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Phase stability in nickel phosphides at high pressures

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We performed first-principles calculations on the crystal structure prediction and relative thermodynamic stability for Ni–P binary system at 100–400 GPa pressure range. Crystal structures of seven intermediate compositions, Ni₁₄P, Ni₁₂P, Ni₁₀P, Ni₈P, Ni₇P, Ni₅P, Ni₃P, and Ni₂P stable against decomposition on the mixture of Ni and P are predicted in all investigated pressure range. First seven of them, present substitutional solid solutions of phosphorus in nickel face-centered cubic structure. Thus, up to 25 mol.% of P can be dissolved in crystal structure of Ni at low temperature and temperature can sufficiently increase this limit. For Ni₃P nickel phosphide, a new high-pressure phase with *Cmca* space group, which can be also considered as (Ni,P) solid solution within highly deformed *fcc* Ni structure, was found. This phase is stable in the range ... GPa. Ni₂P is found to adopt allabogdanite structure at pressures above ... The *P-T* phase diagrams of Ni₂P and Ni₃P phosphides were calculated by the lattice dynamics method in the quasi-harmonic approximation.

1 Introduction

Phosphides play a significant role in the mineralogy of iron meteorites as a component of the ternary Fe–Ni–P system. Although being rare, accessory minerals with composition (Fe,Ni)_xP, gives important information about phosphorus geochemistry on the early stages of the universe formation.^{1–7} The occurrence of these minerals in meteoritic samples is believed to originate either from the equilibrium condensation of protoplanetary materials taking place in solar nebulae or from crystallization processes in the cores of parent bodies.

Fe end-members were intensively studied using both experimental and theoretical techniques. So far, most of the high-pressure investigations on iron phosphides have been restricted on Fe₄P,¹ Fe₃P,² Fe₂P^{3–5} and FeP.⁶ Several structural and magnetic phase transitions have been revealed as the result. Dera et al. observed that on heating at 8 GPa phase of Fe₂P transforms to a high-pressure modification, which could be quenched to ambient conditions.⁷ Theoretical modelling demonstrates that the stable phase of Fe₂P should be the *Pnma* with the lowest total energy at lower pressure, and the *P62m*

and *Pnma* phases would transform to the *P3̄m* phase with larger coordination number of iron at 125 GPa and 153 GPa, respectively.⁷ Theoretical studies have shown that Fe₃P could decompose into Fe₂P and Fe₄P at pressures higher than 214 GPa², and Fe₃P and Fe would react with formation of Fe₄P at ~100 GPa.² Fe₃P exhibits a structural phase transition from *I4* to *P4/mnc* at 64 GPa and 1600 K accompanied with an electronic state transition from high spin to low spin at around 20–40 GPa.^{2–4} Upon compression, Fe₄P undergoes transition from ferromagnetic to nonmagnetic state at 80 GPa.⁷ Britvin et al. reported two new structures of FeP (*Pnma*) and FeP₂ (*Pnnm*), found in the pyrometamorphic rocks.^{8–9}

Alloying effect of Ni on physical properties and structure of Fe and its alloys with light elements is also of geological interest, as according to geochemical assessment Earth's core could contain up to 10 mol% of Ni (Уточнить и поставить ссылку на Чёрную Книжку (?)). Addition of nickel to iron phosphides affect the structure and phase stability. The example of Fe₂P shows, that a small addition of Ni and Co stabilise the structure of allabogdanite against ...^{10–12}, and also slightly increases the bulk modulus of the allabogdanite phase.⁷ А может здесь сослаться на нашу статью по алабогданиту (Bekker, Sagatov et al., 2020)? The incorporation of Ni in nonmagnetic Fe₄P results in reduction of the compressional and shear wave velocities enhancing their anisotropy.⁷

There are numerous phases were revealed in Ni–P system at ambient pressure. Among them are Ni₃P, Ni₈P₃, Ni₁₂P₅, Ni₂P, Ni₅P₄, NiP, NiP₂, and NiP₃. However, the data on this system at high-pressures, especially above 100 GPa, are limited. Donohue et al.¹³ studied P-rich compositions (NiP_{2.2–2.5}) at 1.5–

