GLOBAL VALUE NUMBERING IN FACTOR

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To Lindsay—he is my rock

Abstract

Compilers translate code in one programming language into semantically equivalent code in another language—canonically from a high-level language to low-level machine primitives. Generally, the further removed a language's abstractions get from those of a computer, the harder it gets to compile code into an efficient representation. What isn't redundant in the source language may map to repetitive target instructions that waste time recomputing results. To combat this, compilers try to optimize away redundancies by looking for values that are provably equivalent when the program is run.

This thesis explores the theory and implementation of a particularly aggressive analysis called global value numbering in a particularly high-level language called Factor. Factor is a stack-based, dynamically-typed, object-oriented language born in late 2003. A baby among languages (now at version 0.94), its compiler craves all the optimizations it can get. By altering the existing local value numbering pass, redundancies can be identified and eliminated across entire programs, rather than isolated regions of code. This induces speedups as high as 45% across the majority of benchmarks. The results from these comparatively simple changes hold much promise for future improvements in making Factor programs more efficient.

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1 Introduction

Compilers translate programs written in a source language (e.g., Java) into semantically equivalent programs in some target language (e.g., assembly code). They let us make our source language arbitrarily abstract so we can write programs in ways that humans understand while letting the computer execute programs in ways that machines understand. In a perfect world, such translation would be straightforward. Reality, however, is unforgiving. Straightforward compilation results in clunky target code that performs a lot of redundant computations. To produce efficient code, we must rely on less-than-straightforward methods. Typical compilers go through a stage of optimization, whereby a number of semantics-preserving transformations are applied to an intermediate representation of the source code. These then (hopefully) produce a more efficient version of said representation. Optimizers tend to work in phases, applying specific transformations during any given phase.

Global value numbering (GVN) is such a phase performed by many highly-optimizing compilers. Its roots run deep through both the theoretical and the practical. Using the results of this analysis, the compiler can identify expressions in the source code that produce the same value—not just by lexical comparison (i.e., comparing variable names), but by proving equivalences between what's actually computed at runtime. These expressions can then be simplified by further algorithms for redundancy elimination. This is the very essence of most compiler optimizations: avoid redundant computation, giving us code that runs as quickly as possible while still following what the programmer originally wrote.

High-level, dynamic languages tend to suffer from efficiency issues. They're often interpreted rather than compiled, and perform no heavy optimization of the source code. However, the Factor language (http://factorcode.org) fills an intriguing design niche, as it's very high-level yet still fully compiled. It's still young, though, so its compiler craves all the improvements it can get. In particular, while the current Factor version (as of this writing, 0.94) has a *local* value numbering analysis, it is inferior to GVN in several significant ways.

In this thesis, we explore the implementation and use of GVN in improving the strength

of optimizations in Factor. Because Factor is a young and relatively unknown language, Chapter 2 provides a short tutorial, laying a foundation for understanding the changes. Chapter 3 describes the overall architecture of the Factor compiler, highlighting where the exact contributions of this thesis fit in. Finally, Chapter 4 goes into detail about the existing and new value numbering passes, closing with a look at the results achieved and directions for future work.

In the unlikely event that you want to cite this thesis, you may use the following BibT_FX entry:

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2 Language Primer

Factor is a rather young language created by Slava Pestov in September 2003 [Factor 2010]. Its first incarnation was an embedded scripting language for a game that targeted the Java Virtual Machine (JVM). As such, its feature set was minimal. Factor has since evolved into a general-purpose programming language, gaining new features and redesigning old ones as necessary for larger programs. Today's implementation sports an extensive standard library and has moved away from the JVM in favor of native code generation. In this chapter, we cover the basic syntax and semantics of Factor for those unfamiliar with the language. This should be just enough to understand the later material in this thesis. More thorough documentation can be found via Factor's website, http://factorcode.org.

2.1 Stack-Based Languages

Like Reverse Polish Notation (RPN) calculators, Factor's evaluation model uses a global stack upon which operands are pushed before operators are called. This naturally facilitates postfix notation, in which operators are written after their operands. For example, instead of 1 + 2, we write 1 2 +. Figure 1 on the following page shows how 1 2 + works conceptually:

- 1 is pushed onto the stack
- 2 is pushed onto the stack
- + is called, so two values are popped from the stack, added, and the result (3) is pushed back onto the stack

Other stack-based programming languages include Forth [American National Standards Institute and Computer and Business Equipment Manufacturers Association 1994], Cat [Diggins 2007], and PostScript [Adobe Systems Incorporated 1999].

The strength of this model is its simplicity. Evaluation essentially goes left to right: literals (like 1 and 2) are pushed onto the stack, and operators (like +) perform some computation using values currently on the stack. This "flatness" makes parsing easier,



Figure 1: Visualizing stack-based calculation

since we don't need complex grammars with subtle ambiguities and precedence issues. Rather, we basically just scan left-to-right for tokens separated by whitespace. In the Forth tradition, functions are called *words* since they're made up of any contiguous non-whitespace characters. This also lends to the term *vocabulary* instead of "module" or "library". In Factor, the parser works as follows:

- If the current character is a double-quote ("), try to parse ahead for a string literal.
- Otherwise, scan ahead for a single token.
 - If the token is the name of a parsing word, that word is invoked with the parser's current state.
 - If the token is the name of an ordinary (i.e., non-parsing) word, that word is added to the parse tree.
 - Otherwise, try to parse the token as a numeric literal.

Parsing words serve as hooks into the parser, letting Factor users extend the syntax dynamically. For instance, instead of having special knowledge of comments built into the parser, the parsing word! scans forward for a newline and discards any characters read (adding nothing to the parse tree).

Similarly, there are parsing words for what might otherwise be hard-coded syntax for data structure literals. Many act as sided delimeters: the parsing word for the left-delimiter will parse ahead until it reaches the right-delimiter, using whatever was read in between to add objects to the data structure. For example, { 1 2 3 } denotes an array of three numbers. Note the deliberate spaces in between the tokens, so that the delimeters are themselves distinct words. In $\{ \sqcup 1 \sqcup 2 \sqcup 3 \sqcup \}$ (with spaces as marked), the parsing word $\{ \}$ parses objects until it reaches $\{ \}$, collecting the results into an array. The $\{ \}$ word would not

Figure 2: Data structure literals in Factor



Figure 3: Quotations

be called if not for that space, whereas $\{1_{\sqcup}2_{\sqcup}3\}$ parses as the word $\{1$, the number 2, and the word 3}—not an array. Further, since the left-delimeter words parse recursively, such literals can be nested, contain comments, etc. Other literals include those in Figure 2.

A particularly important set of parsing words in Factor are the square brackets, [and]. Any code in between such brackets is collected up into a special sequence called a *quotation*. Essentially, it's a snippet of code whose execution is suppressed. The code inside a quotation can then be run with the **call** word. Quotations are like anonymous functions in other languages, but the stack model makes them conceptually simpler, since we don't have to worry about variable binding and the like. Consider a small example like

You can think of call working by "erasing" the brackets around a quotation, so this example behaves just like 1 2 +. Figure 3 shows its evaluation: instead of adding the numbers immediately, + is placed in a quotation, which is pushed to the stack. The quotation is then invoked by call, so + pops and adds the two numbers and pushes the result onto the stack. We'll show how quotations are used in Section 2.5 on page 16.

2.2 Stack Effects

Everything else about Factor follows from the stack-based structure outlined in Section 2.1. Consecutive words transform the stack in discrete steps, thereby shaping a result. In a way, words are functions from stacks to stacks—from "before" to "after"—and whitespace is effectively function composition. Even literals (numbers, strings, arrays, quotations, etc.) can be thought of as functions that take in a stack and return that stack with an extra element pushed onto it.

With this in mind, Factor requires that the number of elements on the stack (the *stack height*) is known at each point of the program in order to ensure consistency. To this end, every word is associated with a *stack effect* declaration using a notation implemented by parsing words. In general, a stack effect declaration has the form

```
( input1 input2 ... -- output1 output2 ... )
```

where the parsing word (scans forward for the special token -- to separate the two sides of the declaration, and then for the) token to end the declaration. The names of the intermediate tokens don't technically matter—only how many of them there are. However, names should be meaningful for clarity's sake. The number of tokens on the left side of the declaration (before the --) indicates the minimum stack height expected before executing the word. Given exactly this number of inputs, the number of tokens on the right side is the stack height after executing the word.

For instance, the stack effect of the + word is (x y -- z), as it pops two numbers off the stack and pushes one number (their sum) onto the stack. This could be written any number of ways, though. (x x -- x), (number1 number2 -- sum), and (m n -- m+n) are all equally valid. Further, while the stack effect (junk x y -- junk z) has the same relative height change, this declaration would be wrong, since it requires at least three inputs but + might legitimately be called on only two.

For the purposes of documentation, of course, the names in stack effects do matter. They correspond to elements of the stack from bottom-to-top. So, the rightmost value



Figure 4: Stack shuffler words and their effects

on either side of the declaration names the top element of the stack. We can see this in Figure 4, which shows the effects of standard stack shuffler words. These words are used for basic data flow in Factor programs. For example, to discard the top element of the stack, we use the **drop** word, whose effect is simply (x --). To discard the element just below the top of the stack, we use **nip**, whose effect is (x y -- y). This stack effect indicates that there are at least two elements on the stack before **nip** is called: the top element is y, and the next element is x. After calling the word, x is removed, leaving the original y still on top of the stack. Other shuffler words that remove data from the stack are **2drop** with the effect (x y -- y), and **2nip** with the effect (x y -- y).

The next stack shufflers duplicate data. **dup** copies the top element of the stack, as indicated by its effect (x -- x x). **over** has the effect (x y -- x y x), which tells us that it expects at least two inputs: the top of the stack is y, and the next object is x. x is copied and pushed on top of the two original elements, sandwiching y between two xs. Other shuffler words that duplicate data on the stack are **2dup** with the effect (x y -- x y x y), **3dup** with the effect (x y z -- x y z x y z), **2over** with the effect (x y z -- x y z x y z), and **pick** with the effect (x y z -- x y z x z).

True to the name swap, the final shuffler in Figure 4 permutes the top two elements of the stack, reversing their order. The stack effect (x y -- y x) indicates as much. The

left side denotes that two inputs are on the stack (the top is y, the next is x), and the right side shows the outputs are swapped (the top element is x and the next is y). Factor has other words that permute elements deeper into the stack. However, their use is discouraged because it's harder for the programmer to mentally keep track of more than a couple items on the stack. We'll see how more complex data flow patterns are handled in Section 2.5 on page 16.

2.3 Definitions

```
: hello-world ( -- )
"Hello, world!" print;
```

Figure 5: Hello World in Factor

Using the basic syntax of stack effect declarations described in Section 2.2, we can now understand how to define words. Most words are defined with the parsing word:, which scans for a name, a stack effect, and then any words up until the; token, which together become the body of the definition. Thus, the classic example in Figure 5 defines a word named hello-world which expects no inputs and pushes no outputs onto the stack. When called, this word will display the canonical greeting on standard output using the print word.

A slightly more interesting example is the norm word in Figure 6. This squares each of the top two numbers on the stack, adds them, then takes the square root of the sum. Figure 7 on the following page shows this in action. By defining a word to perform these steps, we can replace virtually any instance of dup * swap dup * + sqrt in a program simply with norm. This is a deceptively important point. Data flow is made explicit via

```
: norm ( x y -- norm )
dup * swap dup * + sqrt ;
```

Figure 6: The Euclidean norm, $\sqrt{x^2 + y^2}$

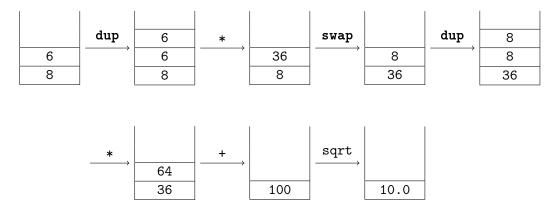


Figure 7: norm example

Figure 8: norm refactored

stack manipulation rather than being hidden in variable assignments, so repetitive patterns become painfully evident. This makes identifying, extracting, and replacing redundant code easy. Often, you can just copy a repetitive sequence of words into its own definition verbatim. This emphasis on "factoring" your code is what gives Factor its name.

