

Assignment #4

Math 1P05

Michael W., 6402176

27 Nov

1. a) $f(t) = t + 2 \cos t, -2\pi \leq t \leq 2\pi$

i) domain: $(-2\pi, 2\pi)$

ii) No VA or HA

iii-vi) $f' = 1 - 2 \sin t$

$$0 = 1 - \sin t$$

$$-2 \sin t = -1$$

$$\sin t = \frac{1}{2}$$

$$t = \frac{\pi}{6}, t = \frac{5\pi}{6}, t = -\frac{11\pi}{6}, t = -\frac{7\pi}{6}$$

$f'(t)$	$t = -2\pi$	$-2\pi < t < -\frac{\pi}{6}$	$t = -\frac{4\pi}{6}$	$-\frac{4\pi}{6} < t < -\frac{\pi}{6}$
Sign behavior	NA	+	0	0

$t = -\frac{3\pi}{6}$	$-\frac{7\pi}{6} < t < \frac{\pi}{6}$	$\frac{\pi}{6}$	$\frac{\pi}{6} < t < \frac{5\pi}{6}$
0	+	0	-

$5\pi/6$	$5\pi/6 < t < 2\pi$	2π
0	+	NA

$$f(-2\pi) = -2\pi + 2\cos(-2\pi)$$

$$= -2\pi + 2$$

\therefore Minimum $(-2\pi, -2\pi + 2)$

$$f\left(-\frac{11\pi}{6}\right) = -\frac{11\pi}{6} + 2\cos\left(-\frac{11\pi}{6}\right)$$

$$= -\frac{11\pi}{6} + \sqrt{3}$$

\therefore Maximum $\left(-\frac{11\pi}{6}, -\frac{11\pi}{6} + \sqrt{3}\right)$

$$f\left(-\frac{7\pi}{6}\right) = -\frac{7\pi}{6} + 2\cos\left(-\frac{7\pi}{6}\right)$$

$$= -\frac{7\pi}{6} - \sqrt{3}$$

\therefore Minimum $\left(-\frac{7\pi}{6}, -\frac{7\pi}{6} - \sqrt{3}\right)$

$$f\left(\frac{\pi}{6}\right) = \frac{\pi}{6} + 2\cos\left(\frac{\pi}{6}\right)$$

$$= \frac{\pi}{6} + \sqrt{3}$$

\therefore Maximum $\left(\frac{\pi}{6}, \frac{\pi}{6} + \sqrt{3}\right)$

$$f\left(\frac{5\pi}{6}\right) = \frac{5\pi}{6} + 2\cos\left(\frac{5\pi}{6}\right)$$

$$= \frac{5\pi}{6} - \sqrt{3}$$

\therefore Minimum $\left(\frac{5\pi}{6}, \frac{5\pi}{6} - \sqrt{3}\right)$

\therefore Intervals of increasing, $-2\pi < t < -\frac{11\pi}{6}, -\frac{7\pi}{6} < t < \frac{\pi}{6}, \frac{5\pi}{6} < t < 2\pi$
 \therefore Intervals of decrease, $\frac{\pi}{6} < t < \frac{5\pi}{6}$

$$f''(t) = -\cos t$$

$$0 = -\cos t$$

$$t = \frac{\pi}{2}, \frac{3\pi}{2}, -\frac{3\pi}{2}, -\frac{\pi}{2}$$

f''	$-2\pi \leq t \leq -\frac{3\pi}{2}$	$-\frac{3\pi}{2}$	$-\frac{3\pi}{2} \leq t \leq \frac{\pi}{2}$	$-\frac{\pi}{2}$	$-\frac{\pi}{2} \leq t < \frac{\pi}{2}$	$\frac{\pi}{2}$
Sign	-	0	+	0	-	
Behaviour	Concave down	Inflection	Concave up	Inflection	Concave down	

$\pi/2$	$\pi/2 < t < 3\pi/2$	$3\pi/2$	$3\pi/2 < t \leq 2\pi$
0	+	0	-
Inflection	Concave up	Inflection	Concave Down