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Table 1 Structural data for the predicted phases of Ni–P system. Параметры ячейки лучше округлить до тысячных, четвёртая цифра абсолютно не значима. Координаты атомов – до десятичных (именно так делает большинство авторов, например К. Пикард, лично я бы всё до тысячных округлял))

Phase	Pressure (GPa)	Space group	Lattice parameters (Å, degree)	Atomic coordinates			
				Atom	x	y	z
Ni ₁₄ P	400	<i>C2/m</i> (#12)	$a=6.8686\text{Å}$ $\alpha=90$	$b=6.2097\text{Å}$ $\beta=119.559$	$c=5.0749\text{Å}$ $\gamma=90$	Ni1	0.00000
						Ni2	0.16860
						Ni3	0.00000
						Ni4	0.30065
						Ni5	0.00000
						P1	0.33474
Ni ₁₂ P	400	<i>R3</i> (#148)	$a=7.4609\text{Å}$ $\alpha=90.00$	$b=7.4609\text{Å}$ $\beta=90.00$	$c=5.0755\text{Å}$ $\gamma=120$	Ni1	0.16860
						Ni2	0.00000
						Ni3	0.30065
						Ni4	0.00000
						Ni5	0.33474
						P1	0.19837
Ni ₁₀ P	300	<i>P1</i> (#2)	$a=3.6654\text{Å}$ $\alpha=107.482$	$b=4.7295\text{Å}$ $\beta=104.937$	$c=4.7339\text{Å}$ $\gamma=97.456$	Ni1	0.00000
						Ni2	0.38422
						Ni3	0.00000
						Ni4	0.40876
						Ni5	0.33153
						P1	0.00000
Ni ₈ P	200	<i>P1</i> (#2)	$a=3.7669\text{Å}$ $\alpha=75.00$	$b=3.7719\text{Å}$ $\beta=82.569$	$c=4.8694\text{Å}$ $\gamma=80.481$	Ni1	0.00000
						Ni2	0.56082
						Ni3	0.00000
						Ni4	0.66740
						Ni5	0.21845
						P1	0.11085
Ni ₇ P	100	<i>P1</i> (#2)	$a=3.7553\text{Å}$ $\alpha=73.032$	$b=3.7772\text{Å}$ $\beta=89.980$	$c=4.3925\text{Å}$ $\gamma=79.849$	Ni1	0.00000
						Ni2	0.56082
						Ni3	0.00000
						Ni4	0.66740
						Ni5	0.21845
						P1	0.11085
Ni ₅ P	200	<i>P6₃/mcm</i> (#193)	$a=3.7732\text{Å}$ $\alpha=90.00$	$b=3.7732\text{Å}$ $\beta=90.00$	$c=7.0786\text{Å}$ $\gamma=120$	Ni1	0.00000
						Ni2	0.25000
						Ni3	0.00000
						Ni4	0.25000
						Ni5	0.00000
						P1	0.00000
Ni ₃ P	100	<i>Cmca</i> (#64)	$a=13.1666\text{Å}$ $\alpha=90.00$	$b=4.4854\text{Å}$ $\beta=90.00$	$c=4.4851\text{Å}$ $\gamma=90.00$	Ni1	0.00000
						Ni2	0.18176
						Ni3	0.00000
						Ni4	0.81801
						Ni5	0.25000
						P1	0.00000

6.5 GPa. Dera et. al.[?] synthesized a cubic NiP₂ phase at 6.5 GPa during heating at 1200°C and subsequent cooling to 900°C. Incongruent melting associated with formation of pyrite-type NiP₂ and amorphous Ni–P alloy was found at an intermediate pressure range, between 6.5 and 40 GPa. The phase transitions in Ni₂P were not observed in these experiments at pressures up to 50 GPa consistently with theoretical modelling.[?] Several reversible phase transitions were established in NiP at ambient temperature: (a) from *Pbca* to *Cmc2₁* at 3.5 GPa, (b) to *Pnma*-phase at 8.5 GPa and again to *Cmc2₁*-phase, but with different crystal structure at 25 GPa.^{??} Litasov et.al. studied the melting processes and subsolidus phase relations in the Ni–Ni₂P system at 6 GPa and 900–1600°C.[?] Хорошо бы в этой и других подобных ссылках отметить конкретный результат. А так получается просто констатация факта, что кто-то что-то исследовал. А что получено в результате? The stability of four intermediate compositions, Ni₃P, Ni₈P₃/Ni₅P₂, Ni₁₂P₅, and Ni₂P transjordanite was found. The Ni₁₂P₅ phase becomes unstable at 900°C and decomposes into Ni₅P₂ and Ni₂P.

