```
In[ \circ ] := Ibias = \{3, 3, 5, 5, 2.5\}
      input1[t_] := 1 \sin[\pi t/400] HeavisideTheta[t - 00.1]
      inputAnti[t] := 1 \sin[(\pi (t-400) / 400)] HeavisideTheta[t-00.1]
     inputAdv[t_] := 1 Sin[(\pi (t-50) / 400)] HeavisideTheta[t-00.1]
      inputLag[t] := 1 \sin[(\pi(t+50)/400)] HeavisideTheta[t-00.1]
     (*f1 = 3(*input corrisponding to 1*)
          f2 = 3(*input corrisponding to 0*)
           θ=40
            input1[t_]:=f1 Iinj[100,300][t]+f1 Iinj[500,300][t]+f2 Iinj[900,300][t]
               input2[t_]:=f1 \ Iinj[100+\theta,300][t]+f2 \ Iinj[500+\theta,300][t]+f1 \ Iinj[900+\theta,300][t]
     *)
     time = 1200
     Fv[V_{, W_{, [Ii_{, k_{, b_{, i}}}]} := -3 V + ((1/k) * V^2 + 40 + 100 b - W + Ii)
     Fw[V_{, W_{, a}}[a_{, b_{, a}}] := a(b(V) - W)
     Iinj [start_, dur_][t_] := HeavisidePi[(t - start)/dur - 1/2]
     T[x_] := Transpose[x]
     L[x_] := Length[x]
     (*base parameters of the neurons*)
     k = 25
      a = 1/10.
     b = .2
      c = 10
      d = .01
      tau = 10
     (*synaptic weights*)
      go = 4
      gee = 2
      gei = 5
      gie = -10
      gii = -10
      ClassicalRungeKuttaCoefficients[4, prec_] :=
       With[{amat = {{1/2}, {0, 1/2}, {0, 0, 1}}}, bvec = {1/6, 1/3, 1/3, 1/6}, cvec = {1/2, 1/2, 1}},
        N[{amat, bvec, cvec}, prec]]
```

```
Out[ • ]=
          \{3, 3, 5, 5, 2.5\}
Out[ • ]=
           1200
Out[ • ]=
           25
Out[ • ]=
           0.1
Out[0]=
           0.2
Out[ • ]=
           10
Out[ • ]=
           0.01
Out[ • ]=
           10
Out[ • ]=
           4
Out[ • ]=
           2
Out[ • ]=
           5
Out[0]=
          -10
Out[ • ]=
          -10
```

NOR

```
\label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
      tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] = Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]\},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    \{t, 0, time\}, Method \rightarrow \{"TimeIntegration" \rightarrow "Adams"\}, Compiled \rightarrow True;
solAntiNOR = NDSolve
    {(*neuron e1*)
      Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
         input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
      tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
         inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
      tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
      (*neuron i1*)
```

tau Se2 '[t] == -Se2[t], Se2[0] == 0,

```
Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
solAdvNOR = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
```

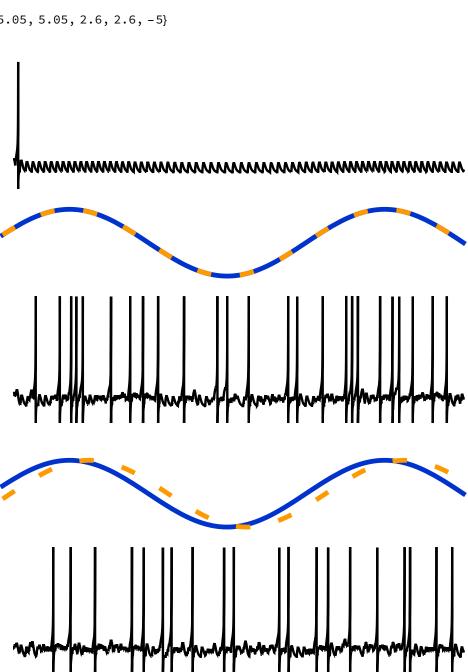
```
WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuroni2*)
         Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
               inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
         Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
          tau Si2 '[t] == -Si2[t], Si2[0] == 0,
         WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron out*)
         Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
         Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
         WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
       {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
       {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagNOR = NDSolve
       {(*neuron e1*)
         Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
               input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
         We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
          tau Se1 '[t] == -Se1[t], Se1[0] == 0,
         WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron e2*)
         Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
         We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
          tau Se2 '[t] == -Se2[t], Se2[0] == 0,
         WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron i1*)
         \label{eq:vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[t] + gii Si2[t] + gei Se1[t] + Ibias[t] + gii Si2[t] + gei Se1[t] + Ibias[t] + gii Si2[t] + gei Se1[t] + gii Se1[t] +
         Vi1[0] == 0,
         Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
          tau Si1'[t] == -Si1[t], Si1[0] == 0,
         WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuroni2*)
         Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
```