\therefore Inflection points $(\pi/2, \pi/2), (-\pi/2, -\pi/2), (3\pi/2, 3\pi/2), (-3\pi/2, -3\pi/2)$

\therefore Concave Down: $-2\pi \leq t < -3\pi/2, \frac{\pi}{2} < t < \pi/2, \frac{3\pi}{2} < t \leq 2\pi$

\therefore Concave Up: $-\frac{3\pi}{2} < t < -\frac{\pi}{2}, \frac{\pi}{2} < t < \frac{3\pi}{2}$

b) $g(x) = (1+e^x)^{-2}$

i) domain: $(-\infty, \infty)$

ii) No vertical asymptote

$$\begin{aligned} & \lim_{x \rightarrow \infty} \frac{1}{(1+e^x)^2} & \lim_{x \rightarrow -\infty} (1+e^x)^{-2} \\ &= \frac{1}{\lim_{x \rightarrow \infty} (1+e^x)^2} &= \left(\lim_{x \rightarrow -\infty} (1) + \lim_{x \rightarrow -\infty} e^x \right)^{-2} \\ &= 0 &= \left(1 + e^{\lim_{x \rightarrow -\infty} x} \right)^{-2} \\ & &= -\infty \\ & & \therefore \lim_{x \rightarrow -\infty} g(x) = 1 \end{aligned}$$

\therefore The horizontal asymptotes for $g(x)$ are $0 \nparallel 1$.

$$\begin{aligned} g' &= -\frac{2}{(1+e^x)^3} \cdot \frac{d}{dx}(1+e^x) \\ &= -\frac{2}{(1+e^x)^3} e^x \\ &= -\frac{2e^x}{(1+e^x)^3} \end{aligned}$$

$$g' \quad -4 < x < -1 \quad -1 < x < 4$$

Sign - +

Behaviour dec increasing

∴ Intervals of increase $-1 < x < 4$

∴ Intervals of decrease $-4 < x < -1$

IV) No local extrema since the function is asymptotically bound between $y=1$, $y=0$.

$$V) g'' = \frac{d}{dx} \left(\frac{-2e^x}{(1+e^x)^3} \right)$$

$$= -2 \frac{d}{dx} \left(\frac{e^x}{(1+e^x)^3} \right)$$

$$= -2 \frac{e^x (1+e^x)^3 - 3(1+e^x)^2 e^x e^x}{((1+e^x)^3)^2}$$

$$= - \frac{2e^x(-2e^x+1)}{(1+e^x)^4}$$

$$\begin{aligned} f(x) \\ \frac{f(x)}{g(x)} = 0 \end{aligned}$$

$$0 = \boxed{}$$

$$0 = -2e^x + 1$$

$$2e^x = 1$$

$$e^x = \frac{1}{2}$$

$$\ln(e^x) = \ln(\frac{1}{2})$$

$$x = \ln(\frac{1}{2})$$

$$x = -\ln(2)$$

g''	$x < -\ln(2)$	$-\ln(2)$	$x > -\ln(2)$
Sign	-	0	+
Behaviour	Concave down	Inflection	Concave up

\therefore The interval for concave down is $x < -\ln(2)$ and the interval for concave up is $x > -\ln(2)$

vi) The inflection point is when $g''(0) = 0$
 This the inflection point is $-\ln(2)$.

$$i) R(x) = \frac{x}{x^3 - 1}$$

i) Domain $(-\infty, 1) \cup (1, \infty)$

$$\text{ii) VA} = x^3 - 1 \\ 1 = x^3$$

\therefore The Vertical asymptote is $x = 1$.

$HA = 0$ because the numerator is greater than the denominator thus we get $= 0/x^3 - 1$ which we can't divide.