The phase stability, elastic properties, hardness and related electronic structures of Ni–P crystal phases at ambient pressure and zero temperature were studied theoretically in Ref.^{??}. According to calculations, at atmospheric pressure and zero tem-

perature, Ni–P compounds can be ordered as the formation enthalpy increases as follows: Ni₅P₄ < Ni₂P < Ni₁₂P₅ < NiP < Ni₈P₃ < Ni₃P < NiP₂ < NiP₃. Как я понял, здесь считается энтальпия образования на атом, без учёта какой это атом. И какая информация получается в результате? что Ni₅P₄ стабильнее Ni₂P? Информативно ли это? Мне кажется что нет, но видимо я что-то не понимаю.

The equations of state and structural parameters of Ni₂P, NiP₂ (pyrite type) and Ni-doped Fe₂P (allabogdanite) at high pressures were determined with first-principles calculations.[?] There was not found barringerite-allabogdanite phase transition in Ni₂P at pressures up to 50 GPa. Bulk modulus of (Fe_{1–x}Ni_x)₂P (allabogdanite) increases with Ni concentration. Increasing the concentration of Ni decreases the stability of structure and suppresses the total magnetic moment of the system.

In present research, we theoretically investigate Ni–P compounds in the pressure range from 100 to 400 GPa. A search for new crystalline structures is carried out. The relative stability of all predicted and well-known experimentally observed structures of the Ni–P system is investigated. The phase diagram of the Ni₂P system is calculated, where barringerite-allabogdanite structural phase transition occurs at pressures of 77–87 GPa

depending on temperature. Similar calculations of the phase equilibrium between the new high-pressure Ni₃P phase and the schreibersite structure are also performed.

2 Computation Details

The structure predictions were performed using USPEX code based on evolutionary algorithms^{???} and AIRSS based on a random sampling method.^{??} Crystal structure prediction calculations were divided into two stages. At the first stage, the search for stable structures of intermediate compositions was performed using the USPEX package. At the second stage, the predictions were performed for the fixed compositions represented on the convex hull constructed at the first stage using USPEX and AIRSS. The calculations of the electronic structure were carried out within the DFT using the VASP 5.4 package.^{??} The exchange-correlation interaction was taken into account in the generalized gradient approximation (GGA) in the form of the Perdew-Burke-Ernzerhof (PBE) functional[?] in a plane-wave basis set along with projector augmented-wave (PAW) pseudopotentials.[?] For all studied structures, calculations were performed, taking into account the spin polarization. It was found that in all cases, except for the new predicted phases Ni₁₀P, Ni₁₂P, and Ni₁₄P, the magnetic moment is equal to zero. The computation parameters were as follows: energy cut-off – 450 eV; the density of the grid of Monkhorst-Pack k-point mesh – 0.5Å⁻¹. The most promising predicted structures were then optimized with higher accuracy at various pressures. In these calculations, the cut-off energy was 700 eV and the density of k-points was 0.2Å⁻¹.

To take into account the temperature effect and predict the phase diagrams, we used the method of lattice dynamics within the quasi-harmonic approximation (QHA). For this task, the phonon frequencies were calculated with the PHONOPY code.[?]

3 Results and Discussion

3.1 The analysis of HP crystal structures

Structural data of the new phases predicted with USPEX and AIRSS codes are summarized in Table 1 and shown in Fig. 1. All found structures are dynamically stable, the corresponding phonon spectra presented in Supporting Information (SI).