As a simple case in point, we see the subexpression **dup** * appears twice in the definition of **norm** in Figure 6 on the previous page. We can easily factor that out into a new word and substitute it for the old expressions, as in Figure 8. By contrast, programs in more traditional languages are laden with variables and syntactic noise that require more work to refactor: identifying free variables, pulling out the right functions without causing finicky syntax errors, calling a new function with the right variables, etc. Though Factor's stackbased paradigm is atypical, it is part of a design philosophy that aims to facilitate readable code focusing on short, reusable definitions.

Be that as it may, every once in awhile stack code gets too complicated to do away with more traditional notation. For these cases, Factor has a vocabulary called locals, which

```
:: norm ( x y -- norm )
    x x * :> x^2
    y y * :> y^2
    x^2 y^2 + sqrt;
```

Figure 9: norm with local variables

introduces syntax for defining words that use named lexical variables. Defining words with :: instead of : turns the stack effect declaration into a full-fledged parameter list. The inputs are assigned to their corresponding names in the effect, which are used throughout the body in lieu of stack manipulation. The outputs just mean the same thing as before (i.e., the right side of the effect doesn't declare any variables like the left does). We can also assign local variables in the body of the word by using the syntax :> destination, which assigns destination to the value on the top of the stack. Figure 9 shows a version of norm that uses these features, though they aren't really necessary here. Interestingly, locals is implemented entirely in high-level Factor code, using parsing words to convert the syntax into equivalent stack manipulations.

2.4 Object Orientation

You may have noticed that the examples in Section 2.3 did not use type declarations. While Factor is dynamically typed for the sake of simplicity, it does not do away with types altogether. In fact, Factor is object-oriented. However, its object system doesn't rely on classes possessing particular methods, as is common. Instead, it uses *generic words* with methods implemented for particular classes. To start, though, we must see how classes are defined.

Tuples

The central data type of Factor's object system is called a *tuple*, which is a class composed of named *slots*—like instance variables in other languages. Tuples are defined with the **TUPLE:** parsing word as shown in Figure 10 on the following page. A class name is

```
TUPLE: class
    slot-spec1 slot-spec2 slot-spec3 ...;

TUPLE: subclass < superclass
    slot-spec1 slot-spec2 slot-spec3 ...;</pre>
```

Figure 10: Basic tuple definition syntax

specified first; if it is followed by the < token and a superclass name, the tuple inherits the slots of the superclass. If no superclass is specified, the default is the **tuple** class. Any number of slot specifiers follow, and the definition is terminated by the ; token.

Tuple definitions automatically generate several different words, most of which depend on how slots are specified. There are various ways to specify slots, but we use only two basic forms in later code examples. We can see both in the first tuple of Figure 11 on the next page, which defines an object to represent regular expressions. The first three slots have the form { name read-only }, which specifies a slot named name that can't be modified once initialized, akin to a final variable in Java. The next two specifiers are simpler, being just the names of the slots. Such slots can be modified freely. The following words are automatically defined for the first tuple:

- The regexp class word acts like a literal representing the class. This gets used for instantiation and method definitions, which we'll see later.
- The regexp? class predicate is a word with the stack effect (object --?). That is, it returns a boolean (either t or f, conventionally written in stack effects as a single question mark) indicating whether the top of the stack is an instance of the regexp class. This is like a class-specific variant of Java's instanceof.
- Each slot has an associated *reader* word with the stack effect (object -- value). These are analogous to "getter" methods in other languages. Each one is named after the slot whose value is extracted, so this example defines raw>>, parse-tree>>, options>>, dfa>>, and next-match>>.

Figure 11: Sample tuple definitions from Factor's regexp vocabulary

- Similarly, any slot that is not marked read-only has a corresponding writer word
 with the stack effect (value object --). These destructively write the value into
 the eponymous slot of the object. Here, only two are defined, named dfa<< and
 next-match<<.
- Extra setter words are defined in terms of writers. These will have the stack effect (object value -- object'), leaving the modified instance on top of the stack. The first tuple in Figure 11 defines >>dfa and >>next-match, which are equivalent to over dfa<< and over next-match<<, respectively. The shuffler duplicates object and pushes it to the top of the stack. More accurately, it duplicates a reference to object, as Factor's data stack is actually a stack of pointers. That way, changes to the new top of the stack with dfa<< or next-match<< will be reflected in the original object, which is left over at the end.
- Changer words are also created with the stack effect (object quot -- object').

 Here, change-dfa and change-next-match are defined. The quotation is called on the slot's current value in object. The result of calling the quotation is then stored in the slot. For instance, incrementing an integer slot named foo could be done with [1+] change-foo.

The second tuple in Figure 11 also defines a class word and predicate. Since it inherits from regexp, reverse-regexp gets the same five slots. If we had any other slot specifiers in the definition, it would have those in addition to the slots of its parent class. The reader, writer, setter, and changer methods will work on instances of reverse-regexp, since

```
TUPLE: color ;

: <color> ( -- color )
    color new ;

TUPLE: rgb < color red green blue ;

: <rgb> ( r g b -- rgb )
    rgb boa ;
```

Figure 12: Tuple constructors

inheritance establishes an "is-a" relationship from subclass to superclass—any instance of reverse-regexp is also an instance of regexp, though the reverse is not necessarily true. That is, regexp? will return t on instances of reverse-regexp, but reverse-regexp? will only return t on instances of regexp that are also reverse-regexps. By viewing a class as the set of all objects that respond positively to the class predicate, we may partially order classes with the subset relationship. This fact will be important later.

To construct an instance of a tuple, we can use either **new** or **boa**. **new** will not initialize any of the slots to a particular input value—all slots will default to Factor's canonical false value, **f**. For example, **new** is used in Figure 12 to define <color> (by convention, the constructor for foo is named <foo>). First, we push the class color, then just call **new**, leaving a new instance on the stack. Since this particular tuple has no slots, using **new** makes sense. We might also use it to initialize a class, then use setter words to only assign a particular subset of slots' values (as long as the slots aren't read-only).

However, we often want to initialize a tuple with values for each of its slots. For this, we have **boa**, which works similarly to **new**. This is used in the definition of **rgb** in Figure 12. The difference here is the additional inputs on the stack—one for each slot, in the order they're declared. That is, we're constructing the tuple **by order** of arguments, giving us the fun pun "**boa** constructor". So, 1 2 3 **rgb** will construct an **rgb** instance with the **red** slot set to 1, the **green** slot set to 2, and the **blue** slot set to 3.

Generics and Methods

Unlike more common object systems, we do not define individual methods that "belong" to particular tuples. In Factor, for a given generic word you define a method that specializes on a class. When the generic word is called on an object, it selects the method most specific to the object's class. This is determined by the aforementioned partial ordering of classes by their inheritance relationships.

Generic words are declared with the syntax

```
GENERIC: word-name ( stack -- effect )
```

Words defined this way will then dispatch on the class of the top element of the stack (necessarily the rightmost input in the stack effect). To define a new method with which to control this dispatch, we use the syntax

M: class word-name definition...;

Factor's sets vocabulary gives us an accessible example of a generic word. set is a mixin class, defined by the MIXIN: parsing word. That is, the set class is a union of other classes, and users may extend the members of this union with the INSTANCE: word. We can this in Figure 13 on the following page, which shows the standard members of the set mixin. Note that the USING: form specifies vocabularies being used (like Java's import) and IN: specifies the vocabulary in which the definitions appear (like Java's package). We can see here that instances of the sequence, hash-set, and bit-set classes are all instances of set, so will respond t to the predicate set?. Similarly, sequence is a mixin class with many more members, including array, vector, and string.

Figure 14 on the next page shows the cardinality generic from Factor's sets vocabulary, along with its methods. This generic word takes a set instance from the top of the stack and pushes the number of elements it contains. For instance, if the top element is a bit-set, we extract its table slot and invoke another word, bit-count, on that. But if the top element is **f** (the canonical false/empty value), we know the cardinality is 0.

```
USING: bit-sets hash-sets sequences;
IN: sets

MIXIN: set
INSTANCE: sequence set
INSTANCE: hash-set set
INSTANCE: bit-set set
```

Figure 13: Set instances

```
IN: sets
GENERIC: cardinality ( set -- n )

USING: accessors bit-sets math.bitwise sets;
M: bit-set cardinality table>> bit-count;

USING: kernel sets;
M: f cardinality drop 0;

USING: accessors assocs hash-sets sets;
M: hash-set cardinality table>> assoc-size;

USING: sequences sets;
M: sequence cardinality length;

USING: sequences sets;
M: set cardinality members length;
```

Figure 14: Set cardinality using Factor's object system

For any sequence, we may offshore the work to a different generic, length, defined in the sequences vocabulary. The final method gives a default behavior for any other set instance, which simply uses members to obtain an equivalent sequence of set members, then calls length.

We can see how the class ordering is used when cardinality selects the proper method for the object being dispatched upon. For instance, while no explicit method for array is defined, any instance of array is also an instance of sequence. In turn, every instance of sequence is also an instance of set. We have methods that dispatch on both set and sequence, but the latter is more specific, so that is the method invoked on an array. If

we define our own class, foo, and declare it as an instance of set but not as an instance of sequence, then the set method of cardinality will be invoked. Sometimes resolving the precedence gets more complicated, but these edge-cases are beyond the scope of our discussion.

2.5 Combinators

Quotations, introduced in Section 2.1, form the basis of both control flow and data flow in Factor. Not only are they the equivalent of anonymous functions, but the stack model also makes them syntactically lightweight enough to serve as blocks akin to the code between curly braces in C or Java. Higher-order words that make use of quotations on the stack are called *combinators*. It's simple to express familiar conditional logic and loops using combinators, as we'll show first. In the presence of explicit data flow via stack operations, even more patterns arise that can be abstracted away. The last half of this section explores how we can use combinators to express otherwise convoluted stack-shuffling logic more succinctly.

Control Flow

The most primitive form of control flow in typical programming languages is, of course, the if statement, and the same holds true for Factor. The only difference is that Factor's if isn't syntactically significant—it's just another word, albeit implemented as a primitive. For the moment, it will do to think of if as having the stack effect (? true false --). The third element from the top of the stack is a boolean condition, and it's followed by two quotations. The first quotation (true) is called if the condition is true, and the second quotation (false) is called if the condition is false. Specifically, f is a special object in Factor for falsity. It is a singleton object—the sole instance of the f class—and is the only false value in the entire language. Any other object is necessarily boolean true. For a canonical boolean, there is the t object, but its truth value exists only because it is not f.

```
5 even? [ "even" print ] [ "odd" print ] if
{ } empty? [ "empty" print ] [ "full" print ] if
100 [ "isn't f" print ] [ "is f" print ] if
```

Figure 15: Conditional evaluation in Factor

Basic **if** use is shown in Figure 15. The first example will print "odd", the second "empty", and the third "isn't f". All of them leave nothing on the stack.

However, the simplified stack effect for ${\tt if}$ is quite restrictive. Because the effect (? true false --) has no extra inputs and no outputs at all, it intuitively means that the true and false quotations both have the effect (--). We'd like to loosen this restriction, but per Section 2.2, Factor must know the stack height after the ${\tt if}$ call. We could give ${\tt if}$ the effect (x ? true false -- y) so that the two quotations could each have the stack effect (x -- y). This would work for the example1 word in Figure 16 on the next page, yet it's just as restrictive. For instance, the example2 word would need ${\tt if}$ to have the effect (x y ? true false -- z), since each branch has the effect (x y -- z). Furthermore, the quotations might even have different effects, but still leave the overall stack height balanced. Only one item is left on the stack after a call to example3 regardless, even though the two quotations have different stack effects: + has the effect (x y -- z), while drop has the effect (x --).

In reality, there are infinitely many correct stack effects for **if**. Factor has a special notation for such *row-polymorphic* stack effects. If a token in a stack effect begins with two dots, like ..a or ..b, it is a *row variable*. If either side of a stack effect begins with a row variable, it represents any number of inputs or outputs. Thus, we could give **if** the stack effect

```
( ..a ? true false -- ..b )
```

to indicate that there may be any number of inputs below the condition on the stack, and that any number of outputs will be present after the call to **if**. Note that these numbers

```
: example1 ( x -- 0/x-1 )
    dup even? [ drop 0 ] [ 1 - ] if ;

: example2 ( x y -- x+y/x-y )
    2dup mod 0 = [ + ] [ - ] if ;

: example3 ( x y -- x+y/x )
    dup odd? [ + ] [ drop ] if ;
```

Figure 16: if's stack effect varies

aren't necessarily equal, which is why we use distinct row variables (..a and ..b) in this case. However, this still isn't quite enough to capture the stack height requirements. It doesn't communicate that true and false must affect the stack in the same ways, which has remained tacit to this point. For this, the notation quot: (stack -- effect) gives quotations a nested stack effect. Using the same names for row variables in both the "inner" and "outer" stack effects will refer to the same number of inputs or outputs. Thus, our final (correct) stack effect for if is

```
( ..a ? true: ( ..a -- ..b ) false: ( ..a -- ..b ) -- ..b )
```

This tells us that the true quotation and the false quotation will each leave the stack at the same height as **if** does overall, and that neither expects any extra inputs.