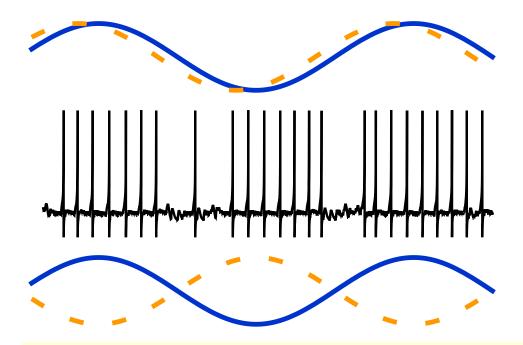
```
inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
                         Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
                          tau Si2 '[t] == -Si2[t], Si2[0] == 0,
                         \label{eq:whenevent_vi2[t] == 130, vi2[t] are c, wi2[t] are wi2[t] + d, Si2[t] are Si2[t] + 1},
                                 "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
                         (*neuron out*)
                         Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
                         Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
                         WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
                                "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
                  {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
                  {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
NORout = Column
                  Plot[Vo[t]/. solSyncNOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, ImageSize \rightarrow 500
                         PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
                        AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
                  Plot[{input1[t], input1[t]},
                         \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                                      {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
                         ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
                  Plot[Vo[t]/. solAdvNOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, ImageSize \rightarrow 500,
                         PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
                          AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}|,
                    , Plot[{input1[t], inputAdv[t]},
                         \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                                       {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
                         ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
                  Plot[Vo[t]/. solLagNOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, Imag
                         PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
                        AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
                  Plot[{input1[t], inputLag[t]},
                         \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                                      {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
                          ImageSize \rightarrow 500, AspectRatio \rightarrow \left(1/\left(4 \text{ GoldenRatio}\right)\right), Axes \rightarrow False],
                  Plot[Vo[t]/. solAntiNOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
                         PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
                         AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
                   Plot[{input1[t], inputAnti[t]},
```

 $\{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},\}$ {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None, ImageSize \rightarrow 500, AspectRatio $\rightarrow \left(1/\left(4 \text{ GoldenRatio}\right)\right)$, Axes \rightarrow False]

}]

Out[•]= {5.05, 5.05, 2.6, 2.6, -5}





NXOR

```
In[*]:= Ibias = {3.6, 3.6, 3.3, 3.3, -2.05}
       solSyncNXOR = NDSolve
           {(*neuron e1*)
            Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
                input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
            We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
            tau Se1 '[t] == -Se1[t], Se1[0] == 0,
            \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
              "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
            (*neuron e2*)
            Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
                input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
            We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
            tau Se2 '[t] == -Se2[t], Se2[0] == 0,
            \label{eq:we2[t] self} WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
              "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
            (*neuron i1*)
            Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
            Vi1[0] == 0,
            Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
            tau Si1'[t] == -Si1[t], Si1[0] == 0,
            \label{eq:whenevent_vii} WhenEvent[Vii[t] == 130, \{Vii[t] \rightarrow c, \, Wii[t] \rightarrow Wii[t] + d, \, Sii[t] \rightarrow Sii[t] + 1\},
```

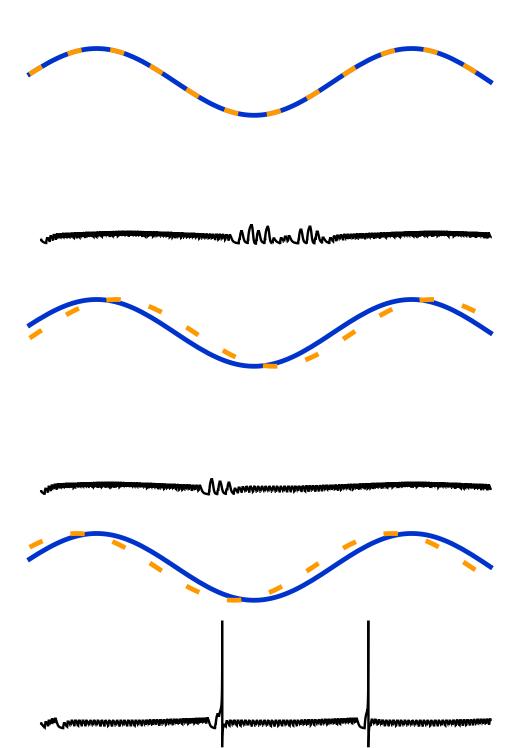
```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAntiNXOR = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
```

```
Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
solAdvNXOR = NDSolve
    \{(*neuron e1*)\}
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     \label{eq:WhenEvent} WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

```
(*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
solLagNXOR = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b]+
        inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
```

```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
NXORout = Column[{
    Plot Vo[t] /. solSyncNXOR, {t, 30, time}, ImageSize \rightarrow 500, PlotRange \rightarrow {0, 140},
     PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], input1[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1 / (4 GoldenRatio)), Axes \rightarrow False,
    Plot Vo[t] /. solAdvNXOR, {t, 30, time}, ImageSize \rightarrow 500, PlotRange \rightarrow {0, 140},
     PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}|,
    , Plot[{input1[t], inputAdv[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
    Plot[Vo[t]/. solLagNXOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
     PlotPoints \rightarrow 10000, PlotStyle \rightarrow {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot {input1[t], inputLag[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1 / (4 GoldenRatio)), Axes \rightarrow False,
    Plot Vo[t] /. solAntiNXOR, {t, 30, time}, ImageSize → 500,
     PlotRange → {0, 140}, PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], inputAnti[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False
  }]
```

 ${3.6, 3.6, 3.3, 3.3, -2.05}$



NAND