The structures of Ni₁₄P, Ni₁₂P, Ni₁₀P, Ni₈P, Ni₇P, Ni₅P, and Ni₃P are characterized by *fcc* packing, with Ni atoms partially substituted by P atoms. The pure Ni also present in the *fcc* form up to 400 GPa. Thus, the found structures can be considered as (Ni,P) solid solutions. This type of isomorphism between *d*-metal and light element is unusual at ambient pressures. At extreme pressures of the Earth's core, when elements which are typical non-metals like sulphur adopt metallic properties[?], this isomorphism became typical. Isomorphic replacement of iron on sulphur within *hcp* or *bcc* crystal structures can be given as example[?]. Я здесь в обоих случаях на себя ссылаюсь, хорошо бы добавить и другие ссылки (например на Cote и Vocadlo), но сходу ничего предложить не могу. Typical for solid solutions, P atoms in found structures tend to

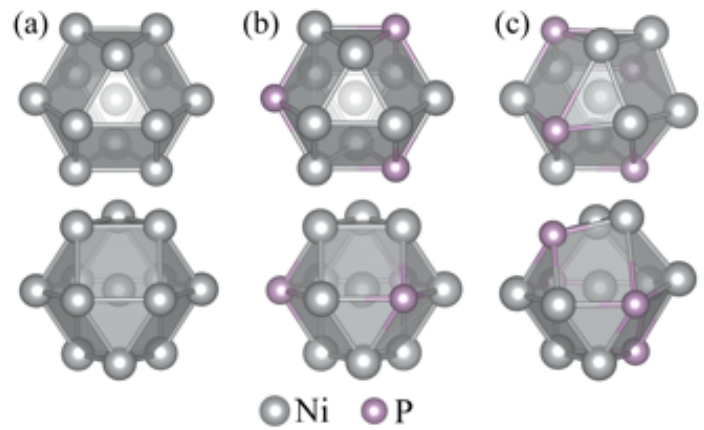


Fig. 1 Coordination cube-octahedron around Ni atoms in fcc-Ni (a), Ni₅P-*P6₃/mcm* (b), and Ni₃P-*Cmca* (c) structures; upper row – view along three-fold axis, lower row – perpendicular to the three-fold axis. Коллеги, я здесь запутался, получается что Ni₃P-*Cmca* – это тоже твёрдый раствор (Ni,P) просто сильно деформированный, т.е. при давлении выше 70 ГПа просто стабилизируется твёрдый раствор, то же самое имеет место и в отношении других составов, кроме Ni₂P. К рисунку с выпуклой оболочкой хорошо бы добавить ещё рисунок с фазовыми переходами, как мы это обычно делаем, их там практически нет, но всё равно, лучше для наглядности сделать, потому что мне было не просто разобраться. Структуру аллабоданита я бы тоже добавил, под буквой (d), а для имеющихся структур оставил только одну проекцию вдоль оси третьего порядка, слегка наклонённую. Ni₈P₃ – поду буквой (e)

be homogeneously spread through the structure, without clustering or group formation.

The deformation of the ideal cubic *fcc* structure increases with increasing amount of phosphorus. The deformation of coordination cube-octahedron of ligand Ni and P atoms around central Ni atom can be traced by the changes of Ni-P and Ni-N bond lengths, shown in Supporting information Figure ???. Ni₁₄P, Ni₁₂P, Ni₁₀P, Ni₈P, Ni₇P, Ni₅P structures are characterised by almost ideal *fcc* packing, with both Ni-Ni and Ni-P bonds of the same length, equal to 2.7 Å at 100 GPa. The Ni-Ni bond in the pure *fcc* Ni is characterised by the same length. Ni₃P structure is sufficiently deformed, as shown on Figure 1, the Ni-P bond is equal to 2.25 Å while length of Ni-Ni bonds vary in the range 2.25-2.35 Å. The found Ni₂P-*Pnma* structure is the analogue of allabogdanite mineral with composition Fe₂P and it is sufficiently different from the described solid solutions, which indicate on the limit of (Ni,P) isomorphism. The calculations, which results will be presented below, show that experimentally synthesised at ambient pressure Ni₈P₃ structure is also stable up to 400 GPa. As well as Ni₂P, the structure of this phase are also not related to the described solid solutions. Thus, around 15 mol.% of P can be dissolved in *fcc* structure of Ni, without heating. As temperature increases the limits of isomorphism, this value can be accepted as the lower boundary for (Ni,P) isomorphism at conditions of the cores of the Earth or planets. The fact, that similar isomorphism was not found in Fe-P systems, likely shows that solubility of P in (Fe,Ni) alloy will be higher than in the pure Fe.