Though **if** is necessarily a language primitive, other control flow constructs are defined in Factor itself. It's simple to write combinators for iteration and looping as recursive words that invoke quotations. Figure 17 on the following page showcases some common looping patterns. The most basic yet versatile word is **each**. Its stack effect is

```
( ... seq quot: ( ... x -- ... ) -- ... )
```

Each element x of the sequence seq will be passed to quot, which may use any of the underlying stack elements. Here, unlike if, we enforce that quot's output stack height is exactly one less than the input. Otherwise, depending on the number of elements in seq, we might dig arbitrarily deep into the stack or flood it with a varying number of

```
{ "Lorem" "ipsum" "dolor" } [ print ] each

0 { 1 2 3 } [ + ] each

10 iota [ number>string print ] each

3 [ "Ho!" print ] times

[ t ] [ "Infinite loop!" print ] while

[ f ] [ "Executed once!" print ] do while
```

Figure 17: Loops in Factor

values. The first use of **each** in Figure 17 is balanced, as the quotation has the effect (str --) and no additional items were on the stack to begin with (i.e., ... stands in for 0 elements). Essentially, it's equivalent to "Lorem" print "ipsum" print "dolor" print. On the other hand, the quotation in the second example has the stack effect (total n -- total+n). This is still balanced, since there is one additional item below the sequence on the stack (namely 0), and one element is left by the end (the sum of the sequence elements). So, this example is the same as 0 1 + 2 + 3 +.

Any instance of the extensive sequence mixin will work with each, making it very flexible. The third example in Figure 17 shows iota, which is used here to create a *virtual* sequence of integers from 0 to 9 (inclusive). No actual sequence is allocated, merely an object that behaves like a sequence. In Factor, it's common practice to use iota and each in favor of repetitive C-like for loops.

Of course, we sometimes don't need the induction variable in loops. That is, we just want to execute a body of code a certain number of times. For these cases, there's the times combinator, with the stack effect

```
( ... n quot: ( ... -- ... ) -- ... )
```

This is similar to **each**, except that n is a number (so we needn't use **iota**) and the quotation doesn't expect an extra argument (i.e., a sequence element). Therefore, the

```
{ 1 2 3 } [ 1 + ] map
{ 1 2 3 4 5 } [ even? ] filter
{ 1 2 3 } 0 [ + ] reduce
```

Figure 18: Higher-order functions in Factor

example in Figure 17 on the previous page is equivalent to "Ho!" print "Ho!" print "Ho!" print.

Naturally, Factor also has the while combinator, whose stack effect is

```
( ..a pred: ( ..a -- ..b ? ) body: ( ..b -- ..a ) -- ..b )
```

The row variables are a bit messy, but it works as you'd expect: the pred quotation is invoked on each iteration to determine whether body should be called. The do word is a handy modifier for while that simply executes the body of the loop once before leaving while to test the precondition as per usual. Thus, the last example in Figure 17 on the preceding page executes the body once, despite the condition being immediately false.

In the preceding combinators, quotations were used like blocks of code. But really, they're the same as anonymous functions from other languages. As such, Factor borrows classic tools from functional languages, like map and filter, as shown in Figure 18. map is like each, except that the quotation should produce a single output. Each such output is collected up into a new sequence of the same class as the input sequence. Here, the example produces { 2 3 4 }. filter selects only those elements from the sequence for which the quotation returns a true value. Thus, the filter in Figure 18 outputs { 2 4 }. Even reduce is in Factor, also known as a left fold. An initial element is iteratively updated by pushing a value from the sequence and invoking the quotation. In fact, reduce is defined as swapd each, where swapd is a shuffler word with the stack effect (x y z -- y x z). Thus, the example in Figure 18 is the same as 0 { 1 2 3 } [+] each, as in Figure 17 on the preceding page.

These are just some of the control flow combinators defined in Factor. Several variants exist that meld stack shuffling with control flow, or can be used to shorten common patterns such as empty false branches. An entire list is beyond the scope of our discussion, but the ones we've studied should give a solid view of what standard conditional execution, iteration, and looping looks like in a stack-based language.

Data Flow

While avoiding variables makes it easier to refactor code, keeping mental track of the stack can be taxing. If we need to manipulate more than the top few elements of the stack, code gets harder to read and write. Since the flow of data is made explicit via stack shufflers, we actually wind up with redundant patterns of data flow that we otherwise couldn't identify. In Factor, there are several combinators that clean up common stack-shuffling logic, making code easier to understand.

The first combinators we'll look at are **dip** and **keep**. These are used to preserve certain stack elements, do a computation, then restore said elements. For an uncompelling but illustrative example, suppose we have two values on the stack, but we want to increment the second element from the top. without-dip1 in Figure 19 on the next page shows one strategy, where we shuffle the top element away with **swap**, perform the computation, then **swap** the top back to its original place. A cleaner way is to call **dip** on a quotation, which will execute that quotation just under the top of the stack, as in with-dip1. While the stack shuffling in without-dip1 isn't terribly complicated, it doesn't convey our meaning very well. Shuffling the top element out of the way becomes increasingly difficult with more complex computations. In without-dip2, we want to call - on the two elements below the top. For lack of a more robust stack shuffler, we use **swap** followed by **swapd** to rearrange the stack so we can call -, then **swap** it back to the desired order. This is even less clear, plus **swapd** is actually a deprecated word in Factor, since its use starts making code harder to reason about. Alternatively, we could dream up a more complex stack shuffler with exactly the stack effect we wanted in this situation. But this solution doesn't scale: what if we had

```
: without-dip1 ( x y -- x+1 y )
    swap 1 + swap ;
: with-dip1 ( x y -- x+1 y )
    [1 + ] dip;
: without-dip2 ( x y z -- x-y z )
    swap swapd - swap;
: with-dip2 ( x y z -- x-y z )
    [ - ] dip;
: without-keep1 ( x -- x+1 x )
    dup 1 + swap ;
: with-keep1 ( x -- x+1 x )
    [1 + ] keep;
: without-keep2 ( x y -- x-y y )
    swap over - swap ;
: with-keep2 ( x y -- x-y y )
    [ - ] keep ;
```

Figure 19: Preserving combinators

to calculate something that required more inputs or produced more outputs? Clearly, dip provides a cleaner alternative in with-dip2.

keep provides a way to hold onto the top element of the stack, but still use it to perform a computation. In general, [...] keep is equivalent to dup [...] dip. Thus, the current top of the stack remains on top after the use of keep, but the quotation is still invoked with that value. In with-keep1 in Figure 19, we want to increment the top, but stash the result below. Again, this logic isn't terribly complicated, though with-keep1 does away with the shuffling. without-keep2 shows a messier example where a simple dup will not save us, as we're using more than just the top element in the call to -. Rather, three of the four words in the definition are dedicated to rearranging the stack in just the right way, obscuring the call to - that we really want to focus on. On the other hand, with-keep2 places the subtraction word front-and-center in its own quotation, while keep

does the work of retaining the top of the stack.

The next set of combinators apply multiple quotations to a single value. The most general form of these so-called *cleave* combinators is the word **cleave**, which takes an array of quotations as input, and calls each one in turn on the top element of the stack. So,

takes the top element, x, and applies each quotation to it: a is applied to x, then b to x, then c to x. Of course, for only a couple of quotations, wrapping them in an array literal becomes cumbersome. The word bi exists for the two-quotation case, and tri for three quotations. Cleave combinators are often used to extract multiple slots from a tuple. Figure 20 on the next page shows such a case in the with-bi word, which improves upon using just keep in the without-bi word. In general, a series of keeps like

is the same as

which is more readable. We can see this in action in the difference between without-tri and with-tri in Figure 20 on the following page. In cases where we need to apply multiple quotations to a set of values instead of just a single one, there are also the variants 2cleave and 3cleave (and the corresponding 2bi, 2tri, 3bi, and 3tri), which apply the quotations to the top two and three elements of the stack, respectively.

To apply multiple quotations to multiple values, Factor has *spread* combinators. Whereas cleave combinators abstract away repeated instances of **keep**, spread combinators replace nested calls to **dip**. The archetypical combinator, **spread**, takes an array of quotations, like **cleave**. However, instead of applying each one to the top element of the stack, each one corresponds to a separate element of the stack. Thus,

```
TUPLE: coord x y ;

: without-bi ( coord -- norm )
        [ x>> sq ] keep y>> sq + sqrt ;

: with-bi ( coord -- norm )
        [ x>> sq ] [ y>> sq ] bi + sqrt ;

: without-tri ( x -- x+1 x+2 x+3 )
        [ 1 + ] keep [ 2 + ] keep 3 + ;

: with-tri ( x -- x+1 x+2 x+3 )
        [ 1 + ] [ 2 + ] [ 3 + ] tri ;
```

Figure 20: Cleave combinators

invokes a on x and b on y. Much like cleave, there are shorthand words for the two- and three-quotation cases. These are suffixed with asterisks to indicate the spread variants, so we have bi* and tri*. In Figure 21 on the next page, the without-bi* word shows the simple dip pattern that bi* encapsulates. Here, we're converting the string str1 (the second element from the top) into uppercase and str2 (the top element) to lowercase. In with-bi*, the >upper ("to uppercase") and >lower ("to lowercase") words are seen first, uninterrupted by an extra word. More compelling is the way that tri* replaces the dips that can be seen in without-tri*. In comparison, with-tri* is less nested and easier to comprehend at first glance. While there are 2bi* and 2tri* variants that spread quotations to two values apiece on the stack, they are uncommon in practice.

Finally, apply combinators invoke a single quotation on multiple stack entries in turn. While there is a generalized word, it's more common to use the corresponding shorthands. Here, they are suffixed with at-signs, so **bi@** applies a quotation to each of the top two stack values, and **tri@** to each of the top three. This way, rather than duplicate code for each time we want to call a word, we need only specify it once. This is demonstrated clearly in Figure 22 on the following page. In without-bi@, we see that the quotation [sq] (for squaring numbers) appears twice for the call to bi*. In general, we can replace spread combinators whose quotations are all the same with a single quotation and an

```
: without-bi* ( str1 str2 -- str1' str2' )
       [ >upper ] dip >lower ;

: with-bi* ( str1 str2 -- str1' str2' )
       [ >upper ] [ >lower ] bi* ;

: without-tri* ( x y z -- x+1 y+2 z+3 )
       [ [ 1 + ] dip 2 + ] dip 3 + ;

: with-tri* ( x y z -- x+1 y+2 z+3 )
       [ 1 + ] [ 2 + ] [ 3 + ] tri* ;
```

Figure 21: Spread combinators

```
: without-bi@ ( x y -- norm )
    [ sq ] [ sq ] bi* + sqrt ;

: with-bi@ ( x y -- norm )
    [ sq ] bi@ + sqrt ;

: without-tri@ ( x y z -- x+1 y+1 z+1 )
    [ 1 + ] [ 1 + ] [ 1 + ] tri* ;

: with-tri* ( x y z -- x+1 y+1 z+1 )
    [ 1 + ] tri@ ;
```

Figure 22: Apply combinators

apply combinator. Thus, with-bi@ cuts down on the duplicated [sq] in without-bi@. Similarly, we can replace the three repeated quotations passed to tri* in without-tri@ with a single instance passed to tri@ in with-tri@. Like other data flow combinators, we have the numbered variants. 2bi@ has the stack effect (w x y z quot --), where quot expects two inputs, and is thus applied to w and x first, then to y and z. Similarly, 2tri@ applies the quotation to the top six objects of the stack in groups of two. Like their spread counterparts, they are not used very much.

This concludes our overview of Factor. Various other features are hidden away in different vocabularies, most of which are understandable based on the basics we've covered. For the purposes of this thesis, it's not important to know every little detail about Factor. Fu-

ture code snippets will always be accompanied by further explanation, though they should generally be readable given this short tutorial.

