Problem Statement 1:

In each of the following situations, state whether it is a correctly stated hypothesis testing problem and why?

1. H0: μ = 25, H1: $\mu \neq$ 25

Yes, because values in both statement are about population or distribution, have equal values and has inequality in null hypothesis.

2. $H0: \sigma > 10, H1: \sigma = 10$

No, because null hypothesis has an eqaulity claim and alternate hypothesis has inequality.

3. *H*0: x = 50, *H*1: $x \neq 50$

No, because hypothesis is stated in terms of statistics and not sample data

4. H0: p = 0.1, H1: p = 0.5

No, because values in both hypothesis is different and has equal sign.

5. H0: s = 30, H1: s > 30

No, because hypothesis are always statements about population or distribution and not about sample

Problem Statement 2:

The college bookstore tells prospective students that the average cost of its textbooks is Rs. 52 with a standard deviation of Rs. 4.50. A group of smart statistics students thinks that the average cost is higher. To test the bookstore's claim against their alternative, the students will select a random sample of size 100. Assume that the mean from their random sample is Rs. 52.80. Perform a hypothesis test at the 5% level of significance and state your decision.

```
In [2]: from scipy.stats import norm
        import numpy as np
        import math
        import scipy.stats as stats
        from scipy.stats import chi2 contingency
        pop mean = 52
        pop std = 4.50
        n = 100
        sam mean = 52.80
        # Significance value
        alpha=0.05
        #standard Error
        SE = pop std/n**0.5
        Z = (sam mean - pop mean)/SE
        print("Z score is:",Z)
        print("Critical region is ", norm.ppf(alpha/2), -norm.ppf(alpha/2))
        print("\n Z score is less than critical value so we accept null hypothe
        sis")
```

```
Z score is: 1.777777777775
Critical region is -1.9599639845400545 1.9599639845400545
```

Z score is less than critical value so we accept null hypothesis

Problem Statement 3:

A certain chemical pollutant in the Genesee River has been constant for several years with mean μ = 34 ppm (parts per million) and standard deviation σ = 8 ppm. A group of factory representatives whose companies discharge liquids into the river is now claiming that they have lowered the average with improved filtration devices. A group of environmentalists will test to see

if this is true at the 1% level of significance. Assume \ that their sample of size 50 gives a mean of 32.5 ppm. Perform a hypothesis test at the 1% level of significance and state your decision

```
In [7]: pop_mean = 34
    pop_std = 8
    n = 50
    sam_mean = 32.5
# Significance value
    alpha=0.01
#standard Error
SE = pop_std/n**0.5

Z = (sam_mean-pop_mean)/SE
    print("Z score is: ",Z)
    print("Critical region is ",norm.ppf(alpha/2), -norm.ppf(alpha/2))
    print("\n Z score is less than critical value so we accept null hypothe sis")
```

Z score is: -1.3258252147247767 Critical region is -2.575829303548901 2.575829303548901

Z score is less than critical value so we accept null hypothesis

Problem Statement 4:

Based on population figures and other general information on the U.S. population, suppose it has been estimated that, on average, a family of four in the U.S. spends about \$1135 annually on dental expenditures. Suppose further that a regional dental association wants to test to determine if this figure is accurate for their area of country. To test this, 22 families of 4 are randomly selected from the population in that area of the country and a log is kept of the family's dental expenditure for one year. The resulting data are given below. Assuming, that dental expenditure is normally distributed in the population, use the data and an alpha of 0.5 to test the dental association's hypothesis.

1008, 812, 1117, 1323, 1308, 1415, 831, 1021, 1287, 851, 930, 730, 699, 872, 913, 944, 954, 987, 1695, 995, 1003, 994

t_Score is -2.070747228595759 Critical Region is -0.6863519891164291 0.6863519891164291

t score is greater than critical value so we reject null hypothesis

Problem Statement 5:

In a report prepared by the Economic Research Department of a major bank the Department manager maintains that the average annual family income on Metropolis is $48,\,$

432. What doyou conclude about the validity of the report if a random sample of 40 with a standard deviation of 2000?

```
Z = (sam_mean-pop_mean)/SE
alpha=0.05
print("Z score is: ",Z)
print("Critical region is ", norm.ppf(alpha/2), -norm.ppf(alpha/2))
print("\n Z score is less than critical value so we accept null hypothe sis")
```

Z score is: 1.42 Critical region is -1.9599639845400545 1.9599639845400545

Z score is less than critical value so we accept null hypothesis

Problem Statement 6:

