Load the Iris Dataset

```
In [9]: iris = pd.read_csv('iris.csv')
iris
```

```
Out[9]:
```

	sepal_length	sepal_width	petal_length	petal_width	species
0	5.1	3.5	1.4	0.2	setosa
1	4.9	3.0	1.4	0.2	setosa
2	4.7	3.2	1.3	0.2	setosa
3	4.6	3.1	1.5	0.2	setosa
4	5.0	3.6	1.4	0.2	setosa
...	...	...	...	...	...
145	6.7	3.0	5.2	2.3	virginica
146	6.3	2.5	5.0	1.9	virginica
147	6.5	3.0	5.2	2.0	virginica
148	6.2	3.4	5.4	2.3	virginica
149	5.9	3.0	5.1	1.8	virginica

150 rows × 5 columns

```
In [10]: x = iris.drop(columns = "species")
y = iris['species'].map({
    "setosa" : 0,
    "virginica" : 1,
    "versicolor" : 2
})
print("Dimension of iris", x.shape)
```

Dimension of iris (150, 4)

## Step 2: Standardize the data (zero mean)

```
In [12]: x_meaned = x - np.mean(x, axis = 0)
print("Data after centering (first 5 rows): \n", x_meaned[:5])
print(x_meaned.shape)
```

Data after centering (first 5 rows):

	sepal_length	sepal_width	petal_length	petal_width
0	-0.743333	0.442667	-2.358	-0.999333
1	-0.943333	-0.057333	-2.358	-0.999333
2	-1.143333	0.142667	-2.458	-0.999333
3	-1.243333	0.042667	-2.258	-0.999333
4	-0.843333	0.542667	-2.358	-0.999333

(150, 4)

## Step 3: Compute the Covariance Matrix

```
In [13]: cov_mat = np.cov(x_meaned, rowvar = False)
print("Covariance matrix shape:", cov_mat.shape)
print(cov_mat)
```

Covariance matrix shape: (4, 4)

```
[[ 0.68569351 -0.042434  1.27431544  0.51627069]
 [-0.042434   0.18997942 -0.32965638 -0.12163937]
 [ 1.27431544 -0.32965638  3.11627785  1.2956094 ]
 [ 0.51627069 -0.12163937  1.2956094   0.58100626]]
```

## Step 4: Compute eigenvalues and eigenvectors

```
In [17]: eigen_values, eigen_vectors = np.linalg.eigh(cov_mat)
print("Eigenvalues:\n", eigen_values)
```

Eigenvalues:

```
[0.02383509 0.0782095  0.24267075 4.22824171]
```

```
In [18]: print("Eigenvecctors (first 2):\n", eigen_vectors)
```

```
Eigenvecctors (first 2):  
[[ 0.31548719  0.58202985  0.65658877 -0.36138659]  
 [-0.3197231  -0.59791083  0.73016143  0.08452251]  
 [-0.47983899 -0.07623608 -0.17337266 -0.85667061]  
 [ 0.75365743 -0.54583143 -0.07548102 -0.3582892  ]]
```

## Step 5: Compute eigenvalues and eigenvectors

```
In [19]: sorted_index = np.argsort(eigen_values) [::-1]  
sorted_eigenvalues = eigen_values[sorted_index]  
sorted_eigenvectors = eigen_vectors[:, sorted_index]  
print("sort index", sorted_index)  
print("sort eigen_value", sorted_eigenvalues)  
print("sort eigen_vector", sorted_eigenvectors)  
  
sort index [3 2 1 0]  
sort eigen_value [4.22824171 0.24267075 0.0782095  0.02383509]  
sort eigen_vector [[-0.36138659  0.65658877  0.58202985  0.31548719]  
 [ 0.08452251  0.73016143 -0.59791083 -0.3197231 ]  
 [-0.85667061 -0.17337266 -0.07623608 -0.47983899]  
 [-0.3582892  -0.07548102 -0.54583143  0.75365743]]
```

