Aalto University, Department of Computer Science ITMO University, Faculty of Information Security and Computer Technologies

Master's Programme in Computer, Communication and Information Sciences International double degree programme

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Automated Analysis of Weak Memory Models

Master's Thesis Espoo, Finland & Saint Petersburg, Russia 18.6.2018

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Master's Programme in Computer, Communication and Information Sciences
International double degree programme ABSTRACT

Author:	Artem Yushkovskiy		
Title:	Automated Analysis of Weak Memory Models		
Date:	18.6.2018	Pages: vi + 73	
Supervisors: Assoc. Prof. Keijo Heljanko Docent Igor I. Komarov			

Software verification is considered to be a hard computational problem vulnerable to the state explosion problem. Concurrent software verification raises the complexity of the problem to a power determined by all the possible interleavings of states of the system. Moreover, the architecture of a modern shared-memory multi-core processor and optimisations performed by a compiler can cause program behaviour that is unexpected from the point of view of traditional concurrency. The guarantees that an execution environment can provide to a programmer are formalised in its *Weak Memory Model (WMM)*. Over the last decade, weak memory models were defined for multiple hardware architectures and programming languages. This opens new challenges in software verification with respect to a weak memory model.

Most existing tools that perform memory model-aware software analysis examine behaviours of the program against a single memory model. The first tool that analyses the *portability* of a concurrent program from one platform to another is *Porthos* [PFH⁺17a] released in April 2017. Porthos can verify that the program is portable from the source platform $\mathcal S$ to the target platform $\mathcal T$ by checking that the program has no extra states under $\mathcal T$. For that, it performs an SMT-based bounded reachability analysis by encoding the constraints of the program and two memory models $\mathcal M_{\mathcal S}$ and $\mathcal M_{\mathcal T}$ into a single SMT-formula.

Although the approach has been proven to be efficient, the tool accepts as input the small C-like toy language. Current thesis aims to rework Porthos by extending its input language, so that it is able to process real-world C programs. However, current implementation of Porthos seems to be hard to extend, which raises the need to redesign its whole architecture in order to increase the robustness, transparency, efficiency and extensibility. The result of the work is *PorthosC*, a framework for SMT-based memory model-aware analysis.

Keywords:	Weak memory models, concurrent programming, software
	verification, portability analysis, bounded reachability analy-
	sis, SMT-encoding
Language:	English

Acknowledgements

<TODO>

Espoo, Finland & Saint Petersburg, Russia 18.6.2018

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Abbreviations

AST Abstract Syntax Tree

BDD Binary Decision Diagrams

BNF Backus-Naur form

BMC Bounded Model Checking

CF Control-Flow

CPU Central Processor Unit CTL Computational Tree Logic

DF Data-Flow

DFS Deep-First Search

DSA Dynamic Single-Assignment form

DTO Data-Transfer Object
LTL Linear Temporal Logic

NP Non-deterministic Polynomial time OOP Object-Oriented Programming

SB Store Buffering

SC Sequential Consistency
SAT Satisfiability problem

SMP Symmetric Multiprocessor architecture SMT Satisfiability Modulo Theories problem

SSA Static Single-Assignment form UMC Unbounded Model Checking UML Unified Modeling Language

WMM Weak Memory Model

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Chapter 1

Introduction

1.1 Problem statement

Most modern computer systems contain large parts that operate concurrently. Although the parallelisation of a system can drastically improve its performance, it opens numerous of problems regarding correctness, robustness and reliability, which makes the concurrent program design one of the most difficult problems of programming [McK]. In this work, we consider only *Symmetric Multiprocessor (SMP)* parallelism (systems with multiple processors connected to a single shared memory), leaving aside the discussion on distributed concurrency (systems with autonomous nodes that communicate with each other by passing messages through the network). We are discussing mostly the questions on the *memory consistency* rather than performance benefits of the concurrency as the inconsistent memory operations can create new program behaviours, unexpected from the programmer's point of view (as well as the loss of expected behaviours), which all can be considered as a security flaw.

Traditionally, studies related to concurrent programming focus on more fundamental theoretical questions of designing race-free and lock-free parallel algorithms, asynchronous data structures and synchronisation primitives of a programming language [Ben06]. Unfortunately, when it comes to real-world concurrent programs, the algorithmic level of abstraction is not enough for guaranteeing their correctness. The reasons of this fact lie in the code optimisations that both compiler and hardware perform in order to increase performance of the system [AG96].

As an example, consider two x86 assembly programs in Figure 1.1 (such little code examples that explain specific behaviour of the concurrent

{ x=0;	y=0; }				
P0	P1				
MOV [x],1	MOV [y],1				
MOV EAX,[y]	MOV EBX,[x]				
exists (0:EAX=0, 1:EBX=0)					
x86-TSO: allowed					

1	(a)	Without synchronisation
٨	a	i vviiiioui synchioniisuiioni

{ x=0;	y=0; }		
P0	P1		
MOV [x],1	MOV [y],1		
MFENCE	MFENCE		
MOV EAX,[y]	MOV EBX,[x]		
exists (0:EAX=0,1:EBX=0)			
x86-TSO: for	bidden		

(b) With synchronisation

Figure 1.1: Store buffering (SB): A litmus test illustrating the write-read reordering allowed by the x86-TSO memory model

execution environment are called *litmus tests*). Two programs are the same, except the right-hand program uses the synchronisation instruction MFENCE after the store to the shared memory. In both programs, the process P0 writes the value 1 to the shared variable x and reads a value of the shared variable y, and the process P1 writes to the y and reads the x.

Taking into account all possible interleavings of the read and write instructions, both litmus tests allow the following final states:

- (0:EAX=0, 1:EBX=1),
- (0:EAX=1, 1:EBX=0),
- (0:EAX=1, 1:EBX=1).

However, in the left-hand (non-synchronised) litmus test, the state '(0:EAX=0, 1:EAX=0)' is also allowed on the x86 architecture as its processors may cache the writes to the shared memory into their local *store buffers* so that the updated value does not immediately become visible by processes running on other cores. This behaviour is known as *Store Buffering (SB)*. For preventing such a behaviour, the x86 architecture offers the synchronisation instruction MFENCE that flushes the store buffer of the process. In Figure 1.1b, this instruction is inserted for both processes after the store instructions, thus once it is executed in one process, the other process will read the updated value of this shared memory location. The work [McK10] gives a comprehensive review of common hardware architectures from the perspective of the structure of their caches and write buffers, that determine the effect of memory operations, and memory barriers they provide.

The formal way to define the semantics of memory operations and synchronisation primitives of a parallel *execution environment* (hardware, programming language, compiler, database, operation system, etc.) is to

define its *memory model*. There are two main types of formal memory models. Models of the first type characterise the behaviour of the system (its *operational semantics*) in terms of the abstract machine executing the code, as it was done for the SB example above. Models of the second type define the *axiomatic semantics* of the system by specifying a set of assertions over states of the program. Although the former type of memory models may be easier to describe and interpret, existing numerous formal verification tools and methods address the research towards axiomatic memory models.

Chronologically the first memory model for a concurrent system was formulated by Leslie Lamport back in 1979 [Lam79]. This memory model, called the *Sequential Consistency (SC)*, allows only those executions that produce the same result as if the operations had been executed in an interleaved fashion in a single process¹. This means that the order of operations executed by a process is strictly defined by the program (the code) it executes. The SC model does require the write to a shared variable performed in one process to become visible by all other processes *instantly* as each process writes directly to the shared memory, without local buffering. Another important requirement of the SC memory model is that it forbids reordering of memory operations within a single process (the order is strictly defined by the program). Originally, the operational semantics was defined for the SC model, however there exist axiomatic specifications for it [MGZ15].

The SC model is considered to be a *strong memory model* in the sense that it provides firm guarantees regarding the ordering and effect of memory operations. Weakening of the guarantees (such as memory operations reordering, write buffering, etc.) is called *relaxation* of the memory model. The relaxations of the SC model lead to *Weak Memory Models (WMMs)* that specify how processes interact through the shared memory, when a write becomes visible to processes running on other cores, and what value a read operation can get. Thus, WMMs serve as a set of guarantees made by designers of an execution environment to programmers on which behaviours of their concurrent code they can rely on.

¹In order to prescind from the implementation details while discussing the memory models theory, we avoid the use of the software-specific term *thread* and the hardware-specific term *processor*. Instead, we adhere the terminology of the theory of concurrency employed by Ben-Ari [Ben06] by naming a concurrent piece of code the *process*.

1.2 Related work

Research on weak memory models firstly aims to *formalise* an approach of understanding programs with respect to weak memory models, which is *systematic*, *sound* and *complete*. One of the most well-known frameworks for weak memory model-aware analysis was formalised by J. Alglave in 2010 [Alg10]. It is the event-based non-deterministic model without global time (see Section 2.1 for details).

In addition to developing the theoretical basis, researchers work on extracting the memory models for hardware architectures from existing implementations or from the specifications, which are written in natural language and thus suffer from ambiguities and incompleteness. Over the last decade, memory models have been defined for most mainstream multiprocessor architectures, such as x86-TS0 and Sparc-TS0 (for *Total Store Order*) model for x86 and Sparc architectures [OSS09], much more relaxed memory model for Power and ARM architectures [AFI+09; SSA+11; AMT14], etc. There are projects for validating hardware architectures wrt. a memory model as well, e.g., [LPM14; LSM+16].

Most modern high-level programming languages rely on relaxed memory models as well. Thus, the memory model for Java is based on the *happens-before* principle [Lam78] and was introduced in J2SE 5.0 in 2004 [MPA05]. The transformations valid under the Java memory model are discussed in [Šev09]. The weak memory model for C and C++ was defined the C++11 standard [ISO11]. The standard introduced a set of hardware-independent synchronisation fences and atomic operations, which were formalised in the work [BOS+11]. The native support for the synchronisation primitives by the programming language, defined in the standard, has replaced the library-based approach for concurrency, therefore the compiler became aware of the concurrent parts of the code. Nonetheless, in 2015 some common compiler transformations were shown to be invalid under the C11 memory model [VBC+15].

Weak memory models are being formalised for even more abstract software environments. The notable project in this area is the project on formalising the Linux kernel memory model, which is under active development nowadays [AMM+18; MAM+17; MSH+17]. This project has also an influence on the C language: the revision P0124R4 of the C standard [MWP+17] compares the Linux kernel and C11 memory models (including variable access, memory barriers, locking and atomic operations).

Furthermore, there exists a wide range of tools that perform memory model-aware analysis.

- A state-of-the-art tool is diy (*do it yourself*), developed by researchers from INRIA institute, France and University of Cambridge, UK. The diy² is a software suite for designing and testing weak memory models. It is firstly released back in 2010, and since that time it remained to be the only tool for testing weak memory models. The diy consists of several modules: the litmus tests generators diy, diycross and diyone, the litmus test concrete executor litmus that runs tests on a physical machine and collects its behaviours, and the weak memory model simulator herd that implements reachability analysis for exploring states reachable under the specified WMM.
- Some tools that perform the weak memory model-aware program verification and model checking. The notable examples are the stateless model checkers RCMC [KLS⁺17], CHESS [MQ08], Nidhugg [AAA⁺17], Trencher [BDM13], and others.
- Some tools tackle the problem of automated synthesis of the synchronisation primitives, such as the automatic fence insertion tool musketeer [AKN⁺14a], and the automatic verification and fence inference tool blender [KVY11].
- Along with synthesis of synchronisation primitives, some tools were designed to perform the automatic synthesis of litmus tests for the weak memory model, for example litmustestgen by the NVidia Research [LWP+17].
- The framework Alloy [WBS⁺17] can be used for understanding WMMs; it can automatically generate conformance tests between two memory models, distinguish two WMMs, and check monotonicity and compiler mappings of a program.
- Some other tools perform static instrumentation of concurrent C programs and encode the WMM into the program representation so that it can be model-checked by standard tools. The examples are:
 - the instrumenting compiler goto-cc which is a part of CBMC model checker [KT14],
 - the tool that performs the sequentialisation of concurrent programs [AKN⁺13],
 - the tool Weak2SC generates weak memory model descriptions of the program, which can be fed into standard model checking

²The diy project web site: http://diy.inria.fr/

tools (such as SPIN [Hol97] or NuSMV [CCG⁺00]) for performing memory model-aware analysis [TW16].

All the tools listed above consider only a single memory model, however, in real life we face serious engineering problems involving more than one execution environment. One of these problems is the *portability analysis* of the program from one hardware architecture to another. A program written in a high-level language is compiled for different hardware architectures. Even if all the compiler optimisations were disabled (which is a rare case nowadays), the behaviour of two compiled versions of the same program may differ due to differences between hardware memory models. As the result, a program compiled under the platform $\mathcal T$ can reach states that are unreachable on the platform $\mathcal S$, which is a *portability bug* from the source platform $\mathcal S$ to the target platform $\mathcal T$ [PFH+17a].

The very first tool that performs the WMM-aware portability analysis is Porthos³ introduced in April 2017 [PFH⁺17a]. This tool reduces described problem to a bounded reachability problem, which can be solved via an SMT-solver (see Section 3.2). This approach allows to capture symbolically the semantics of analysing program and both weak memory models into a single SMT-formula, augmented by the reachability assertion. As most modern SMT-solvers are efficient enough to be able to operate the state space of size millions of variables bounded by millions of constraints ([MZ09]), the used method can be applicable in solving the real-world problems.

1.3 Task specification

The current work aims to rework the proof-of-concept tool *Porthos* by extending the input language, which currently represents the minimum subset of C, and revising the general architecture of the tool in order to enhance performance, extensibility, reliability and maintainability. One of the directions of development was the ability to process the *kernel litmus tests* written in C [MSH⁺17]. For that, in addition to supporting the C syntax (augmented by litmus-style definitions such as initialisation or assertion statements), the tool must be able to recognise kernel-specific functions and macros (such as the macro READ_ONCE that guarantees memory read) and be easily extensible for defining new functions (have the separate module for the purpose of a knowledge base).

³The Porthos project web site: http://github.com/hernanponcedeleon/PORTHOS

As the general architecture and almost all components of Porthos were to be redesigned, the tool received a new name *PorthosC* ⁴. Considering the enhancements of the architectural design, PorthosC represents a generalised framework for SMT-based memory model-aware analysis, which can not only perform the reachability and portability analysis, but serve as a basis for other kinds of static analysis of concurrent programs.

1.4 Thesis structure

The thesis is organised as following. Chapter 2 gives a general view on the weak memory model-aware analysis. Chapter 3 examines the portability analysis as an bounded reachability problem that can be encoded into an SMT-formula in order to be solved automatically by an SMT solver. Chapter 4 delves into the description of architectural solutions and implementation details of the PorthosC framework. Chapter 5 gives a comparison of key features of PorthosC and Porthos v1 by providing examples of the compilation and the unrolling stages; and it provides some performance benchmarks of PorthosC in both reachability and portability analysis modes. Chapter 6 summarises results of the work and proposes possible directions of the future work.