3 The Factor Compiler

If we could sort programming languages by the fuzzy notions we tend to have about how "high-level" they are, toward the high end we'd find dynamically-typed languages like Python, Ruby, and PHP—all of which are generally more interpreted than compiled (though there has been compelling work on this front [e.g., Biggar 2009]). Despite being as high-level as these popular languages, Factor's implementation is driven by performance. Factor source is always compiled to native machine code using either its simple, non-optimizing compiler or (more typically) the optimizing compiler that performs several sorts of data and control flow analyses. In this chapter, we look at the general architecture of Factor's implementation, after which we place a particular emphasis on the transformations performed by the optimizing compiler.

3.1 Organization

At the lowest level, Factor is written atop a C++ virtual machine (VM) that is responsible for basic runtime services. This is where the non-optimizing base compiler is implemented. It's the base compiler's job to compile the simplest primitives: operations that push literals onto the data stack, call, if, dip, words that access tuple slots as laid out in memory, stack shufflers, math operators, functions to allocate/deallocate call stack frames, etc. The aim of the base compiler is to generate native machine code as fast as possible. To this end, these primitives correspond to their own stubs of assembly code. Different stubs are generated by Factor depending on the instruction set supported by the particular machine in use. Thus, the base compiler need only make a single pass over the source code, emitting these assembly instructions as it goes.

This compiled code is saved in an *image file*, which contains a complete snapshot of the current state of the Factor instance, similar to many Smalltalk and Lisp systems [Pestov, Ehrenberg, and Groff 2010]. As code is parsed and compiled, the image is updated, serving as a cache for compiled code. This modified image can be saved so that future Factor instances needn't recompile vocabularies that have already been loaded.

The VM also handles method dispatch and memory management. Method dispatch incorporates a *polymorphic inline cache* to speed up generic words. Each generic word's call site (i.e., every point in the code at which we invoke a generic) is associated with a state:

- In the *cold* state, the call site's instruction performs relatively expensive computations to find the right method for the class being dispatched upon, which we'd like to avoid. To speed up future calls at that site, a polymorphic inline cache stub is generated, thus transitioning it to the next state.
- In the *inline cache* state, a stub has been generated that caches the locations of methods for classes that have already been seen. This way, if a generic word at a particular call site is invoked often upon only a small number of classes (as is often in the case in loops, for example), we don't need to waste as much time doing method lookup. By default, if more than three different classes are dispatched upon, we transition to the next state.
- In the *megamorphic* state, the call instruction points to a larger cache that is allocated for the specific generic word (i.e., it is shared by all call sites). While not as efficient as an inline cache, this can still improve the performance of method dispatch.

To manage memory, the Factor VM uses a generational garbage collector (GC), which carves out sections of space on the heap for objects of different ages. Garbage in the oldest generation is collected with a mark-sweep-compact algorithm, while younger generations rely on a copying collector [Wilson 1992]. This way, the GC is specialized for large numbers of short-lived objects that will stay in the younger generations without being promoted to the older generation. In the oldest space, even compiled code can be compacted. This is to avoid heap fragmentation in applications that must call the compiler at runtime, such as Factor's interactive development environment [Pestov, Ehrenberg, and Groff 2010].

Values are referenced by tagged pointers, which use the three least significant bits of the pointer's address to store type information. This is possible because Factor aligns objects

on an eight-byte boundary, so the three least significant bits of an address are always 0. These bits give us eight unique tags, but Factor has more than eight data types. So, to indicate that the type information is stored elsewhere, two tags are reserved. One is for VM types without their own tag, and the other is for tuples, each of which defines its own type. Sufficiently small integers (e.g., 29-bit integers on a 32-bit machine, since the other 3 bits are used for the type tag) are stored directly in the pointer, so they needn't be heap-allocated (i.e., "boxed"). Larger integers and floating point numbers are normally boxed, but the optimizing compiler may find ways to store floats in registers.

The VM is meant to be minimal, as Factor is mostly self-hosting. That is, the real workhorses of the language are written in Factor itself, including the standard libraries, parser, object system, and the optimizing compiler. It's possible for the compiler to be written in Factor because of the bootstrapping process that creates a new image from scratch. First, a minimal boot image is created from an existing host Factor instance. When the VM runs the boot image, it initiates the bootstrapping process. Using the host's parser, the base compiler will compile the core vocabularies necessary to load the optimizing compiler. Once the optimizing compiler can itself be compiled, it is used to recompile (and thus optimize) all of the words defined so far. With the basic vocabularies recompiled, any additional vocabularies can be loaded using the optimized compiler and saved into a new, working image.

Thus, while the Factor VM is important, it is a small part of the code base. Since the bootstrapping process allows the optimizing compiler (hereafter just "the compiler") to be written in the same high-level language it's compiling, we can avoid the fiddly low-level details of the C++ backend. This is more conducive to writing advanced compiler optimizations, which are often complicated enough without having a concise, dynamically-typed, garbage-collected language like Factor to help us.

3.2 High-level Optimizations

To manipulate source code abstractly, we must have at least one intermediate representation (IR)—a data structure representing the instructions. It's common to convert between several IRs during compilation, as each form offers different properties that facilitate particular analyses. The Factor compiler optimizes code in passes across two different IRs: first at a high-level using the compiler.tree vocabulary, then at a low-level with the compiler.cfg vocabulary. In this section, we look at the former IR and the optimizations performed on it.

Representation

The high-level IR arranges code into a vector of node objects, which may themselves have children consisting of vectors of nodes—a tree structure that lends to the name compiler.tree. This ordered sequence of nodes represents control flow in a way that's effectively simple, annotated stack code. Figure 23 on the next page shows the definitions of the tuples that represent the "instruction set" of this stack code. Each object inherits (directly or indirectly) from the node class, which itself inherits from identity-tuple. This is a tuple whose equal? method is defined to always return f so that no two instances are equivalent unless they are the same object in memory.

Notice that most nodes define some sort of in-d and out-d slots, which mark each of them with the input and output data stacks. This represents the flow of data through the program. Here, stack values are denoted simply by integers, giving each value a unique identifier. An #introduce instance is inserted wherever the next node requires stack values that have not yet been named. Thus, while #introduce has no in-d, its out-d introduces the necessary stack values. Similarly, #return is inserted at the end of the sequence to indicate the final state of the data stack with its in-d slot.

The most basic operations of a stack language are, of course, pushing literals and calling functions. The #push node thus has a literal slot and an out-d slot, giving a name to the single element it pushes to the data stack. #call is used for normal word invocations.

```
TUPLE: node < identity-tuple ;
TUPLE: #introduce < node out-d ;
TUPLE: #return < node in-d info ;
TUPLE: #push < node literal out-d ;
TUPLE: #call < node word in-d out-d body method class info ;
TUPLE: #renaming < node;
TUPLE: #copy < #renaming in-d out-d;
TUPLE: #shuffle < #renaming mapping in-d out-d in-r out-r;
TUPLE: #declare < node declaration ;
TUPLE: #terminate < node in-d in-r;
TUPLE: #branch < node in-d children live-branches;
TUPLE: #if < #branch;
TUPLE: #dispatch < #branch;
TUPLE: #phi < node phi-in-d phi-info-d out-d terminated;
TUPLE: #recursive < node in-d word label loop? child;
TUPLE: #enter-recursive < node in-d out-d label info;
TUPLE: #call-recursive < node label in-d out-d info ;</pre>
TUPLE: #return-recursive < #renaming in-d out-d label info;
TUPLE: #alien-node < node params;
TUPLE: #alien-invoke < #alien-node in-d out-d;
TUPLE: #alien-indirect < #alien-node in-d out-d;
TUPLE: #alien-assembly < #alien-node in-d out-d;
TUPLE: #alien-callback < node params child;
```

Figure 23: High-level IR nodes

```
V{
    T{ #push { literal 1 } { out-d { 6256273 } } }
    T{ #introduce { out-d { 6256274 } } }
    T{ #call
        { word + }
        { in-d V{ 6256274 6256273 } }
        { out-d { 6256275 } }
}
    T{ #return { in-d V{ 6256275 } }
}
```

Figure 24: [1 +] build-tree

The in-d and out-d slots effectively serve as the stack effect declaration. In later analyses, data about the word's definition may be stored across the body, method, class, and info slots.

The word build-tree takes a Factor quotation and constructs the equivalent high-level IR form. In Figure 24, we see the output of the simple example [1 +] build-tree. Note that T{ class { slot1 value1 } { slot2 value2 } ... } is the syntax for tuple literals. The first node is a #push for the 1 literal, which is named "6256273". Since + needs two input values, an #introduce pushes a new "phantom" value. + gets turned into a #call instance. The sum is pushed to the data stack, so the out-d slot is a singleton that names this value. Finally, #return indicates the end of the routine, its in-d indicating the value left on the stack (the sum pushed by #call).

The next tuples in Figure 23 on the previous page reassign existing values on the stack to fresh identifiers. The #renaming superclass has the two subclasses #copy and #shuffle. The former represents the bijection from elements of in-d to elements of out-d in the same position; corresponding values are copies of each other. Stack shufflers are translated to more general #shuffle nodes with mapping slots that dictate how the new values in out-d correspond to the input values in in-d. For instance, Figure 25 on the following page shows how swap takes in the values 6256132 and 6256133 and outputs 6256134 and 6256135, where the first output is mapped to the second input and the second output is mapped to the first input. The in-r and out-r slots of #shuffle correspond to the retain stack,

```
V{
    T{ #introduce { out-d { 6256132 6256133 } } }
    T{ #shuffle
        { mapping { 6256134 6256133 } { 6256135 6256132 } } }
        { in-d V{ 6256132 6256133 } }
        { out-d V{ 6256134 6256135 } }
}
    T{ #return { in-d V{ 6256134 6256135 } } }
}
```

Figure 25: [swap] build-tree

```
V{
    T{ #introduce { out-d { 6256069 } } }
    T{ #declare { declaration { 6256069 fixnum } } }
    T{ #return { in-d V{ 6256069 } }
}
```

Figure 26: [{ fixnum } declare] build-tree

which is an implementation detail beyond the scope of this discussion.

#declare is a miscellaneous node used for the declare primitive. It simply annotates type information to stack values, as in Figure 26. #terminate is another one-off node, but a much more interesting one. While Factor normally requires a balanced stack, sometimes we purposefully want to throw an error. #terminate is introduced where the program halts prematurely. When checking the stack height, it gets to be treated specially so that terminated stack effects unify with any other effect. That way, branches will still be balanced even if one of them unconditionally throws an error. Figure 27 on the following page shows #terminate being introduced by the throw word.

Next, Figure 23 on page 31 defines nodes for branching based off the superclass #branch. The children slot contains vectors of nodes representing different branches. live-branches is filled in during later analyses to indicate which branches might be executed so "dead" ones that are never taken may be removed. Mostly, we'll see #if, which will have two elements in its children slot representing the true and false branches. On the other hand, #dispatch has an arbitrary number of children. It corresponds to the

```
V{
    T{ #push { literal "Error!" } { out-d { 6256051 } } }
    T{ #call
        { word throw }
        { in-d V{ 6256051 } }
        { out-d { } }
    }
    T{ #terminate { in-d V{ } } { in-r V{ } } }
}
```

Figure 27: ["Error!" throw] build-tree

dispatch primitive, which is an implementation detail of the generic word system used to speed up method dispatch.

You may have noted the emphasis on introducing new values, instead of reassigning old ones. Even #shuffles output unique identifiers, letting their values be determined by the mapping. The reason for this is that compiler.tree uses static single assignment (SSA) form, wherein every variable is defined by exactly one statement. This simplifies the properties of variables, which helps optimizations perform faster and with better results [Cytron et al. 1991]. By giving unique names to the targets of each assignment, the SSA property is guaranteed. However, #branches introduce ambiguity: after, say, an #if, what will the out-d be? It depends on which branch is taken. To remedy this problem, after any #branch node, Factor will place a #phi node—the classical SSA "phony function", ϕ . While it doesn't perform any literal computation, conceptually ϕ selects between its inputs, choosing the "correct" argument depending on control flow. This can then be assigned to a unique value, preserving the SSA property. In Factor, a #phi node's arguments are represented by the phi-in-d slot, which is a sequence of sequences. Each element corresponds to the out-d of the respective child of the preceding #branch node. The #phi's out-d gives unique names to the output values.

