What's in a Proof?

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An Anecdote



The Reason

Theorem a: 2 + 2 = 4.

The Reason

```
Theorem a: 2 + 2 = 4.
```

```
Proof.
trivial.
Qed.
```

Coa



- An interactive theorem prover started in 1984
- Provides a formal language and environment for mathematical definitions, algorithms, theorems, and machine-checked proofs
- Language based on a derivative of the calculus of constructions (CoC)

Example

```
Theorem two_and_two_make_four: 2 + 2 = 4.
Proof.
  trivial.
```

Qed.

Coq



- An interactive theorem prover started in 1984
- Provides a formal language and environment for mathematical definitions, algorithms, theorems, and machine-checked proofs
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Example

```
Theorem two_and_two_make_four: 2 + 2 = 4.
Proof.
   auto 1.
```

Qed.

Proof Automation

Rough Algorithm

```
auto n =
  if no more subgoals then
     success
  if n == 0 then
     failure
  foreach term in | hypotheses \cup hints |:
     try
        apply term.
       foreach subgoal generated:
          auto (n - 1) on that subgoal
```