$\therefore HA y = 0$.

$$\begin{aligned}
 \text{(iii)} \quad R' &= \frac{4}{3}x(x)(x^3-1) - \frac{4}{3}x(x^3-1)x \\
 &= \frac{4x(x^3-1)}{(x^3-1)^2} = \frac{4x(x^3-1)}{(x^3-1)^2} = \frac{4x(x^3-1)}{(x^3-1)^2} \\
 R'(x) &= \frac{-2x^3-1}{(x^3-1)^2} \quad \rightarrow -2x^3-1 = 0 \\
 &\quad -2x^3 = 1 \\
 &\quad x^3 = -\frac{1}{2} \\
 R'(1) &= \text{Undef} \\
 x &= -\sqrt[3]{\frac{1}{2}}
 \end{aligned}$$

R'	$(-\infty, -\sqrt[3]{\frac{1}{2}})$	$(-\sqrt[3]{\frac{1}{2}}, 1)$	$(1, \infty)$
Sign behaviour	+	-	-
	Inc	Dec	Dec

$\therefore R(x)$ is increasing on the interval $(-\infty, -\sqrt[3]{\frac{1}{2}})$ and decreasing over intervals, $(-\sqrt[3]{\frac{1}{2}}, 1), (1, \infty)$.

$$\begin{aligned}
 \text{(iv)} \quad x &= -\sqrt[3]{\frac{1}{2}} \quad \therefore \text{The local extrema}\\
 R &= \frac{-\sqrt[3]{\frac{1}{2}}}{(-\sqrt[3]{\frac{1}{2}})^3 - 1} \quad \text{has a maximum} \\
 &= \frac{\frac{2}{3}}{3}
 \end{aligned}$$

$$U) R'(x) = \frac{-2x^3 - 1}{(x^3 - 1)^2}$$

$$\begin{aligned} R''(x) &= \frac{\partial}{\partial x} \left(\frac{(-2x^3 - 1)(x^3 - 1)}{(x^3 - 1)^2} \right) - \frac{\partial}{\partial x} \left(\frac{(x^3 - 1)^2}{(x^3 - 1)^2} \right) - 2x^3 - 1 \\ &= \frac{-6x^2(x^3 - 1)^2 - 6x^2(x^3 - 1)(-2x^3 - 1)}{(x^3 - 1)^4} \end{aligned}$$

$$R'' = \frac{6x^2(-x^3 - 2)}{(x^3 - 1)^3}$$

$$\begin{aligned} 6x^2(-x^3 - 2) &= 0 \\ -6x^2(x + 3\sqrt[3]{2})(x^2 - 3\sqrt[3]{2}x + 2^{\frac{2}{3}}) &= 0 \end{aligned}$$

$$\begin{aligned} x + 3\sqrt[3]{2} &= 0 \\ x &= -3\sqrt[3]{2} \end{aligned}$$

$$x = 0, x = 1$$

R''	$(-\infty, -3\sqrt[3]{2})$	$(-3\sqrt[3]{2}, 0)$	$(0, 1)$	$(1, \infty)$
Sign behaviour	$+ \text{CU}$	$- \text{CD}$	$- \text{CD}$	$+ \text{CU}$

\therefore The interval for concave up is $(-\infty, -3\sqrt[3]{2})$ and $(1, \infty)$. Interval for concave down is $(-3\sqrt[3]{2}, 0)$ and $(0, 1)$.

$$V1) R'''(-\sqrt[3]{2}) = 0$$

$$R(-\sqrt[3]{2}) = \frac{-\sqrt[3]{2}}{(\sqrt[3]{2})^3 - 1}$$

$$= \frac{\sqrt[3]{2}}{3}$$

∴ The inflection point for $R(x)$ is $(-\sqrt[3]{2}, \sqrt[3]{2}/3)$.