⁴Hereinafter with the names *Porthos* and *Porthos* v1 we refer to the tool Porthos of version 1, whereas the new implementation of Porthos is called *PorthosC*.

Chapter 2

Memory model-aware analysis

The main idea behind the memory model-aware program analysis is that the set of all possible executions of the concurrent program (the *anarchic semantics*) can be specified by the axiomatic constraints of the memory model that filter out executions inconsistent in particular architecture (the *analytic semantics*) [ACM16]. The anarchic semantics of the program is a truly parallel semantics with no global time that describes all possible computations with all possible communications. However, the analytic semantics captures the program behaviours on a certain execution environment more precisely.

2.1 Event-based program representation

The classical approach for analysing concurrent programs is to model it as the set of sequentially consistent programs, obtained by enumerating all possible interleavings. These models are deterministic as they include the notion of the *global time*. Although these models are easy to build and analyse, the number of all possible interleavings grows exponentially (known as the *combinatorial explosion*), which affects the completeness of an analysis method in general case.

One way to fight the combinatorial explosion is to exclude the global time from the model and treat executions from one equivalence class together in a non-deterministic fashion. For instance, such an equivalence class can be the set of computations performed by a processor locally that do not affect the global state. This idea is used in the *event-based* model, that represents the program as a directed graph of events (the *event-flow graph*) [Alg10; AMT14]. The vertices of such a graph represent *events* (see Section 2.1.1), and edges represent basic relations (see Section 2.1.2). The

graph represents the set of executions (sequences of events; see Section 2.1.3) defined by the non-deterministic guesses of certain relations on some states.

There are three main types of sources of non-determinism in concurrent programs [MQ08]:

- 1. *input non-determinism*, which is a standard undecidable problem for all static analysis methods: to resolve the user input, system call from the environment, unresolved function calls, etc.;
- 2. *scheduling non-determinism*, caused by the interleavings, which in turn are caused by the scheduler activity; and
- 3. *memory-model non-determinism*, caused by hardware and compiler relaxations.

The event-based program model is able to emulate effectively the second and the third types of sources of non-determinism, while the first one can be coped by standard static analysis methods [Lan92; BCD⁺18].

2.1.1 Events

An *event* is a fact of executing the low-level primitive atomic operation such as memory access, threads synchronisation, computation over the local-memory, control-flow jump, etc.

A memory event $e_m \in \mathbb{E}$ represents the fact of access to the memory. Only memory events change the state of an abstract machine executing the code, since it is completely determined by values stored in its memory. Since memory is the crucial low-level resource shared by multiple processes, most relations are defined over memory events. The processes can access a shared memory location (denoted by l_i , for location), or a local one (denoted by r_i , for register). A memory event can access at most one shared memory location, high-level instructions that address more than one shared variable must be transformed into a sequence of events. A memory event is specified by its direction with respect to the shared variable, its location $loc(e_m)$, its processor label $proc(e_m)$, and a unique event label $id(e_m)$ [Alg10].

The set of memory events \mathbb{M} is divided into write events \mathbb{W} (that write values to shared-memory locations) and read events \mathbb{R} (that read values stored in shared-memory locations). We add a restriction that each memory event uses at most one shared location, so that the write instruction $i = write(l_1, l_2)$, that encodes the write from the shared location l_2 to the shared location l_1 , is represented as two consequent events $e_1 = load(r_1 \leftarrow l_2)$; $e_2 = store(l_1 \leftarrow r_1)$. Also, it is important to sepa-

rate the set of initial write events $\mathbb{IW} \subseteq \mathbb{W}$ that perform initialisation of program variables.

A computation event $e_c \in \mathbb{C} \subseteq \mathbb{E}$, represents a low-level assembly computation operation performed solely on local-memory arguments. An example of computation event may be the event $e_c = r_1 \leftarrow add(r_2, 1)$ that writes the sum of values stored in register r_2 and constant 1 (which is modelled as a register as well) to the register r_1 . For modelling branching statements, we define the set $\mathbb{C}_g \subseteq \mathbb{C}$ of *guard* computation events (also called as *branching events*), that are evaluated to a boolean value.

Synchronisation instructions (fences) cause *barrier events*, which do not perform any computation or memory value transfer, instead, they the set of program behaviours by adding barrier relations to the program model. Functionally, a fence may be a synchronisation barrier or a instruction for flushing memory caches into the main memory, etc. For instance, the mfence instruction of the x86 assembly flushes the store buffers of the thread, and thus does not allow the rf-relation (see Section 2.1.2) to point to

2.1.2 Relations

The relation $r \subseteq \mathbb{E} \times \mathbb{E}$ is a set of pairs of events (a subset of Cartesian product of two sets of events). There are two kinds of relations between events: *basic relations* that capture the semantics of the program, and *derived relations* that are defined from the basic relations and events in the weak memory model specification. Constraints over relations that are specified by weak memory models are defined as requirements of *acyclicity*, *irreflexivity* or *emptiness* of specific relations [ACM16].

The basic relations are the following [Alg10]:

- The *control-flow* of a program is defined by the *program-order* relation po $\subseteq \mathbb{E} \times \mathbb{E}$, which represents the total order of events of same process. For instance, if the instruction i_1 generates the event e_1 and the instruction i_2 follows i_1 and generates the event e_2 , then $e_1 \stackrel{\text{po}}{\rightarrow} e_2$.
- The data-flow of a program is defined by communication relations:
 - the *read-from* relation $rf \subseteq W \times \mathbb{R}$ that maps each write event to the read event that reads the value written by write event; and
 - o the *coherence-order* relation $co \subseteq W \times W$ that defines the total order on writes to the same location across all processes (also called the *write serialisation*, ws-relation).

• Events from the same process are related by the *scope relation* sr ⊆ E × E. In contrast to the herd tool, PorthosC does not use hierarchy of scopes (depicted as the scope tree); instead, it uses simple labels that indicate which process has produced certain event.

Below we enumerate some derived relations [Alg10]:

• the *from-read* relation fr ⊆ ℝ × W that maps a read event to all write events succeeding the write event from which the read event gets its value:

$$r \xrightarrow{\mathsf{fr}} w \triangleq (\exists w'. w' \xrightarrow{\mathsf{rf}} r \land w' \xrightarrow{\mathsf{co}} w);$$

• the *communication* relation po over memory events, that fully describes the data-flow of a program:

$$m_1 \stackrel{\text{com}}{\to} m_2 \triangleq ((m_1 \stackrel{\text{rf}}{\to} m_2) \vee (m_1 \stackrel{\text{co}}{\to} m_2) \vee (m_1 \stackrel{\text{fr}}{\to} m_2));$$

• the *external* (and *internal*) *from-read* relations that restrict the fr-relation to the different (respectively, same) processes:

$$\begin{array}{ccc} w \stackrel{\mathsf{fre}}{\to} r & \triangleq & (w \stackrel{\mathsf{fr}}{\to} r \land \mathsf{proc}(w) = \mathsf{proc}(r)), \\ w \stackrel{\mathsf{fri}}{\to} r & \triangleq & (w \stackrel{\mathsf{fr}}{\to} r \land \mathsf{proc}(w) \neq \mathsf{proc}(r)); \end{array}$$

• the po-loc relation that is the po-relation over events that access to the same shared variable:

$$m_1 \stackrel{\text{po-loc}}{\to} m_2 \triangleq (m_1 \stackrel{\text{po}}{\to} m_2 \land \text{loc}(m_1) = \text{loc}(m_2));$$
 and

• the semantics of *fences* (memory barriers) specific for different architectures may be defined as derived relations.

2.1.3 Executions

The semantics of a concurrent program is represented as the set of allowed executions. An *execution* is a path in the event-flow graph defined by poand rf-relations and set of final writes to a given memory location that is valid under certain memory model [AMT14]. It can be interpreted as a sequence of guesses which event is to be executed next. A *candidate execution* is an execution that is not yet constrained by a memory model.

Figure 2.1 illustrates four possible candidate executions for the litmus test Example 1.1 (the pictures are generated by the herd7 tool, version 7.47). Since there are no conditional jumps, the po-relation is defined and we do not need to guess it. Since each thread performs a single write followed

by a single read, the co-relation is also defined (it relates the initial write event with the write event to the same location).

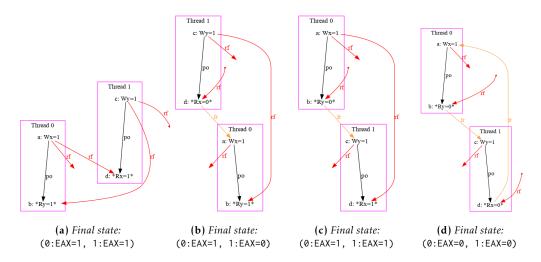


Figure 2.1: Candidate executions for the litmus test in Example 1.1

Thus, there are only four possible executions defined by the choice of rf-relation. The candidate executions pictured in Figures 2.1a–2.1c are consistent both under strong memory model SC and under relaxed memory models x86–TSO, POWER, ARM, and some others. However, the execution shown in Figure 2.1c is still consistent under relaxed-memory architectures, but it becomes inconsistent under SC architecture as it forbids cycles over $fr \cup po$.

2.2 The CAT language

Weak memory models are defined via CAT language [ACM16]. It is a domain specific language for describing consistency properties of concurrent programs. The language combines expressive power of a functional language (being inspired by OCaml, it adopts the OCaml types, first-class functions, pattern matching and some other features) with concepts of memory models (sets of events, relations, operations and assertions over relations). In CAT, new relations can be defined via the keyword let and the following operators over relations [ACM16].

Below we enumerate pre-defined operations over relations and sets of events:

1. *Unary operations*:

- the *complement* of a relation r is ~r,
- the *transitive closure* of a relation r is r+,
- the reflexive closure of a relation r is r?,
- the reflexive-transitive closure of a relation r is r*, and
- the *inverse* of a relation r is r^{-1} .

2. Binary operations:

- the *union* of two relations r1 and r2 is r1 | r2,
- the *intersection* of two relations r1 and r2 is r1 & r2,
- the *difference* of two relations r1 and r2 is r1 \times r2, and
- the sequence of two relations r1 and r2 is r1; r2, which is defined
 as the set of pairs (x,y) such that there exists an intervening z,
 such that (x,z) ∈ r1 and (z,y) ∈ r2.

For instance, the fr-relation is defined as a sequence of inverted rf-relation and co-relation: $fr = (rf^{-1}; co)$. As an example of memory model definition in CAT language, Figure 2.2 presents the excerpt from the x86-TS0 memory model [AM10]. This memory model specification asserts acyclicity of the communication relation (the union of rf-, fr- and co- relations), po-loc -relation, mfence-relation and some other derived relations [OSS09].

```
let po_ghb = WW(po) | RM(po)
let implied = PA(poWR) | WR(po)
let GHB = mfence | implied | po_ghb | rfe | fr | co
let com = rf | fr | co
empty atom & (fre;coe)
acyclic po-loc | com
acyclic GHB
```

Figure 2.2: Excerpt from the x86-TSO memory model in the CAT language

Chapter 3

Portability analysis as an SMT problem

As it was discussed in Chapter 1, a concurrent program may behave differently when compiled for different hardware architectures. This may cause the portability bugs, the behaviour that is allowed under one architecture and forbidden under another. This Chapter provides the short introduction into the general model checking and reachability analysis problem, after which it describes of the concurrent software portability analysis stated as a *bounded reachability* problem, which in turn can be reduced to an SMT problem [PFH+17b].

3.1 Model checking and reachability analysis

The *model checking* is the problem of verifying the system (the *model*) against a set of constraints (the *specification*) [DKW08]. As the state machine is the most widespread mathematical model of computation, most classical model checking algorithms explore the state space of a system in order to find states that violate the specification.

The general scheme of model checking is the following. The analysing system is represented as a transition system, a directed graph with labelled nodes representing states of the system. Each state corresponds to the unique subset of atomic propositions that characterise its behavioural properties. Once the model has been constructed, it can be checked for compliance to the specification, a set of constraints.

Usually, the specification defines temporal constraints over the system properties. For instance, the specification can assert that the property *always*

holds (the *safety* property) or the property will *eventually* hold (the *liveness* property). Commonly, the *Linear Temporal Logic (LTL)* or *Computational Tree Logic (CTL)* (along with their extensions) is used as a specification language due to the expressiveness and verifiability of their statements [CGP99].

In the described scheme, the model checking problem is reducible to the reachability analysis, an iterative process of a systematic exhaustive search in the state space. This approach is called *Unbounded Model Checking (UMC)*. However, all model checking techniques are exposed to the *state explosion problem* as the size of the state space grows exponentially with respect to the number of state variables used by the system (its size). In case of modelling concurrent systems, this problem becomes much more serious due to the exponential number of possible interleavings of states. Therefore, over past 30 years the research in model checking has been fighting the state explosion problem mostly by optimising search space, search strategy or basic data structures of existing algorithms [CGJ+01].

One of the first techniques that optimises the search space considerably is the symbolic model checking with *Binary Decision Diagrams (BDDs)* [BCM+92]. Instead of processing each state individually, in this approach the set of states is represented by the BDD, a data structure that allow to perform operations on large boolean formulas efficiently [CKN+12]. The BDD representation can be linear of size of variables it encodes if the ordering of variables is optimal, otherwise the size of BDD is exponential. The problem of finding such an optimal ordering is known as NP-complete problem, which makes this approach inapplicable in some cases.

The other idea is to use satisfiability solvers for symbolic exploration of state space [CBR $^+$ 01]. In this approach, the state space exploration consists of the sequence of queries to the SAT-solver, represented as boolean formulas that encode the constraints of the model and the finite path to a state in the corresponding transition system. This technique is called *Bounded Model Checking (BMC)* as the search process is being repeated up to the user-defined bound k, which may result to *incomplete analysis* in general case (not all the state space has been checked). However, there exist numerous techniques for making BMC complete for finite-state systems (e.g., [Sht00]).

At present time, satisfiability solvers are behind the numerous verification and bounded model checking tools. Although, as most modern programming languages are typed, the SAT-formula that encodes the constraints of a program must include non-boolean constraints encoded as boolean variables, which is ineffective, therefore most software analysis

and verification tools use *Satisfiability Modulo Theories* (*SMT*) -solvers, that integrate first-order reasoning with the background theory reasoning [KS08]. For example, the Integer theory includes operators '+', '-', ' \geq ' and others). Most modern SMT-solvers support integer arithmetic, real arithmetic, fixed-size bit-vectors, arrays, and other theories. The direction of the development of SMT-solvers is provided by the SMT-LIB standard [BFT17], which provides definition of the unified language for defining SMT-formulas, and description of most common underlying logics and theories.