For example, the #phi in Figure 28 on the following page will select between the 6256248 return value of the first child or the 6256249 output of the second. Either way, we can refer to the result as 6256250 afterwards. The terminated slot of the #phi tells us if there was

```
٧{
    T{ #introduce { out-d { 6256247 } } }
    T{ #if
        { in-d { 6256247 } }
        { children
            {
                ٧{
                     T{ #push
                         { literal 1 }
                         { out-d { 6256248 } }
                     }
                }
                ₹{
                    T{ #push
                         { literal 2 }
                         { out-d { 6256249 } }
                     }
                }
            }
        }
    T{ #phi
        { phi-in-d { { 6256248 } { 6256249 } } }
        { out-d { 6256250 } }
        { terminated V{ f f } }
    }
    T{ #return { in-d V{ 6256250 } } }
}
```

Figure 28: [[1] [2] **if**] build-tree

a #terminate in any of the branches.

The #recursive node encapsulates *inline recursive* words. In Factor, words may be annotated with simple compiler declarations, which guide optimizations. If we follow a standard colon definition with the **inline** word, we're saying that its definition can be spliced into the call site, rather than generating code to jump to a subroutine. Inline words that call themselves must additionally be declared **recursive**. For example, we could write: foo (--) foo; **inline recursive**. The nodes #enter-recursive, #call-recursive, and #return-recursive denote different stages of the recursion—the beginning, recursive call, and end, respectively. They carry around a lot of metadata

about the nature of the recursion, but it doesn't serve our purposes to get into the details. Similarly, we gloss over the final nodes of Figure 23 on page 31, which correspond to Factor's foreign function interface (FFI) vocabulary, called alien. At a high level, #alien-node, #alien-invoke, #alien-indirect, #alien-assembly, and #alien-callback are used to make calls to C libraries from within Factor.

Optimizations

Now that we're familiar with the structure of the high-level IR, we can turn our attention to optimization. Figure 29 on the following page shows the passes performed on a sequence of nodes by the word optimize-tree. Before optimization can begin, we must gather some information and clean up some oddities in the output of build-tree. analyze-recursive is called first to identify and mark loops in the tree. Effectively, this means we detect loops introduced by #recursive nodes. Future passes can then use this information for data flow analysis. Afterwards, normalize makes the tree more consistent by doing two things:

- All #introduce nodes are removed and replaced by a single #introduce at the beginning of the whole program. This way, further passes needn't handle #introduce nodes.
- As constructed, the in-d of a #call-recursive will be the entire stack at the time of the call. This assumption happens because we don't know how many inputs it needs until the #return-recursive is processed, because of row polymorphism (refer to Section 2.5). So, here we figure out exactly what stack entries are needed, and trim the in-d and out-d of each #call-recursive accordingly.

Once these passes have cleaned up the tree, propagate performs probably the most extensive analysis of all the phases. In short, it performs an extended version of sparse conditional constant propagation (SCCP) [Wegman and Zadeck 1991]. The traditional data flow analysis combines global copy propagation, constant propagation, and constant folding in a flow-sensitive way. That is, it will propagate information from branches that it knows

```
: optimize-tree ( nodes -- nodes' )
     analyze-recursive
     normalize
     propagate
     cleanup
     dup run-escape-analysis? [
          escape-analysis
          unbox-tuples
     ] when
     apply-identities
     compute-def-use
     remove-dead-code
      ?check
      compute-def-use
     optimize-modular-arithmetic
      finalize
 ] with-scope;
```

Figure 29: Optimization passes on the high-level IR

are definitely taken (e.g., because #if is always given a true input). Instead of using the typical single-level (numeric) constant value lattice, Factor uses a lattice augmented by information about numeric value ranges, array lengths/bounds, and classes (which form a partial order, as described briefly in Section 2.4). Additionally, the pass may inline certain calls if enough information is present. As values are refined, they propagate to other values that depend on them. For example, by refining the range of possible values a particular numeric variable can have, we might discover that, say, it's small enough to fit in a fixnum rather than a bignum. Then a math operator called on it may be inlined to a more specific version. Or, if the interval has zero length, we may replace the value with a constant, which contributes to constant folding.

propagate iterates through the nodes collecting all of this data until reaching a stable point where inferences can no longer be drawn. Technically, this information doesn't alter the tree at all; we merely store it so that speculative decisions may be realized later. The next word in Figure 29, cleanup, does just this by inlining words, folding constants, removing overflow checks, deleting unreachable branches, and flattening inline-recursive

```
TUPLE: data-struct
    { a read-only }
    { b read-only };

: escaping-via-#return ( -- data-struct )
        1 2 data-struct boa;

: escaping-via-#call ( -- )
        1 2 data-struct boa pprint;

: non-escaping ( -- a+b )
        1 2 data-struct boa [ a>> ] [ b>> ] bi +;
```

Figure 30: Escaping vs. non-escaping tuple allocations

words that don't actually wind up calling themselves (e.g., because the calls got constant-folded).

The next major pass is escape-analysis, whose information is used for the actual transformation unbox-tuples. This discovers tuples that escape by getting passed outside of a word. For instance, the inputs to #return obviously escape, as they are passed to the world outside of the word in question. Similarly, inputs to the #call of another word escape. So, though the tuples in escaping-via-#return and escaping-via-#call in Figure 30 both escape, we can see the one in non-escaping does not. Because it does not escape to another location that may potentially use it, the last allocation is unnecessary. By identifying this, unbox-tuples can then rewrite the code to avoid allocating a data-struct altogether, instead manipulating the slots' values directly. Note that this only happens for immutable tuples, all of whose slots are read-only. Otherwise, we would need to perform more advanced pointer analyses to discover aliases.

apply-identities follows to simplify words with known identity elements. If, say, one argument to + is 0, we can simply return the other argument. This converts the #call to + into a simple #shuffle. These identities are defined for most arithmetic words.

Another few simple passes come next in Figure 29 on the previous page. True to its name, compute-def-use computes where SSA values are defined and used. Values

that are never used are eliminated by remove-dead-code. ?check conditionally performs some consistency checks on the tree, mostly to make sure that no errors were introduced in the stack flow. If a global variable isn't toggled on, this part is skipped. We run compute-def-use again to update the information after altering the tree with dead code elimination.

Finally, optimize-modular-arithmetic performs a form of strength-reduction on arithmetic words that only use the low-order bits of their inputs/results, which may also remove unnecessary overflow checks. finalize cleans up a few random miscellaneous bits of the tree (removing empty shufflers, deleting #copy nodes, etc.) in preparation for lower-level optimizations.

3.3 Low-level Optimizations

Representation

The low-level IR in compiler.cfg takes the more conventional form of a control flow graph (CFG). A CFG (not to be confused with "context-free grammar") is an arrangement of instructions into basic blocks: maximal sequences of "straight-line" code, where control does not transfer out of or into the middle of the block. Directed edges are added between blocks to represent control flow—either from a branching instruction to its target, or from the end of a basic block to the start of the next one [Aho et al. 2007]. Construction of the low-level IR proceeds by analyzing the control flow of the high-level IR and converting the nodes of Section 3.2 into lower-level instructions typical of assembly code. There are over a hundred of these instructions, but many are simply different versions of the same operation. For instance, while instructions are generally called on virtual registers (represented in Factor simply by integers), there are immediate versions of instructions. The ##add instruction, as an example, represents the sum of the contents of two registers, but ##add-imm sums the contents of one register and an integer literal. Other instructions are inserted to make stack reads and writes explicit, as well as to balance the height.

For posterity, below is a categorized list of all the instruction objects (each one is a subclass of the insn tuple). It's not imperative to know each of these instructions. Their names generally indicate their purposes clearly enough. If need be, though, you can refer back to this list.

- Loading constants: ##load-integer, ##load-reference
- Optimized loading of constants, inserted by representation selection:

 ##load-tagged, ##load-float, ##load-double, ##load-vector
- Stack operations: ##peek, ##replace, ##replace-imm, ##inc-d, ##inc-r
- Subroutine calls: ##call, ##jump, ##prologue, ##epilogue, ##return
- Inhibiting tail-call optimization (TCO): ##no-tco
- Jump tables: ##dispatch
- Slot access: ##slot, ##slot-imm, ##set-slot, ##set-slot-imm
- Register transfers: ##copy, ##tagged>integer
- Integer arithmetic: ##add, ##add-imm, ##sub, ##sub-imm, ##mul, ##mul-imm,

 ##and, ##and-imm, ##or, ##or-imm, ##xor, ##xor-imm, ##shl, ##shl-imm, ##shr,

 ##shr-imm, ##sar, ##sar-imm, ##min, ##max, ##not, ##neg, ##log2, ##bit-count
- Float arithmetic: ##add-float, ##sub-float, ##mul-float, ##div-float, ##min-float, ##max-float, ##sqrt
- Single/double float conversion: ##single>double-float, ##double>single-float
- Float/integer conversion: ##float>integer, ##integer>float
- Single instruction, multiple data (SIMD) operations: ##zero-vector,
 ##fill-vector, ##gather-vector-2, ##gather-int-vector-2,
 ##gather-vector-4, ##gather-int-vector-4, ##select-vector,
 ##shuffle-vector, ##shuffle-vector-halves-imm, ##shuffle-vector-imm,

##tail>head-vector, ##merge-vector-head, ##merge-vector-tail,
##float-pack-vector, ##signed-pack-vector, ##unsigned-pack-vector,
##unpack-vector-head, ##unpack-vector-tail, ##integer>float-vector,
##float>integer-vector, ##compare-vector, ##test-vector,
##test-vector-branch, ##add-vector, ##saturated-add-vector,
##add-sub-vector, ##sub-vector, ##saturated-sub-vector, ##mul-vector,
##mul-high-vector, ##mul-horizontal-add-vector, ##saturated-mul-vector,
##div-vector, ##min-vector, ##max-vector, ##avg-vector, ##dot-vector,
##sad-vector, ##horizontal-add-vector, ##horizontal-sub-vector,
##sqrt-vector, ##and-vector, ##andn-vector, ##or-vector, ##sor-vector,
##sqrt-vector, ##shl-vector-imm, ##shr-vector-imm, ##shl-vector,
##shr-vector

- Scalar/vector conversion: ##scalar>integer, ##integer>scalar,
 ##vector>scalar, ##scalar>vector
- Boxing and unboxing aliens: ##box-alien, ##box-displaced-alien,
 ##unbox-any-c-ptr, ##unbox-alien
- Zero-extending and sign-extending integers: ##convert-integer
- Raw memory access: ##load-memory, ##load-memory-imm, ##store-memory, ##store-memory-imm
- Memory allocation: ##allot, ##write-barrier, ##write-barrier-imm,
 ##alien-global, ##vm-field, ##set-vm-field
- The FFI: ##unbox, ##unbox-long-long, ##local-allot, ##box, ##box-long-long, ##alien-invoke, ##alien-indirect, ##alien-assembly, ##callback-inputs, ##callback-outputs
- Control flow: ##phi, ##branch

- Tagged conditionals: ##compare-branch, ##compare-imm-branch, ##compare, ##compare-imm
- Integer conditionals: ##compare-integer-branch,
 ##compare-integer-imm-branch, ##test-branch, ##test-imm-branch,
 ##compare-integer, ##compare-integer-imm, ##test, ##test-imm
- Float conditionals: ##compare-float-ordered-branch,
 ##compare-float-unordered-branch, ##compare-float-ordered,
 ##compare-float-unordered
- Overflowing arithmetic: ##fixnum-add, ##fixnum-sub, ##fixnum-mul
- GC checks: ##save-context, ##check-nursery-branch, ##call-gc
- Spills and reloads, inserted by the register allocator: ##spill, ##reload

Optimizations

By translating the high-level IR into instructions that manipulate registers directly, we reveal (and sometimes introduce) further redundancies that can be optimized away. The optimize-cfg word in Figure 31 on the following page shows the passes performed in doing this. The first word, optimize-tail-calls, performs tail call elimination on the CFG. Tail calls are those that occur within a procedure and whose results are immediately returned by that procedure. Instead of allocating a new call stack frame, we may convert tail calls into simple jumps, since afterwards the current procedure's call frame isn't really needed. In the case of recursive tail calls, we can convert special cases of recursion into loops in the CFG, so that we won't trigger call stack overflows. For instance, consider Figure 32 on page 44, which shows the effect of optimize-tail-calls on the following definition:

Note the recursive call (trivially) occurs at the end of the definition, just before the return point. When translated to a CFG, this is a ##call instruction, as seen in block 4 to

```
: optimize-cfg ( cfg -- cfg' )
    optimize-tail-calls
    delete-useless-conditionals
    split-branches
    join-blocks
    normalize-height
    construct-ssa
    alias-analysis
    value-numbering
    copy-propagation
    eliminate-dead-code ;
```

Figure 31: Optimization passes on the low-level IR

the left of Figure 32 on the following page. This is also just before the final ##epilogue and ##return instructions in block 8, as blocks 5–7 are effectively empty (these excessive ##branches will be eliminated in a later pass). Because of this, rather than make a whole new subroutine call, we can convert it into a ##branch back to the beginning of the word, as in the CFG to the right.