Spin-polarized calculations show the presence of a magnetic moment in structures with a relatively high nickel content from Ni₁₄P to Ni₈P, as shown in Fig. 4. In all other cases, the magnetic order is absent. The magnetic moment per nickel atom decreases with an increase in the specific phosphorus content in the system. With increasing pressure, the magnetic moment and magnetic ordering completely disappear at a pressure of 315, 360, 350, and 115 GPa for the Ni₁₄P, Ni₁₂P, Ni₁₀P, and Ni₈P lattices, respectively. Unlike the considered phosphides, the magnitude of the magnetic moment in pure nickel weakly depends on external pressure. With an increase in pressure from 100 to 200 GPa, the magnetic moment per nickel atom decreases from 0.58 μ_B to 0.5 μ_B and then remains practically unchanged.

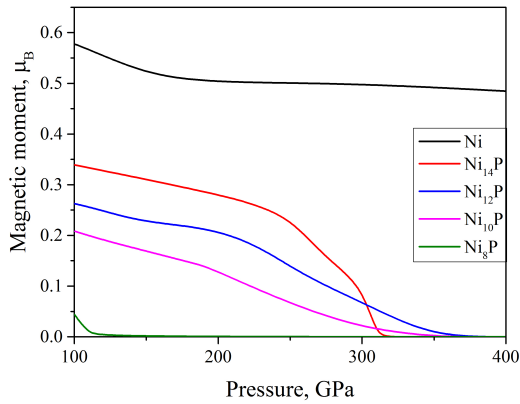


Fig. 2 Pressure dependence of magnetic moment (in Bohr magneton, μ_B) per Ni atom for predicted Ni-P crystal structures. The dependence of the magnetic moment on pressure for pure nickel is given for comparison.

3.2 Thermodynamic of Ni-P compounds

Both sets of the predicted and experimentally observed Ni-P binary compounds were used to evaluate the formation enthalpy ΔH with respect to the elemental solids Ni and P according to Eq. 1, in order to explore the thermodynamic stability of Ni-P:

$$\Delta H(\text{Ni}_n\text{P}_m) = \frac{H(\text{Ni}_n\text{P}_m) - nH(\text{Ni}) - mH(\text{P})}{Z(n+m)}, \quad (1)$$

where $H = U + PV$ is the enthalpy of each compound, Z is a number of structure units in the unit cell and ΔH is the enthalpy of formation per formula unit. Herein, U , P , and V are internal energy, pressure and volume, correspondingly. Detailed information about the element solids can be found in SI.

The relative stabilities of the considered compositions at the selected pressures of 100, 200, 300, and 400 GPa, with ΔH evaluated per atom, are shown in Fig. 5. The stable phase lies on the convex hulls (the global stability lines). А почему в единственном числе? Here, we take into consideration the Ni₂P with allabogdanite structure and the new predicted Ni₃P structure. As will be shown below, these polymorphs are more thermodynamically favorable in the pressure range considered in the present paper.

All predicted Ni₁₄P, Ni₁₂P, Ni₁₀P, Ni₈P, and Ni₇P phases are stable through the entire range of considered pressures. The Ni₅P structure is metastable at a pressure of 100 GPa ($\Delta H=0.035$ eV/atom), but it stabilizes at pressures of 200 GPa and higher. Ni₃P and Ni₂P become thermodynamically stable at pressures above 200 GPa. The structure of pyrite NiP₂ becomes metastable at pressures above 300 GPa.

