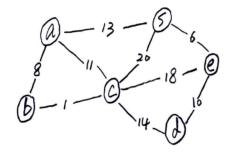
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Problem 1.

Prim's Algorithm



olly] = the weight of the lighters edge between V and S

TI (V) = the lighters edge between V and S

V and S

(TI (V), V).

				6		ſ	1	1	T	0
iteration	2. Vertex addled to S	d	TT	1	-	20 5	d	TT	6	5
1	5	13	5	N	+			-	1	-
2	e	13/	5	MI	- '	le l	10	el		
3	\perp d	13/	5/	× L	14	d				
4	a		18	3 / a	11	a	1	7	1	1
5	Ь		\perp		1	6	1		1	1
6	C									

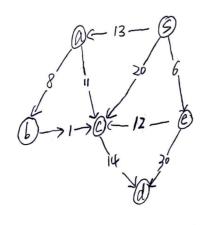
Problem 2.

Dizkstra's Algorithm

	11.16	a		Ь		C		d		0	
iteration	vertex added to S in iteration i	d	TT	d	II	d	TT	d	Ti	d	TI
	in todariore 2	13	5	60	L	20	5	80	1	6	5
1		13	5	p	1	18	9	36	e		
3	e			21	a	18	e	36	e		
3	a	-+		21	a			32	C	-	
4	C	-						32	C	and the same of th	, 30 Marie 9
5	Ь	_		-		A COUNTY OF THE PERSON NAMED IN COUN	OLF VINCES				
6	d	entral secretary	YOU WANTED	and the same of th		The state of the s			The second se		and the second s

d[v] = the shortest poth from 5 to V

11(V) = the power of V in the shortest path tree



Problem 3.

Undirected Groph G=(V,E), Non-negotive edge wayther (We)est

(3a) Yes.

proof: Changing the weight of every edge e from We to We doesn't change the ordering of the edge weights.

Let T be the original MST of G. And T^* be the often MST. For every CUI (U, VVU), T has one edge e and T^* has one edge e

to connect the cut. Let e=(v,v) and $e^{*}=(v,v^{*})$. Assume $e\neq e^{*}$

According to the definition $W(u,v) \subseteq W(u^*,v^*)$ and $W^2_{(u,v)} \supset W^2_{(u,v)} \times V$

Since We are no-negative and difference.

Then 0 and 0 canot be correct of the same time. As a result the assument is wrong. We have $e=e^* \Rightarrow T=T^*$

T is still the minum spany tree of G.

(36.) No

Courter - example

$$\frac{5}{3} + \frac{5}{a} = \frac{5}{4}$$

$$\Rightarrow \frac{25}{9} = \frac{7}{a} = \frac{7}{16}$$
Original
Original

Assume we only have three vertices 5, t, and a.

In the original Graph the shortest poth from 5 to t

is P (5-t) = 5

In the After graph, p is no longer unique.

Since 5-t = 25 = 5-a + 6-7

Problem 4.

d [u] + w (uv) < d (v)

Assume for every edge (u,v) (E, that d(u) + w(u,v) >d(v) Lee the negrone cycle be $C = (a_1, a_2 \cdots a_n)$ not. So we have 0 > W(a1, a2) + W(a2, a3) - + W(an, an) + W(an, a1) According to the assumptimen: d(a) + w(a, a) > d(a) d (an-1) + w (an-1, an) > d (an) d (an) + W(an, a) > d (ai) $= \left[d(a_1) + W(a_1, a_2) \right] + \cdots \left[d(a_n) + W(a_n, a_1) \right] \ge d(a_2) + \cdots + d(a_n) + d(a_n)$ => [d(a1)+d(a2)+111 d(an)] + [W(a1,a2)+111 W(an,a1)] > [d(a1)+111 d(an)] obiviously 0=3 and 2 is the regardue yelle. So 0<0 As a sesule the assumption is wrong. So there exists edge such that