2.4.4 #38

$$= \lim_{x \rightarrow 0} \frac{x^2 \sin x}{\sin x - x}$$

$$= \frac{0}{0}$$

4 LHR

$$= \lim_{x \rightarrow 0} \frac{1}{x^2} (\bar{x}^2 \sin x)$$

$$x+0 \cdot \frac{d}{dx} (\sin x - x)$$

$$= \lim_{x \rightarrow 0} \frac{2x \sin x + (\cos x - 1)}{\cos x - 1}$$

$$= \frac{2(0)\sin(0) + \cos x x^2}{\cos(0) - 1} = \frac{0}{0}$$

$\frac{d}{dx} 2x \sin x + \frac{d}{dx} (\cos x x^2)$
 $2 \sin x + 2x \cos x - x^2 \sin x$
 $+ 2x \cos$

* LHR

$$= \lim_{x \rightarrow 0} \frac{d/dx(2x \sin x + \cos x \cdot x^2)}{d/dx(\cos x - 1)}$$

$$= \lim_{x \rightarrow 0} \frac{-x^2 \sin x + 4x \cos x + 2 \sin x}{-\sin x}$$

$$= -(0)^2 \sin(0) + 4(0) \cos + 2 \sin(0) = \frac{0}{0}$$

LHR

$$\lim_{x \rightarrow 0} \frac{\frac{d}{dx}(-x^2 \sin x + 4x \cos x + 2 \sin x)}{\frac{d}{dx}(\sin x)}$$

$$\lim_{x \rightarrow 0} \frac{\frac{d}{dx}(x^2 \sin x) - \frac{d}{dx}(4x \cos x) - \frac{d}{dx}(2 \sin x)}{\frac{d}{dx}(\sin x)}$$

$$= \lim_{x \rightarrow 0} \frac{2x \sin x + \cos x x^2 - (4 \cos x - 4x \sin x) - 2 \cos x}{\cos x}$$

$$= 2x \sin x + \cos x x^2 - 4 \cos x + 4x \sin x - 2 \cos x$$

$$= x^2 \cos x + 2x \sin x + 4x \sin x - 6 \cos x$$

$$= x^2 \cos x + 6x \sin x - 6 \cos x$$

$$\lim_{x \rightarrow 0} x^2 \cos x + 6x \sin x - 6 \cos x$$

$$= \frac{(0)^2 \cos(0) + 6(0) \sin(0) - 6 \cos(0)}{\cos(0)}$$

$$= \frac{-6}{1} = -6$$

$$\therefore \lim_{x \rightarrow 0} \frac{x^2 \sin x}{\sin x - x} = -6 \text{ using LHR.}$$

3) 4.4 #46

$$\lim_{x \rightarrow -\infty} x \ln\left(1 - \frac{1}{x}\right) = 0 \cdot 0$$

Indeterminate

* LHR

$$\lim_{x \rightarrow -\infty} \frac{d/dx \ln(1 - 1/x)}{d/dx 1/x}$$

$$\lim_{x \rightarrow -\infty} \frac{\frac{1}{1 - 1/x}}{-1/x^2} = \frac{\frac{1}{1 - 1/x} \cdot x^2}{-1/x^2} = \frac{x^2}{x(x-1)} = \frac{x^2}{x^2 - x} = \frac{x}{x-1}$$

$$= \lim_{x \rightarrow -\infty} \frac{x}{x-1}$$

* LHR

$$\lim_{x \rightarrow -\infty} \frac{d/dx -x}{d/dx(x-1)}$$

$$\lim_{x \rightarrow -\infty} \left(\frac{-1}{1}\right)$$

$$= -1$$

$$\therefore \text{The } \lim_{x \rightarrow -\infty} x \ln\left(1 - \frac{1}{x}\right) = -1.$$

