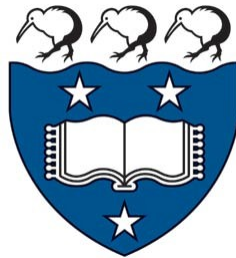


# Improvements to the ‘dvir’ Package

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# 1 Executive summary

$\text{\TeX}$  has many desirable features, such as math equation formatting and typesetting, which are currently not available in R. The `dvir` package extends R to draw  $\text{\TeX}$  output on R graphics. By extending the usability and functionality of the `dvir` package it better streamlines the workflow of making R graphics with some  $\text{\TeX}$  output - rather than making some graphics in R and exporting to  $\text{\LaTeX}$  itself or an image editor like Photoshop to add  $\text{\TeX}$  or  $\text{\TeX}$ -like output, this can all be done in R through a simple interface from the `dvir` package. Three improvements to the `dvir` package are investigated and discussed in this report.

Running functions from the `dvir` package took a long time which. The speed of the package was increased by making two changes - removing redundant code that meant the `dvir` package was searching for fonts three times instead once, and allowing font information to be cached so once font information was found the `dvir` package did not need to search again for that font.

The latest version of R adds functionality of linear and radial gradient fills. This means gradient fill information from  $\text{\TikZ}$  graphics, a  $\text{\TeX}$  package, could be generated by `dvir` and manipulated to be fed into R. This was not implemented as the complexity of the gradient definition from  $\text{\TikZ}$  resulted in “warped” gradient fills which are not possible in R.

The `dvir` package currently performs any alignment based on the bounding box of the text but aligning with the baseline of the text is more desirable.  $\text{\TeX}$  output does not explicitly state a baseline value for a piece of text so some algorithms for determining the text baselines were implemented in an R function to test their usefulness. One of these algorithms performs particular well for all tested examples, including multi-line text.

The magnitude of the speed increase alone makes `dvir` much more practical as it allows much faster testing of code and allows for more complicated graphics with many calls to the `dvir` package. The ability to align text to its baseline means graphics with the addition of  $\text{\TeX}$ , for example in lattice plot headers, can be aligned with one another and not require “touching up” outside of R.

This report, source code and associated files can be found on GitHub<sup>1</sup>.

---

<sup>1</sup>[https://github.com/ajvandervoorn/honours\\_dissertation](https://github.com/ajvandervoorn/honours_dissertation)

## 2 Introduction

R (R Core Team 2021) has the ability to display mathematical symbols and equations in graphics using the “plotmath” feature (Murrell and Ihaka 2000), interpreting everything within a call to `expression()` as a mathematical equation.

```
x <- 1:5
y <- x ^ 2 / 2
expr <- expression(frac(mu ^ 2, 2))
# par(mar = par()$mar + c(0, 1, 0, 0))
plot(x, y, xlab = expression(mu), ylab = "", yaxt = "n", type = "l")
axis(2, las = 1)
mtext(expr, side = 2, line = 3, las = 1)
```

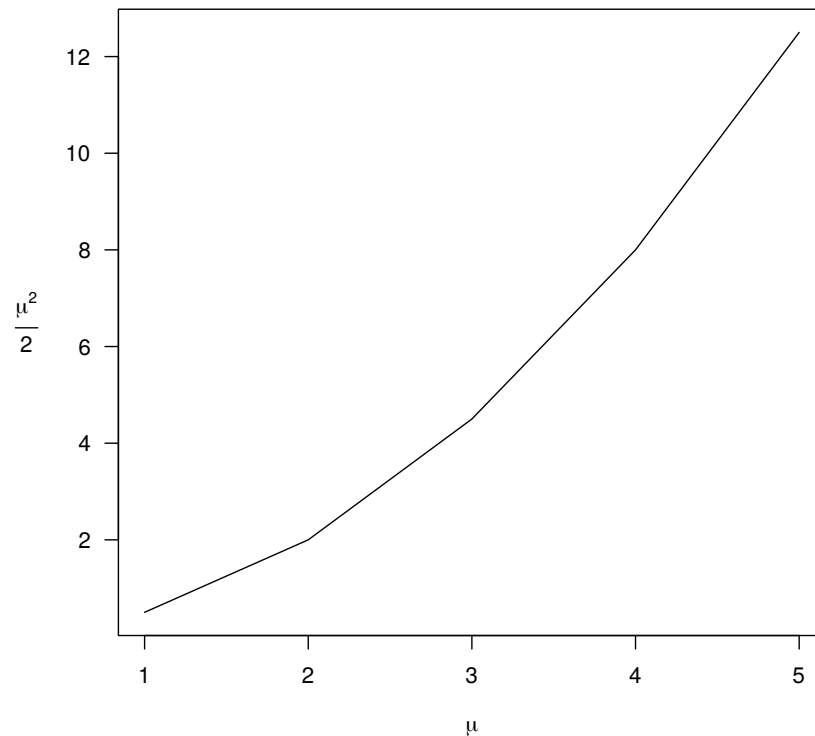


Figure 1: A plot with axis labels made using `expression()`.

This provides us with most of the symbols used for equations, such as brackets and fractions, and formats them in a layout resembling  $\text{\TeX}$  (Knuth 1986), but it is limited in its fonts. Compare the y-axis title above with how it looks when created by  $\text{\LaTeX}$  in figure 2.

The difference is stark and Murrell (2018) describes several approaches in R, and their limitations, which can get us closer to the  $\text{\LaTeX}$  result as motivation for the `dvir` package. The approaches are replicated here.

$$\frac{\mu^2}{2}$$

Figure 2: The y-axis title from above, created with L<sup>A</sup>T<sub>E</sub>X

The `extrafont` package (Chang 2014) with the `fontcm` package extension (Chang, Kryukov, and Murrell 2014) works for this particular example but not if we wanted to include other T<sub>E</sub>X symbols.

```
library(grid)
library(extrafont)
font_install('fontcm')
loadfonts("pdf")
pdf("extrafont.pdf", width = 1, height = 1)
grid.text(expr, gp = gpar(fontfamily = "CM Roman"))
dev.off()
embed_fonts("extrafont.pdf", outfile = "extrafont-embed.pdf")
```

$$\frac{\mu^2}{2}$$

Figure 3: The axis title using the `extrafont` package

```
expr2 <- expression(bgroup("(", frac(x - mu, sigma), ")"))
pdf("extrafont-2.pdf", width = 1, height = 1)
grid.text(expr2, gp = gpar(fontfamily = "CM Roman"))
dev.off()
embed_fonts("extrafont-2.pdf", outfile = "extrafont-2-embed.pdf")
```

$$\left( \frac{x - \mu}{\sigma} \right)$$

Figure 4: Another equation using the `extrafont` package

In the case of figure 4, note how `extrafont` has once again used the correct font for the greek symbols, but does not quite replicate the rest of the result from L<sup>A</sup>T<sub>E</sub>X, as in figure 2.

```
# Using the 'tikzDevice' package
library(tikzDevice)
options(tikzDocumentDeclaration = "\\documentclass[12pt]{article}")
packages <- c(getOption("tikzLatexPackages"),
              "\\usepackage{amsmath}\\n")
```

$$\left(\frac{x - \mu}{\sigma}\right)$$

Figure 5: A  $\text{\LaTeX}$  equation with brackets

```
options("tikzLatexPackages" = packages)

tikz("tikzDevice.tex", standalone = TRUE)
opar <- par(mar = par()$mar + c(0, 1, 0, 0))
plot(x, y, xlab = "$\\mu$", ylab = "", yaxt = "n", type = "l")
axis(2, las = 1)
mtext("$\\dfrac{\\mu^2}{2}$", side = 2, line = 3, las = 1)
dev.off()
```