~~The trend of phase stability for Ni-P compounds at zero pressure is Ni₅P₄ > Ni₂P > Ni₁₂P₅ > NiP > Ni₈P₃ > Ni₃P > NiP₂ > NiP₃.~~ Я уже приводил эту последовательность выше в Введении. Если лучше сослаться туда, можно это место переписать. As mentioned above, at atmospheric pressure Ni-P compounds can be ordered as the formation enthalpy increases as Ni₅P₄ < Ni₂P < Ni₁₂P₅ < NiP < Ni₈P₃ < Ni₃P < NiP₂ < NiP₃.? ? Я бы избегал тут понятие тренд. Нигде кроме одной работы китайских исследователей я не видел. Опять же как считать стабильность в тренде? По идее нужно считать относительно соседей, т.к. именно эта разница энергий определяет стабильность, а здесь, как я понял, считается относительно Ni и P. With increasing pressure, this sequence changes. At a low phosphorus content, structures with an increase in their enthalpy of formation per atom are ordered as follows: Ni₃P < Ni₅P < Ni₇P < Ni₈P < Ni₁₀P < Ni₁₂P < Ni₁₄P. As mentioned above, structure Ni₅P is metastable at 100 GPa, and structure Ni₃P stabilizes at a pressure above 200 GPa. However, the value by which it is necessary to lower the enthalpies of these compounds to stabilize them is small and practically lies within the calculation error. At $P=100$ GPa, the most stable structure is NiP₂, whose enthalpy grows (with increasgin pressure?) with increasing pressure relative to the Ni₂P and Ni₈P₃, and it is metastable at a pressure of 400 GPa. At pressures of 200, 300, and 400 GPa, the most stable is the Ni₈P₃. Other intermediate compounds with known lattices stable at atmospheric pressure under the considered conditions become metastable

It has to be emphasized that the results presented in Fig.5 are obtained neglecting thermal effects. For their full consideration in the framework of the lattice dynamics method, it is necessary to calculate the vibrational spectra of all the structures considered. We performed phonon mode calculations for all considered Ni-P structures except the Ni₈P₃ lattice. For this structure, we encountered a technical difficulty related to the fact that the unit cell of this crystal contains 132 atoms on one side. On the other hand, due to its low symmetry, PHONOPY software generates 264 different unit cells with displaced atoms to calculate phonon modes. Our computer resources do not allow us to carry out such massive calculations, and we leave this question for further research in the future. However, using the experimental data of Oryshchyn et al.[?], we can assume that the Ni₈P₃ phase is likely unstable at atmospheric pressure and 800°C. This structure is expected to be unstable at the higher pressures and sufficiently high temperatures.

3.2.0.1 PT phase diagrams of Ni₂P and Ni₃P Structure prediction studies reveal the well-known allabogdanite structure of Ni₂P to be the most favorable phase in the range of 100-

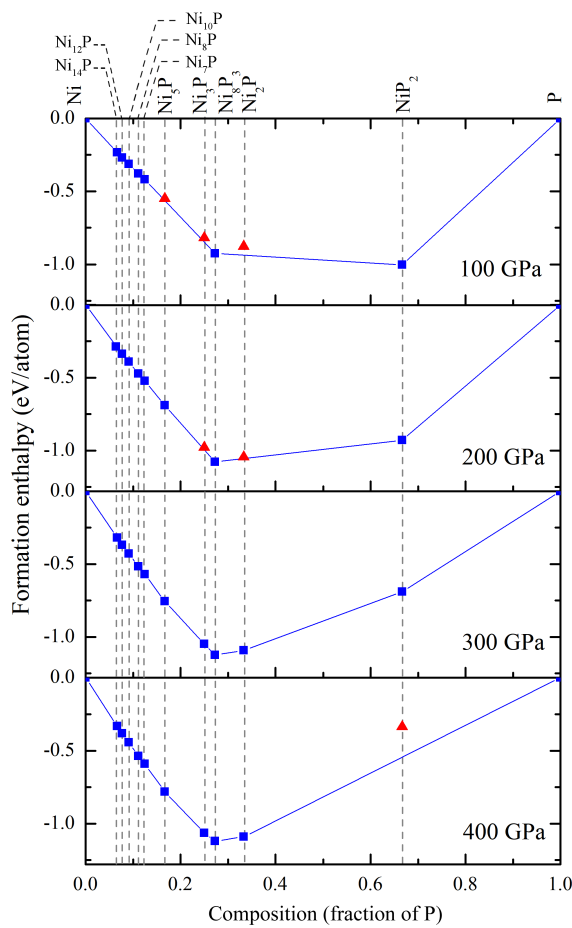


Fig. 3 Convex hulls of Ni-P system at various pressures and 0 K. Blue squares denote stable structures, red triangles - metastable structures.