4) 4.4 # 62

$$\lim_{x \rightarrow \infty} (e^x + 10x)^{1/x}$$

$$\lim_{x \rightarrow \infty} e^{\frac{1}{x} \ln(e^x + 10x)}$$

$$g(x) = \frac{1}{x} \ln(e^x + 10x) \quad f(u) = e^u$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} \ln(e^x + 10x)$$

$$\lim_{x \rightarrow \infty} \frac{\ln e^x + 10x}{x}$$

$$= \frac{\infty}{\infty}$$

* LHR

$$\lim_{x \rightarrow \infty} \frac{\frac{d}{dx} \ln e^x + 10x}{\frac{d}{dx} x}$$

$$= \frac{e^x + 10}{e^x}$$

$$\lim_{x \rightarrow \infty} \frac{e^x + 10x}{1}$$

$$\begin{aligned} & \frac{1}{e^x + 10x} \cdot \frac{d}{dx}(e^x + 10x) \\ &= \frac{1}{e^x + 10x} \cdot e^x \\ &= \frac{e^x + 10}{e^x + 10x} \end{aligned}$$

$$\lim_{x \rightarrow \infty} \frac{e^x}{e^x + 10} = \frac{\infty}{\infty}$$

* LHR

$$\lim_{x \rightarrow \infty} \frac{\frac{d}{dx} e^x}{\frac{d}{dx}(e^x + 10)}$$

$$\lim_{x \rightarrow 0} \frac{e^x}{e^x} = 1$$

$$\lim_{x \rightarrow 0} 1 = 1$$

$$\lim_{u \rightarrow 1} e^u = e^1 = e$$

∴ The $\lim_{x \rightarrow 0} (e^x + 10x)^{1/x} = e$ using LHR.

5.4.4 #74

$$f(x) = 2x \sin x, g(x) = \sec x - 1$$

$$\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = \lim_{x \rightarrow 0} \frac{2x \sin x}{\sec x - 1}$$

$$= \frac{0}{0}$$

* LHR

$$2 \cdot \lim_{x \rightarrow 0} \frac{\frac{d}{dx}(2x \sin x)}{\frac{d}{dx}(\sec x - 1)}$$

$$2 \cdot \lim_{x \rightarrow 0} \frac{\sin x + x \cos x}{\sec x \tan x} = \frac{0}{0}$$

$$\begin{aligned} & \frac{d}{dx}(\sec x) \tan x + \frac{d}{dx}(\tan x) \sec x \\ &= \sec x \tan x \tan x + \sec^2 x \end{aligned}$$

* LHR

$$2 \cdot \lim_{x \rightarrow 0} \frac{\frac{d}{dx}(\sin x + x \cos x)}{\frac{d}{dx}(\sec x \tan x)}$$

$$= -\sec x + 2 \sec^3 x$$

$$= 2 \cdot \lim_{x \rightarrow 0} \left(\frac{2(\cos x - x \sin x)}{-\sec x + 2 \sec^3 x} \right)$$

$$= 2 \cdot \left(\frac{2(\cos 0 - 0 \sin 0)}{-\sec 0 + 2 \sec^3 0} \right)$$

$$= 4$$

\therefore The $\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = 4$ using L'H.R.

7. Perimeter of Sector = 16m

$$R = ?$$

$$P = 2r + \theta r$$

$$2r + \theta r = 16 \quad A = \frac{1}{2} r^2 \theta$$

$$\theta = \frac{16 - 2r}{r}$$

$$A = \frac{1}{2} r^2 \left(\frac{16 - 2r}{r} \right)$$

$$= \frac{1}{2} (16r - 2r^2)$$

$$= 8r - r^2$$

$$\cancel{\theta/r}$$

$$P = 16m$$

$$A' = \frac{d}{dr} (8r - r^2)$$

$$= 8 - 2r$$

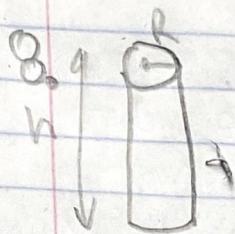
$$0 = 8 - 2r$$

$$r = 4m$$

\therefore The largest burning radius of the circle is 4m, $r = 4m$.