In general, a BMC problem aims to examine the non-reachability of the "undesirable" states of a finite-state system. Let $\vec{x} = (x_1, x_2, ..., x_n)$ be a vector of n variables that uniquely distinguishes states of the system; let $Init(\vec{x})$ be an initial-state predicate that defines the set of initial states of the system; let $Trans(\vec{x}, \vec{x}')$ be a transition predicate that signifies whether there the transition from state \vec{x} to state \vec{x}' is valid; let $Bad(\vec{x})$ be a bad-state predicate that defines the set of undesirable states. Then, the BMC problem, stated as the reachability of the undesirable state withing k steps, is formulated as following: $SAT(Init(\vec{x_0}) \land Trans(\vec{x_0}, \vec{x_1}) \land ... \land Trans(\vec{x_{k-1}}, \vec{x_k}) \land Bad(\vec{x_k}))$.

3.2 Portability analysis as a bounded reachability problem

A portability analysis problem may be stated as a reachability problem, where the undesirable state is one reachable under the target $\mathcal{M}_{\mathcal{T}}$ memory model and unreachable under the source memory model $\mathcal{M}_{\mathcal{S}}$. Consider the function $cons_{\mathcal{M}}(P)$ which calculates the set of executions of the program P that are consistent under the memory model \mathcal{M} . The program P is called portable from the source architecture (memory model) $\mathcal{M}_{\mathcal{S}}$ to the target architecture $\mathcal{M}_{\mathcal{T}}$ if all executions consistent under $\mathcal{M}_{\mathcal{T}}$ are consistent under $\mathcal{M}_{\mathcal{S}}$ [PFH⁺17a]:

Definition 3.2.1 (Portability). Let $\mathcal{M}_{\mathcal{S}}$, $\mathcal{M}_{\mathcal{T}}$ be two weak memory models. The program P is portable from $\mathcal{M}_{\mathcal{S}}$ to $\mathcal{M}_{\mathcal{T}}$ if $cons_{\mathcal{M}_{\mathcal{T}}}(P) \subseteq cons_{\mathcal{M}_{\mathcal{S}}}(P)$

Note that the definition of portability requirements against *executions* is strong enough, as it implies the portability against *states* (the *state-portability*) [PFH⁺17b]. The result SMT-formula ϕ that encodes the portability problem should contain both encodings of control-flow ϕ_{CF} and data-flow ϕ_{DF} of the program, and assertions of both memory models:

 $\phi = \phi_{CF} \wedge \phi_{DF} \wedge \phi_{\mathcal{M}_T} \wedge \phi_{\neg \mathcal{M}_S}$. If the formula is satisfiable, there exist a portability bug.

3.2.1 Encoding for the control-flow

The control-flow of a program can be represented by the *control-flow graph*, a directed acyclic connected graph with a single source and one or multiple sink nodes. Each control-flow edge contains the label that denotes the transition predicate called *guard*. The empty guard (a *true* predicate) is denoted as 'e'. A guard represents a variable or a computational expression over local variables. As a guard depends on the data-flow of the program, it is liable to the weak memory model relaxations. The branching expressions that support more than two outgoing control-flow edges may be useful for describing non-deterministic transition systems, where the guards are not necessarily mutually exclusive. However, as the C language supports only binary logic (*if-then-else* branching), PorthosC builds only two possible outcomes of evaluating a computation (the *primary* and *alternative* transitions), see Section 4.3.1.2 for details.

While working on PorthosC, we have applied some modifications to the encoding scheme for the control-flow. These changes were motivated by the need to process an arbitrary control-flow produced by conditional and unconditional jumps of the C language. For that, we compile the *Abstract Syntax Tree* (*AST*) of the parsed C-code to the plain event-flow graph. The new encoding is to be smaller than the old one used in Porthos since it does not produce new variables for each high-level statement of the input language.

For instance, Porthos v1 uses the encoding scheme where the control-flow of the sequential instruction $i_1 = i_2; i_3$ is encoded recursively as $\phi_{CF}(i_2;i_3) = (cf_{i_1} \Leftrightarrow (cf_{i_2} \wedge cf_{i_3})) \wedge \phi_{CF}(i_2) \wedge \phi_{CF}(i_3)$, and the control-flow of the branching instruction $i_1 = (c?i_2:i_3)$ was encoded recursively as $\phi_{CF}(c?i_2:i_3) = (cf_{i_1} \Leftrightarrow (cf_{i_2} \vee cf_{i_3})) \wedge \phi_{CF}(i_2) \wedge \phi_{CF}(i_3)$. In contrast, the new encoding scheme implemented in PorthosC firstly compiles the recursive high-level instructions into the linear low-level event-flow graph, which is then encoded into an SMT-formula. A guard in the event-flow graph is a value of conditional variable on the branching event, which is encoded as a data-flow constraint (see Section 3.2.2). In general, the new encoding scheme follows the one proposed in [EH08, Chapter 5.1.2] for encoding Petri-nets.

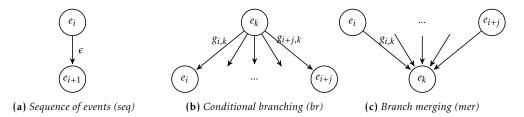


Figure 3.1: Possible mutual arrangements of events in an event-flow graph

Let $\mathbf{x}: \mathbb{E} \to \{0,1\}$ be the predicate that signifies the fact that the event has been executed (and, consequently, has changed the state of the system). Consider the possible mutual arrangements of nodes in an event-flow graph presented in Figure 3.1. For these cases, we propose the encoding scheme that uniquely encodes each node of graph and at the same time allows to encode partially executed program:

$$\phi_{CF_{seq}} = \mathbf{x}(e_{i+1}) \Rightarrow \mathbf{x}(e_i)$$

$$\phi_{CF_{br}} = [\mathbf{x}(e_i) \Rightarrow \mathbf{x}(e_k)] \wedge \cdots \wedge [\mathbf{x}(e_{i+j}) \Rightarrow \mathbf{x}(e_k)]$$

$$\wedge [\mathbf{x}(e_i) \wedge \mathbf{x}(e_k) \Rightarrow g_{i,k}] \wedge \cdots \wedge [\mathbf{x}(e_{i+j}) \wedge \mathbf{x}(e_k) \Rightarrow g_{i+j,k}]$$

$$\wedge \cdots$$

$$\wedge (\bigvee_{e_l \in \text{succ}(e_m)} \bigvee_{\substack{e_n \in \text{succ}(e_k) \\ e_n \neq e_m}} \neg [\mathbf{x}(e_m) \wedge \mathbf{x}(e_n)])$$

$$\phi_{CF_{mer}} = \mathbf{x}(e_k) \Rightarrow (\bigvee_{\substack{e_p \in \text{pred}(e_k)}} \mathbf{x}(e_p))$$

$$(3.2)$$

Equation 3.1 shows the encoding for the sequential control-flow represented in Figure 3.1a and reflects the fact that the event e_2 can be executed iff the event e_1 has been executed. Equation 3.2 shows the encoding for the branching control-flow depicted in Figure 3.1b, that considers both transitions and guards. Also, adding negations of pairwise conjunctions over all successors of the branching node, the encoding forbids the execution of two branches simultaneously. Equation 3.3 shows the encoding for the control-flow of a merge-point represented in Figure 3.1c: the event e_k is executed if either of its predecessors has been executed, regardless the type of the transition. Note that the sequential control-flow is a special case of branching with the only transition guard ϵ (that is encoded as true).

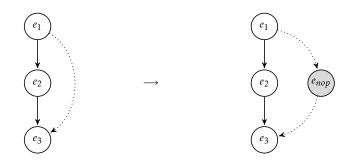


Figure 3.2: Transformation of the forward-jump control-flow

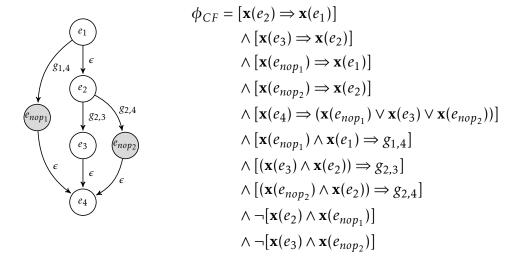


Figure 3.3: Example of encoding for the control-flow of the X-graph

For sake of correctness and simplicity of the encoding, we require all branches to have at least one event. Thus, for branching statements that do not have any events in one of the branches (such branch represents a conditional jump forward), we add a synthetic *nop-event* as it is shown in Figure 3.2.

As an example of the control-flow encoding, consider the event-flow graph in Figure 3.3, which has two branching points and one merge point with three incoming transitions. To illustrate the correctness of the encoding, consider the path $e_1 \rightarrow e_2 \rightarrow e_4$. This means, in the formula ϕ_{CF} , the SMT-variables $\mathbf{x}(e_1)$, $\mathbf{x}(e_2)$ and $\mathbf{x}(e_4)$ should be assigned to 1, and the variable $\mathbf{x}(e_3)$ should be assigned to 0.

Note that the generalised encoding scheme does not require the branching transitions to be mutually-exclusive (for instance, consider two branch-

ing transitions from the event e_2 , both labelled by non-epsilon guards $g_{2,3}$ and $g_{2,4}$). Next, consider the path $e_1 \rightarrow e_3 \rightarrow e_4$, which is not allowed by the control-flow graph. The corresponding model $\mathbf{x}(e_1) = 1$, $\mathbf{x}(e_2) = 0$, $\mathbf{x}(e_3) = 1$ and $\mathbf{x}(e_4) = 1$ does not satisfy the formula ϕ_{CF} . The proposed encoding for the control-flow works also for encoding the partial graph. For example, the assignment $\mathbf{x}(e_1) = 1$, $\mathbf{x}(e_2) = 1$, $\mathbf{x}(e_3) = 0$ and $\mathbf{x}(e_4) = 0$, which encodes the path $e_1 \rightarrow e_2$, satisfies ϕ_{CF} .

3.2.2 Encoding for the data-flow

To encode the data-flow constraints, we use the *Static Single-Assignment (SSA) form* in order to be able to capture an arbitrary data-flow into a single SMT-formula. The SSA form requires each variable to be assigned only once within entire program. In contrast, Porthos v1 uses the *Dynamic Single-Assignment (DSA)* form, that requires indices to be unique only within a control-flow branch. Although the number of variable references (each of which is encoded as unique SMT-variable) on average is logarithmically less in the case of the DSA form than the SSA form, the result SMT-formula still needs to be complemented by same number of equality assertions when encoding the data-flow of merge points [PFH+17a].

Following [PFH⁺17b], the indexed references of variables are computed in accordance with the following rules: (1) any access to a shared variable (both read and write) increments its SSA-index; (2) only writes to a local variable increment its SSA-index (reads preserve indices); (3) no access to a constant variable or computed (evaluated) expression changes their SSA-index. These rules determine the following encoding of load, store and computation events within a single thread:

$$\phi_{DF_{e=load}(r \leftarrow l)} = [\mathbf{x}(e) \Rightarrow (r_{i+1} = l_{i+1})]$$
(3.4)

$$\phi_{DF_{e=\text{store}(l\leftarrow r)}} = [\mathbf{x}(e) \Rightarrow (l_{i+1} = r_i)]$$
(3.5)

$$\phi_{DF_{e=\text{eval}(\cdot)}} = [\mathbf{x}(e) \Rightarrow \mathbf{v}(e)]$$
(3.6)

In Equation 3.6, the function $\mathbf{v}:\mathbb{C}\to\mathbb{R}$ evaluates the computation event (the value is determined by co- and rf- relations). To convert the program into SSA form, for each event each variable that is declared so far (either local or shared) is mapped to its indexed reference; this information is stored in the SSA-map "event *to* variable *to* SSA-index". The SSA-map is computed iteratively while traversing the event-flow graph in topological order as it is described in Algorithm 1.

Algorithm 1 Algorithm for computing the SSA-indices

Input: The event-flow graph $G = \langle N, E \rangle$ where V is the set of nodes (events), E is the set of control-flow transitions, e_0 is the entry node

Output: The SSA-map of the form "{ event : { variable : index }}"

```
1: function Compute-SSA-Map(G)
        S \leftarrow \text{empty map}; S[e_0] \leftarrow \text{empty map}
        for each event e_i \in G.N in topological order do
3:
            for each predecessor e_i \in \text{pred}(e_i) do
4:
5:
                 S[e_i] \leftarrow \text{copy}(S[e_i])
                 for each variable v_k \in \text{set of variables accessed by } e_i do
6:
                     S[e_i][v_k] \leftarrow \max(S[e_i][v_k], S[e_i][v_k])
7:
8:
                     if need to update the index of v_k then
                                                                              ▶ cases (1)-(2)
                          S[e_i][v_k] \leftarrow S[e_i][v_k] + 1
9:
```

The time of described algorithm is linear of the event-flow graph size as the algorithm performs only a single graph traverse.

As it has been described before, the rf-relation links data-flow between events. The encoding of this linkage has been left untouched as it is implemented in Porthos v1:

$$\phi_{DF_{mem}}(e_1, e_2) = [\mathsf{rf}(e_1, e_2) \Rightarrow (l_i = l_j)]$$
 (3.7)

where the variable of location l is mapped to the SSA-variable l_i for event e_1 , and to the SSA-variable l_j for event e_2 ; and the predicate $rf(e_1, e_2)$ is encoded as a boolean variable, which itself equals true if $e_1 \stackrel{\mathsf{rf}}{\to} e_2$ (i.e., if e_2 reads the shared variable that was written in e_1).

3.2.3 Encoding for the memory model

The basic scheme for encoding the memory model was proposed in [PFH+17a]. The encoding consists of two parts: encoding of the *derived relations* and encoding of the memory model *assertions*.

In the SMT-formula, a relation $x \xrightarrow{r} y$ is represented by a boolean variable r(x,y) that indicates whether the relation holds. Derived relations are encoded by fresh boolean variables according to the following rules [PFH⁺17b]:

```
• r_1 \cup r_2(e_1, e_2) = r_1(e_1, e_2) \vee r_2(e_1, e_2);
```

•
$$r_1 \cap r_2(e_1, e_2) = r_1(e_1, e_2) \wedge r_2(e_1, e_2);$$

```
• r_1 \setminus r_2(e_1, e_2) = r_1(e_1, e_2) \land \neg r_2(e_1, e_2);

• r^{-1}(e_1, e_2) = r(e_2, e_1);

• r^*(e_1, e_2) = r^+(e_1, e_2) \lor (e_1 = e_2);

• r_1; r_2(e_1, e_2) = \bigvee_{e_k \in \mathbb{E}} r_1(e_1, e_k) \land r_2(e_k, e_2); and

• r^+(e_1, e_2) = \operatorname{tc}_{\lceil \log \mid \mathbb{E} \mid \rceil}(e_1, e_2), where

\operatorname{tc}_0(e_1, e_2) = r(e_1, e_2), and

\operatorname{tc}_{i+1}(e_1, e_2) = r(e_1, e_2) \lor (\operatorname{tc}_i(e_1, e_3); \operatorname{tc}_i(e_3, e_2)).
```

Note that CAT language allows mutually-recursive definitions of relations (for example, ' $r_1 = r_2 \cup (r_1; r_1)$ '). The basic idea of using the Kleene fixpoint iteration for encoding such relations was also proposed in [PFH⁺17a]: for any pair of events $e_1, e_2 \in \mathbb{E}$ and relation $r \subseteq \mathbb{E} \times \mathbb{E}$, we encode a new integer variable $\Phi^r_{e_1,e_2}$ that represents the round of Kleene iteration on which the variable $r(e_1,e_2)$ has been set.