The next pass in Figure 31 is delete-useless-conditionals, which removes branches that go to the same basic block. This situation might occur as a result of optimizations performed on the high-level IR. To see it in action, Figure 33 on page 45 shows the transformation on a purposefully useless conditional, [] [] if. On the left, the CFG ##peeks at the top of the data stack (D 0), storing the result in the virtual register 1. This value is popped, so we decrement the stack height in block 2 using ##inc-d -1. Then, ##compare-imm-branch compares the value in the virtual register 2 (which is a copy of 1, the top of the stack) to the immediate value f to see if it's not equal (signified by cc/=)—that is, to see if we should take the "then" branch or the "else" one. However, both branches jump through several empty blocks and merge at the same destination. Thus, we can remove them and replace ##compare-imm-branch with an unconditional ##branch to the eventual destination. We see this on the right of Figure 33 on page 45.

In order to expose more opportunities for optimization, split-branches will actually duplicate code. We use the fact that code immediately following a conditional will be

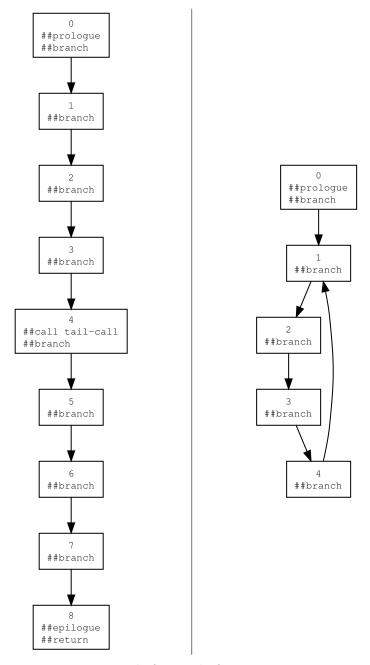


Figure 32: tail-call before and after optimize-tail-calls

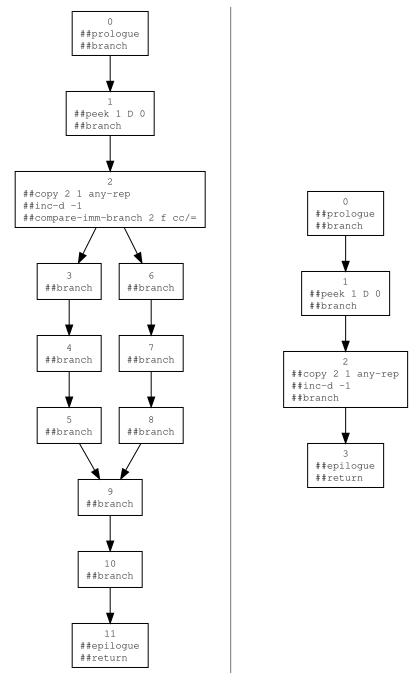


Figure 33: [] if before and after delete-useless-conditionals

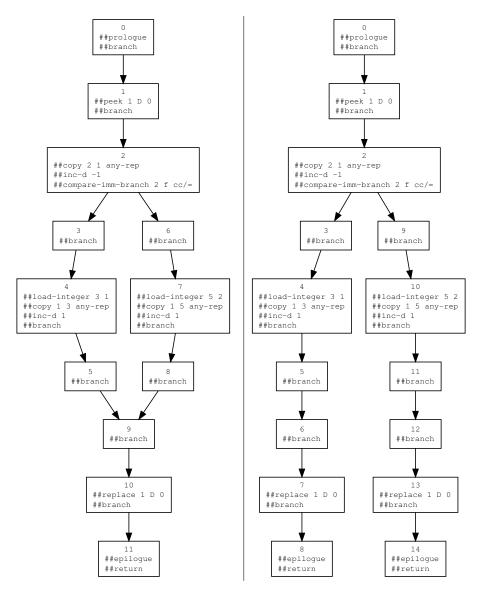


Figure 34: [1] [2] if dup before and after split-branches

executed along both branches regardless. If it's sufficiently short, we copy it up into the branches individually. That is, we change [A] [B] if C into [AC] [BC] if, as long as C is small enough. Later analyses may then, for example, more readily eliminate one of the branches if it's never taken. Figure 34 shows what such a transformation looks like on a CFG. The example [1] [2] if dup is essentially changed into [1 dup] [2 dup] if thus splitting the block with two predecessors (block 9) on the left.

The next pass, join-blocks, compacts the CFG by joining together blocks involved in only a single control flow edge. Mostly, this is to clean up the myriad of empty or short

blocks introduced during construction, like sequences of a bunch of ##branches. Figure 35 on the next page shows this pass on the CFG of 0 100 [1 fixnum+fast] times, which increments the top of the stack 100 times. fixnum+fast is a specialized version of + that suppresses overflow and type checks. We use it here to keep the CFG simple. We'll be using this particular code to illustrate all but one of the remaining optimization passes in Figure 31 on page 43, as it's a motivating example for the work in this thesis. None of the passes before join-blocks change the CFG seen on the left in Figure 35 on the next page, but we get rid of the useless ##branch blocks, giving us the CFG on the right.

Figure 36 on page 49 shows the result of applying normalize-height to the result of join-blocks. This phase combines and canonicalizes the instructions that track the stack height, like ##inc-d. While the shuffling in this example isn't complex enough to be interesting, neither is this phase. It amounts to more cleaning: multiple height changes are combined into single ones at the beginnings of the basic blocks. In Figure 36 on page 49, this means that ##inc-d is moved to the top of block 1, as compared to the right of Figure 35 on the following page.

In converting the high-level IR to the low-level, we actually lose the SSA form of compiler.tree. Not only does the construction do this, but split-branches also copies basic blocks verbatim, so any value defined will have a duplicate definition site, violating the SSA property. construct-ssa recomputes a so-called pruned SSA form, wherein ϕ functions are inserted only if the variables are live after the insertion point. This cuts down on useless ϕ functions [Briggs et al. 1998; Das and Ramakrishna 2005]. Figure 37 on page 50 shows the reconstructed SSA form of the CFG from Figure 36 on page 49, where ##phis are inserted at the start of block 2. Not only is there one for the element we're incrementing with fixnum+fast, but times introduces an induction variable to track how many iterations have been done. As block 2 is the entry for the loop, it either gets the values of these variables from the beginning (block 1) for from the actual body of the loop (block 3). Hence, we need ##phis to distinguish the values.

The next pass, alias-analysis, doesn't change the CFG we're currently working with, so we won't have an accompanying figure. At a high level, alias-analysis is easy to

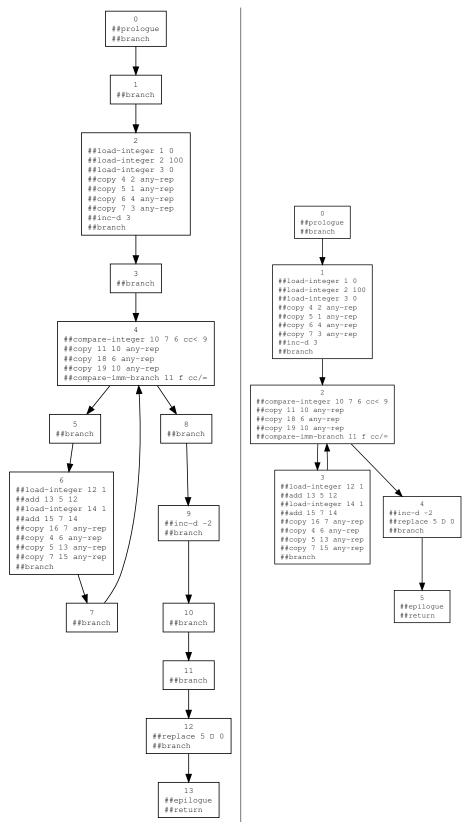


Figure 35: 0 100 [1 fixnum+fast] times before and after join-blocks

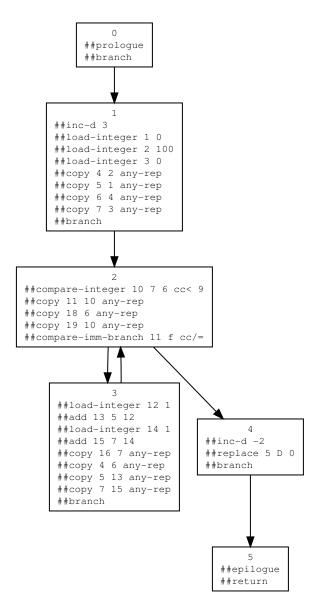


Figure 36: 0 100 [1 fixnum+fast] times after normalize-height

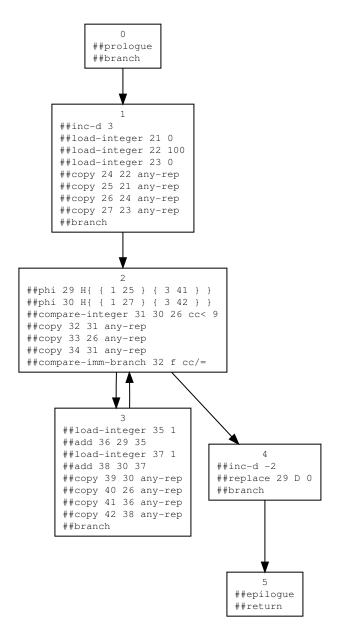


Figure 37: 0 100 [1 fixnum+fast] times after construct-ssa

understand: it eliminates redundant memory loads and stores by rewriting certain patterns of memory access. If the same location is loaded immediately after being stored, we convert the load into a ##copy of the value we wrote. Two reads of the same location with no intermittent write gets the second read turned into a ##copy. Similarly, if we see two writes without a read in the middle, the first write can be removed.

value-numbering is the key focus of this thesis. It will be detailed in Chapter 4. For now, it does to think of it as a combination of common subexpression elimination and constant folding. In Figure 38 on the next page, we see several changes from this pass:

- ##load-integer 23 0 in block 1 of Figure 37 on the preceding page (which assigns the value 0 to the virtual register 23) is redundant, so is replaced by ##copy 23 21.
- The last instruction in block 2 is redundant. The original

intuitively means "if REG[32] \neq **f**, go to ...". Its replacement,

means "if REG[30] < REG[26], go to...". This is because the source register (32) of the original is a ##copy of 31, which itself is computed by

In pseudo-code, this is like REG[31] \leftarrow (REG[30] < REG[26]), where 9 is a temporary virtual register used for calculation. So, the ##compare-imm-branch is equivalent to a simple ##compare-integer-branch, because the former is saying "if (REG[30] < REG[26]) \neq **f**, go to...", while the latter simply says "if REG[30] < REG[26], go to...". Converting it means that the calculation of 31 is unnecessary, so may be pruned away later.

• The second operands in both ##adds of block 3 are just constants stored by ##load-integers. So, these are turned into ##add-imms.

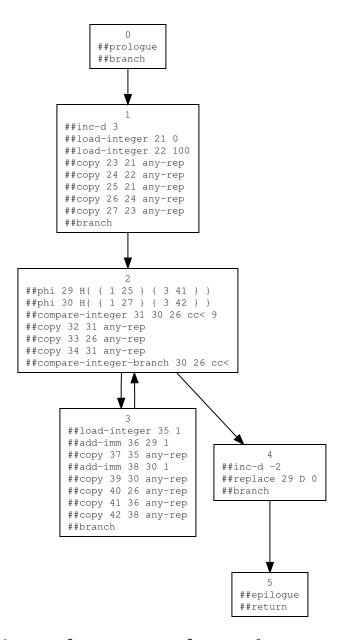


Figure 38: 0 100 [1 fixnum+fast] times after value-numbering

• Also, the second ##load-integer in block 3 just loads 1 like the first instruction in the block. Therefore, it's replaced by a ##copy.

In Chapter 4, we'll see how and why this pass fails to identify other equivalences.