$$750 = \pi r^2 h$$

$$h = \frac{750}{\pi r^2}$$



$$V = 750 \text{ m}^3$$

$$h$$

$$m = 1.5$$

$$s = 0.45$$

$$V = \pi r^2 h$$

$$S = 2\pi r h + 2\pi r^2$$

$$L = 2(2\pi r) + h$$

$$= 4\pi r + h$$

$$\text{Cost} = S(1.5) + L(0.45)$$

$$= (2\pi r h + 2\pi r^2)(1.5) + (4\pi r + h)(0.45)$$

$$= 1.5(2\pi r(\frac{750}{\pi r^2}) + 2\pi r^2) + (4\pi r + \frac{750}{\pi r^2})0.45$$

$$C = \frac{2250}{r} + 3\pi r^2 + 1.8\pi r + \frac{337.5}{\pi r}$$

$$\begin{aligned} 9.a) f(x) &= 2\cos x - \sqrt{e^{2x}} \\ &= \int 2\cos x - \sqrt{e^{2x}} \, dx \\ &= \int 2\cos x \, dx - \int \sqrt{e^{2x}} \, dx \\ &= 2\sin x - e^x + C \end{aligned}$$

$$\begin{aligned} &\sqrt{e^{2x}} \\ &e^{\frac{x}{2}} \\ &e^x \end{aligned}$$

$$\begin{aligned} F(x) &= 2\sin x - e^x + C \\ \frac{d}{dx} F(x) &= \frac{d}{dx}(2\sin x - e^x + C) \end{aligned}$$

$$F'(x) = 2\cos x - e^x$$

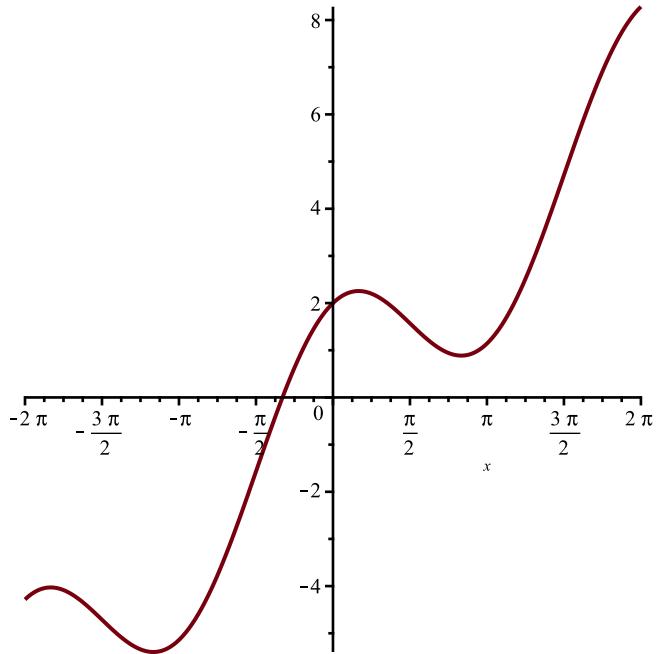
\therefore The $\int F(x) \, dx = 2\sin x - e^x + C$ and differentiating $F(x)$, $F'(x) = 2\cos x - e^x$

A4
mw17an
6402176

> $f := x + 2 \cos(x);$

$$f := x + 2 \cos(x) \quad (1)$$

> $\text{plot}(f);$



Min values are $(-2\pi, -2\pi + 2), (-7\pi/6, -7\pi/6 - \sqrt{3}), (5\pi/6, 5\pi/6 - \sqrt{3})$

Max Values are $(-11\pi/6, -11\pi/6 + \sqrt{3}), (\frac{\pi}{6}, \frac{\pi}{6} + \sqrt{3})$

Intervals of increase $-2\pi < t < \frac{-11\pi}{6}, \frac{-7\pi}{6} < t < \frac{\pi}{6}, \frac{5\pi}{6} < t < 2\pi$

Intervals of decrease $\frac{\pi}{6} < t < \frac{5\pi}{6}$

Inflection Points $(\frac{\pi}{2}, \frac{\pi}{2}), (-\frac{\pi}{2}, -\frac{\pi}{2}), (\frac{3\pi}{2}, \frac{3\pi}{2}), (-\frac{3\pi}{2}, -\frac{3\pi}{2})$

