A Domain Specific Language (DSL) for Legal Rules

Introduction

Overview

This notebook defines a package of Wolfram Language functions that facilitates the modeling of legal rules. This is a domain specific language (DSL) - a high-level programming vocabulary tailored to a specific purpose. The larger context of why one would want to do this and numerous other aspects of policy automation are explained elsewhere.

A DSL for legal rules has to do four basic things:

    1. **Information-seeking:** Dynamically seek out missing information in order to make a determination;
    2. **Handling uncertainty:** Keep track of various kinds of uncertainty;
    3. **Time series operators:** Handle certain time series computations; and
    4. **Proof trees:** Provide justifications for its determinations.

These features are defined below, along with unit tests that verify their correctness and demonstrate how to use them.

The functions in this library fall into two categories. Some of the functions generalize ordinary Wolfram Language functions to time series operators. For example, the arithmetic operations are generalized to time series objects, so you can add, subtract, multiply, and divide entire time series together, just as you would ordinarily add two scalar quantities (like 2+2) together. Other functions, while also applying to time series objects, have no counterpart in the Wolfram Language. For example, a group of functions determine how much time has elapsed during which a Boolean time series has been true. So this DSL generalizes a small subset of the Wolfram Language, and also extends it to include certain time-related operations. This DSL also provides functions for easily generalizing a Wolfram Language function to a time series, so that it can be extended even further when necessary, with very little effort.

Development Conventions

Where a function in this DSL generalizes an existing Wolfram Language function, the naming and syntax generally follow the Wolfram Language conventions. However, this is not always the case. Some function signatures have not been generalized, and occasionally it was not possible for the names to be used consistently. All of this is explained in a separate syntax reference document.

Typically, user-defined Wolfram Language functions start with lower case letters, to avoid conflicts with functions that are part of the core language. However, in this library, function names start with capital letters, for two reasons. First, this ensures that they will stand out from functions defined by users of

this DSL. And second, functions that start with upper case letters are omitted from proof trees (see below). If the function names in this DSL end up conflicting with functions released in future versions of the Wolfram Language, adjustments will have to be made.

Interface to this Package

This defines the package's interface to the outside world. In other words, these are the functions that are expected to be used to model the legal/policy rules. (Note that overloaded Wolfram Language functions are tentatively not included in this list. Also, many functions that have not yet been defined are not currently included in this list.)

```
BeginPackage["DSL`"];

AlwaysQ::usage = "";
AnnualTimeLine::usage = "";
ApplyRules::usage = "";
Ask::usage = "";
AsOf::usage = "";
Date::usage = "";
DawnOfTime::usage = "";
EndOfTime::usage = "";
EverQ::usage = "";
IfThen::usage = "asdfasdf";
InterviewPopup::usage = "";
InterviewAPI::usage = "";
InterviewWidget::usage = "";
MissingData::usage = "";
Numeric::usage = "";
ProofTree::usage = "";
RuleStub::usage = "";
SwitchThen::usage = "";
TimeLine::usage = "";
TimeLineMap::usage = "";
TimeLinePlot::usage = "";
TrueBefore::usage = "";
TrueBetween::usage = "";
TrueOnOrAfter::usage = "";
Uncertain::usage = "";

Begin["`Private`"];
Clear[x]; (* make sure that x has no value from same kernel session *)
```

Background: Modeling Legal Rules

Facts

Facts are represented as relations (symbolic expressions), with associated values. For example:

```
gender["Mary"] → "Female"
married["Mary", "Tom"] → True
datePurchased["Joan", "Whiteacre"] → DateObject[{2016, 4, 1}]
```

Rules

Rules derive new facts from existing ones, using `Ask` to mark inputs. Base-level facts are undefined symbols. The following functions are used to demonstrate the syntax and for testing purposes.

```
qualifyingRelativeOf[a_, b_] :=
 age[a] < 18 &&
 age[b] ≥ 18 &&
 Ask[gender[b]] == "Female" &&
 Ask[pregnantQ[b]] &&
 Ask[familyRelationship[a, b]] == "Child";


(* age[p_]:= QuantityMagnitude[DateDifference[Ask[doB[p]],Now,"Year"]]; *)

qualifyingRelationship[a_, b_] := Ask[age[a]] > 18 && Ask[gender[b]] == "Female";
```

Information-Seeking

Identifying Needed Inputs

Ask

The `Ask` function doesn't take any action on its own; it's just a wrapper used to mark inputs, for example `Ask[doB[p]]`. It may later be expanded to include question definitions: `Ask[fact_, q_QuestionObject]`.

ApplyRules

This function resolves goals by applying the rules that we defined to a set of facts:

In[1]:=
```
ApplyRules[goals_List, facts_Association] :=
   Quiet[goals //. Normal[KeyMap[Ask[#] &, facts]]];
 SetAttributes[ApplyRules, HoldAll];
```

MissingData

The `MissingData` function harvests the `Ask` expressions from the expression that results from the application of rules to facts. TODO: Overload the definition of this function to give it a signature like `ApplyRules`?