Suppose that in past years the average price per square foot for warehouses in the United States has been 32.28. A national real estate investor wants to determine whether that figure has changed now. The investor hires a researcher who randomly samples 19 warehouses that are for sale across the United States and finds that the mean price per square foot is 31.67, with a standard deviation of 1.29. assume that the prices of warehouse footage are normally distributed in population. If the researcher uses a 5% level of significance, what statistical conclusion can be reached? What are the hypotheses?

```
print("\n t score is within critical value so we accept null hypothesis")

Null hypothesis: H0:µ = 32.28
Alternative hypothesis: H1:µ ≠ 32.28
t_score is -2.1
Critical region is -2.1 2.1
```

t score is within critical value so we accept null hypothesis

Problem Statement 7:

Fill in the blank spaces in the table and draw your conclusions from it. image.png

```
In [25]: # Calculate Beta at Mu1 = 52
         n = 10
         Sig = 2.5
         Mu1 = 52
         a = (48.5 - Mu1)/(Sig/math.sgrt(n))
         b = (51.5 - Mu1)/(Sig/math.sgrt(n))
         \# As b > a, so our z score lies in between these two b < z < a.
         # probability at these z score
         P11 = 0
         P12 = 0.2643
         Betal1 = P12 - P11
         print("Beta at Mu1 = 52 is : ",Betall)
         # Calculate Beta at Mu2 = 50.5
         n1 = 10
         Sig = 2.5
         Mu2 = 50.5
```

```
c = (48.5 - Mu2)/(Sig/math.sqrt(n1))
         d = (51.5 - Mu2)/(Sig/math.sqrt(n1))
         \# z score lies in between these two c < z < d.
         # probability at these z score
         P13 = 0.0057
         P14 = 0.8962
         # now Beta = p13 + (1 - p14)
         Beta12 = P13 + (1 - P14)
         print("Beta at Mu2 = 50.5 is : ",Beta12)
         Beta at Mu1 = 52 is : 0.2643
         Beta at Mu2 = 50.5 is : 0.1095
In [26]: # Calculate Beta at Mu1 = 52
         n2 = 10
         Sig = 2.5
         Mu1 = 52
         a = (48.0 - Mu1)/(Sig/math.sqrt(n2))
         b = (51.0 - Mu1)/(Sig/math.sqrt(n2))
         \# As p22 > p21, so our z score lies in between these two b < z < a.
         # Find probability at these z score
         P21 = 0
         P22 = 0.1038
         \# now Beta = p22 - p21
         Beta21 = P22 - P21
         print("Beta at Mu2 = 52 is : ",Beta21)
         # Calculate Beta at Mu2 = 50.5
         n2 = 10
         Sig = 2.5
         Mu2 = 50.5
         c = (48 - Mu2)/(Sig/math.sqrt(n2))
```

```
d = (51 - Mu2)/(Sig/math.sqrt(n2))
         # so our z score lies in between these two c < z < d.
         # Find probability at these z score
         P23 = 0.0008
         P24 = 0.7357
         \# now Beta = p13 +(1 - p14)
         Beta22 = P23 + (1 - P24)
         print(f"Beta at Mu2 = 50.5 is : {Beta22}")
         Beta at Mu2 = 52 is : 0.1038
         Beta at Mu2 = 50.5 is : 0.2651
In [27]: # Calculate Beta at Mu1 = 52
         n3 = 16
         Sig = 2.5
         Mu1 = 52
         a = (48.81 - Mu1)/(Sig/math.sqrt(n3))
         b = (51.9 - Mu1)/(Sig/math.sqrt(n3))
         # so our z score lies in between these two a < z < b.
         # Find probability at these z score
         P31 = 0.4364
         P32 = 0
         \# now Beta = p31 - p32
         Beta31 = P31 - P32
         print("Beta at Mu2 = 52 is : ",Beta31)
         # Calculate Beta at Mu2 = 50.5
         n3 = 16
         Sig = 2.5
         Mu2 = 50.5
         c = (48.81 - Mu2)/(Sig/math.sqrt(n3))
         d = (51.9 - Mu2)/(Sig/math.sqrt(n3))
         # so our z score lies in between these two c < z < 1- d.
         # Find probability at these z score
```

```
P33 = 0.0032
         P34 = 0.9875
         \# now Beta = P33 + 1- P34
         Beta32 = P33 + 1 - P34
         print("Beta at Mu2 = 50.5 is : ",Beta32)
         Beta at Mu2 = 52 is : 0.4364
         Beta at Mu2 = 50.5 is : 0.015700000000000047
In [28]: # Calculate Beta at Mu1 = 52
         n4 = 16
         Sig = 2.5
         Mu1 = 52
         a = (48.42 - Mu1)/(Sig/math.sqrt(n4))
         b = (51.58 - Mu1)/(Sig/math.sqrt(n4))
         # As P42> P41, so our z score lies in between these two b < z < a.
         # Find probability at these z score
         P41 = 0.0
         P42 = 0.2514
         \# now Beta = p31 - p32
         Beta41 = P42 - P41
         print(f"Beta at Mu2 = 52 is : {Beta41}")
         # Calculate Beta at Mu2 = 50.5
         n4 = 16
         Sig = 2.5
         Mu2 = 50.5
         c = (48.42 - Mu2)/(Sig/math.sqrt(n4))
         d = (51.58 - Mu2)/(Sig/math.sqrt(n4))
         # so our z score lies in between these two c < z < 1- d.
         # Find probability at these z score
         P43 = 0.0035
         P44 = 0.9875
         # now Beta = P43 + 1 - P44
```

```
Beta42 = P43 +(1 - P44)

print("Beta at Mu2 = 50.5 is : ",Beta42)

Beta at Mu2 = 52 is : 0.2514

Beta at Mu2 = 50.5 is : 0.01599999999999955
```