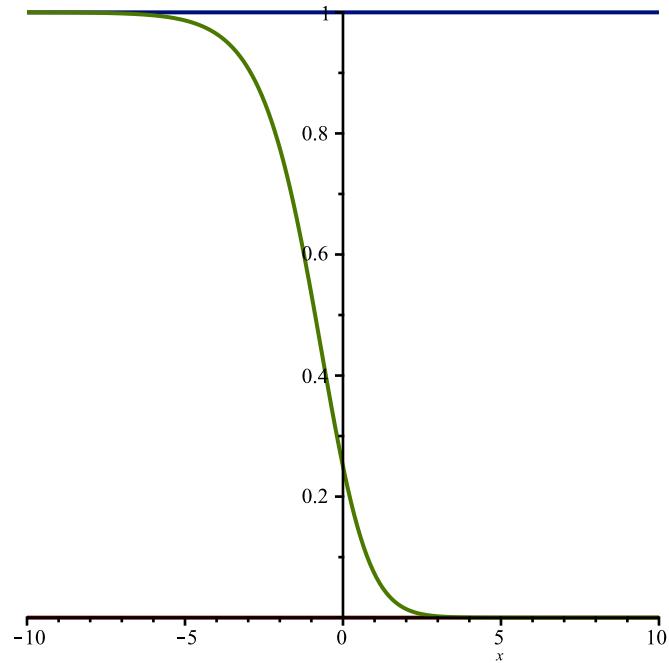
Concave Down $(-2\pi, -\frac{3\pi}{2}), (\frac{\pi}{2}, \frac{3\pi}{2})$