```
In[*]:= Ibias = {4, 4, 3.75, 3.75, -2.}
      solSyncNAND = NDSolve
          {(*neuron e1*)
           Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
               input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
           We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
            tau Se1 '[t] == -Se1[t], Se1[0] == 0,
           WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuron e2*)
           Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
           We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
            tau Se2 '[t] == -Se2[t], Se2[0] == 0,
           WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuron i1*)
           Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
           Vi1[0] == 0,
           Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
           tau Si1'[t] == -Si1[t], Si1[0] == 0,
           WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuroni2*)
           Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
           Vi2[0] == 0,
           Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
            tau Si2 '[t] == -Si2[t], Si2[0] == 0,
           WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuron out*)
           Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
           Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
           WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
             "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]\},
          {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
          {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
```

solAntiNAND = NDSolve

```
{(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvNAND = NDSolve
   {(*neuron e1*)
     Ve1 '[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
```

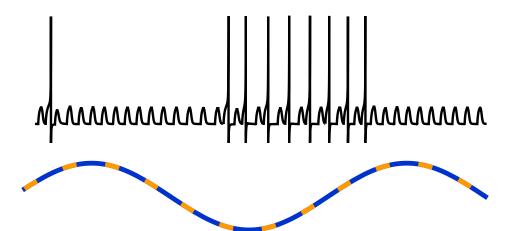
We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,

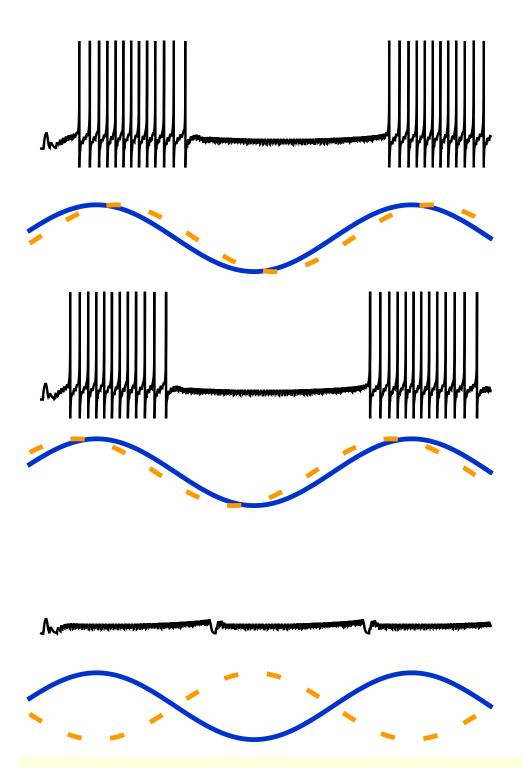
```
tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     \label{eq:vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,} \\
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagNAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

```
(*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
         inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
         inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
NANDout = Column[{
    Plot[Vo[t]/. solSyncNAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
     PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot [input1[t], input1[t]],
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 GoldenRatio)), Axes \rightarrow False],
    Plot[Vo[t]/. solAdvNAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
     PlotPoints \rightarrow 10000, PlotStyle \rightarrow {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
```

```
, Plot[{input1[t], inputAdv[t]},
   \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
      {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
   ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
 Plot[Vo[t]/. solLagNAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
   PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
   AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
 Plot[{input1[t], inputLag[t]},
  \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
      {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
   ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
 Plot[Vo[t]/. solAntiNAND, {t, 30, time}, ImageSize \rightarrow 500,
   PlotRange → {0, 140}, PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
  AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{ None}],
 Plot[{input1[t], inputAnti[t]},
   \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
      {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
   ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False
}]
```

Out[•]= $\{4, 4, 3.75, 3.75, -2.\}$





NOR

In[*]:= Ibias = {4, 4, 4.5, 4.5, -2.} solSyncAND = NDSolve[

```
{(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAntiAND = NDSolve
   {(*neuron e1*)
     Ve1 '[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
```

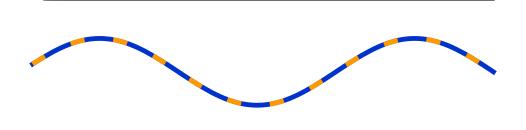
```
tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b]+
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,

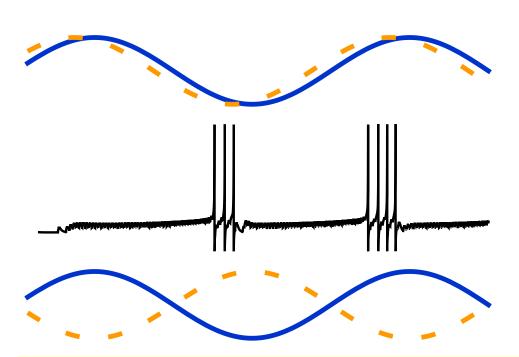
```
(*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + goSe1[t] + goSe2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagAND = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
```

```
tau Se2 '[t] == -Se2[t], Se2[0] == 0,
      WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
      (*neuron i1*)
      Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
      Vi1[0] == 0,
      Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
      tau Si1'[t] == -Si1[t], Si1[0] == 0,
      WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
      (*neuroni2*)
      Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
         inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
      Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
      tau Si2 '[t] == -Si2[t], Si2[0] == 0,
      WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
      (*neuron out*)
      Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
      Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
      WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
NOR2out = Column {
    Plot Vo[t] /. solSyncAND, {t, 30, time}, ImageSize \rightarrow 500, PlotRange \rightarrow {0, 140},
      PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], input1[t]},
      {t, 30, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
         \label{thm:constraints} $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}, Exclusions $\to None, $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}.
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
    Plot[Vo[t]/. solAdvAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
      PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
    , Plot[{input1[t], inputAdv[t]},
      \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         \label{thm:constraints} $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}, Exclusions $\to None, $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}.
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
```