The memory model can assert acyclicity, irreflexivity of emptiness of a relation or a set of events. As it has been proposed in [PFH⁺17a], encoding the acyclicity assertion uses numerical variable $\Psi_e \in \mathbb{N}$ for each event e in the relation to be asserted: $acyclic(r) = (r(e_1, e_2) \Rightarrow (\Psi_{e_1} < \Psi_{e_2}))$. The irreflexivity assertion as $irreflexive(r) = \bigwedge_{e_k \in (E)} \neg r(e_k, e_k)$.

Chapter 4

PorthosC: The implementation

The main call for commencing the work on PorthosC was the need for processing real-world C programs, which, at first, requires the input language to be extended. This implies the support not only for new syntactic structures of the C language (such as the switch statement or the postfix increment operator i++), but also for its fundamental concepts and features (such as types, pointer arithmetic or first-order functions), which requires revision of the whole architecture of the tool. Yet far from all the C language is supported (which, considering its complexity and numerous pitfalls, goes far beyond current thesis¹), we consider the accomplished work as a step towards it.

4.1 General principles

The Porthos v1 does not distinguish the event-based program model from the high-level AST, and they both are encoded into a single SMT-formula (see classes of package 'dartagnan.program' of Porthos v1). Moreover, the syntax tree is implemented in Porthos v1 as a mutable data structure, which is being modified at all stages of the program (for instance, see the methods 'dartagnan.program.Program.compile(...)' of Porthos v1 that recursively compute some properties of the AST and change its state). We are inclined to consider the old architecture to be fast to develop, but difficult to maintain (since it is difficult to guarantee the correctness of the program) and extend

¹To ensure this, one merely has to look at existing C compiler implementations, for instance, the open-source gcc compiler, which uses the C parser written in more than 18.5 thousand lines of code (see https://github.com/gcc-mirror/gcc/blob/master/gcc/c-parser.c)

(since adding the support for a new high-level instruction requires changing multiple components of the program, from parser to encoder).

Therefore, while working on the new design of PorthosC, we clearly separated the high-level intermediate code representation (the AST structure) from the low-level event-based representation (the event-flow graph). Such a modular architecture will allow to support multiple input languages² by parsing them and converting parsed syntax trees to a simplified AST.

All data-transfer objects (DTOs) used by PorthosC must be immutable, so that it is possible to guarantee the correctness of the program by controlling preservation of its invariants. The immutability in PorthosC is implemented via final fields that are assigned by the immutable-object values (either a primitive type, or another user-defined immutable object, or an immutable collection provided by the library Guava by Google³).

During the development of PorthosC, we mainly followed the KISS principle, which can be exhaustively described in 17 Unix Rules of Eric Raymond [Ray03]. The following list summarises the main rules we followed during the development of PorthosC:

1. Robustness:

- 1.1. completeness of the analysis,
- 1.2. modular architecture: each module can be tested independently,
- 1.3. usage of software design patterns where necessary, and
- 1.4. usage of immutable data structures for all DTOs.

2. Transparency:

- 2.1. following the principles of simplicity and readability,
- 2.2. clear and informative program output, and
- 2.3. following the clear code style.

3. Efficiency:

- 3.1. keeping the trade-off between execution time and memory usage.
- 4. Extensibility:
 - 4.1. clear modular architecture.

²Apart from the C language, PorthosC should be able to analyse litmus tests in different assembly languages and, as a compatibility mode, the input language of Porthos v1.

³The Guava project repository: https://github.com/google/guava/

Robustness of the analysis is the main criterion of PorthosC as a verification tool. Although it makes the analysis more sensitive to the combinatorial explosion, it preserves the completeness of analysis, which is necessary for a model-checking tool. As a robust and transparent tool, PorthosC must adhere to the strategy of aborting its work on any unexpected outcome (for instance, if a parser failed to parse the string and the recovery algorithm is not described). One of the transparency principles is following the clear code style. This mainly means the clear and informative naming of classes, functions and fields. It also implies the unified ordering of methods in classes, minimised size of methods code, clear tabulation, etc.

As its predecessor, PorthosC uses the open-source SMT-solver Z3⁴ by Microsoft Research [DB08]. However, unlike its predecessor, PorthosC has an additional abstraction level, Z-formula (see Section 4.3.1.4), that allows the use any other SMT-solver.

As its predecessor, PorthosC is written in Java, firstly, in order to be able to reuse some parts and concepts of Porthos also written in Java, and secondly, because the authors find the concepts of Object-Oriented Programming (OOP) inherent in Java suitable for modelling the programming languages. Although Java does not show the best results in performance benchmarks (for example, compared to C++ [Hun11]), the performance cornerstone of PorthosC (as well as any other SMT-based code analyser) is the phase of solving the SMT-formula, which is left to the third-party SMT-solver invoked by PorthosC via a Java API. However, considering the perspective of using PorthosC as a static analyser for real-world programs, the memory optimisation problem must also be taken into account during both encoding and solving stages. It is worth noting that, for the reasons of simplicity, PorthosC is not a concurrent program, however, we believe that due to its modular architecture it can be easily parallelised on the level of program modules.

Currently, PorthosC can operate only in the intra-procedural analysis mode (not supporting invocations of the user-defined functions), assuming that each function defined in the input file is being executed in a separate thread. However, the redesigned architecture of PorthosC can be easily extended to support the inter-procedural (cross-function) analysis by inlining user-defined functions calls and binding variable contexts. In this mode, instead of analysing a single source code file, the tool can process the whole code project, where the functions to be executed in parallel are

⁴The Z3 project repository: https://github.com/Z3Prover/z3

specified separately by the user. Also, the tool can be extended to detect the concurrent parts of the code automatically at the pre-compilation stage. For that, the pre-compiler should recognise functions that commence a new process (such as pthread_create from pthread.h) and resolve the argument that points to the thread function. This functionality is left beyond current thesis.

4.2 Program input

Both Porthos v1 and PorthosC use the ANTLR parser generator⁵ [Par13] for creating the input-language parsers. The ANTLR takes as input the user-defined grammar of the target language in a BNF-like form and produces the LL(*)-parser and optionally some auxiliary classes (such as listeners and visitors for the syntax tree). Although this parser may not be as efficient as a hand-written language-optimised parser, it reduces the overhead of implementing the parser significantly. Among other advantages ANTLR, it has a rather large collection of officially supported grammars. Nonetheless, the intuitive syntax for defining grammars and numerous of tools for debugging grammars make the ANTLR an attractive instrument for processing languages.

Figure 4.1 represents the grammar sketch in BNF syntax of the input language used by Porthos v1. The input language parser used by Porthos v1 suffers from several disadvantages. Firstly, it contains the parser code inlined directly into the grammar, so that the grammar serves as a template for the parser code (which is called semantic actions in ANTLR). Such a combining of two expressive languages makes the code hardly understandable and, therefore, poorly maintainable. In PorthosC, we clearly separated the parser (generated from the grammar file '<grammar>.g4') from converting the ANTLR syntax tree to the AST, that is one for all languages of an input program.

Secondly, Porthos resolves the semantics of operations syntactically (it was defined in the ANTLR grammar), whereas it should be resolved by a separate module operating on the AST level, so that it does not require to change grammar for encoding the semantics of a new function. As the reader might have noticed from the grammar sketch in Figure 4.1, different kinds of memory operations of of the Porthos v1 input language vary syntactically as well. For example, the assignment of a local computation to a register uses

⁵The ANTLR project repository: https://github.com/antlr/antlr4

```
⟨program⟩
  : ⟨initialisation⟩ ⟨thread⟩+ ⟨assertion⟩
⟨thread⟩
   : thread (thread-id) (instruction)
⟨instruction⟩
   : (atom)
         '{' \( \( \text{instruction} \) '}'
       (instruction) ';' (instruction)
       'while' '(' \langle bool-expr\rangle ')' \langle instruction\rangle
       'if' (bool-expr) '{' (instruction) '}' (instruction)
⟨atom⟩
       ⟨register⟩ '<-' ⟨expression⟩
       ⟨register⟩ '<:-' ⟨location⟩
       ⟨location⟩ ':=' ⟨register⟩
       \(\text{register}\) '=' \langle \(\text{location}\) '.' '\(\text{load'} '(' \langle \text{atomic}\)' \(\text{location}\) '=' \langle \(\text{register}\) '.' '\(\text{store'} '(' \langle \text{atomic}\)''
       ('mfence' | 'sync' | 'lwsync' | 'isync')
⟨bool-expr⟩
   : 'true'
       'false'
   | ⟨expression⟩ ('and' | 'or') ⟨expression⟩
       \langle expression \rangle ('==' | '!=' | '\rangle' | '\rangle=' | '<' | '>=') \langle expression \rangle
⟨expression⟩
   : [0-9]
        (register)
        ⟨expression⟩ ('*' | '+' | '-' | '/' | '%') ⟨expression⟩
```

Figure 4.1: Sketch of the input language grammar used by Porthos v1

the symbol '<-', the atomic non-relaxed load operation is denoted by <:-', atomic non-relaxed store operation is denoted by ':=', and the semantics of relaxed load and store is resolved syntactically by matching the function name and arguments. Moreover, only the operator '<-' accepts an expression as the source of data, which means that expressions could be assigned only to registers. In PorthosC, the semantics of the data-flow operation is determined according to the types of operands, that are determined during the pre-compilation stage (see Section 4.3.2.4). The semantics of the functions also being resolved during the compilation stage via the *invocation hooking* mechanism (see Section 4.3.2.5).

Thirdly, the grammar used by Porthos v1 accepts only a restricted set of operations. For example, the computation expressions can use only local variables. Thus, in the assignment expression 'r <- (x + 1);', the variable x will be parsed as a local variable even though it can be used as a shared

variable in other parts of the program, which may lead to the inconsistency of analysis. In PorthosC, all shared variables involved into a computation expression are tentatively copied to temporary local variables.

Fourthly, Porthos v1 supports only integer constants and expressions. In PorthosC, we extended support for primitive types supported by the Z3 solver (32-bit integers are encoded as Ints of Z3, floats are encoded as Reals). Although the Z3 supports the array theory (characterised by the select-store axioms [MB11]), the complexity of pointer analysis for the arrays of non-constant size moves the full support of arrays and pointers out of the scope of current thesis.

Finally, the grammar used by Porthos has the following minor drawbacks. The operators are non-associative (expressions of the form '1 + 2 * 3' can not be parsed). Comparing to C statements, which must end with the semicolon punctuator ';', statements defined in the grammar of Porthos v1 use the semicolon as a separator between statements (the final statement must not end with semicolon). The litmus test-specific syntax for variables initialisation is used only for declaring the shared variables (all of them are initialised with default value 0), however, this syntax should be used as an initial assignment of both shared and local variables with arbitrary values.

PorthosC uses the C language grammar of proposed in the C11 standard [ISO11], that was extended by litmus test-specific syntax such as initialisation and final-state assertion statements (the original ANTLR grammar can be found in the official repository containing the collection of ANTLR v4 grammars⁶). Current version of PorthosC does not recognise C processor directives (it ignores them), however, in future it can be extended to support them.

4.3 Architecture

The general processing scheme of old tool Porthos v1 is the following. The input program is parsed to the AST, where leaves are the events. The instructions of the AST are then encoded into the ϕ_{CF} (see Section 3.2.1) and the events are processed by the single function ('dartagnan.wmm.Domain.encode') that loops over all events, checks their properties (the kind of event, the operands of the memory event, the type of the barrier event, etc.) and adds corresponding relations assertions to the formula. Encoding all the relations (the *program domain encoding*) in a single

⁶ANTLR grammars repository path: https://github.com/antlr/grammars-v4

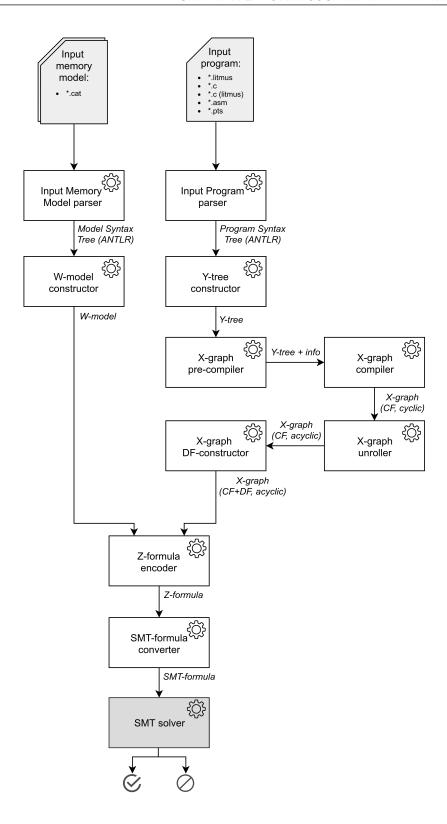


Figure 4.2: The general architecture of PorthosC

function is error-prone and hardly manageable. Moreover, this function does not consider the memory model, therefore the result formula can contain relations that are not constrained by the memory model specified by the user and thus are redundant (for instance, the TSO memory model does not contain POWER-specific relations ii, ic, ci, etc., that are always encoded regardless the memory model). In PorthosC, we moved the encoding logic into a separate module 4.3.2.8 that accepts the input program and the user-defined memory model, therefore does not add constraints over unused relations to the result SMT-formula.

The high-level architecture of PorthosC is presented in Figure 4.2. The program takes as input the program to be analysed and one (the reachability analysis mode) or two (the portability analysis mode) memory models. However, instead of parsing memory models from the CAT file, the tool may operate with pre-defined memory models (SC, TSO, PSO, RMO, ALPHA, POWER, ARM; this feature is inherited from Porthos v1). The parsed program syntax tree is then converted (Section 4.3.2.3) to a program AST called Y-tree⁷ (Section 4.3.1.1), which then is being preprocessed at the precompilation stage (Section 4.3.2.4) in order to collect information necessary for the compilation. The Y-tree then is being compiled (Section 4.3.2.5) to an X-graph representation (Section 4.3.1.2). The compiled X-graph then is being converted to an acyclic form (Section 4.3.2.6) in order to be encoded into a Z-formula (Section 4.3.1.4). Apart from that, the memory-model constructor (Section 4.3.2.2) constructs the abstract syntax tree of derived relations of the weak memory model W-model (Section 4.3.1.3). Thereafter, W-model and acyclic X-graph are encoded (Section 4.3.2.8) to a Z-formula representation (a wrapper over an SMT-formula), which then is translated to an SMT-formula (Section 4.3.2.9), which then is solved by the SMT-solver (Section 4.3.2.10).

