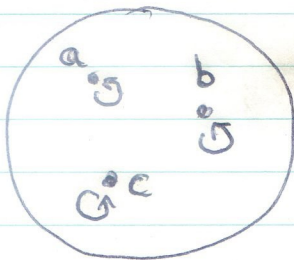


## Chapter 15

### 2) Discrete category



$C(a, -)$  objects

$$= C(a, a), C(a, b), C(a, c)$$

$$= \{Id_a, \{\}\}$$

$C(a, -)$  morphisms

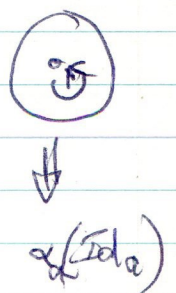
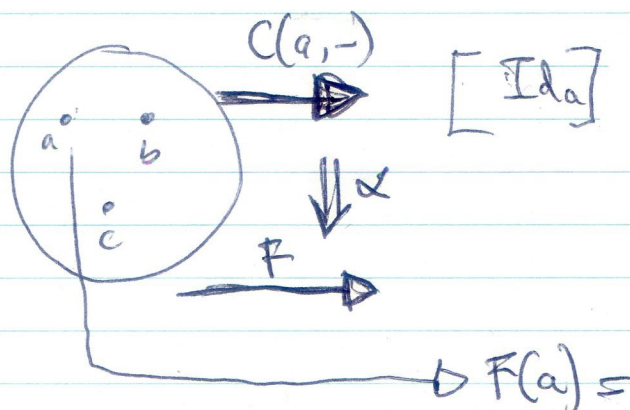
$$= C(a, Id_a), C(a, Id_b), C(a, Id_c)$$

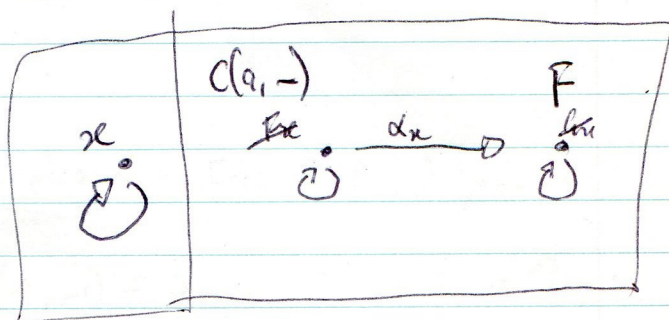
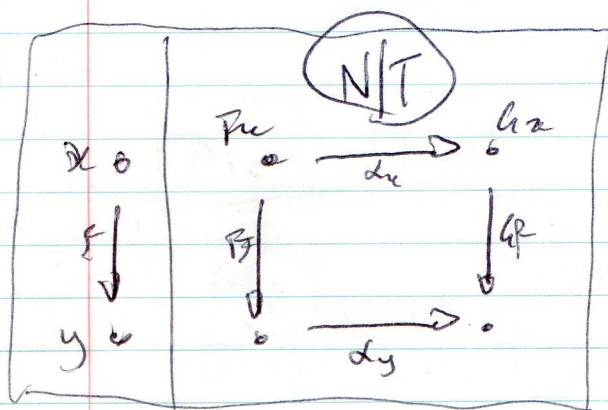
$$C(a, Id_a) = \left\{ Id_a \circ f : C(a, a) \rightarrow C(a, a) \right. \\ \left. \text{such that } f \in C(a, a) \right\}$$

$$= Id_a : C(a, a) \rightarrow C(a, a)$$

$$C(a, Id_b) = \{\}$$

$$C(a, Id_c) = \{\}$$





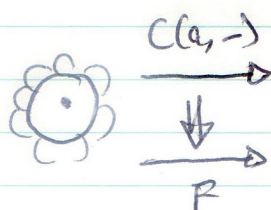
$$F(a) \cong \alpha_a (Id_a)$$

Monoid (Int)

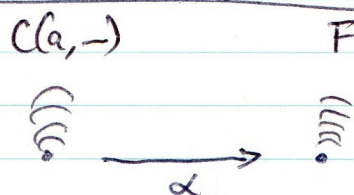
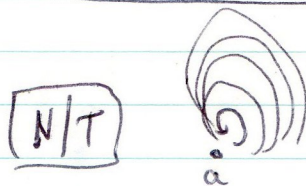


Morphisms =  $Id_a, f, f^2, f^3, \dots$

$$C(a, -) = \{ \downarrow \} = S$$



$$S \cong \mathbb{N}$$



$$F(a) \cong \{ \alpha(f^n) \}$$