```
Plot[Vo[t]/. solLagAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, Imag
                                                      PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
                                                      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
                                                 Plot[{input1[t], inputLag[t]},
                                                      {t, 30, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
                                                                  {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
                                                      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
                                                Plot[Vo[t]/. solAntiAND, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
                                                      PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
                                                      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
                                                Plot[{input1[t], inputAnti[t]},
                                                      \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                                                                  {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
                                                      ImageSize \rightarrow 500, AspectRatio \rightarrow (1 / (4 GoldenRatio)), Axes \rightarrow False
                                           }]
Out[ • ]=
                               \{4, 4, 4.5, 4.5, -2.\}
Out[ • ]=
```







AND

```
In[*]:= Ibias = {3.5, 3.5, 3.1, 3.1, -2.1}
                                solSyncAND = NDSolve
                                                      {(*neuron e1*)
                                                             \label{eq:Ve1[t]} $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1]], k, b] + $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[t]], k, b] + $$ Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[t]], k, b] + $$ Ve1'[t] == Fv[Ve1[t]], We1[t]][Ibias[t]], k, b] + $$ Ve1'[t] == Fv[Ve1[t]], We1[t]][Ibias[t]], k, b] + $$ Ve1'[t] == Fv[Ve1[t]], We1[t]][Ibias[t]], ve1'[t] == Fv[Ve1[t]], ve1'[t] == Fv[Ve1[t]
                                                                             input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
                                                             We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
                                                              tau Se1 '[t] == -Se1[t], Se1[0] == 0,
                                                             \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
                                                                      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
                                                             (*neuron e2*)
```

Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +

```
input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     \label{eq:whenevent_vi2[t] == 130, vi2[t] are c, wi2[t] are wi2[t] + d, Si2[t] are Si2[t] + 1}, \\
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
solAntiAND = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     \label{eq:Wellt} $$ WhenEvent[Vel[t] == 130, {Vel[t] \to c, Wel[t] \to Wel[t] + d, Sel[t] \to Sel[t] + 1}, $$
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
```

```
WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron i1*)
         Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
         Vi1[0] == 0,
         Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
          tau Si1'[t] == -Si1[t], Si1[0] == 0,
         WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuroni2*)
         Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
               inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
         Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
          tau Si2 '[t] == -Si2[t], Si2[0] == 0,
         \label{eq:whenevent_vi2[t] == 130, vi2[t] of c, wi2[t] of wi2[t] of vi2[t] of vi2[t]
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron out*)
          Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
         Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
         "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]\},
       {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
       \{t, 0, time\}, Method \rightarrow \{"TimeIntegration" \rightarrow "Adams"\}, Compiled \rightarrow True ;
solAdvAND = NDSolve
       {(*neuron e1*)
         Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
               input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
         We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
          tau Se1 '[t] == -Se1[t], Se1[0] == 0,
         WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron e2*)
         Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
         We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
          tau Se2 '[t] == -Se2[t], Se2[0] == 0,
         WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron i1*)
```

Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],

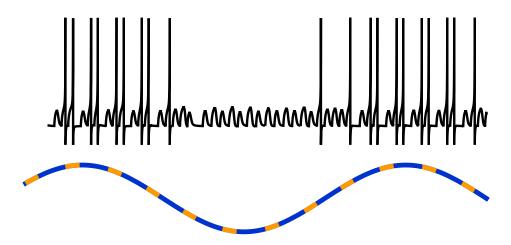
```
Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b]+
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    \{t, 0, time\}, Method \rightarrow {"TimeIntegration" \rightarrow "Adams"}, Compiled \rightarrow True|;
solLagAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
```

```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
             (*neuroni2*)
             Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
                    inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
             Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
             tau Si2 '[t] == -Si2[t], Si2[0] == 0,
             WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
                 "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
             (*neuron out*)
             Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
             Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
             WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
                "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
         {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
         \{t, 0, time\}, Method \rightarrow \{"TimeIntegration" \rightarrow "Adams"\}, Compiled \rightarrow True ;
ANDout = Column {
         Plot[Vo[t]/. solSyncAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
            AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
         Plot[{input1[t], input1[t]},
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                   {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
            ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
         Plot[Vo[t]/. solAdvAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
            AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
          , Plot[{input1[t], inputAdv[t]},
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                   {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
             ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
         Plot[Vo[t] /. solLagAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, Ima
             PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
            AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
         Plot[{input1[t], inputLag[t]},
             {t, 60, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
                   {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
             ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
         Plot[Vo[t]/. solAntiAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
```

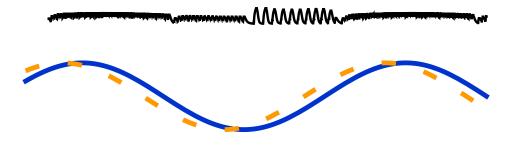
```
PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
 AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
Plot[{input1[t], inputAnti[t]},
 \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},\}
    {Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]}}, Exclusions \rightarrow None,
 ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False
```

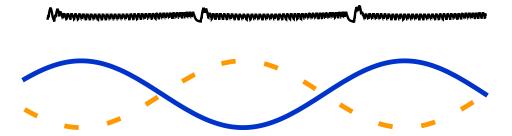
}]

Out[•]= $\{3.5, 3.5, 3.1, 3.1, -2.1\}$









OR