4.3.1 Internal representations

For keeping the architecture transparent, we build all abstraction levels with interfaces, even if some of them does not add any new functionality.

⁷In order to avoid confusion between different internal representations, we prefix the names of elements of each internal representation with a letter. For instance, we picked the letter 'Y' to denote the AST code representation as drawing of this letter resembles the tree branching; with letter 'X' we prefix elements of the event-flow graph as the events are to be executed; and with letter 'W' we prefix elements of the weak memory model AST.

4.3.1.1 Y-tree

The first internal representation used by PorthosC is the *Y-tree*, which represents an untyped high-level recursively defined AST⁸. The Apendix A.1 presents the file tree of the main classes that constitute the Y-tree hierarchy (as the inheritance tree might be obvious for the C-like AST, we confine ourselves to presenting the classes file tree only, which we tend to retain clearly structured).

The abstract syntax tree, Y-tree, is an abstraction level suitable for compiling the program to a low-level representation (in the case of processing low-level assembly code, it may be directly converted to the X-graph representation). In terms of Porthos v1, the Y-tree is the level of *instructions*. However some details of the syntax might have been abstracted away (for instance, array operations may be emulated by functions invocations, see [Gri12, Chapter 5]), we find this level of abstraction suitable enough for modelling a high-level language.

Each Y-tree element implements the interface YEntity and carries the Origin (original code coordinates) instance that contains information about the coordinates of the input text that has generated the Y-tree element. The origin can be translated to the code citation by the CitationService.

Following the C11 standard [ISO11], we distinguish a *statement* ("an action to be performed") from an expression ("a sequence of operators and operands that specifies computation of a value, or that designates an object or a function, or that generates side effects, or that performs a combination thereof"). All Y-tree expressions implement the YExpression interface. Although the pointer arithmetic is not fully supported by PorthosC, the Y-tree contains information about the *pointer level* of an expression (which is modelled as an integer number). We distinguish the subset of expressions that imply no side-effects, they implement the interface YAtom and can be global or local (which is determined syntactically).

The Y-tree expressions are the following:

• YBinaryExpression that model the C binary operator (*relative* operator that compares two expressions of any type, *logical* that processes two boolean expressions, and *numerical* that processes two integer or real expressions);

⁸Hereinafter we use the term *recursive* data structure (also called *inductive* data structure) to refer a complex data type that can contain elements of the same type.

- YUnaryExpression that model the C unary expression (logical negation, numeric prefix and postfix increment and decrement, bitwise complement);
- YMemberAccessExpression that has an arbitrary expression of type YExpression as its base expression (it will be resolved during the compilation stage, see Section 4.3.2.5);
- YIndexerExpression and YInvocationExpression that as arbitrary expression as its base or arguments (strictly speaking, the indexer expression is an unary-function invocation, but as the SMT-solver we use supports the constant-array theory, we can maintain the array type);
- YAssignmentExpression that assigns an YExpression to an YAtom;
- YVariableRef that stores the untyped "reference" to a variable (viz., the name only);
- YLabeledVariableRef that represents the litmus-specific local variable reference for a certain the process (e.g., 'P0:x' which means the local variable x of the process P0);
- YParameter that represents a typed variable (the type was declared, similarly to the variable definition); and
- YConstant that represents an untyped non-named constant.

Similarly to expressions, all Y-tree statements implement the YStatement interface. The statements are the following:

- YBranchingStatement representing the if-then-else statement;
- YLoopStatement representing both while- and for- loops;
- YJumpStatement representing unconditional jump (goto-jump to a label and loop-jumps break and continue);
- YCompoundStatement (block statement) representing sequence of N statements grouped into one syntactic unit;
- YLinearStatement representing a single expression; and

• YVariableDeclarationStatement containing the information about the variable type during the variable declaration.

On the Y-level of abstraction, we define the YType as a *reference* for the type (since the Y-tree is not typed, the YType is used for storing the type information on variables or types declarations). It consists type modifiers and qualifiers, that will be converted to the X-type by the Y2XTypeConverter during the pre-compilation stage (see Section 4.3.2.4).

According to the C standard, "any statement may be preceded by a prefix that declares an identifier as a label name". The Y-tree statements of follow this rule, however they these labels are symbolic, and they need to be resolved at the pre-compilation stage. Apart from the set of statements listed before, we define the YFunctionDefinition and its inheritor a litmus-specific declaration YProcessDefinition used in intra-procedural analysis mode. The function definition contains the YCompoundStatement body and the YMethodSignature signature (method name and types of formal parameters), which is used in the function resolution during the pre-compilation stage. The other litmus-specific statements are YPreludeStatement that carries the list of YStatement initial writes, and YPostludeStatement that carries the YExpression binary expression to be asserted by the litmus test.

The syntax tree that contains set of definitions (e.g., litmus-initialisations, function definitions, litmus-asserts) is modelled by the class YSyntaxTree.

4.3.1.2 X-graph

The Y-tree is compiled into the low-level event-based program representation called *X-graph*. The mathematical structure of event-flow graph was discussed in Section 2.1. The nodes of the graph are events, and the edges are basic relations: the control-flow relation po and the data-flow relations co and rf. Hereinafter, we denote the X-graph with only control-flow edges as X-graph_{CF}, the X-graph with only data-flow edges as X-graph_{CF}. The complete X-graph is X-graph_{CF+DF} = X-graph_{CF} \cup X-graph_{DF}. The UML diagram on Figure 4.3 represents the hierarchy of main interfaces of the X-abstraction level. Internally, the graph is represented by an adjacency matrix (to be exact, by multiple adjacency matrices that store edges of different kinds, see more details in Section 4.3.1.2).

All elements of X-graph implement the interface XEntity. There are two main kinds of X-entity: *events* that implement the XEvent interface, and *memory-units* that implement the XMemoryUnit interface.

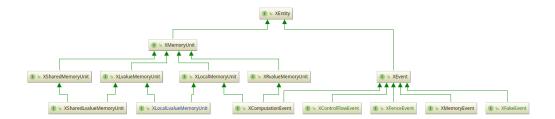


Figure 4.3: The inheritance tree of interfaces of X-graph

Following the format of litmus tests, we distinguish three types of X-graph: one for the parallel processes, one for the litmus-initialisation block and one for the assertion statement. However, all three types of the X-graph are modelled by the same graph structure XProcess with certain restrictions complied by the corresponding type of X-interpreter that constructs the graph. This simplifies drastically the processing of different types of code blocks as they all are modelled by the same data structure. The examples of restrictions on X-graphs are the following: the initialisation block can not have branchings, fence events; the process cannot have assertion events; the assertion block can not have shared-memory events or fence events. We discuss the interpretation of different types of statements in more detail in Section 4.3.2.5.

Memory units. An *X-memory unit* is a memory cell of an abstract machine executing the code (that represents the X-graph). The abstract machine has infinite number of arbitrary-sized *registers* (local memory units) and *locations* (shared memory units). Local memory units extend the XProcessLocalElement interface, that stores the ID of the owning process. Figure 4.4 represents inheritance hierarchy of memory units.

Following the terminology of the C standard, we distinguish the *r-value* and *l-value* memory units (unlike r-values, the l-values may be assigned a new value). As r-values cannot change their value, they can be seen as the value itself (therefore the XComputationEvent is modelled as an local r-value memory unit, see more detailed discussion further in current Section).

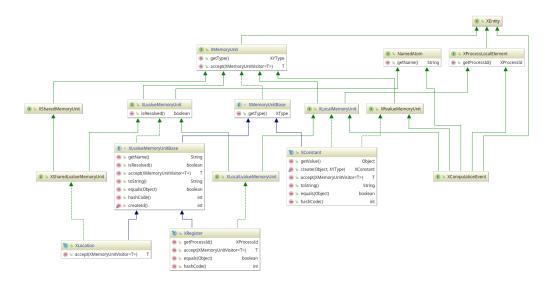


Figure 4.4: The inheritance tree of X-graph memory units

Each memory unit has an XType associated with it. The X-type is a symbolic representation of the C primitive type⁹ that is easily convertible to an SMT-type (modelled as ZType). All X-memory units carry the boolean flag that indicates whether it has been resolved correctly by the X-memory manager.

The memory units are created and stored by the XMemoryManager, which provides interface for accessing memory units during compilation stage. For more detailed description of memory management see Section 4.3.2.5.

Events. An event (XEvent) represents the fact of executing the primitive operation, which is independent from other events. Each event is specified by the process generated them and a unique event label. This information is stored by events in the immutable structure XEventInfo. Also, each event carries the reference to the Y-instruction that has generated it.

The following interfaces model basic kinds of events (see Figure 4.3):

• XMemoryEvent
The memory event defines the transfer of the value from one memory

⁹Here we should note that PorthosC can eventually evolve to be able to analyse programs written in an OOP language (for instance, in C++). In this case, the XType will have more complex structure than a simple enumeration, which it has when we need to emulate only primitive types of C language. See more detailed discussion on input language type system in Section 4.3.2.4.

unit to another. There are four types of memory events (the arrow denotes the direction of the data-flow):

- XRegisterMemoryEvent: (XLocalLvalueMemoryUnit) ← (XLocalMemoryUnit),
- $\hspace{1cm} \circ \hspace{1cm} \texttt{XLoadMemoryEvent:} \\ \hspace{1cm} (\texttt{XLocalLvalueMemoryUnit}) \leftarrow (\texttt{XSharedMemoryUnit}), \\$
- $\begin{tabular}{ll} \circ XStoreMemoryEvent: \\ & (XSharedLvalueMemoryUnit) \leftarrow (XLocalMemoryUnit), and \\ \end{tabular}$
- XInitialWriteEvent: (XLvalueMemoryUnit) ← (XRvalueMemoryUnit).
- XComputationEvent

We distinguish two types of computation events:

- XUnaryComputationEvent that encodes bit negation and nooperation; and
- o XBinaryComputationEvent that encodes numeric operations (such as addition, multiplication, etc.), bit vector operations (such as bit-and, bit-xor, etc.), relative operations (such as greater-then comparison, equality comparison, etc.), and logical operations (such as conjunction and disjunction).

The computation event class implements both XEvent and XMemoryUnit. This is a model-level optimisation, which is possible because a computation event performs computation over local-only memory and does not change value of any memory unit. Thus, the *computation* abstraction (as the CPU time spent for the computation itself) can be safely removed from the model, and the computation event can be seen as a zero-time operation that produces the *value*. For analysing large expressions this optimisation is sensible because it considers the whole expression as a single computation event, encoded therefore as a single SMT-variable.

Note, for the purpose of simplifying the X abstraction level, computation events may have been modelled as invocations of bodiless functions (for instance, the operation 'x + y' may be modelled as the invocation of the function '+' with the arguments x and y). However, current version of PorthosC maintains

the XComputationEvent as the operators are supported by the SMT-solver.

• XControlFlowEvent

The control-flow event indicates a non-linear jump in the code. We distinguish two kinds of control-flow events:

- XJumpEvent that performs no computation and no data operation, it can be safely removed from the model as an optimisation; and
- o XMethodCallEvent that models the function call with the fastcall calling convention (passing arguments in registers). The function call also implements the XLocalMemoryUnit since it represents the computed value returned by the function call. If the function has been resolved, the actual arguments are bind to the formal parameters (treated as temporary local memory units), the called XMethodCallEvent is pushed onto the call stack, and the execution jumps to the function body. The call stack is bounded by the user-defined parameter; once the stack is full, the interpretation continues without jumping to the body of the invoked function (such cases are properly logged). Each return statement creates the assignment of the function call event on the top of call stack. Note, this approach works for any kind of recursion, which is unrolled up the user-defined boundary as well as explicit loops.

If the function has not been resolved, it can be safely assumed to be a no-operation function. In other words, we suppose that the knowledge base of PorthosC is complete and the tool can resolve all memory-operation functions and fence instructions. Although this can affect the completeness of the analysis, it is safe to make such an assumption as the user can check the log file and manually analyse the semantics of an unresolved call and it to the knowledge base if necessary.

XFenceEvent

The fences are implemented as an enumeration XBarrierEvent. Current implementation of PorthosC supports all fences supported by Porthos: mfence, sync, optsync, lwsync, optlwsync, ish, isb, and isync.

• XFakeEvent

The fake events are the auxiliary elements of X-graph.

- XEntryEvent, the per-process unique source event in the event-flow graph,
- XExitEvent, the process sink event,
- XNopEvent, the no-operation event (a jump to the next event), used for correct encoding in case when the control-flow branch does not have any event (see Figure 3.2), and
- XAssertionEvent, the reachability assertion made at the postlude statement of the program. An assertion is modelled as an event for the purpose of encoding the postlude statement as a separate process that is compatible with the encoder.

Edges. As the graph is represented by an adjacency matrix, its edges are stored in (immutable) hash-maps. We distinguish the following kinds of edges:

- the *control-flow edges*:
 - o the *primary edges*, that denote both ϵ -labelled transitions (in case of linear sequence of events) and conditional transition that evaluates the conditional event (the source of the transition) to the *true*, and
 - o the *alternative edges*, that denote conditional transitions for which the conditional event (the source) was evaluated to the *false*; and
- the data-flow edges:
 - the co-relation edges, and
 - o the rf-relation edges.

Graph invariants. Once being constructed, the graph must conform the following requirements (see also Section 3.2.1):

- 1. the graph must have a single source with no ingoing edges, and two sinks of different kinds without outgoing edges,
- 2. the graph must be connected,
- 3. each node of the graph can have either one or two direct control-flow successors,

- 4. only nodes of type XComputationEvent can have two direct control-flow successors,
- 5. a co-edge connects two writes, an rf-relation edge connects a write and a read,
- 6. all write-event nodes except initial write-nodes must have exactly one co-predecessor, and
- 7. all write-event nodes except final write-nodes must have exactly one co-successor.

4.3.1.3 W-model

The *W-model* represents a recursive AST of *computations over relations* and assertion expressions defined by the memory model. The atomic elements of W-model are the basic relations (po, rf and co; see Section 2.1.2) and sets of events (\mathbb{R} , \mathbb{W} , $\mathbb{I}\mathbb{W}$, etc.; see Section 2.1.1). The expressions of W-model are unary (such as complement, transitive closure, etc.) and binary operations (such as union, intersection, etc.) over relations or sets of events; see Section 2.2. For the sake of transparency, each element of a W-model contains the origin location as the coordinates of the string in the model file.

4.3.1.4 **Z-formula**

The *Z-formula* representation is a wrapper for an SMT-formula used as an additional abstraction level used to increase the transparency of the architecture, simplify the debugging process and ease the support of different SMT-solvers. As all other internal representations, the *Z*-formula is implemented as an immutable data structure.