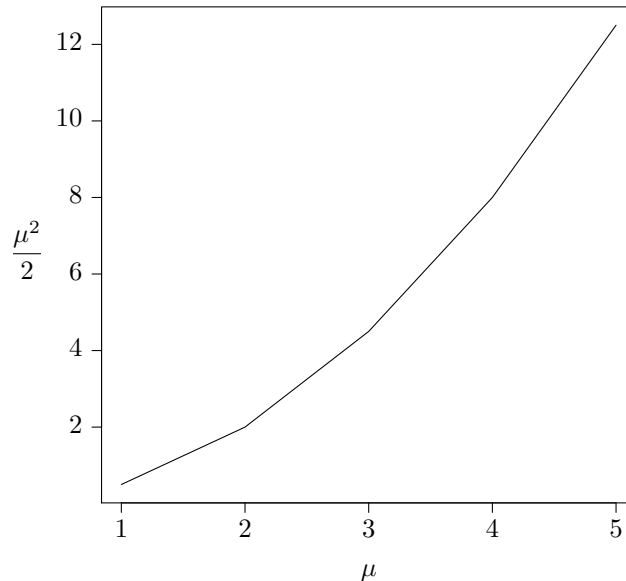


Figure 6: Drawing the plot with the `tikzDevice` package

The `tikzDevice` package in R will draw the axis titles with  $\text{\TeX}$  but will also use  $\text{\TeX}$  for all other text on the plot, like the axis labels in figure 2. This may be appropriate if the graphic is to be included in a  $\text{\TeX}$  document but not so much for other document formats like HTML.

What we want is a middle ground - being able to harness the power of  $\text{\TeX}$  and its typesetting capabilities on *our* choice of text or equation in R graphics. This is where the `dvir` package comes in - providing a simple user interface, in the style of R `grid` graphics, by way of the `grid.latex()` function. Figure 7 recreates figure 1 with the axis titles made using `grid.latex()`.

```
library(dvir)
preamble <- "\\documentclass[12pt]{standalone}\n\\usepackage{amsmath}\n\\begin{document}"
par(mar = par()$mar + c(0, 1, 0, 0))
```

```
plot(x, y, xlab = "", ylab = "", yaxt = "n", type = "l")
axis(2, las = 1)

grid.latex("$\\mu$", x = 0.545, y = 0.07)
grid.latex("$\\dfrac{\\mu^2}{2}$", x = 0.06, preamble = preamble)
```

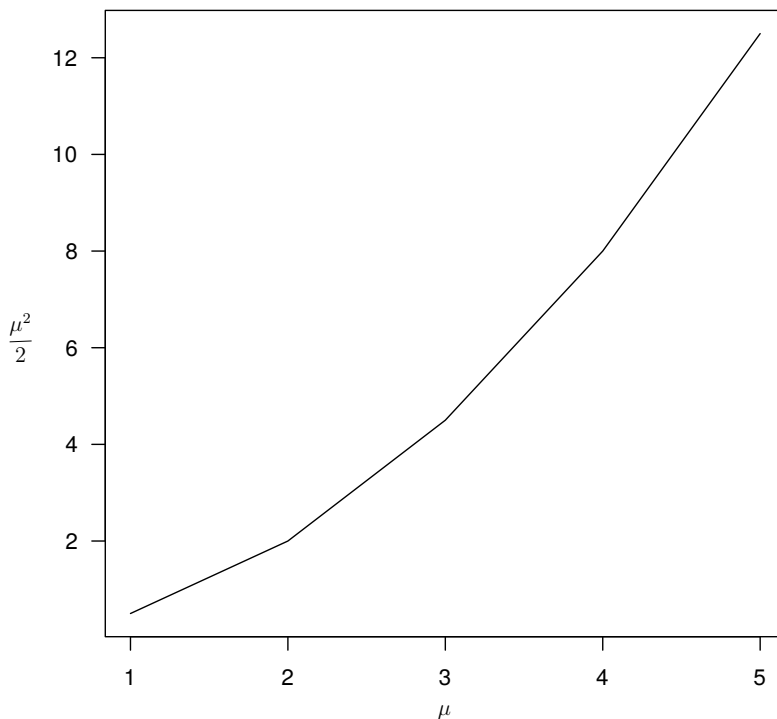


Figure 7: Changing axis titles with `grid.latex()`

## 2.1 Where this project fits in

The `dvir` package already worked really well in a lot of cases. There were however a number of desirable features of  $\text{\TeX}$  and its extensions that had not yet been implemented by `dvir`. The power of this package comes from ensuring it is comprehensive enough to meet a user’s entire  $\text{\TeX}$  needs in R graphics without having to leave R to do annotations in  $\text{\LaTeX}$  itself (or other software like Adobe Photoshop or Illustrator).

By keeping things “in R” users only need to learn R (and basic  $\text{\TeX}$ ) code to create their graphics and their work is in one place and easily reproducible. It may not be realistic to *completely* replicate  $\text{\TeX}$  in R, however several aspects of the package were identified as having the potential to increase its usefulness. The aspects identified were:

- the speed of the package - anecdotally it took a while to generate graphics, especially if there were

many `grid.latex()` calls

- expand `dvir`'s capability of creating *TikZ* drawings by adding support for linear gradient fills
- adding the ability to align text from `grid.latex()` to a baseline - the natural line on which characters sit



## 3 Background

### 3.1 T<sub>E</sub>X

T<sub>E</sub>X is a program to format and typeset text, and includes some basic macros to do this. L<sup>A</sup>T<sub>E</sub>X is a higher-level implementation that sits on top of T<sub>E</sub>X, basically consisting of a lot more macros, creating a much more user-friendly interface to T<sub>E</sub>X. For example, L<sup>A</sup>T<sub>E</sub>X allows one to create a document with numbered sections, title pages and bibliographies without having to write complicated T<sub>E</sub>X macros oneself.

### 3.2 DVI

A T<sub>E</sub>X or L<sup>A</sup>T<sub>E</sub>X file is just plain text so there needs to be a step to translate this plain text to what you will see on a formatted document on a screen or page. T<sub>E</sub>X “engine” like `pdflatex` normally processes T<sub>E</sub>X to PDF but it can also produce a DVI (DeVice Independent) file. A DVI file is a binary file describing the layout of the document. For example, the height of the page, what characters to display and where, and the fonts to be used. DVI provides a format that can be read into R so that we can draw the T<sub>E</sub>X layout in R. This is what the `dvir` package does.

### 3.3 The (pre-existing) `dvir` package

In a simplified form, `dvir` works by providing a high level function, `grid.latex()`, to call with the T<sub>E</sub>X code of the expression or text to be displayed. In this instance, the preamble is changed only because the axis title uses `\dfrac` so the `amsmath` package needs to be specified in the preamble.

```
library(dvir)
texCode <- "$\\dfrac{\\mu^2}{2}$"
newPreamble <-
  "\\documentclass[12pt]{standalone}\\n\\usepackage{amsmath}\\n\\begin{document}"
grid.latex(texCode, preamble = newPreamble)
```

$$\frac{\mu^2}{2}$$

Figure 8: Using the `dvir` function `grid.latex()`

The following steps are taken when `grid.latex()` runs:

1. A T<sub>E</sub>X document is created with the expression and a changeable default preamble and postamble.

```
postamble <- paste0("\\end{document}")
cat(paste(newPreamble,
  texCode,
  postamble,
  sep = "\\n"))
```

```
\\documentclass[12pt]{standalone}
```

```

\usepackage{amsmath}
\begin{document}

$$\frac{\mu^2}{2}$$

\end{document}

```

2. This TeX document is then processed using the local T<sub>E</sub>X installation to create a DVI (DeVice Independent) file.
3. The DVI file is read into R. As DVI files are binary they are not easily readable by humans but the `dvir` function `readDVI()` translates the DVI file into readable text. This is an extract of a DVI file after using `readDVI()`, stating the definition of a font and then "setting", that is, printing, a character "2".

```

fnt_def_1      fontnum=15, checksum=2088458503, scale=524288,
               design=524288, fontname=cmr8
set_char_50    '2'

```

4. Three "sweeps" of the DVI file are completed to extract necessary information about what to display in R (and where and how to display it):
  - Font sweep: Gather the names of all fonts used in the DVI file and locate the relevant font files on the local machine. The font information is stored in a R list as well as a `fontconfig` file.
  - Metric sweep: To determine the overall bounding box (size) of the expression to display. This bounding box is used to create a `grid` viewport which can encompass the entire T<sub>E</sub>X passed to `grid.latex()` expression using the native DVI coordinates.
  - Grid sweep: Convert all text and symbols into *grobs* (grid graphical objects)
5. These grobs are then displayed in the R graphics device as per the `grid` package.