```
In[*]:= Ibias = {4, 4, 3.5, 3.5, -2.1}
      solSyncAND = NDSolve
          {(*neuron e1*)
           Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
              input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
           We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
           tau Se1'[t] == -Se1[t], Se1[0] == 0,
           \label{eq:Wellt} $$ WhenEvent[Vel[t] == 130, \{Vel[t] \to c, Wel[t] \to Wel[t] + d, Sel[t] \to Sel[t] + 1\}, $$
             "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
           (*neuron e2*)
           Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
           We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
           tau Se2 '[t] == -Se2[t], Se2[0] == 0,
```

```
WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron i1*)
         Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
         Vi1[0] == 0,
         Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
          tau Si1'[t] == -Si1[t], Si1[0] == 0,
         WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuroni2*)
         Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
         Vi2[0] == 0,
         Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
          tau Si2 '[t] == -Si2[t], Si2[0] == 0,
         \label{eq:whenevent_vi2[t] == 130, vi2[t] of c, wi2[t] of wi2[t] of vi2[t] of vi2[t]
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron out*)
          Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
         Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
         "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]\},
       {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
       \{t, 0, time\}, Method \rightarrow \{"TimeIntegration" \rightarrow "Adams"\}, Compiled \rightarrow True ;
solAntiAND = NDSolve
       {(*neuron e1*)
         Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
               input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
         We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
          tau Se1 '[t] == -Se1[t], Se1[0] == 0,
         WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron e2*)
         Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
         We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
          tau Se2 '[t] == -Se2[t], Se2[0] == 0,
         WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
            "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
         (*neuron i1*)
          Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
```

```
Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b]+
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
```

```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagAND = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1'[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
```

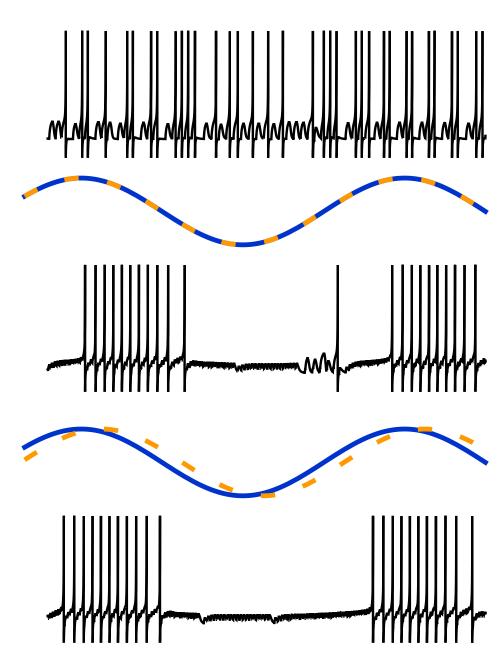
```
Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
      tau Si2 '[t] == -Si2[t], Si2[0] == 0,
      WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
        "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
      (*neuron out*)
      Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
      Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
      WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
        "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
ORout = Column
    Plot[Vo[t]/. solSyncAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
      PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], input1[t]},
      \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
    Plot[Vo[t] /. solAdvAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
      {\tt PlotPoints} \rightarrow {\tt 10\,000}, \, {\tt PlotStyle} \rightarrow \{\{{\tt Thickness[.005]}, \, {\tt Black}\}\},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
     , Plot[{input1[t], inputAdv[t]},
      {t, 60, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
    Plot[Vo[t]/. solLagAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
      {\tt PlotPoints} \rightarrow {\tt 10\,000}, \, {\tt PlotStyle} \rightarrow \{\{{\tt Thickness[.005]}, \, {\tt Black}\}\},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}|,
    Plot|{input1[t], inputLag[t]},
      \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
    Plot[Vo[t]/. solAntiAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
      PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot {input1[t], inputAnti[t]},
      {t, 60, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
```

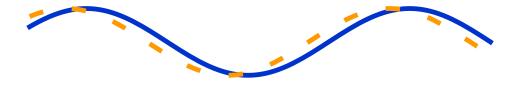
 $\label{eq:continuous} $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}, Exclusions $\to None, $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}.$ ImageSize \rightarrow 500, AspectRatio $\rightarrow \left(1/\left(4 \text{ GoldenRatio}\right)\right)$, Axes \rightarrow False]

}]

Out[•]= {4, 4, 3.5, 3.5, -2.1}

Out[0]=







XOR

