

Chomsky hierarchy



→ Based on the format of production, Chomsky classified the Grammar into 4 types.

- ① Type (0) or REG
- ② Type (1) or CSG
- ③ Type (2) or CFG
- ④ Type (3) or RG

Type-0 Grammar - Recursive ~~enumerable~~ enumerable
grammar / unrestricted grammar

→ used to generate Recursive enumerable
Language (REL) which is accepted by
Turing Machine (T.M)

The Grammar G is said to be
Type (0) or REG if the
production is in the form

$\alpha \rightarrow \beta$ ~~$\alpha \rightarrow \beta$~~

$$\alpha \in (V+T)^* V (V+T)^*$$

$$\beta \in (V+T)^*$$

Type-1 Grammar - Context sensitive grammar /

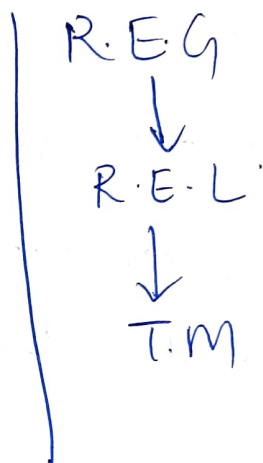
length increasing grammar

→ It generates context sensitive language
which is accepted by Linear bounded
Automata (LBA)

→ The Grammar G is said to be Type (1)
or CSG, if the production is in the form

$\alpha \rightarrow \beta$

$|\alpha| \leq |\beta|$ (Length of α is less than or equal to β)



$$\alpha \in (V+T)^* V (V+T)^*$$

$$\beta \in (V+T)^+ \left\{ \beta \neq \epsilon \right\}$$

$$A \alpha B \rightarrow b b \quad \times$$

$$A a \rightarrow b b \quad \checkmark$$

Note: In CSG we do not have any ~~production~~ production to generate empty string ϵ . i.e. the Language which is generated by CSG does not contain ϵ .

Type-2 Grammar - Context Free Grammar

→ It generates Context Free Language which is accepted by push down automata.

→ The Grammar G is said to be Type(2) or CF if the production is in the form

$$\alpha \rightarrow \beta$$

$\alpha \in V, |\alpha| = 1$ no. of variable will be

$$\beta \in (V+T)^*$$

So at LHS only one variable, but at RHS no restriction.

Type-3 Grammar



Type-3 Grammar - Regular Grammar

→ It generates regular language which is accepted by finite automata.

Left Linear Grammar

$$A \rightarrow a | Ba$$

$$A, B \in V, |A| = |B| = 1$$

$$a \in T^*$$

Right Linear Grammar

$$A \rightarrow a | aB$$

$$A, B \in V, |A| = |B| = 1$$

$$a \in T^*$$

RG



RL



FA