## Step 6: Select the top k eigenvectors (top 2)

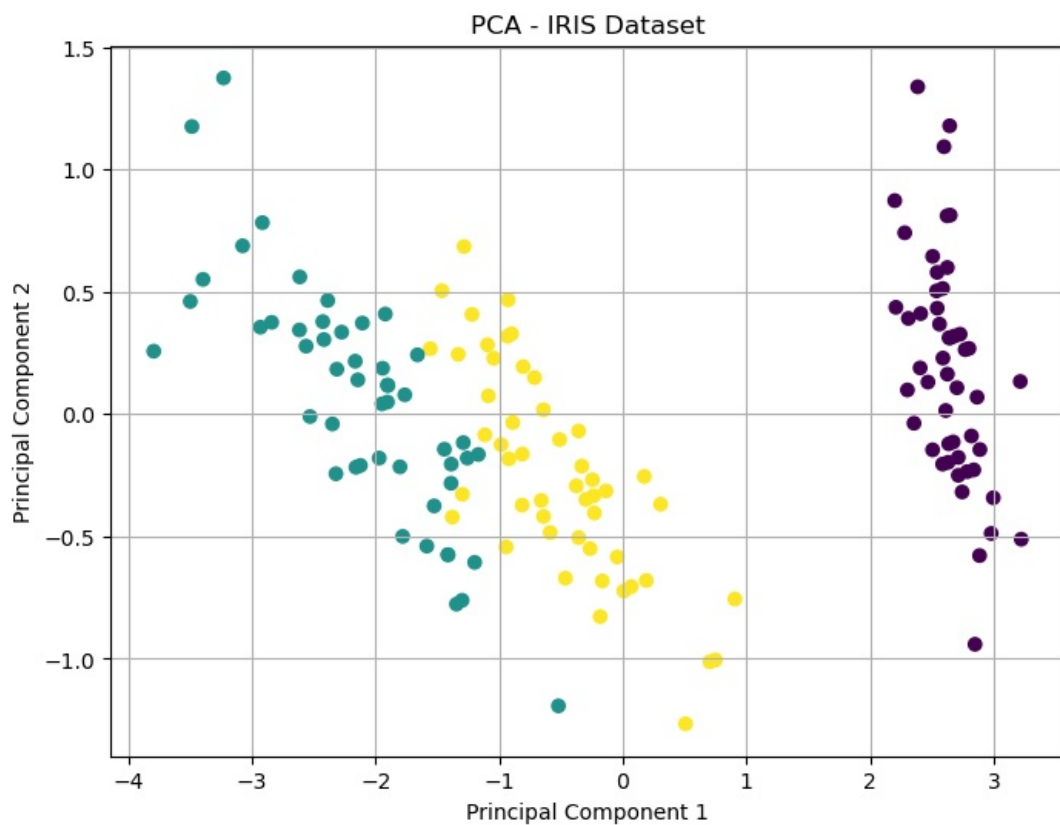
```
In [20]: k = 2  
eigenvector_subset = sorted_eigenvectors[:, 0:k]  
print(eigenvector_subset.shape)  
  
(4, 2)
```

## Step 7: Project the data onto the top k eigenvectors

```
In [21]: x_reduced = np.dot(x_meaned, eigenvector_subset)  
print("Reduced data shape:", x_reduced.shape)  
  
Reduced data shape: (150, 2)
```

## Step 8: Plot the PCA-Reduced Data

```
In [25]: plt.figure(figsize = (8,6))  
plt.scatter(x_reduced[:, 0], x_reduced[:, 1], c=y, cmap='viridis')  
plt.xlabel('Principal Component 1')  
plt.ylabel('Principal Component 2')  
plt.title('PCA - IRIS Dataset')  
plt.grid(True)  
plt.show()
```



## Extra - Bining Method

5,10,11,13,15,35,50,55,72,92,204,215.

Partition them into three bins by each of the following methods: (a) equal-frequency (equal-depth) partitioning (b) equal-width partitioning

```
In [1]: import numpy as np

# Given data
data = [5, 10, 11, 13, 15, 35, 50, 55, 72, 92, 204, 215]
data.sort() # Sort the data

print("Sorted Data:", data)

# (a) Equal-Frequency (Equal-Depth)
n = len(data)
k = 3 # number of bins
size = n // k

print("\n(a) Equal-Frequency Bins:")
for i in range(0, n, size):
    bin_data = data[i:i+size]
    print(f"Bin {i//size + 1}:", bin_data)

# (b) Equal-Width Partitioning
min_val = min(data)
max_val = max(data)
width = (max_val - min_val) / k

print("\n(b) Equal-Width Bins:")
bins = [[] for _ in range(k)]

for val in data:
    index = int((val - min_val) / width)
    if index == k: # include max in the last bin
        index = k - 1
    bins[index].append(val)

for i, b in enumerate(bins):
    print(f"Bin {i + 1}:", b)
```

Sorted Data: [5, 10, 11, 13, 15, 35, 50, 55, 72, 92, 204, 215]

(a) Equal-Frequency Bins:

Bin 1: [5, 10, 11, 13]

Bin 2: [15, 35, 50, 55]

Bin 3: [72, 92, 204, 215]

(b) Equal-Width Bins:

Bin 1: [5, 10, 11, 13, 15, 35, 50, 55, 72]

Bin 2: [92]

Bin 3: [204, 215]