```
In[*]:= Ibias = {2, 2, 2.5, 2.5, 1.1}
       solSyncAND = NDSolve
           {(*neuron e1*)
            Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
                input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
            We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
            tau Se1 '[t] == -Se1[t], Se1[0] == 0,
            \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
              "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
            (*neuron e2*)
            Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
                input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
            We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
             tau Se2 '[t] == -Se2[t], Se2[0] == 0,
            \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
              "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
            (*neuron i1*)
            Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
            Vi1[0] == 0,
            Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
            tau Si1'[t] == -Si1[t], Si1[0] == 0,
            \label{eq:Willing} WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, \, Wi1[t] \rightarrow Wi1[t] + d, \, Si1[t] \rightarrow Si1[t] + 1\},
```

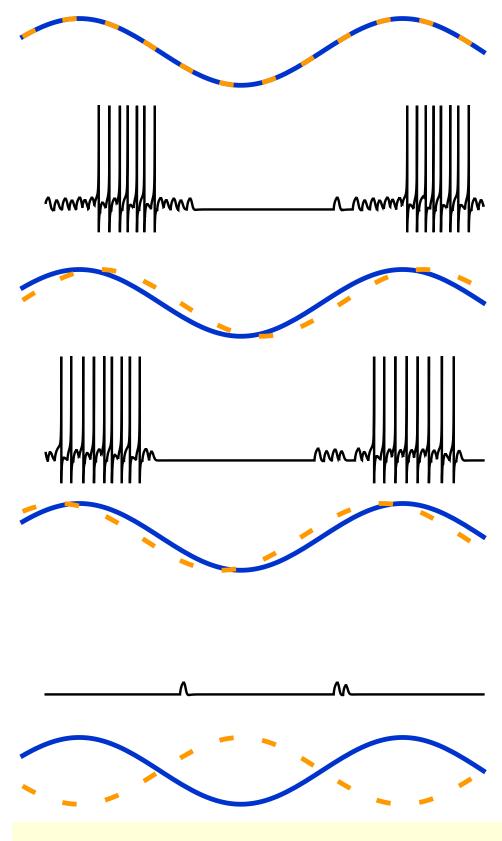
```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAntiAND = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1'[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
```

```
Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvAND = NDSolve
    \{(*neuron e1*)\}
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     \label{eq:WhenEvent} WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

```
(*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
solLagAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b]+
        inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
```

```
"DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
          {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
          {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
XORout = Column[{
          Plot Vo[t] /. solSyncAND, {t, 60, time}, ImageSize \rightarrow 500, PlotRange \rightarrow {0, 140},
             PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
          Plot[{input1[t], input1[t]},
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
             ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
          Plot[Vo[t]/. solAdvAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, Imag
              PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
           , Plot[{input1[t], inputAdv[t]},
             {t, 60, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
                    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
             ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
          Plot[Vo[t] /. solLagAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None}],
          Plot[{input1[t], inputLag[t]},
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
              ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
          Plot[Vo[t]/. solAntiAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
          Plot[{input1[t], inputAnti[t]},
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
              ImageSize \rightarrow 500, AspectRatio \rightarrow (1 / (4 GoldenRatio)), Axes \rightarrow False
      }]
{2, 2, 2.5, 2.5, 1.1}
```

Out[•]=



NIMP

```
In[*]:= Ibias = {1.5, 0, 2.5, 2.5, 2}
      solSyncAND = NDSolve
          {(*neuron e1*)
           Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b]+
               input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
           We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
            tau Se1 '[t] == -Se1[t], Se1[0] == 0,
           WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
             "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
           (*neuron e2*)
           Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
               input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
           We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
            tau Se2 '[t] == -Se2[t], Se2[0] == 0,
           WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuron i1*)
           Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
           Vi1[0] == 0,
           Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
           tau Si1'[t] == -Si1[t], Si1[0] == 0,
           WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuroni2*)
           Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
           Vi2[0] == 0,
           Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
            tau Si2 '[t] == -Si2[t], Si2[0] == 0,
           WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
           (*neuron out*)
           Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
           Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
           WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
             "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
          {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
          {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
```

solAntiAND = NDSolve

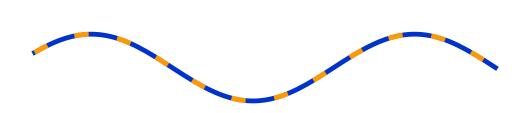
```
{(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvAND = NDSolve
   {(*neuron e1*)
     Ve1 '[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
```

```
tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagAND = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,

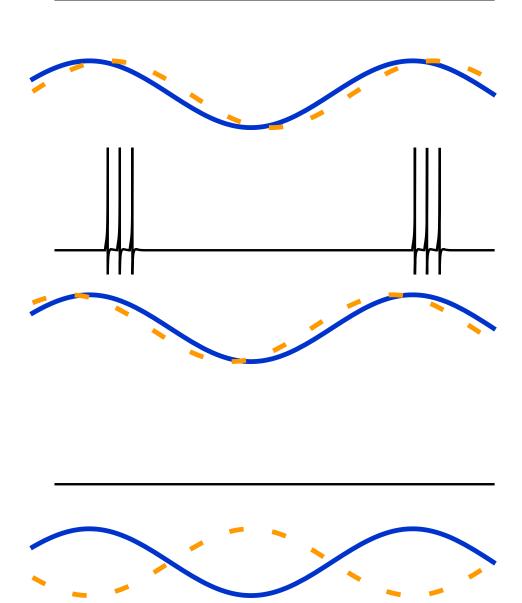
```
(*neuron e2*)
             Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
                    inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
             We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
             tau Se2 '[t] == -Se2[t], Se2[0] == 0,
             \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
                 "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
             (*neuron i1*)
             Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
             Vi1[0] == 0,
             Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
             tau Si1'[t] == -Si1[t], Si1[0] == 0,
             WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
                 "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
             (*neuroni2*)
             Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
                    inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
             Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
             tau Si2 '[t] == -Si2[t], Si2[0] == 0,
             WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
                "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
             (*neuron out*)
             Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
             Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
             WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
                 "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
         {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
         {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True;
NIMPout = Column[{
         Plot[Vo[t] /. solSyncAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
         Plot [input1[t], input1[t]],
             \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
                   {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
             ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 GoldenRatio)), Axes \rightarrow False],
         Plot[Vo[t]/. solAdvAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, ImageSize \rightarrow 500, Imag
             PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
             AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
```