## 4 Code speed (part 1) - removing redundant font sweeps

In the introduction of this report the case for the `dvir` package was motivated with a simple example of a mathematical equation. `dvir` can be used on a larger scale too.

```
grid.latex("\\dots", x = 0.44, y = -0.1, default.units="native")
grid.latex("$Y_* =$", x = 0.5, y = 1.1, default.units="native")
grid.latex("$a_1$", xpos[1], y = -0.1, default.units="native")
grid.latex("$a_2$", xpos[2], y = -0.1, default.units="native")
grid.latex("$a_{L_A}$", xpos[3], y = -0.1, default.units="native")
grid.latex("$Y_{\\pi} \\mid Y_{\\pi} \\notin \\mathcal{A}$",
  x = xpos[4], y = -0.1, default.units="native")
grid.latex("$\\omega_1$", x = 0.18, y = 0.50, default.units="native")
grid.latex("$\\omega_2$", x = 0.32, y = 0.50, default.units="native")
grid.latex("$\\dots$", x = 0.44, y = 0.50, default.units="native")
grid.latex("$\\omega_{L_A}$", x = 0.54, y = 0.50, default.units="native")
grid.latex("$1 - \\sum_{s=1}^{L_A} \\omega_s$", x = 0.95, y = 0.50, default.units="native")
```

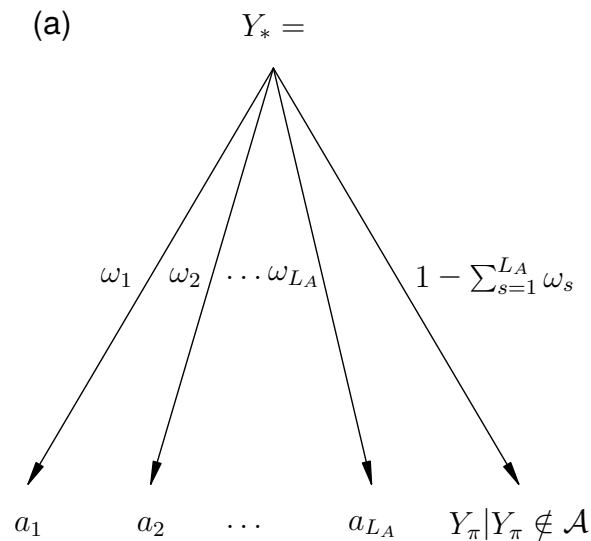


Figure 9: Using nine `grid.latex()` calls with base R graphics.

The example in figure 9 was created by a University of Auckland lecturer using the `dvir` package to help write an assignment.

One of the first things investigated in the package was the speed of running the code. Anecdotally, generating any R graphic with non-trivial  $\text{\TeX}$ , like that in figure 9, took a long time so it was desirable to speed it up.

To look into this the first task was to profile the existing code to let us see where in the package time was being spent. This was in `dvir` version 0.2-1. The profiling results were visualised with `profvis::profvis()`.

We can see the function call stack in figure 10. At the bottom is the call to `grid.latex()`, which immediately calls `grid.draw()` which in turn calls `latexGrob()`. This calls `readDVI()` for about the first 20ms, then



In the top left corner of figure 11 we are told the aggregate time spent with `engine$fontDef` is 1830ms. Compared to the total time of this run (a total of about 2700ms), `dvir` is spending a *lot* of time doing these font sweeps.

What was interesting though was that after the actual font sweep the following sweeps for the metric and grid information *also* called `engine$fontDef`. As the point of the font sweep is that it finds all the font information to be used later on the following metric and grid sweeps should not need to “re-sweep” for the fonts.

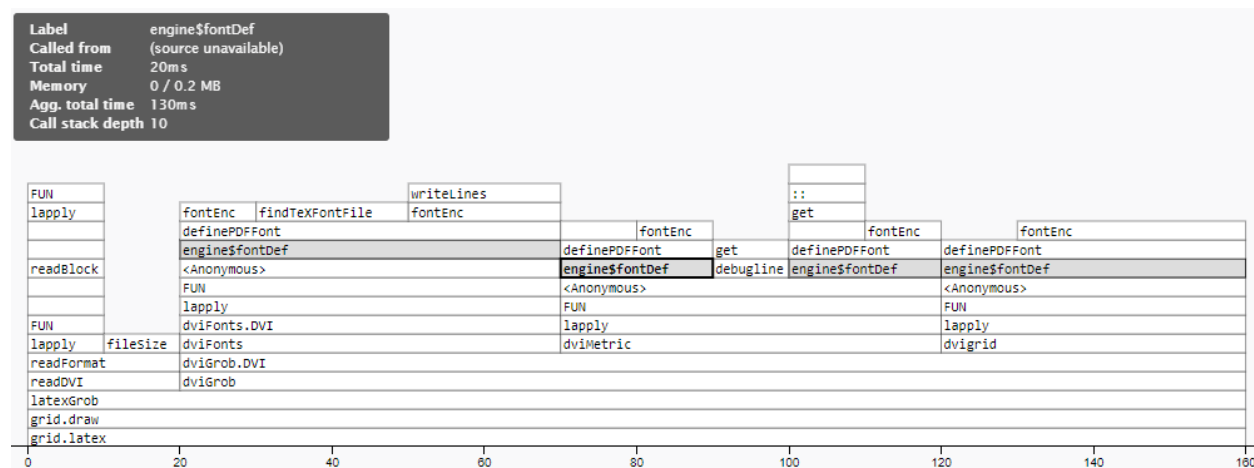


Figure 12: Screenshot of `profvis::profvis()` output for the simple example in `dvir` version 0.2-1, highlighting `engine$fontDef`.

The effect of this is very obvious in figure 12 which is the same as figure 10 but highlights the time spent in `engine$fontDef`. The wrappers for the font, metric and grid sweeps are `dviFonts()`, `dviMetric()` and `dviGrid()` respectively (sixth call from the bottom of the stack). Here we can see nearly all of the time spent in the metric and grid sweeps are actually redoing the font sweep.

The change to be made was simply stopping the metric and grid sweeps from doing the font sweep again.

The font sweep looks in the DVI file for op codes 243 to 246. These are the op codes for font definitions and define the name of a font and give it an identifier to reference in the DVI file when it wants to use that font to display a character.

The following code is taken from the `dvir` package, showing where the metric and grid sweeps also redid the font sweep. `op_font_def` is a function which takes the font definition in the DVI file related to that instance of the op code and searches for and records the font information.

```
metric_info_243 <- op_font_def
grid_op_243 <- op_font_def
```

The following code shows what the code was changed to in `dvir` version 0.2-2. `op_ignore` is an empty function, so when the metric or grid sweeps comes across that op code, they now do nothing.

```
metric_info_243 <- op_ignore
grid_op_243 <- op_ignore
```

Unfortunately these changes by themselves caused an error when running `grid.latex()`. This is because one task undertaken before the font sweep is to reset or overwrite the global fonts list (which the font sweep then writes to). The metric and grid sweeps were also doing this even though it was only intended for it to be done by the font sweep. This meant after the font sweep was completed it was overwritten by the metric and grid sweeps and so when `dvir` tried to draw the characters there was no font information to refer to.