Problem Statement 8:

Find the t-score for a sample size of 16 taken from a population with mean 10 when the sample mean is 12 and the sample standard deviation is 1.5.

```
In [30]: n = 16
    pop_mean = 10
    sample_mean =12
    sample_std =1.5

SE = sample_std/(n**0.5)
    t = (sample_mean-pop_mean)/SE
    print("t_score is ",round((t),1))
```

Problem Statement 9:

t score is 5.3

Find the t-score below which we can expect 99% of sample means will fall if samples of size 16 are taken from a normally distributed population.

Problem Statement 10:

If a random sample of size 25 drawn from a normal population gives a mean of 60 and a standard deviation of 4, find the range of t-scores where we can expect to find the middle 95% of all sample means. Compute the probability that (-t0.05 < t < t0.10).

Range is: 61.651118849302414 58.348881150697586

```
In [33]: p=stats.t.cdf(0.1,df=24)-stats.t.cdf(-0.05,df=24)

print("probability that (-t0.05 < t < t0.10) is ",p)

probability that (-t0.05 < t < t0.10) is 0.05914441613731247
```

Problem Statement 11:

Two-tailed test for difference between two population means Is there evidence to conclude that the number of people travelling from Bangalore to Chennai is different from the number of people travelling from Bangalore to Hosur in a week, given the following: Population 1: Bangalore to Chennai $n1 = 1200 \times 1 = 452 \times 1 = 212 \times 1200 \times 120$

```
alpha=0.05
se=((std1/n1)+(std2/n2))**0.5
z_score=(x1-x2)/se
print("Z_Score is ",z_score)
print("Critical region is ",norm.ppf(alpha/2),-norm.ppf(alpha/2))
print("\nFrom above we can conclude that we reject null hypothesis sinc e it lies within critical region at alpha=5%")
```

```
Z_Score is -7.926428526759299
Critical region is -1.9599639845400545 1.9599639845400545
```

From above we can conclude that we reject null hypothesis since it lies within critical region at alpha=5%

Problem Statement 12:

Is there evidence to conclude that the number of people preferring Duracell battery is different from the number of people preferring Energizer battery, given the following: Population 1: Duracell $n1 = 100 \times 1 = 308 \times 1 = 84$ Population 2: Energizer $n2 = 100 \times 2 = 254 \times 2 = 67$

```
ll battery is different from the number of people preferring Energizer
battery.")
```

```
Z_Score is 5.025702668336442
Critical region is -1.9599639845400545 1.9599639845400545
```

From above we can conclude that we reject null hypothesis since it lies within critical region. So, number of people preferring Duracell battery is different from the number of people preferring Energizer battery.

