1   Language Primer

Factor is a rather young language created by Slava Pestov in September of 2003. Its first incarnation targeted the Java Virtual Machine (JVM) as an embedded scripting language for a game. As such, its feature set was minimal. Factor has since evolved into a general-purpose programming language, gaining new features and redesigning old ones as necessary for larger programs. Today's implementation sports an extensive standard library and has moved away from the JVM in favor of native code generation. In this section, we cover the basic syntax and semantics of Factor for those unfamiliar with the language. This should be just enough to understand the later material in this thesis. More thorough documentation can be found via Factor's website, `http://factorcode.org`.

1.1   Combinators

Quotations, introduced in **??**, form the basis of both control flow and data flow in Factor. Not only are they the equivalent of anonymous functions, but the stack model also makes them syntactically lightweight enough to serve as blocks akin to the code between curly braces in C or Java. Higher-order words that make use of quotations on the stack are called *combinators*. It's simple to express familiar conditional logic and loops using combinators, as we'll show in Section 1.1.1. In the presence of explicit data flow via stack operations, even more patterns arise that can be abstracted away. Section 1.1.2 explores how we can use combinators to express otherwise convoluted stack-shuffling logic more succinctly.

1.1.1   Control Flow

```
5 even? [ "even" print ] [ "odd" print ] if

{ } empty? [ "empty" print ] [ "full" print ] if

100 [ "isn't f" print ] [ "is f" print ] if
```

Listing 1: Conditional evaluation in Factor

The most primitive form of control flow in typical programming languages is, of course, the `if` statement, and the same holds true for Factor. The only difference is that Factor's `if` isn't syntactically significant—it's just another word, albeit implemented as a primitive. For the moment, it will do to think of `if` as having the stack effect (? `true false` --). The third element from the top of the stack is a condition, and it's followed by two quotations. The first quotation (second element from the top of the stack) is called if the condition is true, and the second quotation (the top of the stack) is called if the condition is false. Specifically, `f` is a special object in Factor for falsity. It is a singleton object—the sole instance of the `f` class—and is the only false value in the entire language. Any other object is necessarily boolean true. For a canonical boolean, there is the `t` object, but its truth value exists only because it is not `f`. Basic `if` use is shown in Listing 1.

The first example will print "odd", the second "empty", and the third "isn't f". All of them leave nothing on the stack.

```
: example1 ( x -- 0/x-1 )
  dup even? [ drop 0 ] [ 1 - ] if ;

: example2 ( x y -- x+y/x-y )
  2dup mod 0 = [ + ] [ - ] if ;

: example3 ( x y -- x+y/x )
  dup odd? [ + ] [ drop ] if ;
```

Listing 2: **if**'s stack effect varies

However, the simplified stack effect for **if** is quite restrictive. (? true false --) intuitively means that both the `true` and `false` quotations can't take any inputs or produce any outputs—that their effects are (--). We'd like to loosen this restriction, but per **??**, Factor must know the stack height after the **if** call. We could give **if** the effect (x ? true false -- y), so that the two quotations could each have the stack effect (x -- y). This would work for the `example1` word in Listing 2, yet it's just as restrictive. For instance, the `example2` word would need **if** to have the effect (x y ? true false -- z), since each branch has the effect (x y -- z). Furthermore, the quotations might even have different effects, but still leave the overall stack height balanced. Only one item is left on the stack after a call to `example3` regardless, even though the two quotations have different stack effects: + has the effect (x y -- z), while **drop** has the effect (x --).

In reality, there are infinitely many correct stack effects for **if**. Factor has a special notation for such *row-polymorphic* stack effects. If a token in a stack effect begins with two dots, like ..a or ..b, it is a *row variable*. If either side of a stack effect begins with a row variable, it represents any number inputs/outputs. Thus, we could give **if** the stack effect

$$(\text{..a ? true false -- ..b})$$

to indicate that there may be any number of inputs below the condition on the stack, and any number of outputs will be present after the call to **if**. Note that these numbers aren't necessarily equal, which is why we use distinct row variables in this case. However, this still isn't quite enough to capture the stack height requirements. It doesn't communicate that `true` and `false` must affect the stack in the same ways. For this, we can use the notation quot: (stack -- effect), giving quotations a nested stack effect. Using the same names for row variables in both the "inner" and "outer" stack effects will refer to the same number of inputs or outputs. Thus, our final (correct) stack effect for **if** is

$$(\text{..a ? true: (..a -- ..b) false: (..a -- ..b) -- ..b})$$

This tells us that the `true` quotation and the `false` quotation will each create the same relative change in stack height as **if** does overall.

```
{ "Lorem" "ipsum" "dolor" } [ print ] each

0 { 1 2 3 } [ + ] each

10 iota [ number>string print ] each

3 [ "Ho!" print ] times

[ t ] [ "Infinite loop!" print ] while

[ f ] [ "Executed once!" print ] do while
```