The resetting of the global fonts list was initiated when the sweeps passed op code 247 in the DVI file, which is the preamble at the start of every DVI file. Setting the metric and grid sweeps to do nothing when they pass the preamble of the DVI file, again by way of `op_ignore`, solved this problem as the global fonts list created by the font sweep is now not overwritten.

```
metric_info_247 <- op_ignore
grid_op_247 <- op_ignore
```

To quantify the impact this has on code speed the time to run the examples 20 times was recorded, after an initial run to compile the package after it was loaded. The average of these 20 runs was then calculated.

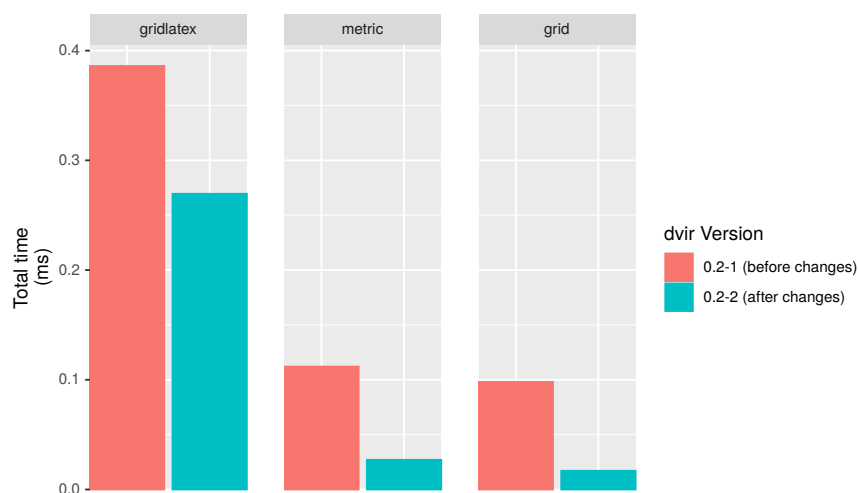


Figure 13: The average time spent in the `grid.latex()` function, metric sweep and grid sweep before and after these changes, over 20 runs of the simple example.

For the simple example the time spent in the metric and grid sweeps have decreased by 76% and 83% respectively. The speed of the overall `grid.latex()` call has decreased by 30%.

Similarly for the more complicated example in figure 14 the metric and grid sweeps have decreased by 83% and 89% respectively, with `grid.latex()` overall taking 47% less time.

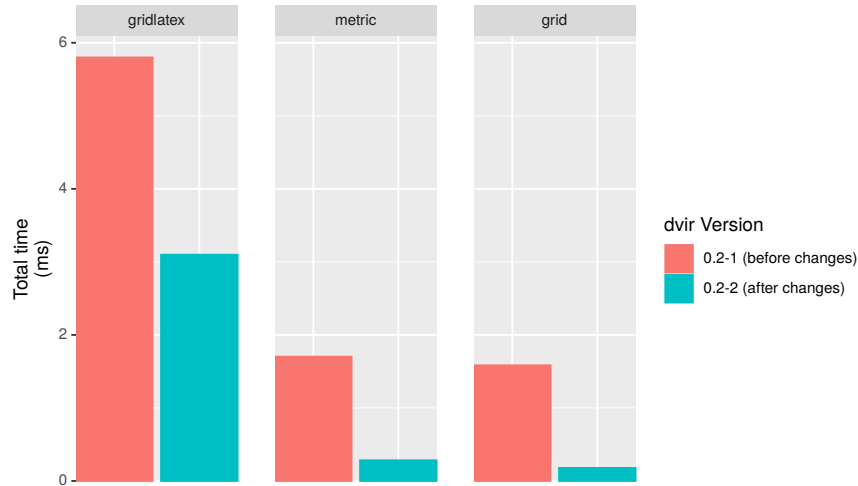


Figure 14: The average time spent in the `grid.latex()` function, metric sweep and grid sweep before and after these changes, over 20 runs of the complicated example.

## 5 Code speed (part 2) - font caching

In the previous section, the speed of `dvir` was increased by stopping it doing something “silly”. The profiling results from the previous section demonstrate how much time `grid.latex()` spends dealing with fonts so this section is about making `dvir` “smarter” by caching the information it gathers about fonts between `grid.latex()` calls.

For example, creating figure 9 requires three `grid.latex()` calls for the same symbol  $\omega$ . Each time, the following font definition appears in the DVI file for `grid.latex()` to search for during its font sweep.

```
fnt_def_1    fontnum=17, checksum=-1209964637, scale=786432, design=786432,
             fontname=cmmi12
```

In fact, the example’s 11 `grid.latex()` calls define fonts 29 times in total, for eight unique fonts.

Caching fonts requires several steps:

- During the font sweep, search all font definitions as per usual.
- For each font definition, check if the font has been cached already.
  - If yes, do nothing. Refer to the existing font information in the cache when the needs to be used
  - If no, search for and store the font information as per usual.

The font information is stored in R as a list. Every time `grid.latex()` processed a “preamble” op code in a DVI file, that is, every time `grid.latex()` was called, the font list was initialised as an empty list in the `dvir` namespace with `dvir::set("fonts", vector("list", 255))`. To stop this initialisation happening by default, the following code was put in its place.

```
if (dvir::get("initFonts") || is.null(dvir::get("fonts"))) dvir::set("fonts", vector("list", 255))
```

Note in this new statement the logical variable `initFonts`, stored in the `dvir` namespace. This lets a user choose whether to initialise the font cache on a `grid.latex()` call. If `initFonts` is `FALSE` or the font list

does not exist, for example after the package is loaded, the font list is initialised. Otherwise, the existing font cache remains. `initFonts` was added as an argument to `grid.latex()` with its default value being equal to the global option `dvir.initFonts`.

In a DVI file, each font definition gives the font a identification number, for example `fontnum=17`. In all the DVI files examined as part of this project, this font identification number is the same when that particular font is used again in another `grid.latex()` call. This number is used as the index of the fonts list where its information is stored.

When the font sweep passes a font definition in the DVI file it checks first whether the index of the font list matching the font number of the new font contains any existing font information:

- If no, then the font information is written to the font list as usual.
- If yes, then it checks if the existing font information is the same as the font information in the DVI file.
  - If yes, do nothing.
  - If no, overwrite the font with the new font information.

The result of this is that across multiple `grid.latex()` calls requiring the same fonts, any future uses of that font are much faster after the font has been used once. Importantly it also has a “fail safe” where if there happens to be a case where the font number was used with a different font in a previous `grid.latex()` call, the font cache is overwritten with the new font so the correct font will be used.

The updated font list is stored in the `dvir` environment to be retrieved the next `grid.latex()` finds a font definition during a font sweep.

The only weakness of this process is if in a *single* DVI file different fonts are defined with the same font number. In this case the second font will be stored in the font cache in that index and so will be used in place of the first font. No instances of this occurring were discovered during this project.

To examine the effect of these changes on code speed we performed profiling as was detailed in the previous section.

For the simple example the time for the font sweep has reduced by 71%, with `grid.latex()` overall taking 45% less time.

Similar results can be seen in for the example in figure 9 - a 76% and 46% decrease in the font sweep and `grid.latex()` respectively.

## 5.1 Profiling environment specifications

The exact results obtained in this and the previous section are specific to the computing environment used. Specific details are provided below. The sampling nature of profiling (intermittent recording of the call stack) will give different results every time it is done.