The Z-abstraction level models the the logical formulas (definitions and assertions) that are put on the assertion stack of the SMT-solver. Generally, a Z-formula represents the S-expression-based syntax of the SMT-LIB language [BFT17]. Currently, the Z-formula supports definitions and assertions over *variables* and binary and unary *expressions*. However, in future it may be extended to support *function symbols* and *binders* (existential and universal quantification, pattern matching and functional type construction).

All expressions of a Z-formula are *typed* (or *sorted*, in terms of SMT-LIB standard). Basically, we distinguish *boolean* and *numeric* (integer, bitvector, real) expressions. The typing of a Z-formula is necessary for checking the basic validity of its expressions and converting it to a typed SMT-LIB

formula. For the sake of transparency, each element of a Z-formula contains the origin location as the reference to the X-element that produced current Z-element.

4.3.2 Processing units

This section describes program units that construct, transform and analyse internal representations described before. We assign unique numbers to the processing units, which can checked in Figure 4.2 (within gears depicted in the top-left corner of each processing unit).

The construction of the X-graph is performed in three stages. First, the Y-tree is compiled to a *cyclic* control-flow event-based graph X-graph_{CF}. Then, this graph is unrolled to an *acyclic* control-flow event-based graph X-graph^U_{CF}. After that, the compiler is able to perform the data-flow analysis and produce the full event-based graph X-graph^U_{CF+DF}, which remains to be *CF-acyclic* (no cycles among control-flow edges).

Most data structures are processed by units that implement the *visitor* pattern [PJ98]. This is a behavioural pattern that separates the program logic from the object implementation by specifying handling methods for each element of the object. The general structure of the visitor pattern is illustrated by the pseudo-java code in Figure 4.5. The visitor pattern performs the double-dispatching, a mechanism for decreasing the cohesion between the DTO (the visitee) and the processor class (the visitor): the visitee implements the *accepting* method that gets the visitor as an argument and invokes its *visiting* method with itself as an argument. Thus, the method call resolution is performed statically at compile-time without any overhead at run-time. In our implementation, the visitor (not the visitee) cares about the continuation of traversing its children.

We consider the visitor pattern as the most natural way for operating the hierarchical data structures such as AST. However, we use its double-dispatching capabilities to reduce cost of multiple type casting performed while traversing the elements of a non-recursive data structure. The operator instance, instead of having a single method that handles and element of the instance, extends the visitor interface and splits the handler method into multiple methods, one for each type of element.

For traversing graph data structures, we mostly follow the *iterator* pattern: the special object Iterator, that has access to elements of the data structure, iterates over them in some order (for example, in topological order as it is implemented for X-graph). The construction of immutable

```
class Visitor<T> {
interface Element {
  <T> T accept(Visitor<T> visitor);
                                          T visit(AnElement e) {
                                            // visiting logic
}
                                            // continue recursively
class AnElement implements Element {
                                            e.getChild().accept(this);
  @Override
  <T> T accept(Visitor<T> visitor) {
                                          T visit(AnOtherElement e) {
    return visitor.visit(this);
  }
                                          }
}
                                        }
```

Figure 4.5: Illustration of the visitor pattern

data structures is performed by units that follow the *builder* pattern. A builder is a mutable object that contains methods "filling" it by the elements that will constitute the result complex object. The methods contain basic validity checks of the elements. Once a builder has been built, it cannot be modified.

4.3.2.1 Input parsers

Both input-language and input-model parsers are implemented via ANTLR parser generator. Details on the input program language grammar are discussed in Section 4.2. Currently, PorthosC does not consider preprocessor instructions (it ignores them). For implementing the inter-procedural mode of Porthos, it is crucial to support inclusion of header files (the #include preprocessor directive). Next step would be implementing the support of macros and conditional compilation directives, that are used often in C code. As preprocessor statements may appear in arbitrary place of a program, the preprocessor must be a stateful processing unit that reads the token stream and dynamically instrument the program by interpreting directives and expanding macros.

The input memory model language CAT is discussed in Section 2.2. The ANTLR grammar for CAT language was extracted from the parser used by herd tool¹⁰ written in OCaml.

¹⁰The herd project repository: https://github.com/herd/herdtools7

4.3.2.2 W-model constructor

The W-model representation is constructed by the stateless visitor Cat2WmodelConverterVisitor from the ANTLR syntax tree CatParser.MainContext of the memory-model defined in CAT language. Currently, the visitor supports the small subset of CAT language, which constitutes only non-functional declarative expressions of the language as the support for functional-style expressions requires implementing the full OCaml interpreter. However, some most commonly used functional-style expressions may be supported by mapping them syntactically to corresponding W-elements by the W-model constructor.

Following the principle of transparency, the W-model constructor aborts its work with the NotSupportedException if met the unrecognised syntax construction (in contrast to the Porthos v1 approach in which the null value was produced in all exceptional states).

4.3.2.3 Y-tree constructor

The Y-tree is constructed by the stateless visitor C2YtreeConverterVisitor from the ANTLR syntax tree C11Parser.MainContext of the C language. As the W-model constructor, the Y-tree constructor aborts its work with the NotSupportedException once it meets an unsupported syntax construction. A syntax exception YConverterException is thrown if the converted syntax tree contains semantic errors that prevent it to be converted to the Y-tree.

As a Y-tree constitutes a generic AST, the Y-tree constructor expands the syntactic sugar expressions and statements (for example, a switch-statement is converted to the equivalent if-statement).

4.3.2.4 X-graph pre-compiler

The precompiler traverses the Y-tree and collects information necessary for its compilation into an X-graph.

The label resolution. The label resolution is necessary for establishing links to labelled statements. In C, labelled statements are declared via the colon-syntax '<label> : <statement>', and the labels are referenced by the jump-statement 'goto <label>'. The label resolution algorithm traverses the Y-tree and collects all declared labels into a map that points a label to the labeled statement. This information is used during compilation to set up unconditional jumps.

Type analysis. C language has a static (resolved at compile-time) manifest (all types are declared explicitly) type system. Comparing to languages that use type inference, the type analysis of a C program constitutes a simple propagating the type information (obtained from variables declarations) to all expressions. Being carried at Y- and X- representation levels, the type is converted to a Z-type at the stage of the Z-formula encoding (see Section 4.3.2.8).

Currently, PorthosC handles only the primitive C types (such as int, char, float, etc.), which is modelled as an enumeration XType. The array dimension is stored at the Y-level as an integer number (currently this information is not used as PorthosC does not support arrays, although this information can be used at the stage of pre-compilation for converting array elements to separate variables). In addition, PorthosC has a built-in extensible database storing the semantics of non-primitive C types stored by the X2ZTypeConverter, which can be requested for converting an X-type to a Z-type.

The type analysis algorithm should consider the type aliases supported by C language (defined by the typedef instruction). For resolving the type aliases, the precompiler should make an extra traverse of the Y-tree before the pre-compilation stage and build up a symbol map.

The type analysis also includes the process of resolving semantics of function invocations. The result is stored in a map of invocation expression to the resolved function signature, so that the compiler can decide either to jump to the function body and interpret it, or to hook the invocation if the semantics of the function is resolved. However, due to lack of polymorphism and function overloading mechanism inherent to OOP languages, the function resolution algorithm may set up the mapping only for the function name and thus may neglect analysis of types of the arguments, we build the mapping for the full function signature so that the type analysis preprocessing unit may be used for analysing the C++ code if needed.

Variable kind analysis. On the compilation stage, once the compiler meets the reference to a variable, it should know whether it refers to a local or global variable. The kinds of variables have to be determined on the pre-compilation stage.

The following types of variables are detected as *global variables*:

- a variable was declared as a pointer;
- a variable whose address was accessed by any process;

- a variable that was declared as a parameter of the process function;
 and
- a variable that was exported by the extern keyword (in the kernelanalysis mode, the functions EXPORT_SYMBOL and EXPORT_SYMBOL_GPL also export symbols for dynamic linking).

4.3.2.5 X-graph compiler

The X-compiler is the main component that transforms the recursive Y-tree data structure to the plain X-graph representation. It is a complex processing unit; Figure 4.6 illustrates the relationship between the principal components of the X-compiler in the UML language.

The main class representing the X-compiler is Y2XConverter. It receives as input the Y-tree, the memory model kind and user settings (for instance, the interpreter mode defining the set of invocation hooks enabled during the analysis run). The Y2XConverter creates an instance of the stateless visitor Y2XConverterVisitor that traverses the Y-tree while invoking the stateful interpreter XInterpreter. The XInterpreter carries the X-graph-builder and provides *action* methods for changing its state and thus the filling in the builder. The interpreter requests the managers such as XMemoryManager, XHookManager, XTypeManager for additional information.

We distinguish three types of processes (each implementing the XInterpreter interface):

- the prelude process XPreludeInterpreter (to be executed before all other processes) that allows only declaration of local or shared variables, computations and memory operations;
- the postlude process XPostludeInterpreter (to be executed after all other processes) that allows only declaration of local variables, memory operations, computations and assertions;
- the process XProcessInterpreter (to be executed in parallel) that allows all X-compiler interface operations except declaration of shared variables and program assertions (i.e., it allows declarations of local variables, computations, barriers, unconditional jumps, non-linear branching statements, and method calls).

As the prelude process can declare shared variables, its compilation must go first. The first event of each process must be the XEntryEvent and the last events must be events of type XExitEvent.



Figure 4.6: Main components of the X-compilation processing unit

Memory manager. The X-graph abstract machine model disposes infinitely many memory units, both local and shared (see Section 4.3.1.2). The X-compiler accesses all memory units via the XMemoryManager, which by the end of pre-compilation stage is already initialised (has registered all shared memory units). However, the memory manager is a stateful component of the compiler as it offers the methods for declaring and removing local memory units dynamically at the compilation time.

The interface methods exposed by the XMemoryManager are presented in Figure 4.7. At each time of the compilation process, the XMemoryManager can resolve the memory unit by its name. Following the C standard, local memory units have higher priority over global ones (the method getDeclaredUnitOrNull returns the first memory unit found, either a global one or a local one, or null if no memory units with requested name have been registered). Since C language allows usage of variables that have the same name to be declared in nested contexts, the XMemoryManager carries the stack of block contexts for local variables.

```
interface XMemoryManager {
   XLocation declareLocation(String name, XType type);

   XRegister declareRegister(String name, XType type);

   XRegister declareTempRegister(XType type);

   XLvalueMemoryUnit declareUnresolvedUnit(String name, boolean global);

   XLvalueMemoryUnit getDeclaredUnitOrNull(String name);

   XRegister getDeclaredRegister(String name, XProcessId processId);
}
```

Figure 4.7: *X-memory manager public interface*

Invocation hook manager. The invocation hooking module serves as a knowledge base that stores the semantics of functions. Once the X-compiler meets the function invocation, it calls the XHookManager, which tries to match the function signature (in the case of program in C language – only the function name) across all signatures it stores. If the signature matches, the hook manager intercepts the function call and interprets the hook action instead of invoking the function directly. The hook manager operates multiple invocation hooks depending on the user-defined mode. All invocation hooks implement the interface XInvocationHook. The result of an invocation hook interception is the XInvocationHookAction, a delayed operation implemented on the top of lambda functions of Java. The hook action is invoked with actual arguments and returns an arbitrary XEntity as the result of invocation.

Current version of PorthosC contains two invocation hooks, the XLegacyInvocationHook for intercepting the compatibility-mode functions of the PorthosC input language, and XKernelInvocationHook for describing the Linux kernel-specific functions. An invocation hook can model any type of operations (memory, fence, computational, etc.). For instance, the XKernelInvocationHook intercepts the call 'WRITE_ONCE(dst_shared, src_local)' and replaces the invocation with its hook action shown in Figure 4.8.

Interpreter. The X-program interpreter is invoked by the Y2XConverterVisitor which walks down the Y-tree recursively. The calls to the X-program interpreter are dispatched to currently maintained X-process interpreter. To be able to properly recognise nested statements of the Y-tree, the X-process interpreter needs to have stacks. On any semantic error, the X-interpreter throws an XInterpretationError.

The interface methods of the XInterpreter are presented in Appendix A.2. Note the clear modular independence of the X-interpreter as it has no methods that operate entities of the Y-level (all conversion work with Y-entities is done by the Y2XConverterVisitor).

All interface methods can be divided into two groups. The first group constitute methods that emit events. These methods construct an event object (as events contain the XEventInfo structure that stores information about the owning process, all events must be created by the process constructor, i.e. X-interpreter) and change the state of interpreter considering the newly created event. Note that the methods createComputationEvent do not emit a computation event but only create one. This is performed as optimisation that removes unused computations from the model (otherwise, for instance, the assignment 'x = 1 * (2 + 3)' would be compiled to two consequent events 'eval(2 + 3); write(register <- eval(1 * eval(2</pre> + 3))); instead of a single event 'write(register <- eval(1 * eval(2 + 3)));'). If the computation event was not used at all (for example, in the following C code: 'foo(); 1; bar();' the execution event 'eval(1)' is skipped by the model), it is also removed from the event-graph (see justification in Section 4.3.1.2). The second group of X-interpreter methods consists of the methods for defining non-linear statements (branchings and loops). These methods change the state of the interpreter and set up additional non-linear control-flow edges.

As a high-level (Y-level) instruction may be compiled into a sequence of low-level instructions (for example, a computation that involves shared

```
class XKernelInvocationHook extends XInvocationHookBase
       implements XInvocationHook {
@Override
public XInvocationHookAction intercept(String functionName) {
   switch (functionName) {
    case "WRITE_ONCE": {
       return new XInvocationHookAction((receiver, arguments) -> {
         if (arguments.length != 2 || receiver != null) {
           return null; // do not intercept
        }
        XMemoryUnit destUnit = arguments[0];
        if (!(destUnit instanceof XSharedLvalueMemoryUnit)) {
           throw new XMethodInvocationError(methodName,
               "arg 1: not a shared l-value memory unit: " + destUnit);
         }
        XSharedLvalueMemoryUnit dest =
               (XSharedLvalueMemoryUnit) destUnit;
        XMemoryUnit srcUnit = arguments[1];
         if (!(srcUnit instanceof XLocalMemoryUnit)) {
           throw new XMethodInvocationError(methodName,
               "arg 2: not a local memory unit: " + srcUnit);
        XLocalMemoryUnit src = (XLocalMemoryUnit) srcUnit;
         return program.emitMemoryEvent(dest, src);
    });
  }
  case "READ_ONCE": {
     . . .
  }
}
}
```

Figure 4.8: Example of the invocation hook for intercepting the Linux kernel-specific functions

variables should firstly load them into the local memory and then process the computation event over local-only memory), the interpreter must maintain the *stack of contexts* and remember the *previous event* to be able to correctly process nested non-linear statements of C language. The context is a data structure that carries the *state* and some additional information in the case of processing non-linear statements (e.g., conditional event, first and last then- and else-branch events for binding, etc.). Once the new event has been emitted, the interpreter sets up control-flow edges w.r.t. state of the context on the top of the stack (the context stack is always non empty: the bottom context is a linear one). The context state is an enumeration of the following values:

- WaitingAdditionalCommand: the interpreter is in the state of defining the complex (non-linear) statement and is not able to process any new event (will throw an exception if any) until the state is not changed;
- WaitingFirstConditionEvent: the first next emitted event will be accepted as the first event of the condition evaluation (later, the loop edges will be set to this event);
- WaitingLastConditionEvent: the next event must be of type XComputationEvent; it will be saved as the conditional branching event;
- WaitingFirstSubBlockEvent: the first next emitted event will be accepted as the first event of the branching statement (later the interpreter will set up jumps to that event);
- WaitingNextLinearEvent: the default interpreter state for processing next linear event, and
- Idle: the interpreter does not set up the edge from the previous event to the new event.