Following value-numbering, copy-propagation performs a global pass that eliminates ##copy instructions. Uses of the copies are replaced by the originals. So, in Figure 39 on the next page, we can see that all of the ##copy instructions have been removed. Also, for

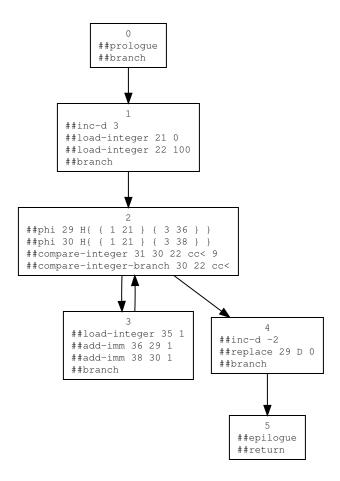


Figure 39: 0 100 [1 fixnum+fast] times after copy-propagation

instance, the use of the virtual register 25 in block 2 has been replaced by 21, since 25 was a copy of it.

Next, dead code is removed by eliminate-dead-code. Figure 40 on the following page shows that the ##compare-integer in block 2 and the ##load-integer in block 3 were removed, since they defined values that were never used.

The final pass in Figure 31 on page 43, finalize-cfg, itself consists of several more passes. We will not get into many details here, but at a high level, the most important passes figure out how virtual registers should map to machine registers. First, we figure out when certain values can be unboxed. Then, instructions are reordered in order to reduce register pressure. That is, we try to schedule instructions around each other so that we don't need to store more values than we have machine registers. That way, we avoid spilling registers onto the heap, which wastes time on slower memory accesses. After removing

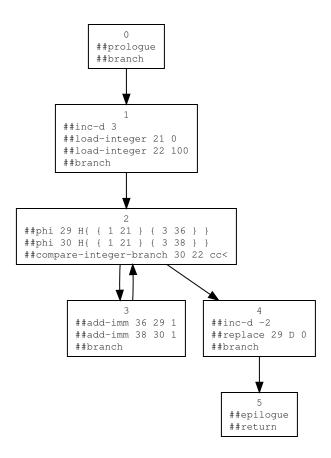


Figure 40: 0 100 [1 fixnum+fast] times after eliminate-dead-code

##phis and leaving SSA form, we perform a *linear scan* register allocation, which replaces virtual registers with machine registers and inserts ##spill and ##reload instructions for the cases we can't avoid. Figure 41 on the following page shows the output on an Intel x86 machine, which has enough registers that we needn't spill anything.

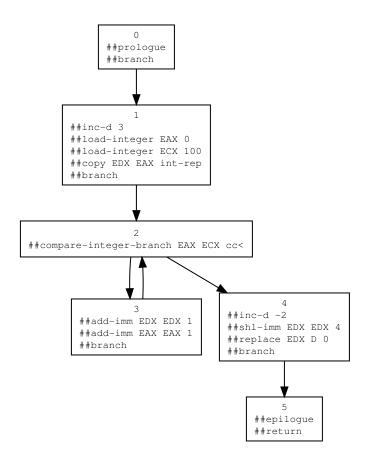


Figure 41: 0 100 [1 fixnum+fast] times after finalize-cfg

4 Value Numbering

At a very basic level, most optimization techniques revolve around avoiding redundant or unnecessary computation. Thus, it's vital that we discover which values in a program are equal. That way, we can simplify the code that wastes machine cycles repeatedly calculating the same values. Classic optimization phases like constant/copy propagation, common subexpression elimination, loop-invariant code motion, induction variable elimination, and others discussed in the de facto treatise, "The Dragon Book" [Aho et al. 2007], perform this sort of redundancy elimination based on information about the equality of expressions.

In general, the problem of determining whether two expressions in a program are equivalent is undecidable. Therefore, we seek a *conservative* solution that doesn't necessarily identify all equivalences, but is nevertheless correct about any equivalences it does identify. Solving this equivalence problem is the work of *value numbering* algorithms. These assign every value in the program a number such that two values have the same value number if and only if the compiler can prove they will be equal at runtime.

Value numbering has a long history in literature and practice, spanning many techniques. In Section 3.3 we saw the value-numbering word, which is actually based on some of the earliest—and least effective—methods of value numbering. Section 4.1 describes the way Factor's current algorithm works, highlighting its shortcomings to motivate the main work of this thesis, which is covered in ????. We finish the chapter by analyzing the results of these changes and reviewing the literature for further enhancements that can be made to this optimization pass.

4.1 Local Value Numbering

Tracing the exact origins of value numbering is difficult. It's thought to have originally been invented in the 1960s by Balke [Simpson 1996]. The earliest tangible reference to value numbering (at least, the earliest point where discussions in the literature seem to start) appears in an oft-cited but unpublished work of Cocke and Schwartz [1970]. The technique is relatively simple, but not as powerful as other methods for reasons described hereafter.

The algorithm considers a single basic block. For each instruction (from top to bottom) in the block, we essentially let the value number of the assignment target be a hash of the operator and the value numbers of the operands. That is, we hash the *expression* being computed by an instruction. Thus, assuming a proper hash function, two expressions are *congruent* if they have the same operators and their operands are congruent. This is our approximation of runtime equivalence. It's important that the hash is based on the value numbers of the statement's operands, not just the operands as they appear in code (i.e., *lexical* equivalence). Any information about congruence is propagated through the value numbers. We'll have discovered any such equivalences among the operands before computing the value number of the assignment target. This is because every value in a basic block is either defined before it's used, or else defined at some point in a predecessor, which we don't care about when only considering one basic block.

This is the first shortcoming of the algorithm. It is local, focusing on only one basic block at a time. Any definitions outside the boundaries of the basic block won't be reused, even if they reach the block. This severely limits the scope of the redundancies we can discover. We could improve upon this by considering the algorithm across an entire loop-free CFG in any $topological\ order$. In such an ordering, a basic block B comes before any other block B' to which it has an edge. Thus, any "outside" variables that instructions in B' rely on must have come from B or earlier, which will have already been computed in a traversal of such an ordering. However, CFGs usually contain cycles or loops (at least interesting ones do), which make such an ordering impossible. We could still pick a topological order that ignores back-edges, but we may encounter operands whose values flow along those back-edges, so haven't been processed yet. We'll address this issue later.

In Factor, expressions are basically instructions (the insn objects discussed in Section 3.3) that have had their destination registers stripped. Instructions can be converted to expressions with the >expr word defined in the compiler.cfg.value-numbering.expressions vocabulary. For instance, an ##add instruction with the destination register 1 and source registers 2 and 3 will be converted into an array of three elements:

- The ##add class word, indicating the expression is derived from an ##add instruction.
- The value number of the virtual register 2.
- The value number of the virtual register 3.

Some instructions are not referentially transparent, meaning they can't be replaced with the value they compute without changing the program's behavior. For example, ##call and ##branch cannot reasonably be converted into expressions. In these cases, >expr merely returns a unique value.

The hashing of expressions takes place in the so-called *expression graph* implemented in the vocabulary shown in Figure 42 on the next page. This consists of three global hash tables that relate virtual registers, value numbers, instructions, and expressions. Since virtual registers are just integers, we actually use them as value numbers, too. vregs>vns maps virtual registers to their value numbers. If a virtual register is mapped to itself in this table, its definition is the canonical instruction that we use to compute the value. This instruction is stored in the vns>insns table. Finally, the most important mapping is exprs>vns. True to its name, it uses expressions as keys, which (of course) are implicitly hashed. Thus, we can use this table to determine the equivalence of expressions.

Other definitions in Figure 42 on the following page manipulate expressions and the graph. The global variable input-expr-counter is used in the generation of unique expressions discussed earlier. init-value-graph initializes this and all the tables. set-vn establishes a mapping from a virtual register to a value number in vregs>vns. vn>insn gives terse access to the vns>insns table. vreg>insn uses vregs>vns and vns>insns to get the canonical instruction that defines a given virtual register. Finally, vreg>vn looks up the value of a key in the vregs>vns table. Importantly, if the key is not yet present in the table, it is automatically mapped to itself—it's assumed that the virtual register does not correspond to a redundant instruction.

This is the second shortcoming of the algorithm. It must make a *pessimistic* assumption about congruences. That is, it starts by assuming that every expression has a unique value number, then tries to prove that there are some values which are actually congruent. This

```
! Copyright (C) 2008, 2010 Slava Pestov.
! See http://factorcode.org/license.txt for BSD license.
USING: accessors kernel math namespaces assocs;
IN: compiler.cfg.value-numbering.graph
SYMBOL: input-expr-counter
! assoc mapping vregs to value numbers
! this is the identity on canonical representatives
SYMBOL: vregs>vns
! assoc mapping expressions to value numbers
SYMBOL: exprs>vns
! assoc mapping value numbers to instructions
SYMBOL: vns>insns
: vn>insn ( vn -- insn ) vns>insns get at ;
: vreg>vn ( vreg -- vn ) vregs>vns get [ ] cache ;
: set-vn ( vn vreg -- ) vregs>vns get set-at ;
: vreg>insn ( vreg -- insn ) vreg>vn vn>insn ;
: init-value-graph ( -- )
   0 input-expr-counter set
   H{ } clone vregs>vns set
   H{ } clone exprs>vns set
   H{ } clone vns>insns set ;
```

Figure 42: The compiler.cfg.value-numbering.graph vocabulary

```
: value-numbering-step ( insns -- insns' )
   init-value-graph
   [ process-instruction ] map flatten ;
: value-numbering ( cfg -- cfg )
   dup [ value-numbering-step ] simple-optimization
   cfg-changed predecessors-changed ;
```

Figure 43: Main words from compiler.cfg.value-numbering

fails to discover congruences for values that flow along back-edges, whether we consider a single basic block or an entire topological ordering.

One the other hand, an advantage of this local value numbering algorithm is its simplicity. It makes a single pass over all the instructions, identifying and replacing redundancies online (i.e., rewriting as it goes). It's straightforward to write, and even to extend. At every step, the currently known value numbers will be sound, so we can use this information for copy/constant propagation, constant folding, and common subexpression elimination.

To see how Factor accomplishes these extensions, we'll take a look at the compiler.cfg.value-numbering vocabulary. Figure 43 shows the main words that start the optimization pass. The value-numbering-step word is called on the sequence of instructions that comprise each basic block. It starts the expression graph from a blank slate with init-value-graph, then maps the word process-instruction on each of them. This is a generic word that we'll study momentarily; it returns either a single insn object or a sequence of them in the case that an instruction is replaced by several others. Then, the work of value-numbering is to just call value-numbering-step on each basic block, which is done with a combinator called simple-optimization. The words cfg-changed and predecessors-changed alter some internal state of the CFG that has been potentially invalidated by some transformations performed by process-instruction.

The methods of process-instruction are shown in Figure 44 on the following page. Skipping the first three normal words for the moment, the default behavior for dispatching on an insn is to invoke yet another generic word, rewrite. This word will return either

```
GENERIC: process-instruction ( insn -- insn')
: redundant-instruction ( insn vn -- insn')
    [ dst>> ] dip [ swap set-vn ] [ <copy> ] 2bi ;
:: useful-instruction ( insn expr -- insn')
    insn dst>> :> vn
   vn vn vregs>vns get set-at
   vn expr exprs>vns get set-at
    insn vn vns>insns get set-at
    insn ;
: check-redundancy (insn -- insn')
    dup >expr dup exprs>vns get at
    [ redundant-instruction ] [ useful-instruction ] ?if ;
M: insn process-instruction
    dup rewrite [ process-instruction ] [ ] ?if ;
M: foldable-insn process-instruction
    dup rewrite
    [ process-instruction ]
    [ dup defs-vregs length 1 = [ check-redundancy ] when ] ?if ;
M: ##copy process-instruction
   dup [ src>> vreg>vn ] [ dst>> ] bi set-vn ;
M: array process-instruction
    [ process-instruction ] map ;
```

Figure 44: The workhorse of compiler.cfg.value-numbering

a replacement insn (or sequence thereof) or f, indicating that no change has taken place. Thus, by recursively calling process-instruction, we can do more specialized processing on this rewritten replacement (e.g., dispatching on insn again, which applies rewrite once more). If the instruction can't be simplified further, we simply return it. (Note that [X] [Y] ?if is the same as dup [nip X] [drop Y] if.)