The profiling results are dependent on the computer setup used and could change depending on the exact computing environment in which the `dvir` package is used.

The profiling results in this report, in this and the previous section, were calculated with the following setup:



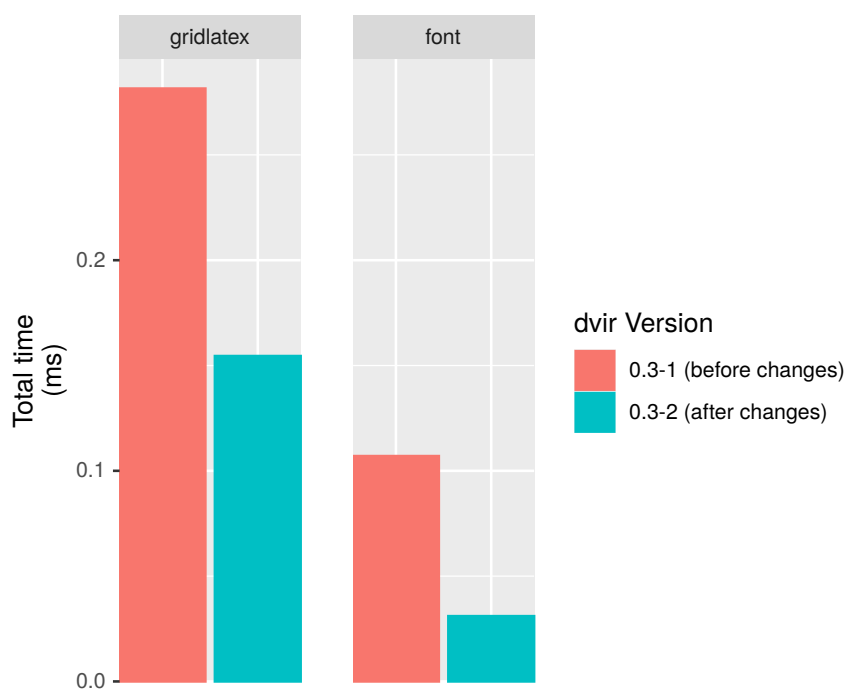


Figure 15: The average time spent in the `gridlatex()` function and font sweep, over 20 runs of the simple example.

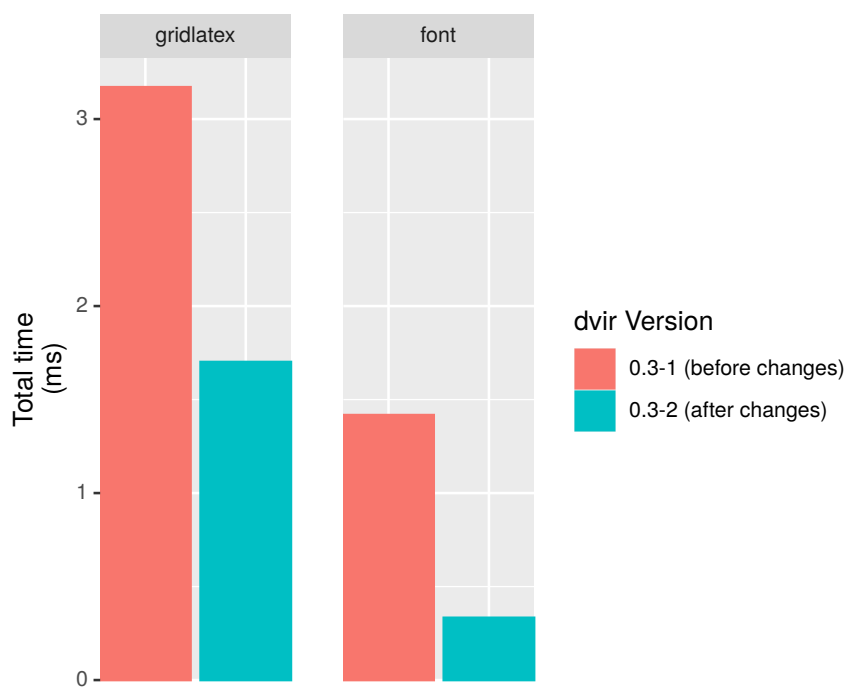


Figure 16: The average time spent in the `gridlatex()` function and font sweep, over 20 runs of the complicated example

- A virtual machine via Oracle VM Virtualbox
- Virtual machine running Ubuntu 18.04.5 LTS
- R version 3.4.4
- `dvir` package versions as described with the profiling results

## 6 Linear gradient fills

### 6.1 TikZ and dvir

TikZ (Tantau 2021) is a T<sub>E</sub>X package that allows drawing of pictures and diagrams in T<sub>E</sub>X documents.

```
\begin{tikzpicture}
\path (0, 1) node[circle,fill=red!40,draw,thick] (x) {$\mu$}
      (3, 0) node[circle,fill=blue!40,draw,thick] (y) {$\dfrac{\mu^2}{2}$};
\draw[->] (x) .. controls (1, 0.5) and (2, 0.5).. (y);
\end{tikzpicture}
```

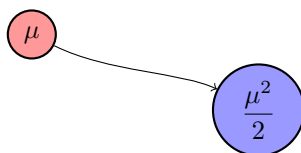


Figure 17: A picture made with TikZ

The original DVI specification only needed to account for text, typesetting and the most basic of rectangles and so was not designed with drawing and graphics in mind. The type of instruction in the DVI file are labelled with an “op code”. Each op code described a type of instruction like defining fonts, setting characters to display and vertical and horizontal cursor movements. There were four op codes however, called *DVI specials*, that can contain almost any form of instruction or values needed, such as text colour, to create a document based on the DVI file, such as Postscript or PDF.

The TikZ package uses these DVI specials to describe shapes, drawings and colours in PGF (portable graphics format) which can be translated to instructions for other viewing formats, like Postscript, PDF or SVG. How the instructions are translated is controlled by a TikZ driver. The dvir package (Murrell 2020a) includes its own TikZ driver to translate the drawing instructions into a form useful to draw the things with R grid graphics [reference Paul dvir TikZ report].

Some TikZ features were not implemented though, notably the ability to have fill colours of shapes as linear or radial gradients or patterns. The primary reason for this is that R did not support these types of fills but the latest R release in May 2021, version 4.1.0, provides support for these fills in the grid package (Murrell 2020b), on which dvir is built.

```
tikzCode <- paste("\\path (0, 1) node[circle,fill=red!40,draw,thick] (x) {$\mu$}",
                 "(3, 0) node[circle,fill=blue!40,draw,thick] (y) {$\dfrac{\mu^2}{2}$};",
                 "\\draw[->] (x) .. controls (1, 0.5) and (2, 0.5).. (y);",
                 sep = "\n")
tikzPreamble <- gsub("\\\\usepackage\\{tikz}",
                    "\\usepackage{tikz}\n\\usepackage{amsmath}",
                    tikzpicturePreamble())
grid.tikzpicture(tikzCode, preamble = tikzPreamble)
```

The use of `grid.tikzpicture()` is demonstrated in figure 18, recreating the diagram from figure 6.1. The alteration to the preamble once again only necessary due to the use of `\dfrac` from the `amsmath` package.

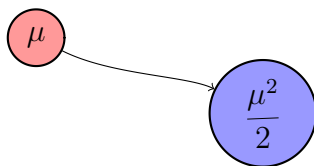


Figure 18: Using `grid.tikzpicture()` to make the earlier diagram

As it is, the TikZ driver simply ignores any gradient or pattern fill information when creating the DVI file for `dvir`.