Each new event emitted by the interpreter is processed considering the state of the context stack: the interpreter iterates over the context stack and sets up the edges by the graph builder depending on the state of each stack. The state WaitingFirstConditionEvent is necessary for correctly interpreting the branching conditions, which shared variables are involved in. If the non-linear statement is a loop statement, the loop back-edges will be set to this event.

Once interpretation of the (non-linear) branch is completed, its non-linear context is being popped out of the context stack (by interpreter method startBlockBranchDefinition) and added to the queue of almostReadyContexts. The almost-ready-context becomes a ready-context

(i.e., it moves to the queue readyContexts) once the non-linear statement definition has finished (the method finishNonlinearBlockDefinition).

Before processing a newly emitted event, the interpreter checks whether the queue readyContexts is not empty. If so, it iterates over all readycontexts and sets up control-flow edges considering that the newly emitted event is an exit-event" of the non-linear context (e.g., for a branching context the interpreter adds primary edges from condition-event to the first-true-branch-event and from the last-true-branch-event to the exit-event, the same is done with alternative edges for the false-branch).

As an example of usage the interpreter, consider the code of the Y2XConverterVisitor for processing if-then-else statement of the Y-tree in Figure ??.

For the sake of simplicity of the interpretation and encoding, jump events (no-computation events) are present in the flow-graph, however they can be removed from it with rebinding ingoing and outgoing edges.

4.3.2.6 X-graph unroller

In order to be encoded into an SMT-formula, the compiled graph needs to be acyclic [PFH $^+$ 17b]. To convert it to an acyclic form, we perform the *unrolling* (sometimes called *unwinding*) transfomation: each cycle is unrolled up to the user-defined bound k. Comparing to Porthos v1, we have changed the meaning of the bound: instead of executing all cycles at most k times, the PorthosC interprets the bound as the maximum number of events in the trace of the unrolled graph 11 . The meaning of a bound was changed in order to increase predictability of the size of the result SMT-formula. Note that recursive function calls create unconditional back-jumps in the event-flow graph, which will also be recognised as a loop and be affected by the unrolling algorithm. The discussion on how to set up the po-relations in the event-flow graph with recursive function calls can be found in [AKN $^+$ 14b].

 $^{^{11}}$ The original specification of PorthosC stated that the unrolling bound k must be interpreted as the maximum number of instruction in the original code (technically, the number of expressions in the ANTLR syntax tree). Nonetheless, current implementation of the X-graph unroller counts the X-level events as it is much simpler to implement (the questions about how to count complex expressions that involve multiple shared variables and method invocations are left open for the future versions of PorthosC). For now, the information about the element of the ANTLR tree that corresponds to the X-event or Y-tree element is being lost during the transformations. Instead, we use the LocationService discussed in Section 4.3.1.1 that in perspective may be extended for providing this information along with the text citation of the original code.

```
public class Ytree2XgraphConverterVisitor implements YtreeVisitor
   XEntity> {
  . . .
  @Override
  public XEvent visit(YBranchingStatement node) {
    program.startBlockDefinition(XInterpreter.BlockKind.Branching);
    program.startBlockConditionDefinition();
    {\tt XComputationEvent\ condition\ =\ program.tryEvaluateComputation(node.)}
   getCondition().accept(this));
    program.finishBlockConditionDefinition(condition);
    program.startBlockBranchDefinition(XInterpreter.BranchKind.Then);
    node.getThenBranch().accept(this);
    program.finishBlockBranchDefinition();
    YStatement elseBranch = node.getElseBranch();
    program.startBlockBranchDefinition(XInterpreter.BranchKind.Else);
    if (elseBranch != null) {
      elseBranch.accept(this);
    }
    else {
      program.emitNopEvent(); // needed for encoding
    program.finishBlockBranchDefinition();
    program.finishNonlinearBlockDefinition();
    return null; //statements return null
    }
}
```

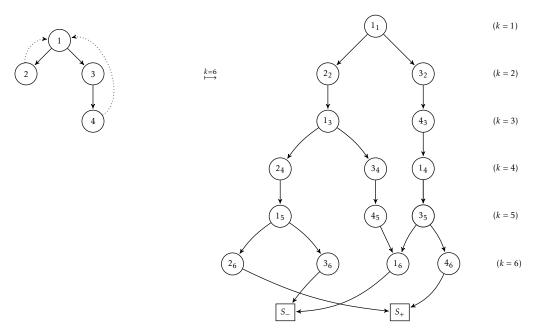


Figure 4.9: Example of the flow graph unrolling up to bound k = 6

Considering the new meaning of the unrolling bound, the graph unrolling may be *complete* (the loop has been executed a whole number of times) or *incomplete* (the unrolling bound has triggered on not-the-last event of the loop), which can be modelled by two types of the sink events. The user may need this information for understanding how the PorthosC interprets the cyclic program. However, current implementation loses this information by having only one sink event. Figure 4.9 illustrates the unrolling for the left-hand side cyclic control-flow graph (the square node S_+ denotes the complete sink node, and the S_- denotes the incomplete sink).

The unrolling procedure is performed by the XFlowGraphUnroller. For unrolling the flow-graph, we perform the *Deep-First Search (DFS)* while counting the Y-level instructions (for the unrolling bound) and keeping track of the depth stack (for detecting back edges needed for determining the type of sink node). Also, during the unrolling each next event increments the *unrolling depth counter* (the *event reference-ID*) – the integer that is stored by the XEvent thus making it *an event reference* on non-zero values. Each XEvent has the method 'XEvent asNodeRef(int refId)' that clones the event-receiver with new value of reference-ID. The methods hashCode and equals consider the reference-ID as the uniqueness field for all events except sink and source events (considering the usage of HashMap and Guava's

ImmutableMap for storing events, proper setting of the hash-code methods is a crucial programming task).

4.3.2.7 X-graph data-flow constructor

Once the graph is unrolled, it can be augmented by data-flow edges. As it was discussed in Section 4.3.1.2, the data-flow edges can represent either rf- or co-relation. The rf-edges join each write event to all read events that access the same location; the co-edges join write events to the same location.

4.3.2.8 Z-formula encoder

The Z-formula encoder accepts as input the program and the input memory models. It visits the recursive memory model AST and each its derived relation definition (recall the 'let' keyword of the CAT language) it transforms to the set of SMT-clauses, generated on the basis of the program events with respect to the encoding scheme described in Chapter 3.

4.3.2.9 SMT-formula converter

As the Z-formula follows the SMT-LIB standard, its translation to an SMT-formula constitutes almost one-to-one mapping. The translation is performed by the stateless visitor Z2SmtTranslator.

4.3.2.10 SMT-solver

As it has been mentioned in Section 4.1, PorthosC uses the third-party SMT-solver Z3, which offers the Java API for constructing requests to the Z3 solver and interpreting its responses.

4.3.3 Program output

The result of execution of PorthosC is the verdict modelled by the class AppVerdict. This is a structure that contains the result of analysis and auxiliary information such as collected errors and time of execution (separately for each stage of computing). The app verdict may be rendered to any format convenient for the user.

Chapter 5

Evaluation

5.1 Comparison with Porthos v1

5.1.1 Compilation and unrolling

Consider two equivalent functions in C (left) and the Porthos v1 input language (right) represented in Figure 5.1. The functions does not compute any useful value, however they contain three nested while-loops and thus can serve as an illustration of the differences in the program compilation and unrolling between Porthos v1 and PorthosC.

The functions are processed by PorthosC or modified version Porthos v1 that is able to print same X-graph_{CF} as the new tool (for that, the control-flow instructions if-then-else, while and sequence are expanded recursively and the head and the tails of each instruction are bind by the method processing its parent). The graph generation is performed via the open-source library Graphviz [EGK $^+$ 01]).

The Figure 5.2 illustrates the data structure which the functions in Figure 5.1 are compiled to. The left-hand side picture represents the non-unrolled X-graph $_{CF}$ generated by PorthosC, and the right-hand picture represents the AST generated by Porthos v1.

In both pictures, the writes are denoted with the left-directed arrow '<-', and the functions load and store denote the type of the shared memory event. The primary transitions that denote unconditional jumps or if-true-transitions are pictured with solid lines, and the alternative transitions that denote if-false-transitions are pictured with dotted lines. The graphs contains a single source event and a single sink event represented by the grey triangles (actually, the graph produced by Porthos v1 does not have

```
void t0(int &x) {
                                             thread t0 {
      int a = 1;
                                                  a <- 1;
      int c = 1;
                                                  c <- 1;
      while (a == 1) {
                                                  while (a == 1) {
          int b = 1;
                                                       b < -1;
          while (b == 1) {
                                                       while (b == 1) {
               while (c == 1) {
                                                            while (c == 1) \{
                   x = c;
                                                                x := c
               }
                                                            };
               x = b;
                                                            x := b
          }
                                                       };
      }
                                                   };
      x = a;
                                                  x := a
 }
                                              }
          (a) An example in the C language
                                              (b) An example in the Porthos v1 input language
```

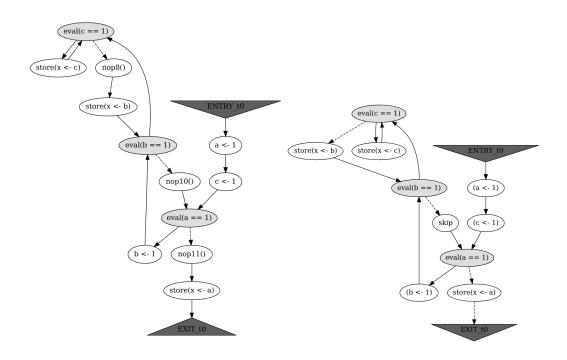
{ x }

Figure 5.1: Example: A demonstrative cyclic function

sink and source nodes, but they were added to the picture for demonstrative purposes). For clarity, all branching events, that in current example serve as the conditional events of loops, are highlighed with light-grey colour.

Two compiled the graphs are equivalent up to the extra nop-events in the PorthosC graph, that are necessary for correct encoding as it was discussed in Section 3.2.1, and skip-events in Porthos v1 graph. However, the unrolled graphs presented in Figure 5.3 are different as PorthosC uses different unrolling algorithm. The labels of events in the left-hand side picture (produced by PorthosC) are augmented by the unrolling depth number, which is separated from the event label by comma.

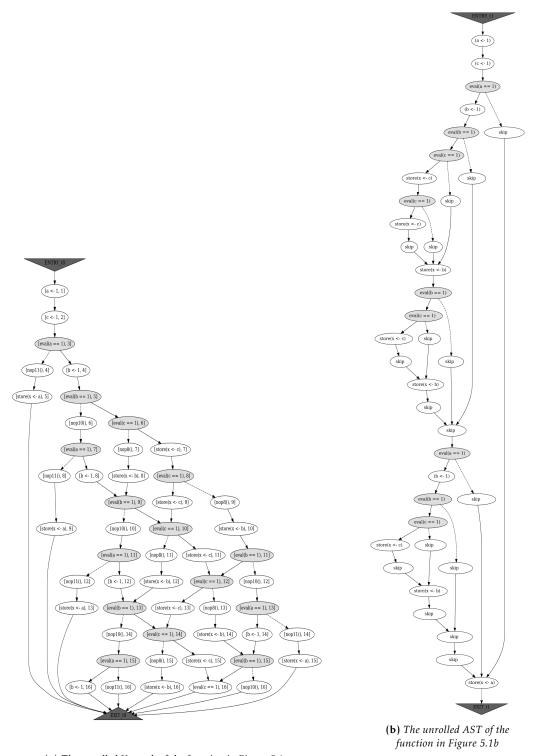
The unrolling algorithm used by Porthos v1 (right-hand side picture) unrolls all loops k times (where k is the unrolling bound), and the unrolling algorithm of PorthosC unrolls loops so that not more than k events are executed. As it is illustrated by the picture, the new algorithm produces a better set of program executions (for example, the unrolled graph of Porthos v1 does not contain executions of the inner loops more than k=2 times, which makes the old unrolling algorithm not complete). As the new unrolling algorithm uses the Deep-First Search, it discovers all possible paths, therefore the result graph contains all possible executions and thus is complete.



(a) The compiled X-graph of the function in Figure 5.1a (b) The compiled AST of the function in Figure 5.1b

Figure 5.2: The control-flow graphs of the functions represented in Figure 5.1

Note that the unrolled graph produced by PorthosC does not necessarily become a tree after removing the sink node. Some branches of the graph are merged when the executions have the same event with the same unrolling depth number. For example, primary transitions of both events '[b <- 1, 8]' and '[store(x <- b), 8]' (produced by executions of the first iteration of the while loop) lead to the same event '[eval(b == 1), 9]' (the first event of the second iteration of the second loop).



(a) The unrolled X-graph of the function in Figure 5.1a

Figure 5.3: The unrolled control-flow graphs of the functions represented in Figure 5.1

5.2 Performance evaluation

As an example of the C program liable for the reachability and portability analysis, consider the Dekker's algorithm for mutual exclusion of two processes, originally described by Dijkstra [Dij62]; the program is presented in Appendix A.3. For testing Porthos v1, we used the same file in old Porthos input language (dekker.pts), which was used in evaluation tests in the original paper [PFH+17a].

5.2.1 State reachability analysis

When running in the state reachability analysis mode, PorthosC produces the following output:

```
$ java PorthosC --reachability --input benchmarks/C11/Dekker.c \
      --bound 27 --target TSO
0.288: Interpretation...
0.426: Unrolling...
0.533: Program encoding...
0.701: Program domain encoding...
#=193 (107)
34.187: Memory model encoding...
36.818: Solving...
  "result": "NonReachable",
  "mainTimer": {
    "elapsedTimeSec": 36.163
  },
  "timers": {
    "Interpretation": {
      "elapsedTimeSec": 0.132
    },
    "ProgramDomainEncoding": {
      "elapsedTimeSec": 32.486
    },
    "Solving": {
      "elapsedTimeSec": 0.345
    "Unrolling": {
      "elapsedTimeSec": 0.061
    },
```

```
"MemoryModelEncoding": {
    "elapsedTimeSec": 2.631
    },
    "ProgramEncoding": {
        "elapsedTimeSec": 0.168
      }
    },
    "errors": []
}
```

For time benchmarking we ran the tool 5 times and computed the median of the encoding time. Benchmarking was performed on the Linux machine 8-core Intel(R) Core(TM) i7-3632QM CPU @ 2.20GHz, Java(TM) SE Runtime Environment (build 1.8.0_161-b12) (Java virtual machine was configured by default parameters). The time was measured by the tool itself via the native Java method System.currentTimeMillis.