Listing 3: Loops in Factor

Though **if** is necessarily a language primitive, other control flow constructs are defined in Factor itself. It's simple to write combinators for iteration and looping as tail-recursive words that invoke quotations. Listing 3 showcases some common looping patterns. The most basic yet versatile word is **each**. Its stack effect is

$$(\ldots \quad \text{seq quot:} \quad (\ldots \quad x \text{ -- } \ldots \text{)} \quad \text{-- } \ldots \text{)}$$

Each element `x` of the sequence `seq` will be passed to `quot`, which may use any of the underlying stack elements. Here, unlike **if**, we enforce that the input stack height is exactly the same as the output (since we use the same row variable). Otherwise, depending on the number of elements in `seq`, we might dig arbitrarily deep into the stack or flood it with a varying number of values. The first use of **each** in Listing 3 is balanced, as the quotation has the effect (str --) and no additional items were on the stack to begin with. Essentially, it's equivalent to *"Lorem"* **print** *"ipsum"* **print** *"dolor"* **print**. On the other hand, the quotation in the second example has the stack effect (total n -- total+n). This is still balanced, since there is one additional item below the sequence on the stack (namely 0), and one element is left by the end (the sum of the sequence elements). So, this example is the same as 0 1 + 2 + 3 +.

Any instance of the extensive **sequence** mixin will work with **each**, making it very flexible. The third example in Listing 3 shows **iota**, which is used here to create a *virtual* sequence of integers from 0 to 9 (inclusive). No actual sequence is allocated, merely an object that behaves like a sequence. In Factor, it's common practice to use **iota** and **each** in favor of repetitive C-like **for** loops.

Of course, we sometimes don't need the induction variable in loops. That is, we just want to execute a body of code a certain number of times. For these cases, there's the **times** combinator, with the stack effect

$$(\ldots \quad \text{n quot:} \quad (\ldots \quad \text{-- } \ldots \text{)} \quad \text{-- } \ldots \text{)}$$

This is similar to **each**, except that `n` is a number (so we needn't use **iota**) and the quotation doesn't expect an extra argument (i.e., a sequence element). Therefore, the example in Listing 3 is equivalent to *"Ho!"* **print** *"Ho!"* **print** *"Ho!"* **print**.

Naturally, Factor also has the `while` combinator, whose stack effect is

```
( ..a pred: ( ..a -- ..b ? ) body: ( ..b -- ..a ) -- ..b )
```

The row variables are a bit messy, but it works as you'd expected: the `pred` quotation is invoked on each iteration to determine whether `body` should be called. The `do` word is a handy modifier for `while` that simply executes the body of the loop once before leaving `while` to test the precondition as per usual. Thus, the last example in Listing 3 on the previous page executes the body once, despite the condition being immediately false.

```
{ 1 2 3 } [ 1 + ] map

{ 1 2 3 4 5 } [ even? ] filter

{ 1 2 3 } 0 [ + ] reduce
```

Listing 4: Higher-order functions in Factor

In the preceding combinators, quotations were used like blocks of code. But really, they're the same as anonymous functions from other languages. As such, Factor borrows classic tools from functional languages, like `map` and `filter`, as shown in Listing 4. `map` is like `each`, except that the quotation should produce a single output. Each such output is collected up into a new sequence of the same class as the input sequence. Here, the example produces `{ 2 3 4 }`. `filter` selects only those elements from the sequence for which the quotation returns a true value. Thus, the `filter` in Listing 4 outputs `{ 2 4 }`. Even `reduce` is in Factor, also known as a *left fold*. An initial element is iteratively updated by pushing a value from the sequence and invoking the quotation. In fact, `reduce` is defined as `swapd each`, where `swapd` is a shuffler word with the stack effect `( x y z -- y x z )`. Thus, the example in Listing 4 is the same as `0 { 1 2 3 } [ + ] each`, as in Listing 3 on the previous page.