400 GPa. On the other hand, it is well known that, at low pressures, the Ni_2P barringerite structure are more stable.[?] Experimental and theoretical studies conducted in the pressure range 0-50 GPa did not show the existence of a structural phase transition between these phases.[?] In the case of Ni_3P compounds, the schreibersite structure is the most stable in the low-pressure region,[?] while at the high-pressure we predicted the existence of the structure with $Cmca$ symmetry. For both compositions, it is necessary to establish the PT stability fields of these polymorphs.

The results of calculations of phase diagrams in the $P-T$ plane, obtained by the lattice dynamics method in the QHA, are presented in Fig. 6. The structural phase transition barringerite-allabogdanite in the Ni_2P system occurs at a pressure of 88 GPa at low temperatures and 78 GPa at $T = 2000$ K. In the Ni_3P system, the pressure at which the phase transition occurs is practically independent of temperature and the structural transformation occurs at 62 GPa.

4 Conclusions

As a result of computer simulation, the existence of seven new crystalline modifications of nickel phosphide of various stoichiometries in the pressure range of 100-400 GPa was predicted.

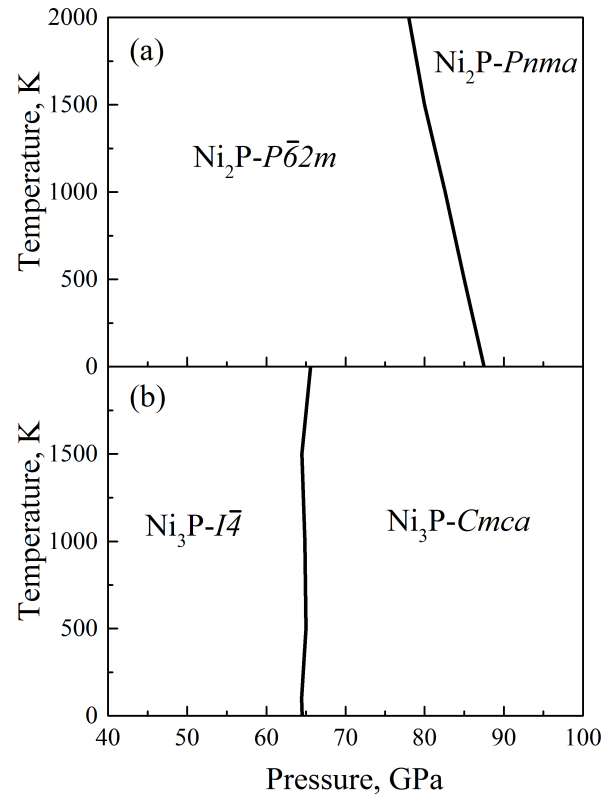


Fig. 4 P - T diagram of (a) Ni_2P and (b) Ni_3P . В обозначения протрсанственных групп буквы пишутся италиком, а цифры – обычным шрифтом, а на рисунке – всё италиком Исправлено

Вот посмотрел я ещё раз на эти seven new crystalline modifications и подумал, а можно ли их рассматривать как новые фазы. Возьмём например твёрдый раствор $(\text{Fe,Mg})_2\text{SiO}_4$. Во всё интервале составов это одна и та же структура, один и тот же минерал, одна и та же модификация. В нашем случае отличие только в том, что атомы по позициям распределены закономерно, а не беспорядочно, но это просто ограничения методики. Поэтому я бы тут так и писал шесть структуры соответствующей одной серии твёрдых растворов. Six of these compounds turn to the fcc lattice of nickel if Ni atoms substitute phosphorus ones. Six new structures are ordered substitutional solid solutions of phosphorus in the fcc lattice of Ni. For the phosphide of the Ni_3P composition, a new high-pressure phase of the $Cmca$ space group is predicted. The transition from the low-pressure phase of $\text{Ni}_3\text{P-I}\bar{4}$ to the $Cmca$ structure occurs at a pressure of 62 GPa, regardless of the external temperature. For Ni_2P , the allabogdanite lattice is a stable structure at high pressure. The phase transformation between these crystalline modifications occurs at a pressure of 88 GPa at low temperatures, and 78 GPa at $T = 2000$ K. New phases with a sufficiently high nickel content of Ni_{14}P , Ni_{12}P , Ni_{10}P , and Ni_8P can have a magnetic order. With increasing phosphorous content, the magnetic moment per nickel atom decreases.

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