

Problem Statement 1

Is gender independent of education level? A random sample of 395 people were surveyed and each person was asked to report the highest education level they obtained. The data that resulted from the survey is summarized in the following table:

High School Bachelors Masters Ph.d. Total

Female 60 54 46 41 201

Male 40 44 53 57 194

Total 100 98 99 98 395

Question: Are gender and education level dependent at 5% level of significance? In other words, given the data collected above, is there a relationship between the gender of an individual and the level of education that they have obtained?

```
In [7]: import scipy.stats as sts
        from scipy.stats import norm
        import math
        import numpy as np
        import pandas as pd

        lfemale = [60,54,46,41]
        lmale = [40,44,53,57]
        s = [40,60]
        b = [44,54]
        m = [53,46]
        p = [57,41]
        marks = lfemale + lmale

        sex = ['Male','Male','Male','Male','Female','Female','Female','Female']
```

```
edu = ['High School', 'Bachelors', 'Masters', 'Ph.d.', 'High School', 'Bachelors', 'Masters', 'Ph.d.']
df_edu = pd.DataFrame({"Sex":sex,"Edu":edu,"Marks":marks})

print(df_edu)
```

```
[60, 54, 46, 41, 40, 44, 53, 57]
      Edu  Marks  Sex
0  High School    60  Male
1    Bachelors    54  Male
2     Masters    46  Male
3       Ph.d.    41  Male
4  High School    40 Female
5    Bachelors    44 Female
6     Masters    53 Female
7       Ph.d.    57 Female
```

```
In [8]: df2 = pd.crosstab(df_edu.Sex, df_edu.Edu, df_edu.Marks, aggfunc="sum", margins=True)

df2.columns = ["Bachelors", "High School", "Masters", "Ph.d.", "row_totals"]
df2.index = ["Female", "Male", "col_totals"]

df2
```

Out[8]:

	Bachelors	High School	Masters	Ph.d.	row_totals
Female	44	40	53	57	194
Male	54	60	46	41	201
col_totals	98	100	99	98	395

```
In [9]: observed = df2.iloc[0:2,0:4] # Get table without totals for later use
observed
```

Out[9]:

	Bachelors	High School	Masters	Ph.d.
Female	44	40	53	57
Male	54	60	46	41

```
In [13]: expected = np.outer(df2["row_totals"][0:2],
                             df2.loc["col_totals"][0:4]) / 395.0
expected = pd.DataFrame(expected)
expected.columns = ["Bachelors", "High School", "Masters", "Ph.d."]
expected.index = ["Female", "Male"]
expected
```

```
Female    194
Male      201
Name: row_totals, dtype: int64
[[19012 19400 19206 19012]
 [19698 20100 19899 19698]]
```

Out[13]:

	Bachelors	High School	Masters	Ph.d.
Female	48.131646	49.113924	48.622785	48.131646
Male	49.868354	50.886076	50.377215	49.868354

```
In [14]: # We call .sum() twice: once to get the column sums and a second time to
         # add the column sums together, returning the sum of the entire 2D table
```

```
chi_squared_stat = (((observed-expected)**2)/expected).sum().sum()
print(chi_squared_stat)
```

```
8.006066246262538
```

```
In [29]: #The degrees of freedom for a test of independence equals the product of
         # the number of categories in each variable minus 1.
         #In this case we have a 2x4 table so df = 1x3 = 3.
```

```
critical = sts.chi2.ppf(q = 0.95, # Find the critical value for 95% confidence*
                        df = 3)  # *

print("Critical value", critical)

p_value = 1 - sts.chi2.cdf(x=chi_squared_stat, df=3) # Find the p-value
print("P value", p_value)

Critical value 7.8147279032511765
P value 0.04588650089174717
```

```
In [16]: sts.chi2_contingency(observed= observed)
```

```
Out[16]: (8.006066246262538,
          0.045886500891747214,
          3,
          array([[48.13164557, 49.11392405, 48.62278481, 48.13164557],
                 [49.86835443, 50.88607595, 50.37721519, 49.86835443]]))
```

The output shows the chi-square statistic = 8, the p-value as 0.045 and the degrees of freedom as 3 followed by the expected counts. The critical value with 3 degree of freedom is 7.815. Since $8.006 > 7.815$, therefore we reject the null hypothesis and conclude that the education level depends on gender at a 5% level of significance.

Problem Statement 2:

Using the following data, perform a oneway analysis of variance using $\alpha=.05$. Write up the results in APA format.

[Group1: 51, 45, 33, 45, 67] [Group2: 23, 43, 23, 43, 45] [Group3: 56, 76, 74, 87, 56]

```
In [28]: Group1 = [51, 45, 33, 45, 67]
```

```

Group2 = [23, 43, 23, 43, 45]
Group3 = [56, 76, 74, 87, 56]

# ANOVA Test
statistic, pvalue = sts.f_oneway(Group1,Group2,Group3)

print("F Statistic value {} , p-value {}".format(statistic,pvalue))

if pvalue < 0.05:
    print('\nTrue')
else:
    print('\nFalse')

print("\nThe test result suggests the groups don't have the same sample means in this case, since the p-value is significant at a 99% confidence level. Here the p-value returned is 0.00305 which is < 0.05")

```

F Statistic value 9.747205503009463 , p-value 0.0030597541434430556

True

The test result suggests the groups don't have the same sample means in this case, since the p-value is significant at a 99% confidence level. Here the p-value returned is 0.00305 which is < 0.05

Problem Statement 3:

Calculate F Test for given 10, 20, 30, 40, 50 and 5,10,15, 20, 25. For 10, 20, 30, 40, 50:

```

In [27]: grp1 = [10, 20, 30, 40, 50]
         grp2 = [5,10,15, 20, 25]

         mean_1 = np.mean(grp1)
         mean_2 = np.mean(grp2)

         sum_grp1 = 0
         sum_grp2 = 0

```

```
for items in grp1:
    sum_grp1 += (items - mean_1)**2

for items in Group2:
    sum_grp2 += (items - mean_2)**2

var1 = sum_grp1/(len(grp1)-1)
var2 = sum_grp2/(len(grp2)-1)

F_Test = var1/var2

print("F Test for given 10, 20, 30, 40, 50 and 5, 10, 15, 20, 25 is : "
      ,F_Test)

F Test for given 10, 20, 30, 40, 50 and 5, 10, 15, 20, 25 is : 4.0
```