These are just some of the control flow combinators defined in Factor. Several variants exist that meld stack shuffling with control flow, or can be used to shorten common patterns like empty false branches. An entire list is beyond the scope of our discussion, but the ones we've studied should give a solid view of what standard conditional execution, iteration, and looping looks like in a stack-based language.

1.1.2   Data Flow

While avoiding variables and additional syntax makes it easier to refactor code, keeping mental track of the stack can be taxing. If we need to manipulate more than the top few elements of the stack, code gets harder to read and write. Since the flow of data is made explicit via stack shufflers, we actually wind up with redundant patterns of data flow that we otherwise couldn't identify. In Factor, there are several combinators that clean up common stack-shuffling logic, making code easier to understand.

The first combinators we'll look at are `dip` and `keep`. These are used to preserve elements of the stack. When working with several values, sometimes we don't want to use all of them at quite

```
: without-dip1 ( x y -- x+1 y )
  swap 1 + swap ;

: with-dip1 ( x y -- x+1 y )
  [ 1 + ] dip ;

: without-dip2 ( x y z -- x-y z )
  2over - swapd nip swapd nip swap ;

: with-dip2 ( x y z -- x-y z )
  [ - ] dip ;

: without-keep1 ( x -- x+1 x )
  dup 1 + swap ;

: with-keep1 ( x -- x+1 x )
  [ 1 + ] keep ;

: without-keep2 ( x y -- x-y y )
  swap over - swap ;

: with-keep2 ( x y -- x-y y )
  [ - ] keep ;
```

Listing 5: Preserving combinators

the same time. Using `drop` and the like wouldn't help, as we'd lose the data altogether. Rather, we want to retain certain stack elements, do a computation, then restore them. For an uncompelling but illustrative example, suppose we have two values on the stack, but we want to increment the second element from the top. `without-dip1` in Listing 5 on the preceding page shows one strategy, where we shuffle the top element away with `swap`, perform the computation, then `swap` the top back to its original place. A cleaner way is to call `dip` on a quotation, which will execute that quotation just under the top of the stack, as in `with-dip1`. While the stack shuffling in `without-dip1` isn't terribly complicated, it doesn't convey our meaning very well. Shuffling the top element out of the way becomes increasingly difficult with more complex computations. In `without-dip2`, we want to call `-` on the two elements below the top. For lack of a more robust stack shuffler, we use `2over` to isolate the two values so we can call `-`. The rest of the word consists of shuffling to get rid of excess values on the stack. It's also worth noting that `swapd` is a deprecated word in Factor, since its use starts making code harder to reason about. Alternatively, we could dream up a more complex stack shuffler with exactly the stack effect we wanted in this situation. But this solution doesn't scale: what if we had to calculate something that required more inputs or produced more outputs? Clearly, `dip` provides a cleaner alternative in `with-dip2`.

`keep` provides a way to hold onto the top element of the stack, but still use it to perform a computation. In general, `[ ... ] keep` is equivalent to `dup [ ... ] dip`. Thus, the current top of the stack remains on top after the use of `keep`, but the quotation is still invoked with that value. In `with-keep1` in Listing 5 on the previous page, we want to increment the top, but stash the result below. Again, this logic isn't terribly complicated, though `with-keep1` does away with the shuffling. `without-keep2` shows a messier example where a simple `dup` will not save us, as we're using more than just the top element in the call to `-`. Rather, three of the four words in the definition are dedicated to rearranging the stack in just the right way, obscuring the call to `-` that we really want to focus on. On the other hand, `with-keep2` places the subtraction word front-and-center in its own quotation, while `keep` does the work of retaining the top of the stack.

```
TUPLE: coord x y ;

: without-bi ( coord -- norm )
  [ x>> sq ] keep y>> sq + sqrt ;

: with-bi ( coord -- norm )
  [ x>> sq ] [ y>> sq ] bi + sqrt ;

: without-tri ( x -- x+1 x+2 x+3 )
  [ 1 + ] keep [ 2 + ] keep 3 + ;

: with-tri ( x -- x+1 x+2 x+3 )
  [ 1 + ] [ 2 + ] [ 3 + ] tri ;
```