```
, Plot[{input1[t], inputAdv[t]},
      \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
    Plot[Vo[t]/. solLagAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
      PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
      AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), Axes \rightarrow \text{None},
    Plot[{input1[t], inputLag[t]},
     \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
    Plot[Vo[t]/. solAntiAND, \{t, 60, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\},
      PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], inputAnti[t]},
      \{t, 60, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
         {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
      ImageSize \rightarrow 500, AspectRatio \rightarrow (1 / (4 GoldenRatio)), Axes \rightarrow False
   }]
\{1.5, 0, 2.5, 2.5, 2\}
```



Out[•]=

Out[•]=



IMP

In[*]:= Ibias = {3.0 - .01, 3.19, 3.5, 3.4, -0} solSyncNXOR = NDSolve

```
{(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[[1]], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     \label{eq:Wellt} WhenEvent[Vel[t] == 130, \{Vel[t] \rightarrow c, Wel[t] \rightarrow Wel[t] + d, Sel[t] \rightarrow Sel[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        input1[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2 '[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] + input1[t] + gii Si1[t] + gei Se2[t] + Ibias[4],
     Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAntiNXOR = NDSolve
   {(*neuron e1*)
     Ve1 '[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
```

We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,

```
tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, {Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAnti[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     \label{eq:whenevent} $$ WhenEvent[Ve2[t] == 130, {Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1}, $$
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAnti[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5]], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solAdvNXOR = NDSolve
    {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
```