Concave Up $(-\frac{3\pi}{2}, -\frac{\pi}{2}), (\frac{\pi}{2}, \frac{3\pi}{2})$

> $g := (1 + e^x)^{-2};$

$$g := \frac{1}{(1 + e^x)^2} \quad (2)$$

> $\text{plot}(\{g, (1), (0)\});$



Horizontal asymptotes $y = 0, y = 1$

Intervals of increase $-1 < x < 4$

Intervals of decrease $-4 < x < -1$

Concave down $x < -\ln(2)$

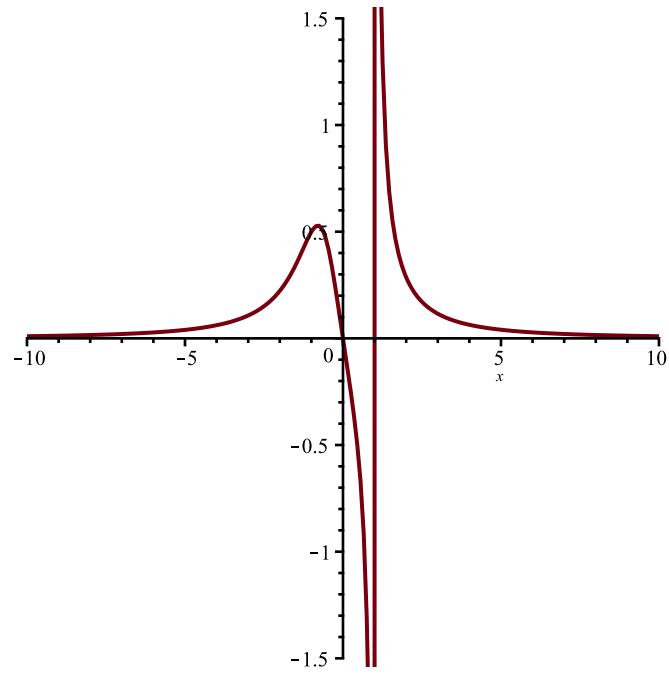
Concave up $x > -\ln(2)$

Inflection point $-\ln(2)$

$$> R := \frac{x}{x^3 - 1};$$

$$R := \frac{x}{x^3 - 1} \quad (3)$$

> $\text{plot}(R);$



Vertical Asymptote $x = 1$

Interval of increase $-\infty < x < -\sqrt[3]{\frac{1}{2}}$

Interval of decrease $-\sqrt[3]{\frac{1}{2}} < x < 1, 1 < x < \infty$

Local Extrema $\left(-\sqrt[3]{\frac{1}{2}}, \frac{2^{\frac{2}{3}}}{3} \right)$

Concave Up $-\infty < x < -\sqrt[3]{2}, 1 < x < \infty$

Concave Down $-\sqrt[3]{2} < x < 0, 0 < x < 1$

Inflection point $\left(-\sqrt[3]{2}, \frac{\sqrt[3]{2}}{3} \right)$

Error, mismatched or missing bracket/operator

$$\left(-\sqrt[3]{\frac{1}{2}} < x < 1, 1 < x < \infty \right) \text{ Local Extrema } \left(\frac{2^{\frac{2}{3}}}{3} \right)$$

Error, mismatched or missing bracket/operator

$$\left(-\sqrt[3]{\frac{1}{2}}, \frac{2^{\frac{2}{3}}}{3} \right)$$

$2^{1/3}, 1 < x < \infty$ Concave Down

Error, mismatched or missing bracket/operator

$$\left(-\sqrt[3]{2} < x \leq 0, 0 < x \leq 1 \right) \text{ Inflection point } \left(\frac{\sqrt[3]{2}}{3} \right)$$

Error, mismatched or missing bracket/operator

$$\left(-\sqrt[3]{2}, \frac{\sqrt[3]{2}}{3} \right)$$

6.)

> $AB := \sqrt{x^2 + 3.2^2};$
 $BC := 12 - x;$

$Total := \frac{AB}{4} + \frac{BC}{6};$

$$AB := \sqrt{x^2 + 10.24}$$

$$BC := 12 - x$$

$$Total := \frac{\sqrt{x^2 + 10.24}}{4} + 2 - \frac{x}{6}$$

(4)

> $TT := diff(Total, x);$
 $TT = 0;$

$$TT := \frac{x}{4\sqrt{x^2 + 10.24}} - \frac{1}{6}$$

(5)

$$\frac{x}{4\sqrt{x^2 + 10.24}} - \frac{1}{6} = 0 \quad (5)$$

> $\text{fsolve}(\%, x);$
 $2.862167011 \quad (6)$

Therefore, the hiker must aim at a point that is 2.862km ahead of the road from point P towards the restaurant.

8)

> $c := \frac{2250}{r} + 3\pi r^2 + 1.8\pi r + \frac{337.5}{\pi r^2};$
 $c := \frac{2250}{r} + 3\pi r^2 + 1.8\pi r + \frac{337.5}{\pi r^2} \quad (7)$

> $C := \text{diff}(c, r);$
 $C := -\frac{2250}{r^2} + 6\pi r + 1.8\pi - \frac{675.0}{\pi r^3} \quad (8)$

> $C = 0$
 $-\frac{2250}{r^2} + 6\pi r + 1.8\pi - \frac{675.0}{\pi r^3} = 0 \quad (9)$

> $\text{evalf}(\%);$
 $-\frac{2250}{r^2} + 6\pi r + 1.8\pi - \frac{675.0}{\pi r^3} = 0. \quad (10)$

> $h := \frac{750}{\pi(4.8)^2};$
 $\text{fsolve}(h);$
 $h := \frac{750}{\pi(4.8)^2} \quad (11)$

> $cc := \text{subs}(r=4.8, c);$
 $cc := 468.7499999 + 77.76\pi + \frac{14.64843750}{\pi} \quad (12)$

Therefore, Radius is 4.8m height is

$$\frac{750}{\pi(4.8)^2} \text{ m, minimum cost is } cc \text{ which is } 468.7499999 + 77.76\pi + \frac{14.64843750}{\pi} \text{ $. (} r=4.8 \text{ m, } h \\ = 10.2 \text{ m, cost = \$717.60)}$$