Listing 6: Cleave combinators

The next set of combinators apply multiple quotations to a single value. The most general form of these so-called *cleave* combinators is the word `cleave`, which takes an array of quotations as input, and calls each one in turn on the top element of the stack. Of course, for only a couple of

quotations, wrapping them in an array literal becomes cumbersome. The word **bi** exists for the two-quotation case, and **tri** for the three quotations. Cleave combinators are often used to extract multiple slots from a tuple. Listing 6 on the preceding page shows such a case in the **with-bi** word, which improves upon using just **keep** in the **without-bi** word. In general, a series of **keep**s like [a] **keep** [b] **keep** c is the same as { [a] [b] [c] } **cleave**, which is more readable. We can see this in action in the difference between **without-tri** and **with-tri** in Listing 6 on the previous page. In cases where we need to apply multiple quotations to a set of values instead of just a single one, there are also the variants **2cleave** and **3cleave** (and the corresponding **2bi**, **2tri**, **3bi**, and **3tri**), which apply the quotations to the top two and three elements of the stack, respectively.

```
: without-bi* ( str1 str2 -- str1' str2' )
  [ >upper ] dip >lower ;

: with-bi* ( str1 str2 -- str1' str2' )
  [ >upper ] [ >lower ] bi* ;

: without-tri* ( x y z -- x+1 y+2 z+3 )
  [ [ 1 + ] dip 2 + ] dip 3 + ;

: with-tri* ( x y z -- x+1 y+2 z+3 )
  [ 1 + ] [ 2 + ] [ 3 + ] tri* ;
```

Listing 7: Spread combinators

To apply multiple quotations to multiple values, Factor has *spread* combinators. Whereas cleave combinators abstract away repeated instances of **keep**, spread combinators replace nested calls to **dip**. The archetypical combinator, **spread**, takes an array of quotations, like **cleave**. However, instead of applying each one to the top element of the stack, each one corresponds to a separate element of the stack. Thus, { [a] [b] } **spread** invokes b on the top element, and a on the element beneath the top. Much like **cleave**, there are shorthand words for the two- and three-quotation cases. These are suffixed with asterisks to indicate the spread variants, so we have **bi*** and **tri***. In Listing 7, the **without-bi*** word shows the simple **dip** pattern that **bi*** encapsulates. Here, we're converting the string **str1** (the second element from the top) into uppercase and **str2** (the top element) to lowercase. In **with-bi***, the **>upper** and **>lower** words are seen first, uninterrupted by an extra word, making the code easier to read. More compelling is the way that **tri*** replaces the **dip**s that can be seen in **without-tri***. In comparison, **with-tri*** is less nested and easier to comprehend at first glance. While there are **2bi*** and **2tri*** variants that spread quotations to two values apiece on the stack, they are uncommon in practice.

Finally, *apply* combinators invoke a single quotation on multiple stack entries in turn. While there is a generalized word, it's more common to use the corresponding shorthands. Here, they are suffixed with at-signs, so **bi@** applies a quotation to each of the top two stack values, and **tri@** to each of the top three. This way, rather than duplicate code for each time we want to call a word, we need only specify it once. This is demonstrated clearly in Listing 8 on the next page. In **without-bi@**, we see that the quotation [**sq**] (for squaring numbers) appears twice for the call to **bi***. In general, we can replace spread combinators whose quotations are all

```
: without-bi@ ( x y -- norm )
  [ sq ] [ sq ] bi* + sqrt ;

: with-bi@ ( x y -- norm )
  [ sq ] bi@ + sqrt ;

: without-tri@ ( x y z -- x+1 y+1 z+1 )
  [ 1 + ] [ 1 + ] [ 1 + ] tri* ;

: with-tri* ( x y z -- x+1 y+1 z+1 )
  [ 1 + ] tri@ ;
```

Listing 8: Apply combinators

the same with a single quotation and an apply combinator. Thus, `with-bi@` cuts down on the duplicated `[ sq ]` in `without-bi@`. Similarly, we can replace the three repeated quotations passed to `tri*` in `without-tri@` with a single instance passed to `tri@` in `with-tri@`. Like other data flow combinators, we have the numbered variants. **2bi@** has the stack effect (`w x y z quot --`), where `quot` expects two inputs, and is thus applied to `w` and `x` first, then to `y` and `z`. Similarly, **2tri@** applies the quotation to the top six objects of the stack in groups of two. Like their spread counterparts, they are not used very much.

Some wrap-up that isn't completely lame.