```
(*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputAdv[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2 '[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
     tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
     tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
        inputAdv[t] + gii Si1[t] + gei Se2[t] + Ibias[[4]], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
     tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
      "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"],
     (*neuron out*)
     Vo '[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"]},
   {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
   {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
solLagNXOR = NDSolve
   {(*neuron e1*)
     Ve1'[t] == Fv[Ve1[t], We1[t]][Ibias[1], k, b] +
        input1[t] + gee Se2[t] + gie Si1[t] + Ibias[1], Ve1[0] == 0,
     We1'[t] == Fw[Ve1[t], We1[t]][a, b], We1[0] == 6,
     tau Se1 '[t] == -Se1[t], Se1[0] == 0,
     WhenEvent[Ve1[t] == 130, \{Ve1[t] \rightarrow c, We1[t] \rightarrow We1[t] + d, Se1[t] \rightarrow Se1[t] + 1\},
      "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron e2*)
     Ve2 '[t] == Fv[Ve2[t], We2[t]][Ibias[2], k, b] +
        inputLag[t] + gee Se1[t] + gie Si2[t] + Ibias[2], Ve2[0] == 0,
     We2'[t] == Fw[Ve2[t], We2[t]][a, b], We2[0] == 6,
```

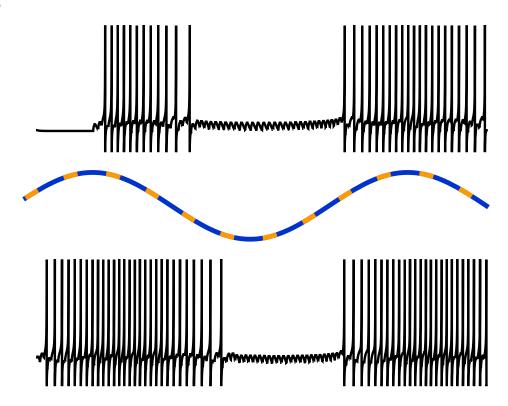
```
tau Se2 '[t] == -Se2[t], Se2[0] == 0,
     WhenEvent[Ve2[t] == 130, \{Ve2[t] \rightarrow c, We2[t] \rightarrow We2[t] + d, Se2[t] \rightarrow Se2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron i1*)
     Vi1'[t] == Fv[Vi1[t], Wi1[t]][Ibias[3], k, b] + input1[t] + gii Si2[t] + gei Se1[t] + Ibias[3],
     Vi1[0] == 0,
     Wi1'[t] == Fw[Vi1[t], Wi1[t]][a, b], Wi1[0] == 6,
      tau Si1'[t] == -Si1[t], Si1[0] == 0,
     WhenEvent[Vi1[t] == 130, \{Vi1[t] \rightarrow c, Wi1[t] \rightarrow Wi1[t] + d, Si1[t] \rightarrow Si1[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuroni2*)
     Vi2'[t] == Fv[Vi2[t], Wi2[t]][Ibias[4], k, b] +
         inputLag[t] + gii Si1[t] + gei Se2[t] + Ibias[4], Vi2[0] == 0,
     Wi2'[t] == Fw[Vi2[t], Wi2[t]][a, b], Wi2[0] == 6,
      tau Si2 '[t] == -Si2[t], Si2[0] == 0,
     WhenEvent[Vi2[t] == 130, \{Vi2[t] \rightarrow c, Wi2[t] \rightarrow Wi2[t] + d, Si2[t] \rightarrow Si2[t] + 1\},
       "DetectionMethod" → "Sign", "LocationMethod" → "LinearInterpolation"],
     (*neuron out*)
     Vo'[t] == Fv[Vo[t], Wo[t]][Ibias[5], k, b] + go Se1[t] + go Se2[t], Vo[0] == 0,
     Wo'[t] == Fw[Vo[t], Wo[t]][a, b], Wo[0] == 6,
     WhenEvent[Vo[t] == 130, \{Vo[t] \rightarrow c, Wo[t] \rightarrow Wo[t] + d\},
       "DetectionMethod" \rightarrow "Sign", "LocationMethod" \rightarrow "LinearInterpolation"]
    {Ve1, We1, Se1, Ve2, We2, Se2, Vi1, Wi1, Si1, Vi2, Wi2, Si2, Vo, Wo},
    {t, 0, time}, Method → {"TimeIntegration" → "Adams"}, Compiled → True|;
IMPout = Column|{
    Plot Vo[t] /. solSyncNXOR, {t, 30, time}, ImageSize \rightarrow 500, PlotRange \rightarrow {0, 140},
     PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    Plot[{input1[t], input1[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        \label{thm:constraints} $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}, Exclusions $\to None, $$\{$Thickness[.01], RGBColor[1, .6, 0], Dashing[\{.03, .06\}]\}$\}.
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False],
    Plot[Vo[t]/. solAdvNXOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
     PlotPoints → 10 000, PlotStyle → {{Thickness[.005], Black}},
     AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
    , Plot[{input1[t], inputAdv[t]},
     \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
        {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions → None,
     ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False,
```

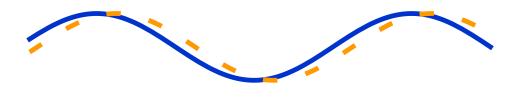
```
Plot[Vo[t]/. solLagNXOR, \{t, 30, time\}, ImageSize \rightarrow 500, PlotRange \rightarrow \{0, 140\}, 
 PlotPoints → 10000, PlotStyle → {{Thickness[.005], Black}},
 AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
Plot[{input1[t], inputLag[t]},
 {t, 30, time}, PlotStyle → {{Thickness[.01], RGBColor[0, .2, .8]},
    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
 ImageSize \rightarrow 500, AspectRatio \rightarrow \left(1/\left(4 \text{ GoldenRatio}\right)\right), Axes \rightarrow False],
Plot[Vo[t]/. solAntiNXOR, \{t, 30, time\}, ImageSize \rightarrow 500,
 PlotRange \rightarrow {0, 140}, PlotPoints \rightarrow 10000, PlotStyle \rightarrow {{Thickness[.005], Black}},
 AspectRatio \rightarrow (1/(2 \text{ GoldenRatio})), \text{ Axes } \rightarrow \text{None}],
Plot[{input1[t], inputAnti[t]},
 \{t, 30, time\}, PlotStyle \rightarrow \{\{Thickness[.01], RGBColor[0, .2, .8]\},
    {Thickness[.01], RGBColor[1, .6, 0], Dashing[{.03, .06}]}}, Exclusions \rightarrow None,
 ImageSize \rightarrow 500, AspectRatio \rightarrow (1/(4 \text{ GoldenRatio})), Axes \rightarrow False
```

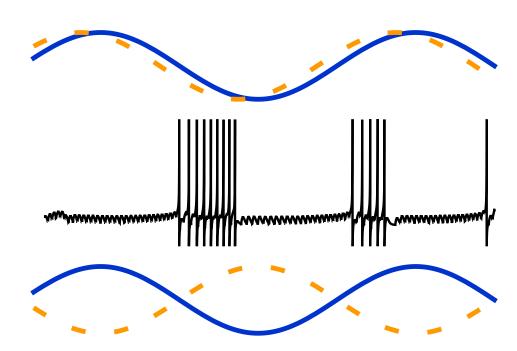
}]

Out[•]= $\{2.99, 3.19, 3.5, 3.4, 0\}$

Out[•]=







In[•]:= Export["/home/ns-cclolab/Desktop/OR.png", ORout] Export["/home/ns-cclolab/Desktop/XOR.png", XORout] Export["/home/ns-cclolab/Desktop/NOR.png", NOR2out] Export["/home/ns-cclolab/Desktop/NXOR.png", NXORout] Export["/home/ns-cclolab/Desktop/AND.png", ANDout] Export["/home/ns-cclolab/Desktop/NAND.png", NANDout] Export["/home/ns-cclolab/Desktop/IMP.png", IMPout] Export["/home/ns-cclolab/Desktop/NIMP.png", NIMPout]

Out[0]= /home/ns-cclolab/Desktop/OR.png

Out[•]= /home/ns-cclolab/Desktop/XOR.png

Out[•]= /home/ns-cclolab/Desktop/NOR.png

Out[•]=	/home/ns-cclolab/Desktop/NXOR.png
Out[•]=	/home/ns-cclolab/Desktop/AND.png
Out[•]=	/home/ns-cclolab/Desktop/NAND.png
Out[•]=	/home/ns-cclolab/Desktop/IMP.png
Out[•]=	/home/ns-cclolab/Desktop/NIMP.png