Problem Statement 13:

Pooled estimate of the population variance Does the data provide sufficient evidence to conclude that average percentage increase in the price of sugar differs when it is sold at two different prices? Population 1: Price of sugar = Rs. 27.50 n1 = 14 x1 = 0.317% s1 = 0.12% Population 2: Price of sugar = Rs. 20.00 n2 = 9 x2 = 0.21% s2 = 0.11%

```
In [19]: n1 = 14
         x1 = 0.317
         s1 = 0.12
         n2 = 9
         x2 = 0.21
         s2 = 0.11
         s 1=s1**2
         s 2=s2**2
         s=((n1-1)*s 1)+((n2-1)*s 2)
         n=(n1+n2-2)
         se=(s/n)**0.5
         n 1=((1/n1)+(1/n2))**0.5
         t score=(x1-x2)/se*n 1
         print("t score is ",t score)
         print("Critical Region is ",stats.t.ppf(1-0.05,df=n))
         print("\n We accept null hypothesis at alpha=5%. So, average price do no
         t increase")
```

t_score is 0.3931089218182991 Critical Region is 1.7207429028118775 We accept null hypothesis at alpha=5%. So, average price do not increas e

Problem Statement 14:

The manufacturers of compact disk players want to test whether a small price reduction is enough to increase sales of their product. Is there evidence that the small price reduction is enough to increase sales of compact disk players? Population 1: Before reduction $n1 = 15 \times 1 =$

```
In [21]: n1 = 15
         x1 = 6598
         s1 = 844
         n2 = 12
         x2 = 6870
         s2 = 669
         s 1=s1**2
         s 2=s2**2
         s=((n1-1)*s 1)+((n2-1)*s 2)
         n=(n1+n2-2)
         se=(s/n)**0.5
         n = ((1/n1) + (1/n2))**0.5
         t score=(x1-x2)/se*n 1
         print("t score is ",t score)
         print("Critical Region is ",stats.t.ppf(0.05,df=n))
         print("\nWe accept null hypothesis at alpha=5%.So average price remains
         same")
```

t_score is -0.1364745051598569 Critical Region is -1.708140761251899

We accept null hypothesis at alpha=5%. So average price remains same

Problem Statement 15:

Comparisons of two population proportions when the hypothesized difference is zero Carry out a two-tailed test of the equality of banks' share of the car loan market in 1980 and 1995.

Population 1: 1980 n1 = 1000 x1 = 53 p 1 = 0.53 Population 2: 1985 n2 = 100 x2 = 43 p 2= 0.53

```
Z_score is 0.0
Critical region is -1.6448536269514729
```

We reject null hypothesis as Z score is above critical region.

Problem Statement 16:

Carry out a one-tailed test to determine whether the population proportion of traveler's check buyers who buy at least \$2500 in checks when sweepstakes prizes are offered as at least 10% higher than the proportion of such buyers when no sweepstakes are on. Population 1: With sweepstakes n1 = 300 x1 = 120 p = 0.40 Population 2: No sweepstakes n2 = 700 x2 = 140 p 2= 0.20

Z_score is 3.303749523611152 Critical region is 1.6448536269514729

We reject null hypothesis at alpha=5%

Problem Statement 17:

A die is thrown 132 times with the following results: Number turned up: 1, 2, 3, 4, 5, 6 Frequency: 16, 20, 25, 14, 29, 28 Is the die unbiased? Consider the degrees of freedom as p - 1.

```
In [29]: obs= [16, 20, 25, 14, 29, 28]
    exp= [22,22,22,22,22,22]
    result=stats.chisquare(obs,exp)
    print("Chi square value is",result[0])
    print("p-value is",result[1])
    print('Dice is unbiased.')
```

Chi square value is 9.0 p-value is 0.1090641579497725 Dice is unbiased.

Problem Statement 18:

In a certain town, there are about one million eligible voters. A simple random sample of 10,000 eligible voters was chosen to study the relationship between gender and participation in the last election. The results are summarized in the following 2X2 (read two by two) contingency table:

download.png

We would want to check whether being a man or a woman (columns) is independent of having voted in the last election (rows). In other words, is "gender and voting independent"?

```
In [37]: observed voted men=2792
         observed voted women=3591
         observed not voted men=1486
         observed not voted women=2131
         total voted=2792+3591
         total not voted=1486+2131
         total men=2792+1486
         total women=3591+2131
         expected voted men=(total voted*total men)/10000
         expected voted women=(total voted*total women)/10000
         expected not voted men=(total not voted*total men)/10000
         expected not voted women=(total not voted*total women)/10000
         chisquare1=(((observed voted women-expected voted women)**2)/expected v
         oted women)
         chisquare2=(((observed voted men-expected voted men)**2)/expected voted
          men)
         chisquare3=(((observed not voted men-expected not voted men)**2)/expect
         ed not voted men)
         chisquare4=(((observed not voted women-expected not voted women)**2)/ex
         pected not voted women)
         chisquare=chisquare1+chisquare2+chisquare3+chisquare4
         print("Chi Square value is ",chisquare)
         print("Critical region with alpha=0.05 is 3.84")
         print("We reject null hypothesis.It is not gender and voting independen
```