## 6.2 Implementing TikZ linear gradient fills in `dvir`

The following steps are required to implement these TikZ fills in `dvir`:

1. Add the fill information (like the gradient colours and their locations) to the DVI file created by `dvir`
2. Store this fill information during a parse by `dvir` to read the DVI file
3. Add the fill information when drawing the shape in R

To tackle step 1, we need to update the `dvir` TikZ driver file to include information about the gradient and pattern fills. As the `dvir` TikZ driver file is based on the SVG TikZ driver file, the SVG support for TikZ fills was used as a base to edit to make it specific to `dvir`.

The information we require for the gradient fills from TikZ via the DVI file is as per the arguments for the `grid::linearGradient(...)`, which is used as an argument to `grid::gpar(fill = linearGradient(...))`, which itself is an argument to a `grid` drawing function, for example `grid::grid.rect(..., gp = gpar(fill = linearGradient(...)))`. The most important parts of defining a linear gradient fill is the colours and stops of the gradient fill. The stops of a gradient fill are the locations along the length of a gradient fill where the specified colours are. In between the stops, the gradient between stop colours either side occurs.

The `colours` and `stops` arguments of `linearGradient()` are simply vectors of colours (a character vector of colour names or hexadecimal RGB values) and locations of those colours as a proportion of the distance between the start and end points of the gradient respectively. This obviously guides us as to what information we need to get from TikZ in the DVI file so we can pass it to `dvir`.

Let us consider a simple example, a rectangle with an orange to green linear gradient fill, like that in figure 6.2.

The following is an extract of the DVI file when the rectangle above is generated using the SVG DVI driver included with the common TeX distributions, `pgfsys-dvisvgm.def`. It has been edited slightly for readability by adding line breaks and removing the line break character string `{?nl}`.

```
xxx1          k=67
              x=dvisvgm:raw <g transform="matrix(1,0,0,1,56.90549,28.45274)">
```

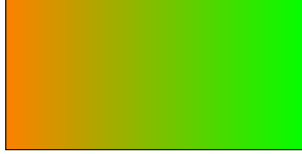


Figure 19: A rectangle with a linear gradient fill using TikZ

```
xxx1      k=67
           x=dvisvgm:raw <g transform="matrix(2.26802,0,0,1.134,0.0,0.0)">
xxx1      k=66
           x=dvisvgm:raw <g transform="matrix(0.0,1.0,-1.0,0.0,0.0,0.0)">
xxx4      k=425
           x=dvisvgm:raw <linearGradient id="pgfsh2" gradientTransform="rotate(90)">
                           <stop offset=" 0.0" stop-color=" rgb(0.0%,100.0%,0.0%) ">/>
                           <stop offset=" 0.25" stop-color=" rgb(0.0%,100.0%,0.0%) ">/>
                           <stop offset=" 0.5" stop-color=" rgb(50.0%,75.0%,0.0%) ">/>
                           <stop offset=" 0.75" stop-color=" rgb(100.0%,50.0%,0.0%) ">/>
                           <stop offset=" 1.0" stop-color=" rgb(100.0%,50.0%,0.0%) ">/>
                           </linearGradient>

xxx1      k=57
           x=dvisvgm:raw <g transform="translate(-50.1875,-50.1875)">
xxx1      k=97
           x=dvisvgm:raw <rect width="100.375" height="100.375"
                           style="fill:url(#pgfsh2); stroke:none"/>
```

We can see from this that the linear gradient definition with stops and colours is defined within a `<linearGradient>` element and given an `id` attribute. In the `<rect>` element a CSS style definition sets the fill of the rectangle by referring to the `id` of the previously defined definition. In the linear gradient definition there are colours defined as RGB values and their respective stops so now we need to get the `dvir` driver file to extract the same information in a “R-friendly” form. There are several  $\text{\TeX}$  macros that were defined to do this. These are based on the `pgfsys-common-svg.def` and `pgfsys-dvisgm.def` SVG drivers that come with most  $\text{\TeX}$  distributions.

A “wrapper” macro of what to do when a gradient fill is requested. Within this, the definition of the fill is created and sent to the DVI file, followed by a rectangle with a fill specified by that definition. For clarity, a line stating when the gradient fill is defined and then again when it is used has been added to the DVI file but these can be removed.

```
\def\pgfsys@shadinginsidepgfpicture#1{%
  #1%
  \pgfsysprotocol@literal{SHADING BEING DEFINED:
                        ShadDefID = \the\pgf@sys@dvir@objectcount}%
  \pgf@sys@dvir@sh@defs%
  \pgf@process{\pgf@sys@dvir@pos}%
  \pgf@xa=-.5\pgf@x%
  \pgf@ya=-.5\pgf@y%
  \pgfsysprotocol@literal{
    <g transform="translate(\pgf@sys@tonumber{\pgf@xa},\pgf@sys@tonumber{\pgf@ya})">%
    \pgfsysprotocol@literal{SHADING BEING USED: ShadDefID = \the\pgf@sys@dvir@objectcount}
    \pgf@sys@dvir@sh%
  }
}
```

In basic cases, a horizontal linear gradient is defined as a vertical gradient with a 90 degree rotation which is why this is called “vert” shading, as it is in the SCG driver file. The definition and use of the gradient specified above are collated here. The stop positions (proportion along the length of the gradient for which a colour specified) and their respective colours are collated and the literal text to build the gradient definition and rectangle using that definition. The biggest difference from the SVG driver was that R needs a vector of stops and a separate vector of colours as arguments to `linearGradient()`. SVG specifies the position and colour of each stop together.

```
\def\pgfsys@vertshading#1#2#3{%
  {%
    \pgf@parsefunc{#3}%
    \global\advance\pgf@sys@dvir@objectcount by1\relax%
    \pgf@sys@dvir@shading@stop%
    \pgf@sys@dvir@shading@stopcolours%
    \expandafter\xdef\csname @pgfshading#1!\endcsname{%
      \def\noexpand\pgf@sys@dvir@sh@defs{
        \noexpand\pgfsysprotocol@literal{\pgf@sys@dvir@thestops}}%
      \def\noexpand\pgf@sys@dvir@sh{\noexpand\pgfsysprotocol@literal{<rect
        width="\pgf@sys@tonumber{\pgf@y}"
        height="\pgf@sys@tonumber{\pgf@x}"
        style="fill:url(\noexpand\#pgfsh\the\pgf@sys@dvir@objectcount);
        stroke:none"/>\noexpand\pgfsys@dvir@newline}}%
      \def\noexpand\pgf@sys@dvir@pos{\noexpand\pgfpoint{\the\pgf@y}{\the\pgf@x}}%
    }%
  }%
}
```

This macro allows us to iteratively add stop positions or colours to the ones we have already gathered.

```
\let\pgf@sys@dvir@thestops=\pgfutil@empty
\def\pgf@sys@dvir@addtostops#1{%
  \edef\pgf@temp{#1}%
  \expandafter\expandafter\expandafter\def
  \expandafter\expandafter\expandafter\pgf@sys@dvir@thestops
  \expandafter\expandafter\expandafter{
    \expandafter\pgf@sys@dvir@thestops\expandafter\space\pgf@temp}%
}
```

The following macros process all the stop locations, collating them into an R friendly vector suitable to parse to `linearGradient()`

```
\def\pgf@sys@dvir@shading@stop{%
  % Step 1: Compute 1/\pgf@sys@shading@end@pos
  \pgf@x=\pgf@sys@shading@end@pos\relax%
  \c@pgf@counta=\pgf@x\relax%
  \divide\c@pgf@counta by4096\relax%
  % Step 2: Insert stops locations
  \pgf@sys@dvir@addtostops{stops={}}%
  \expandafter\pgf@sys@dvir@shading@dostoplocations\pgf@sys@shading@ranges%
  % dummy for end:
  {{\pgf@sys@shading@end@pos}{\pgf@sys@shading@end@pos}}%
  \pgf@sys@dvir@addtostops{}}%
}
```

```
\def\pgf@sys@dvir@shading@dostoplocations#1{%
```

```

\edef\pgf@test{#1}%
\ifx\pgf@test\pgfutil@empty%
\else%
  \expandafter\pgf@sys@dvir@shading@dostoplocation\pgf@test%
  \expandafter\pgf@sys@dvir@shading@dostoplocations
\fi%
}

\def\pgf@sys@dvir@shading@dostoplocation#1#2#3#4{%
  % #1 start pos
  % #2 end pos
  % #3 start rgb
  % #4 end rgb
  \pgf@x=#1%
  \pgf@x=16\pgf@x%
  \divide\pgf@x by \c@pgf@counta\relax%
  \expandafter\pgf@sys@dvir@addtostops{\pgf@sys@tonumber\pgf@x}%
}

