

$$\#24. \sum_{n=1}^{\infty} -\left(-\frac{1}{5}\right)^n = \frac{\frac{1}{5}}{1 + \frac{1}{5}} = \frac{1}{6}$$

초항이 $a_0 = \frac{1}{5}$ 이고 등비가 $r = -\frac{1}{5}$ 인 등비급수다.

Q.E.D

$$\#25. \sum_{n=1}^{\infty} \frac{1}{n(n+1)} = \sum_{n=1}^{\infty} \left(\frac{1}{n} - \frac{1}{n+1} \right)$$

$$= \lim_{n \rightarrow \infty} \left(\sum_{n=1}^n \left(\frac{1}{n} - \frac{1}{n+1} \right) \right)$$

$$= \lim_{n \rightarrow \infty} \left(\left(1 - \frac{1}{2}\right) + \left(\frac{1}{2} - \frac{1}{3}\right) + \dots + \left(\frac{1}{n} - \frac{1}{n+1}\right) \right)$$

$$= \lim_{n \rightarrow \infty} \left(1 - \frac{1}{n+1} \right) = 1.$$

Q.E.D