For instances of foldable-insn (a subclass of insn for those that can be converted to useful expressions with >expr), we similarly invoke rewrite recursively until no more rewriting occurs. When that happens, rather than just return the instruction, we in-

voke check-redundancy—though only if the instruction defines exactly one virtual register, which will be stored in a slot named dst. check-redundancy checks if the expression being computed by the instruction is already a key of the exprs>vns table. If it is, the instruction is redundant, and we call redundant-instruction; otherwise, we call useful-instruction. The former uses set-vn to give the instruction's dst virtual register the same value number as the equivalent expression. Since value numbers are actually virtual registers, we may also use these as the source and destination registers in a new ##copy instruction, which is then returned. On the other hand, useful-instruction saves the instruction's information in the expression graph by setting the appropriate values in vregs>vns, exprs>vns, and vns>insns.

The ##copy method of process-instruction cannot do anything to simplify the instruction, but will set the value number of the destination register to that of the source. By calling vreg>vn on the source register, we make sure to call set-vn between the destination and the canonical value number of the source.

Finally, the array method is used for the purposes of recursion, in the case that rewrite returns a sequence of replacement instructions. The correct action is, of course, to descend into this new sequence of instructions with process-instruction.

Underlying all of the redundancy elimination is the rewrite generic word. It has too many methods to look at the source code in-depth here, but it's instructive to give an overview of the transformations. These methods actually make up the bulk of the compiler.cfg.value-numbering code. They're spread across various sub-vocabularies. compiler.cfg.value-numbering.rewrite defines the generic itself, along with a handful of utilities. The method for the most general instruction class, insn, is defined to unconditionally return f, meaning no rewriting is performed by default. That way, we need only define rewrite methods for more specific instruction classes to get specialized behavior.

compiler.cfg.value-numbering.alien contains methods that simplify nodes related to Factor's FFI. Most involve fusing together the results of intermediate arithmetic. The instructions that access raw memory (namely ##load-memory, ##load-memory-imm, ##store-memory, and ##store-memory-imm) tend to have arguments for address arith-

metic. Each has slots for a base register containing an address and a literal offset from it. But if base is defined by an ##add-imm instruction, we can just update the offset, incrementing it by the literal operand of the ##add-imm. Then, base will just be changed to the register operand of the ##add-imm. This removes the memory instruction's need for the ##add-imm, increasing the chances that the latter will become dead code to be removed later. Unlike the -imm variants, ##load-memory and ##store-memory also take a displacement register, which works like a non-immediate offset. Therefore, ##adds can be similarly fused into ##load-memory-imm and ##store-memory-imm by transforming them into ##load-memory and ##store-memory instructions with the ##add's operand as the displacement. A few other similar transformations are also done, including rewrites for ##box-displaced-aliens and ##unbox-any-c-ptrs.

compiler.cfg.value-numbering.comparisons defines methods for the various branching and comparison instructions (which simply store booleans in registers, rather than branching upon them). The major optimizations performed are as follows:

- If possible, instructions are converted to more specific forms. For example, non-immediate instructions (e.g., ##compare) may be turned into their -imm counterparts (e.g., ##compare-imm) if one of their source registers corresponds to a literal value. ##compare-integer-imm is also converted to ##test if the architecture supports it. This corresponds to a special instruction in x86 that performs a bitwise AND for its side effects on particular flags, discarding the actual result. This can be more efficient when using the AND result as a boolean.
- If both inputs to a comparison or branch are literals, we may constant-fold the instruction. In the case of comparisons, this means converting it into a ##load-reference of the proper boolean. In branches, this modifies the CFG so that the path which isn't taken is removed completely.
- Like a novice programmer writing if (some_boolean != false) { ... } in Java, the compiler may generate redundant boolean comparisons that need cleaning up.

That is, the intermediate boolean values are eliminated when the result of a comparison is used by another comparison, collapsing the whole thing into a single instruction.

compiler.cfg.value-numbering.folding defines some auxiliary words for constant-folding arithmetic. unary-constant-fold and binary-constant-fold perform the actual operation on the one or two constant inputs provided. These words are used in compiler.cfg.value-numbering.math, which predictably simplifies math via standard rules. Arithmetic identities are rewritten. Conceptually, x + 0 becomes just x, for instance. If self-inverting instructions (namely ##neg for numerical negation and ##not for boolean negation) are called on registers that themselves correspond to the same instruction, we can safely rewrite them into ##copy instructions—intuitively turning a double-negative into a positive. Non-immediate instructions are converted to their -imm forms if possible. When both operands are constant, the expression is folded. The most interesting math optimizations use the associative and distributive laws. Reassociation conceptually converts $(x \otimes y) \otimes z$ into $x \otimes (y \otimes z)$ when both y and z are constants and \otimes is associative. So, for example,

##add-imm 1 X Y

##add-imm 2 1 Z

is converted into just

##add-imm 2
$$X$$
 (Y+Z)

where X is a virtual register, and Y and Z are constants. Distribution converts $(x \oplus y) \otimes z$ into $(x \otimes z) \oplus (y \otimes z)$, where y and z are constants, \oplus corresponds to addition or subtraction, and \otimes to multiplication or left bitwise shifts. Therefore,

##add-imm 1 X Y

##mul-imm 2 1 Z

is converted into

```
##mul-imm 3 X Y ##add-imm 2 3 (Y*Z)
```

Notice that a new intermediate virtual register, 3, had to be created. However, if the product of Y and Z can be computed at compile-time and fits in an immediate operand, then we save cycles by using ##mul-imm on smaller numbers (multiplying the contents of X by the constant Y, rather than their sum by Z).

The last few methods of rewrite provide some obvious simplifications. compiler.cfg.value-numbering.simd performs some limited constant-folding for vector operations. compiler.cfg.value-numbering.slots propagates ##add-imm address calculation to ##slot, ##set-slot, and ##write-barrier instructions in a manner similar to compiler.cfg.value-numbering.alien. Finally, compiler.cfg.value-numbering.misc provides a single method to rewrite ##replace into ##replace-imm if possible.

To finish the discussion of local value numbering and Factor's particular implementation, we'll examine the example from Figure 38 on page 52 in depth. For convenience, the before/after snapshot of the CFG is reproduced in Figure 45 on the following page.

value-numbering-step begins at block 1, where process-instruction is mapped across the instructions. ##inc-d 3 does not have a rewrite method, so remains untouched; it is also not a foldable-insn, so it is simply returned. While ##load-integer 21 0 doesn't have a rewrite method, it is a foldable-insn, so process-instruction calls check-redundancy. At this point, the expression graph is empty. Calling >expr converts this instruction into an integer-expr object representing 0. useful-instruction leaves the tables as follows:

```
! vregs>vns
H{ { 21 21 } }

! exprs>vns
H{ { T{ integer-expr { value 0 } } 21 } }
```

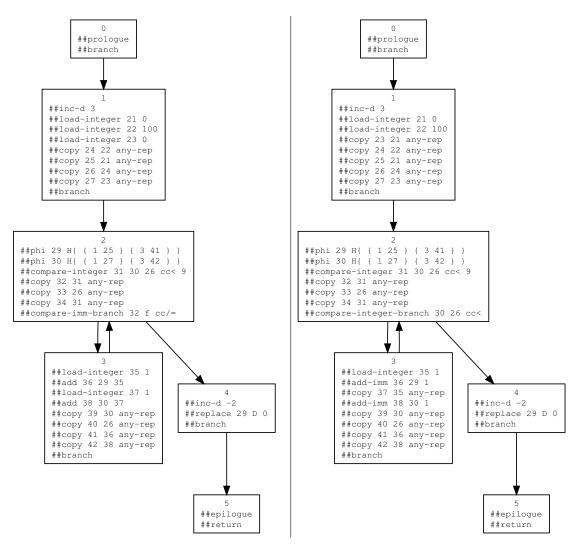


Figure 45: 0 100 [1 fixnum+fast] times before and after value-numbering

```
! vns>insns
H{
     { 21 T{ ##load-integer { dst 21 } { val 0 } { insn# 1 } } }
}
```

The next instruction in block 1, ##load-integer 22 100, behaves similarly, leaving:

```
! vregs>vns
H{ { 21 21 } { 22 22 } }
```

The following instruction is ##load-integer 23 0. In calling check-redundancy, we discover that the integer expression for 0 is already in exprs>vns, so this is turned into a ##copy, and the value number is noted. The remaining instructions in block 1 (aside from ##branch) are all instances of ##copy. process-instruction thus only sets their value numbers in the vregs>vns table, leaving us with the following at the end of block 1:

```
! vregs>vns
H{
     { 21 21 }
     { 22 22 }
     { 23 21 }
     { 24 22 }
     { 25 21 }
     { 26 22 }
     { 27 21 }
```

Next, block 2 in Figure 45 on page 66 is processed. The tables are all reset, so even though block 1 happens to dominate block 2, none of its definitions are known to value-numbering. The ##phis are ignored, as no important methods dispatch upon them. In trying to rewrite the ##compare-integer, we call vreg>vn on the operands. Since they aren't in the vregs>vns table yet, they are assumed to be unique values. This assumption is pessimistic—we'd rather the values be the same, so we can remove redundancy. It happens to be correct here, though, as 26 corresponds to the integer 100, while 30 is an induction variable of the loop. However, ##compare-integer cannot be rewritten into an immediate form, since our focus is local to the basic block, so we don't know that the virtual register 26 has the value 100. The ##copy instructions are processed as usual, and ##compare-imm-branch 32 f cc/= is rewritten into a ##compare-integer-branch, as the virtual register 32 has the same value (through the copies) as the ##compare-integer

result. This is a case of simplifying the

```
if (some_boolean != false) { ... }
```

pattern, and the definition of the register 31 becomes dead code after rewrite finishes with this last instruction. The expression graph is populated as follows by the end of block 2:

```
! vregs>vns
H{
    { 32 31 }
    { 33 26 }
    { 34 31 }
    { 26 26 }
    { 30 30 }
    { 31 31 }
}
! exprs>vns
H{ { { ##compare-integer 30 26 cc< } 31 } }
! vns>insns
H{
    {
        31
        T{ ##compare-integer
            { dst 31 }
            { src1 30 }
            { src2 22 }
            { cc cc< }
            { temp 9 }
            { insn# 2 }
```

```
}
}
}
```

Once again, the tables are reset and we proceed to block 3. The first instruction, ##load-integer 35 1, is entered into the expression graph. Since 35 is an operand of ##add 36 29 35, rewrite changes this instruction into an ##add-imm, as we know the constant value of the operand. The next ##load-integer gets turned into a ##copy, like in block 1, and the next ##add is similarly changed to ##add-imm. The copies do little but set more value numbers. As process-instruction calls vreg>vn on their sources, we'll insert entries into vregs>vns for virtual registers defined outside of the block, like 26. This leaves us with the following tables:

```
! vregs>vns
H{
    { 35 35 }
    { 36 36 }
    { 37 35 }
    { 38 38 }
    { 39 30 }
    { 40 26 }
    { 41 36 }
    { 26 26 }
    { 42 38 }
    { 29 29 }
    { 30 30 }
}
! exprs>vns
H{
```

The fourth invocation of value-numbering-step does not do anything interesting, as the ##replace cannot be changed into a ##replace-imm.

In summary, we managed to replace redundancies within basic blocks online by maintaining some simple hash tables. After copy propagation and dead code elimination, the CFG gets finalized to the one shown in Figure 46 on the following page. Because the value numbering algorithm was local, the ##compare-integer-branch in block 2 could not be simplified to a ##compare-integer-imm-branch, and we instead have to waste a register on the integer 100. But it's important to note that even considering a topological ordering of the CFG wouldn't have worked, as we'd have to ignore back-edges. The ##phis that used to be in block 2 had inputs that flowed along the back-edge, and our pessimistic assumption would have to classify these values as distinct. One is for the counter introduced by times, and the other is from the top value of the stack being incremented by fixnum+fast. In this case, however, these induction variables are actually equal: both start at 0 and are incremented by 1 on each loop iteration. In terms of the CFG in Figure 46 on the next page, the EAX and EDX registers are equivalent. Yet the combination of the pessimism and locality of the algorithm keep us from discovering this.

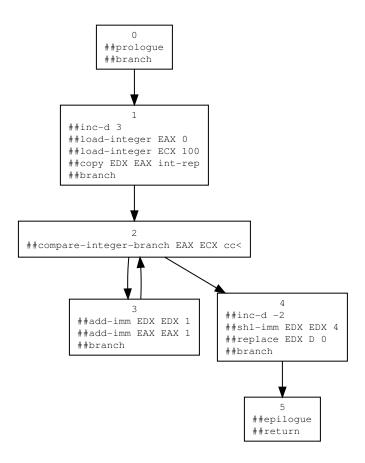


Figure 46: The final representation for 0 100 [1 fixnum+fast] times

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