```

Similar to the above, these collate all the colours of the stops into an R friendly vector.

```

\def\pgf@sys@dvir@shading@stopcolours{%
  % Step 1: Compute 1/\pgf@sys@shading@end@pos
  \pgf@x=\pgf@sys@shading@end@pos\relax%
  \c@pgf@counta=\pgf@x\relax%
  \divide\c@pgf@counta by4096\relax%
  % Step 2: Insert stops RGB colours
  \pgf@sys@dvir@addtostops{, colours={}%
  \expandafter\pgf@sys@dvir@shading@dostopcolours\pgf@sys@shading@ranges%
  % dummy for end:
  {\pgf@sys@shading@end@rgb}{\pgf@sys@shading@end@rgb}{\pgf@sys@shading@end@rgb}}%
  \pgf@sys@dvir@addtostops{)}%
}

```

```

\def\pgf@sys@dvir@shading@dostopcolours#1{%
  \edef\pgf@test{#1}%
  \ifx\pgf@test\pgfutil@empty%
  \else%
    \expandafter\pgf@sys@dvir@shading@dostopcolour\pgf@test%
    \expandafter\pgf@sys@dvir@shading@dostopcolours%
  \fi%
}

```

```

\def\pgf@sys@dvir@shading@dostopcolour#1#2#3#4{%
  % #1 start pos
  % #2 end pos
  % #3 start rgb
  % #4 end rgb
  \expandafter\pgf@sys@dvir@shading@dorgb#3%
}

```

This is a helper function to return formatted RGB values.

```

\def\pgf@sys@dvir@shading@dorgb#1#2#3{%
  \pgf@sys@dvir@color@rgb#1,#2,#3\relax%
  \pgf@sys@dvir@addtostops{\pgf@sys@dvir@prepared}%
}

```

```
}
```

A counter is defined in order to give each gradient definition unique identifier.

```
\newcount\pgf@sys@dvir@objectcount
```

The result of these changes mean that the linear gradient definition is specified in the DVI file in a form usable by R, sans some commas.

```
xxx1      k=118
          x=dvir:: stops=( 0.0 0.25 0.5 0.75 1.0 ) ,
                    colours=( rgb(0,1,0) rgb(0,1,0) rgb(0.5,0.75,0) rgb(1,0.5,0)
                               rgb(1,0.5,0) )
```

Compare this with the linear gradient definition from earlier:

```
xxx4      k=425
          x=dvisvgm:raw <linearGradient id="pgfsh2" gradientTransform="rotate(90)">
                        <stop offset=" 0.0" stop-color=" rgb(0.0%,100.0%,0.0%) "/>
                        <stop offset=" 0.25" stop-color=" rgb(0.0%,100.0%,0.0%) "/>
                        <stop offset=" 0.5" stop-color=" rgb(50.0%,75.0%,0.0%) "/>
                        <stop offset=" 0.75" stop-color=" rgb(100.0%,50.0%,0.0%) "/>
                        <stop offset=" 1.0" stop-color=" rgb(100.0%,50.0%,0.0%) "/>
                        </linearGradient>
```

Unfortunately this was the extent this project could explore implementing TikZ gradient fills in `dvir`. You may notice in both the SVG and `dvir` DVI output that the colour at stops 0 and 0.25 are the same, as is the colour at stops 0.75 and 1. This is related to a larger issue of TikZ using a number of transformations on the “simple” linear gradient definition above which is then clipped to the shape the fill is for. These transformations would require some very detailed work to translate them into a set of instructions to perform the same in R before they are used in `linearGradient()`.

An additional complication is that TikZ will create shapes with these fills by first drawing the shape with a transparent fill and then drawing another shape with the gradient fill clipped to the size of the first shape. R however requires the the fill information as an argument when drawing the shape. In R, any transformations of the gradient, as TikZ does, will need to be done *before* it is parsed to the drawing function.

Radial gradient fills have similar problems with how they are manipulated by TikZ, however the work done so far on linear gradients could be easily replicated for them.

This work is still within step 1 of the workflow in section 6.2. To continue with the implementation, aside from the above obstacles, `dvir` would need to do another sweep of the DVI file, like the font sweep, to achieve step 2. After any transformations or manipulations are made, the gradient definition can be called by a unique identifier to parse the stored fill definitions to the drawing function used as in step 3.



## 7 Text baselines

### 7.1 The problem

Text characters have a baseline, that is, a horizontal line on which the characters naturally sit so all the letters appear to be in line with each other. Some letters, like a lower case *y* or *j*, have a *descender*. A descender is a part of a character that sits below the baseline.

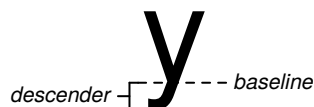


Figure 20: The baseline and descender of the letter *y*

The `grid.text()` function accounts for this baseline so when you bottom-align text at a certain y-value, the descenders will actually fall below the y-value we defined, despite the bottom justification. Unfortunately, `dvir` does not account for text baselines and will do any alignment in relation to bounding box of the text, which, in the case of figure 21, is at the bottom of the descenders.

```
texText <- "{\\LARGE changing to \\LaTeX{}}"
grid.text("An example of ",
  y = 0.1,
  just = c("right", "bottom"),
  gp = gpar(fontsize = 18))
grid.latex(texText, y = 0.1, just = c("left", "bottom"))
grid.lines(y = 0.1, gp = gpar(lwd = 0.5))
```

An example of changing to L<sup>A</sup>T<sub>E</sub>X

Figure 21: Combining `grid.text()` and `grid.latex()`

To fix this, `dvir` needs to obtain or calculate a value for the baseline for any given piece of text to use as an offset for the bounding box alignment when it is rendering the text. From this point on, this offset will be referred to as a baseline value. All of `dvir`'s information comes from the DVI file so it either needs to extract a baseline value from the DVI file itself, or calculate it *from* information in the DVI file. Unfortunately plain DVI files do not state a baseline value, rather they only detail specific placement of each character. As such, some possible methods to obtain a baseline value were explored. These methods are referred to as algorithms from here on due to their heuristic nature.

### 7.2 Implementation

To explore the algorithms detailed below and evaluate their usefulness an R function, `baselines()` has been created. This function can be found in the appendix in the R script file `algorithms.R`. This function takes

several arguments, including the baseline selection algorithm as detailed below, any additional information needed for that particular algorithm, and the `TeX` code as you would use with `grid.latex()`. The output of this function is the baseline value or values. These values are returned as `grid` units as they are distances from the bottom of the bounding box of the text to its baseline.

Once the baselines have been calculated the bounding box of the text can be bottom aligned with the y-value specified but then moved down by the value of the baseline. This means the baseline of the text will be at the specified y-value.

This function has been written to easily allow integration of other algorithms and most of the function could be directly implemented in the `dvir` package, should this baseline algorithm feature be implemented into `dvir` formally.

## 7.3 Potential solutions

Several different algorithms were explored to calculate the baseline for different types of text that could be used with `grid.latex()`. These algorithms are detailed here.