As the unrolling algorithm has been changed, the number of events after unrolling differs considerably. Therefore, the correct performance comparison with Porthos v1 is not manageable as the performance of the tools depends directly on number of events. For example, with the bound $k_1 = 2$ Porthos v1 produces 59 events (among them, 51 shared-memory events) with the program domain encoding time 4.608 sec, and with the bound $k_1 = 3$ Porthos v1 produces 95 events (among them, 107 shared-memory events) with the program domain encoding time 21.475 sec; whereas PorthosC with the bound $k_2 = 17$ produces 57 (31) events with the program domain encoding time 1.734, and with the bound $k_2 = 27$ it produces 193 events (among them, 107 shared-memory events, which equal to the number of shared-memory events produced by Porthos v1 with the bound $k_1 = 3$) with the time 32.673 sec. Therefore, the new unrolling scheme has made the analysis complete but at the same time it reduced the performance considerably.

Note that the time spent by PorthosC for the interpretation and unrolling stages remains to be negligible comparing to the full encoding time. Therefore, we conclude that the new architecture implies no performance overhead comparing to the previous version of the tool. The time spent by the SMT-solver while considering the SMT-formula encoded by PorthosC was 0.039 sec, and in case of Porthos v1 the time was 1.291 sec. The number of events in the event-flow graph of PorthosC is 82 events (among them 59 memory events), and the number of events encoded by Porthos v1 is 95 (among them 51 memory events). Even though the number of memory

events processed by Porthos v1 was less, the time of solving the result SMT-formula was significantly more.

```
<TODO: above as table> <TODO: profile both programs, say sth about memory usage!>
```

5.2.2 Portability analysis

For evaluating the tool working in the portability analysis mode, we used the same file Dekker.c tested for the state-portability from TSO to SC:

```
$ java PorthosC --portability --input benchmarks/C11/Dekker.c \
      --bound 27 --source TSO --target SC --state
0.359: Interpretation...
0.364: Unrolling...
0.590: Unrolling...
0.623: Program encoding...
0.847: Program domain encoding...
#=193 (107)
#=193 (107)
66.541: Memory model encoding...
72.321: Solving...
  "result": "StatePortable",
  "iterations": 0,
  "mainTimer": {
    "elapsedTimeSec": 73.02
  },
  "timers": {
    "ProgramEncoding": {
      "elapsedTimeSec": 0.223
    },
    "MemoryModelEncoding": {
      "elapsedTimeSec": 5.779
    },
    "Interpretation": {
      "elapsedTimeSec": 0.248
    },
    "Solving": {
      "elapsedTimeSec": 0.699
    "ProgramDomainEncoding": {
      "elapsedTimeSec": 65.693
```

```
},
"Unrolling": {
    "elapsedTimeSec": 0.022
}
},
"errors": []
}
```

As the portability analysis requires compiling the program under two memory models, the overall program domain encoding time 65.693 sec is almost double as the same time in reachability analysis mode (Porthos v1 shows program domain encoding time 41.027 sec with the bound $k_1 = 3$).

5.2.3 New features

Apart from redesigning the tool architecture and extending the input language, we added support for basic constructions used in *Kernel litmus tests* [AMM⁺18]. Although, current version of PorthosC only supports some basic macros of the Linux kernel (such as READ_ONCE and WRITE_ONCE for atomic load and store with relaxed memory ordering) as the support for kernel-specific memory barriers goes out of the scope of current thesis. Note that, comparing to the Porthos v1, adding support for new functions in PorthosC does not require changing the input language grammar, this is carried by invocation hooking mechanism described in Section 4.3.2.5.

As an example, consider the SB litmus test for the Linux kernel (which is similar to the one presented in Figure 1.1):

```
{ int x = 0; int y = 0;}

P0(volatile int* y, volatile int* x) {
  int r0;
  WRITE_ONCE(*x,1);
  r0 = READ_ONCE(*y);
}

P1(volatile int* y, volatile int* x) {
  int r0;
  WRITE_ONCE(*y,1);
  r0 = READ_ONCE(*x);
}

exists(x == 0 && y == 0)
```

If verifying this litmus test by PorthosC in the state reachability mode, the test passes for TSO memory model and fails for SC model.

Chapter 6

Conclusion

6.1 Solved tasks and contributions

During the work on this thesis, we solved the following engineering and scientific tasks:

- 1. Firstly, we studied existing weak memory model-aware analysis frameworks and tools to gather deep understanding of the problem (Sections 1.2 and 3.1 and Chapter 2).
- 2. Then, we explored existing implementation of the portability analysis tool *Porthos* and designed the new tool *PorthosC* that accepts higher subset of the C language as input, has modular architecture and disposes the extensible knowledge base of the domain-specific functions. The key aspects of the architectural design and implementations are the following:
 - a. The first stumbling block in the input language extension was the Porthos v1 input language parser, which performs the full semantic analysis of the program. Although this works for a small subset of the C language, the rich and expressive language such as C requires several stages of analysis before the compilation stage. For handling that, we implemented the processing units that operate on the *pre-compilation* stage discussed in Section 4.3.2.4.
 - b. Secondly, Porthos v1 determined the *kind of a variable* (shared or local) syntactically, depending on the operator of the function that uses this variable. This strongly restricts the syntax of the input language, therefore, for processing programs in C, PorthosC

has an additional pre-compilation phase that traverses AST of the program and collects information of all variables accessed in the program (see Section 4.3.2.4). Currently, PorthosC considers a variable to be shared if it was declared as a pointer, or its address is accessed at least once by the code of any process, or it was declared as a parameter of the function that defines a process, or it was exported by extern or other keyword.

- c. In addition, PorthosC supports some *new syntactic constructions* of the C language: break and continue jumps, function invocations, multiple-variable declarations (as 'int a, b=2, z;'), arbitrary expressions (corresponding to the C standard), and others (see Section 4.2).
- d. As the C language supports unconditional goto-jumps that can produce an arbitrary control-flow graph, which cannot be supported solely with the program AST, therefore we needed to compile the AST to the low-level hardware-agnostic program representation X-graph. For that, we implemented the *full C interpreter* discussed in Section 4.3.2.5.
- e. Originally, the control-flow instructions were encoded directly into the SMT-formula [PFH+17a]. In contrast, PorthosC encodes the low-level X-graph representation, which can have arbitrary graph structure. For encoding the X-graph into the SMT-formula, we apply the *new control-flow encoding scheme* that in general follows the one proposed in [EH08, Chapter 5.1.2] (see Section 3.2.1). As the new encoding scheme does not add new variables to every control-flow instruction, the number of variables in the result SMT-formula is expected to be smaller.
- f. For ease of adding support for new domain-specific functions (for example, the Kernel-specific atomic write function atomic_store), we implemented the *invocation hooking*, a flexible mechanism for intercepting the compilation process without changing the interpreter. The invocation hooking mechanism serves as a knowledge base for the program domain, that is to be filled and extended in future. Invocation hooks are defined in Java and thus are flexible, though their extension and modification requires some knowledge of the internals of the tool. We illustrate this mechanism with the basic support for Linux kernel litmus tests.

- g. Since the new tool compiles the program AST to the X-graph before encoding it into the SMT-formula, we decided to change the *unrolling algorithm* from the simple unrolling all loops k times (where k is the user-specified unrolling bound) to the DFS-based algorithm that explores all possible states that the program can reach within k steps (see discussion on the unrolling in Sections 4.3.2.6 and 5.1.1). Although the new algorithm produces considerably more events than the old one and thus takes more time for analysis, PorthosC uses the new algorithm by default as it is complete (finds *all* possible executions).
- 3. As the tests show, the overhead of the new architecture is negligible, therefore we consider the applied architectural changes as acceptable.

Thus, the new tool PorthosC with the extensible program domain knowledge base can be considered as a generalised framework for SMT-based memory model-aware analysis, which can not only perform the reachability and portability analysis, but serve as a basis for other kinds of static analysis of concurrent programs.

6.2 Limitations and directions for future work

Current implementation of PorthosC has the following limitations, that might possibly define the direction of the future work.

• One of the major limitation of PorthosC as a software verification tool is its sensitivity to the *combinatorial explosion* of the state space. As it was shown in Section 5.2, the number of events of the unrolled program grow rapidly as the user increases the unrolling bound. One possible way to reduce the number of the program states might be applying some traditional techniques that target the state explosion problem (such as concrete execution as a part of concolic execution [MS07] before the unrolling stage). However, this must be done carefully and with taking into account the analysing weak memory model, because otherwise it can lead to the loss of states and thus to incorrect analysis results. Nonetheless, the small-size litmus test-like programs (containing hundreds of events after the unrolling) remain to be handleable by PorthosC within reasonable time.

- Extending the knowledge base of domain-specific functions to model synchronisation primitives can be considered as the main future research direction. Thus, to be able to process most Linux kernel litmus tests, PorthosC needs to know the semantics of the barrier and memory operation functions that are specific for the Linux kernel in order to be able to compile them into the X-graph and later encode them into the SMT-formula. Due to modular architecture of PorthosC, the extension of the knowledge base can be done by modifying solely the invocation hooking mechanism. Note that the flip side of the flexibility of invocation hooks is their complexity: being written in Java, in addition they require from the user some knowledge of general architecture of the tool, the interface methods provided by the interpreter, the class hierarchy of the X-graph elements, etc.
- Secondly, the wide range of existing litmus tests may require PorthosC to extend the support for input languages. The first candidates for being supported are the LISA language (Litmus Instruction Set Architecture) [ACM16] and assembly languages of most common architectures (x86, POWER, Alpha, etc.). Note that the programs in low-level languages can be easily compiled to the X-graph representation by existing compiler architecture since low-level assembly-like languages can be considered as the subset of the C language, that restricts the set of non-linear control-flow instructions to the conditional and unconditional jumps (which are supported by the current X-graph compiler of PorthosC).
- Although PorthosC has an extended support for primitive data types (integers, reals, booleans), it still is not able to handle the *complex data types*. However, as the Z3 solver supports the theory of constant-size arrays, it might be relatively easy to extend the support for constant-size arrays (declared as 'int arr[10];'), enumerations and structures. Nevertheless, pointers and variable-size arrays (allocated in the heap by functions malloc, calloc, etc.) require a stronger pre-processing analysis before being encoded into an SMT-formula.
- Currently, PorthosC can operate only in the intra-procedural analysis mode by assuming that each function provided by the user represents a separate thread (so-called litmus test-mode). One future direction of the work could be adding the *inter-procedural analysis mode* for scanning a code project instead of a separate file (see the discussion in Section 4.1).

Although, processing large programs may require serious memory optimisations (for instance, in storing the full unrolled graph data structure), which can possibly lead to worsening the overall performance. In addition, when processing large code projects, PorthosC might need the memory-guarding module that tracks the memory consumption of the tool and aborts its work if necessary.

- As it was mentioned in Section 3.2.1 devoted to the encoding for the control-flow of the program, the new encoding scheme used by PorthosC allows to analyse *partial functions*. Although the current PorthosC interpreter infrastructure is not configured to perform a partial analysis, it can be easily supported.
- During the implementation of PorthosC, we have only done limited *testing of the tool*. Thus, in order to increase the stability of PorthosC, we need to cover its code by unit- and functional tests.
- One might want to compare the performance of PorthosC in cases of usage the different SMT-solvers. Due to the Z-formula abstraction layer, new SMT-solvers may be easily added (the general way to support multiple SMT-solvers is to convert the Z-formula to an SMT-LIB formula [BFT17], that can be passed as input to the SMT-solver run as an external process).
- <parallelised>
- <C processor directives ><TODO: a short summary here>

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Appendices

A.1 File trees of Y-tree and X-graph representations



A.2 Public interface methods of the X-interpreter

```
public interface XInterpreter {
 XProcessId getProcessId();
 void finish();
 XProcess getResult();
 // emitting new events:
 XEntryEvent emitEntryEvent();
 XExitEvent emitExitEvent();
 XBarrierEvent emitBarrierEvent(XBarrierEvent.Kind kind);
 XJumpEvent emitJumpEvent();
 XNopEvent emitNopEvent();
 XAssertionEvent emitAssertionEvent(XBinaryComputationEvent assertion);
 XLocalMemoryEvent emitMemoryEvent(XLocalLvalueMemoryUnit destination,
                                    XLocalMemoryUnit source);
 XSharedMemoryEvent emitMemoryEvent(XLocalLvalueMemoryUnit destination,
                                     XSharedMemoryUnit source);
 XSharedMemoryEvent emitMemoryEvent(XSharedLvalueMemoryUnit destination,
                                     XLocalMemoryUnit source);
 // create computation event without processing it:
 XComputationEvent createComputationEvent(XUnaryOperator operator,
                                           XLocalMemoryUnit operand);
 XComputationEvent createComputationEvent(XBinaryOperator operator,
                                           XLocalMemoryUnit operand1,
                                           XLocalMemoryUnit operand2);
 // non-linear statements interpretation:
 void startBlockDefinition(BlockKind blockKind);
 void startBlockConditionDefinition();
 void finishBlockConditionDefinition(XComputationEvent condition);
 void startBlockBranchDefinition(BranchKind branchKind);
 void finishBlockBranchDefinition();
 void finishNonlinearBlockDefinition();
 void processJumpStatement(JumpKind kind);
 XEntity processMethodCall(String methodName, XMemoryUnit... arguments);
}
```

A.3 Dekker's mutual exclusion algorithm in C

```
{ int flag0 = 0, flag1 = 0, turn = 0; }
void P0() {
    while (true) {
      int a = 1, b = 0;
      flag0.store(memory_order_relaxed, a);
      f1 = flag1.load(memory_order_relaxed);
      while (f1 == 1) {
        t1 = turn.load(memory_order_relaxed);
        if (t1 != 0) {
          flag0.store(memory_order_relaxed, b);
          t1 = turn.load(memory_order_relaxed);
          while (t1 != 0)
            t1 = turn.load(memory_order_relaxed);
          flag0.store(memory_order_relaxed, a);
      }
    }
}
void P1() {
    while (true) {
      int c = 1, d = 0;
      flag1.store(memory_order_relaxed, c);
      f2 = flag0.load(memory_order_relaxed);
      while (f2 == 1) {
        t2 = turn.load(memory_order_relaxed);
        if (t2 != 1) {
          flag1.store(memory_order_relaxed, d);
          t2 = turn.load(memory_order_relaxed);
          while (t2 != 1)
            t2 = turn.load(memory_order_relaxed);
          flag1.store(memory_order_relaxed, c);
        }
      }
    }
}
exists (turn == 10)
```