Chi Square value is 6.660455899328067 Critical region with alpha=0.05 is 3.84 We reject null hypothesis. It is not gender and voting independent

Problem Statement 19:

A sample of 100 voters are asked which of four candidates they would vote for in an election. The number supporting each candidate is given below:image.pngDo the data suggest that all candidates are equally popular? [Chi-Square = 14.96,with $3 \, df$, p 0.05.]

image.png

```
In [38]: #print(np.mean([41,19,24,16]))
    obs=[41,19,24,16]
    exp=[25,25,25,25]
    result=stats.chisquare(obs,exp)
    print("Chi Square value is ",result[0])
    print("Critical region with 3df and alpha=0.05 is 7.82")
    print("We reject null hypothesis. All candidates are not equally popula
    r")
```

Problem Statement 20:

Children of three ages are asked to indicate their preference for three photographs of adults. Do the data suggest that there is a significant relationship between age and photograph preference? What is wrong with this study? [Chi-Square = 29.6, with 4 df: p < 0.05].

image.png

```
In [39]: obs=([[18,22,20],[2,28,40],[20,10,40]])
    result=chi2_contingency(obs)
    print("Chi Square value is ",result[0])
    print("Critical region with 4df and alpha=0.001 is 18.47")
```

print("We reject null hypothesis.There is significant relationship betw een age and photograph preference")

Chi Square value is 29.603174603174608 Critical region with 4df and alpha=0.001 is 18.47 We reject null hypothesis. There is significant relationship between age and photograph preference

Problem Statement 21:

A study of conformity using the Asch paradigm involved two conditions: one where one confederate supported the true judgement and another where no confederate gave the correct response.

image.png

Is there a significant difference between the "support" and "no support" conditions in the frequency with which individuals are likely to conform? [Chi-Square = 19.87, with 1 df: p < 0.05]

```
In [40]: obs=np.array([[18,40],[32,10]])
    result=chi2_contingency(obs)
    print("Chi Square value is", result[0])
    print("Critical region with 1df and alpha=0.001 is 10.83")
    print("We reject null hypoythesis.So,there is significant difference be tween the 'support' and 'no support' conditions in the frequency with w hich individuals are likely to conform")
```

Chi Square value is 18.10344827586207 Critical region with 1df and alpha=0.001 is 10.83 We reject null hypoythesis.So,there is significant difference between the 'support' and 'no support' conditions in the frequency with which in dividuals are likely to conform

Problem Statement 22:

We want to test whether short people differ with respect to their leadership qualities (Genghis Khan, Adolf Hitler and Napoleon were all stature-deprived, and how many midget MP's are

there?) The following table shows the frequencies with which 43 short people and 52 tall people were categorized as "leaders", "followers" or as "unclassifiable". Is there a relationship between height and leadership qualities? [Chi-Square = 10.71, with 2 df: p < 0.01]. \geqslant image.png

```
In [41]: obs=([[12,32],[22,14],[9,6]])
    result=chi2_contingency(obs)
    print("Chi Square value is", result[0])
    print("Critical region with 2df and alpha=0.001 is 13.82")
    print("We accept null hypothesis.there is no relationship between heigh
    t and leadership qualities")
```

Chi Square value is 10.712198008709638 Critical region with 2df and alpha=0.001 is 13.82 We accept null hypothesis.there is no relationship between height and leadership qualities

Problem Statement 23:

Each respondent in the Current Population Survey of March 1993 was classified as employed, unemployed, or outside the labor force. The results for men in California age 35- 44 can be cross-tabulated by marital status, as follows:

```
image.png
```

Men of different marital status seem to have different distributions of labor force status. Or is this just chance variation? (you may assume the table results from a simple random sample.)

```
In [43]: obs = np.array([[679,103,114], [63,10,20],[42,18,25]])
    result=chi2_contingency(obs)
    print("Chi Square value is ",result[0])
    print("Critical region with 4df and alpha=0.001 is 18.47")
    print("We reject null hypothesis at alpha=0.001, there is relationship
    between martial status and employment status")
```

Chi Square value is 31.61310319407798

Critical region with 4df and alpha=0.001 is 18.47 We reject null hypothesis at alpha=0.001, there is relationship between martial status and employment status