### 7.3.1 alex algorithm

This is a simple algorithm which was determined after inspection of some DVI files. In every DVI file, there is a statement specifying the size of the bounding box of the text.

```
xxx1      k=50
          x=ps::%%HiResBoundingBox: 0 0 14.21944pt 25.85977pt.
```

After this statement there appears to consistently be a downward move equal to the height of the bounding box of text (from the top left of the bounding box to the bottom left), and then a move upward before the first character is drawn. This algorithm takes the cursor location after that upward move to be the baseline. In instances where the entire text has no descenders (i.e. the baseline is the bottom of the bounding box) there will be no upward move before the first character and the baseline value returned is 0.

```
baselineValue <- baselines(tex = "$x - \\mu$", algorithm = "alex")
baselineValue
```

```
## [1] 127431scaledpts
```

For plain text this algorithm works quite well. Unfortunately for many equations, particularly ones with superscripts or subscripts, the first upward move is *not* to where the baseline is. Note in figure 7.3.1 the `alex` algorithm has calculated the baseline of the fifth example to be the bottom of the  $\mu$ . This demonstrates that this algorithm is only practical when the first character's baseline is the one to be aligned, and in the case of the second example, does not serve much purpose at all.

### 7.3.2 dviMoves algorithm

This is an extension of the `alex` algorithm. Rather than only taking the location after the second vertical cursor move, this algorithm keeps track of *all* the up and down moves of the cursor. The motivation behind

testing

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

The equation is  $x + \frac{\mu^2}{2}$

$\frac{\mu^2}{2} + x$  is the equation

Multiline, with  
some line wrap-  
ping

Figure 22: The baselines as calculated using the `alex` algorithm

this is that the upward and downward moves in the DVI file should reflect the cursor moving to the baseline value of the next character to be typeset. Once again we assume that the first downward move after the “HiResBoundingBox” statement is from the top left to the bottom left of the bounding box so this algorithm only returns the upward and downward moves from there. As DVI files have the ability to save the current cursor location, move around a bit, then reset back to the saved location, all up and down moves are tracked from the start of the DVI file.

There are two complications with this method:

- As it returns *all* the vertical positions the cursor moves to there are many possible baseline values returned. Any more than one means we have to decide which of them to choose.
- There are often several up and downward moves in the DVI file between typeset characters so in between the “useful” baseline values there can be some which are duplicates or are not very useful.

To account for these considerations, along with the `dviMoves` algorithm, the `baselines()` function also allows a choice of method to select a *single* baseline out of the many returned by the algorithm.

### 7.3.2.1 `dviMoves` selection method `all`

This selection method will return all the baseline values as determined by the algorithm. This is useful for drawing the text with multiple lines representing all the baseline values calculated from this method.

### 7.3.2.2 `dviMoves` selection method `index`

When this selection method is chosen, another argument to the function, `dviMovesSelection`, is used to specify a numeric index. The baseline value corresponding to that index is returned.

### 7.3.2.3 `dviMoves` selection method `bottomUp`

This is similar to the `index` method but the baseline values are first ordered from smallest to largest, before using the `dviMovesSelection` argument to select the index of the baseline value to return.

### 7.3.2.4 dviMoves selection method nextChars

This method will return the first baseline value just after a specified character in the argument `dviMovesSelection`. Characters are specified by a number, entered as a character string. This method is limited for several reasons:

- It cannot return a baseline value for any instance of a character after the first instance of that character
- If multiple cursor moves are made before a character is drawn, the earlier moves are still recorded but with an empty character label
- Some characters are hard to type on a “normal” keyboard, for example  $\mu$
- The DVI file does not actually contain the character, but rather the numeric index of it in the particular font. This is why a number has to be used to select which character it is.

Figure 23: Baselines as calculated using the `dviMoves` algorithm

This algorithm performs very well. In figure 7.3.2.4 nearly every part of all examples has a baseline value associated with it, including the superscripts of math equations and every line of the multiline text. This means alignment would be possible with these parts of the examples.

### 7.3.3 preview algorithm

This algorithm uses the `preview` package (Kastrup 2017) in  $\text{\LaTeX}$ . Giesekeing (2017) describes the use of the algorithm for `dvisvgm`, and it has been implemented here as it has in `matplotlib.texmanager` (Hunter 2007).

When this algorithm is selected, the following code is added to the header of the DVI file:

```
\usepackage[active,showbox,tightpage]{preview}
\def\showbox#1%
{\immediate\write16{MatplotlibBox:(\the\ht#1+\the\dp#1)x\the\wd#1}}
```

This results in the following line being printed in the log file.

```
MatplotlibBox:(8.04175pt+3.00005pt)x62.81718pt
```

The baseline value in this case is the value just after the `+` and can be obtained by searching the log file for this line starting with `MatplotlibBox:` and returning the value just after the `+`.

testing

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

The equation is  $x + \frac{\mu^2}{2}$

$\frac{\mu^2}{2} + x$  is the equation

Multiline, with  
some line wrap-  
ping

Figure 24: Baselines as calculated using the `preview` algorithm

This algorithm also performs very well. In all examples in figure 7.3.3 the natural baseline of the text has been identified and so this algorithm would be suitable in most use cases. For the multiline text, the second line of text has been identified as having “the” baseline.

#### 7.3.4 `dvipng` algorithm

The `dvipng` program (Larsson 2020) turns DVI files into PNG images. An option of `dvipng` is `--depth` which returns the baseline value in pixels. [reference dvipng package - maybe where you egt it from linux?]

The system call `dvipng --depth test.dvi` returns `depth=4` within its output so after recording the output, a simple search for `depth=` will find the baseline value.

testing

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

$$\sum_{n=1}^{\infty} 2^{-n} = 1$$

The equation is  $x + \frac{\mu^2}{2}$

$\frac{\mu^2}{2} + x$  is the equation

Multiline, with  
some line wrap-  
ping

Figure 25: Baselines as calculated using the `dvipng` algorithm

It may not be obvious in printed form in figure 7.3.4 but the only example with which the `dvipng` algorithm has selected a “good” baseline value is one of the equations. The other examples have baseline values which are at least slightly off. This is likely a side effect of this algorithm returning the baseline value in (whole) pixels which does not lend itself well to this detailed application.

## 7.4 Discussion of these algorithms

Of the algorithms considered, the `dviMoves` algorithm performed best. While these algorithms (except `dvipng`) perform well for some or most of the examples, the `dviMoves` algorithm performs well for *all* the examples. Notably, it gives the option to align the baseline of *any* line of multiline text or with almost any character in a mathematical equation, whether it be of a different size, part of a fraction, or a superscript or subscript.

The difficulty with the algorithm is how to choose a *single* baseline value from all the ones calculated. It is possible to manually check them all the baseline values to find the right one but an automated selection method would be desirable. As the `preview` algorithm calculated baseline values for all examples except the multiline text, the algorithms would work well together - an implementation of this functionality in `dvi` could calculate the baseline values with both the `dviMoves` and `preview` algorithms with the default selection being the baseline value from `dviMoves` that is closest to the baseline value calculated by the `preview` algorithm. This could be overridden to select another baseline value calculated by `dviMoves`.

## 8 Discussion

$\text{\TeX}$  and its extensions have more functionality than could realistically be added to R but by targeting the most useful features of  $\text{\TeX}$ , as `dvir` did originally and as has been continued in this project, many use cases are accommodated. The changes discussed in this report have made the `dvir` package better especially for displaying text and equations, graphics with many `grid.latex()` calls, or even when developing graphics with `grid.latex()` which requires rerunning code with small tweaks to get the perfect graphic.

- talk about how text baselines is almost there....

## 9 References

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## 10 Appendix

Files related to this project can be found on GitHub, via the link in the Executive Summary.