In[3]:=
```
MissingData[rs_] :=
   Quiet[DeleteDuplicates[Cases[rs, Ask[_], All]] /. Ask[f_] → f];
SetAttributes[MissingData, HoldAll];
```

Interactive Interviews

InterviewPopup

This function creates a pop up interview (in a Wolfram Language notebook) that can be used to test rules interactively. It is recursively driven by the list of missing facts.

In[5]:=
```
InterviewPopup[goals_List, facts_Association] :=
  Quiet[Block[{re, remd, newFactValue},
    re = ApplyRules[goals, facts];
    remd = MissingData[re];

    (* If there's no more missing data, return the evaluated goal.  Otherwise,
    ask the next question and resubmit. *)
    If[remd === {} , Return[re],
     newFactValue = Input[ToString[remd[[1]]] <> "?"];
     If[newFactValue === quit, Return[re],
      Return[InterviewPopup[goals, Append[facts, remd[[1]] → newFactValue]]]]]
   ]];
SetAttributes[InterviewPopup, HoldFirst];
```

There are no unit tests because this is an interactive feature. Evaluating the code below will trigger an interview. Typing `quit` will abort it.

```
InterviewPopup[{qualifyingRelationship["Lucy", "Sam"]}, <||>]
```
$\{\$Canceled > 18 \,\&\&\, \$Canceled == Female\}$

If you seed `PopupInterview` with facts, those will not be asked:

```
InterviewPopup[{qualifyingRelationship["Lucy", "Sam"]}, <|age["Lucy"] → 26|>]
```
$\{True\}$

Interview API

TODO: Given goals and facts, this function returns information about what is known and what needs to be known in order to reach a determination.

InterviewWidget

TODO: The following code creates a notebook widget that interactively investigates a given goal.

Handling Uncertainty

Introduction

States of uncertainty allow the system to keep track of facts the user doesn't know and legal rules that have not been modeled. They are used to create a system of multivalued logic with the following additional states:

> `RuleStub` - Indicates where the rule logic is incomplete (e.g. `RuleStub["42 U.S.C. 1983"]`)
> `Uncertain` - Indicates what is unknown by the user (e.g. a fact she doesn't know the value of, such as `Uncertain[doB[Mary]]`)

The following are used to simplify outputs:

```
In[7]:=   RuleStub[{}] = RuleStub[];
          Uncertain[{}] = Uncertain[];
```

Tests for States of Uncertainty

The `TimeLine` object is described below.

```
In[9]:=   RuleStubQ[x_] := Head[x] === RuleStub;
          UncertainQ[x_] := Head[x] === Uncertain;
          DSLTypeQ[x_] := TimeLineQ[x] || UncertainQ[x] || RuleStubQ[x];
```

Merging Uncertain States Together

If there are multiple states of the same kind of uncertainty, they need to be merged together.

```
In[12]:=  mergeStubs[list_List] :=
           RuleStub[DeleteDuplicates[Flatten[list /. RuleStub[x___] -> x]]];

          mergeUncertains[list_List] :=
           Uncertain[DeleteDuplicates[Flatten[list /. Uncertain[x___] -> x]]];
```

Short-Circuit Operations

Some operations - And, Or, and Times - short-circuit in their evaluation. For example, False and True short-circuits to False; x * 0 short-circuits to 0. The following functions prevent uncertainty from propagating up the function tree when a short-circuit evaluation is possible. The prefix "static" is intended to distinguish these functions from their time series counterparts.

```
In[14]:=   staticAnd[False, q_] = False;
           staticAnd[p_, False] = False;
           staticAnd[True, True] = True;
           staticAnd[p_, q_] := Which[
               MemberQ[{p, q}, _Uncertain],
             mergeUncertains[Select[{p, q}, UncertainQ]],
               MemberQ[{p, q}, _RuleStub], mergeStubs[Select[{p, q}, RuleStubQ]],
               True, p && q];

           staticOr[True, q_] = True;
           staticOr[p_, True] = True;
           staticOr[False, False] = False;
           staticOr[p_, q_] := Which[
               MemberQ[{p, q}, _Uncertain],
             mergeUncertains[Select[{p, q}, UncertainQ]],
               MemberQ[{p, q}, _RuleStub], mergeStubs[Select[{p, q}, RuleStubQ]],
               True, p || q];

           staticTimes[0, q_] = 0;
           staticTimes[p_, 0] = 0;
           staticTimes[p_, q_] := handleUncertainty[p * q, {p, q}];
```

HandleUncertainty

These are wrapper rules that return the highest-precedence type of uncertainty or, if all items in the
input list are certain, the specified expression.

```
In[25]:=   handleUncertainty[expr_, And, {a_, b_}] := staticAnd[a, b];
           handleUncertainty[expr_, Or, {a_, b_}] := staticOr[a, b];
           handleUncertainty[expr_, Times, {a_, b_}] := staticTimes[a, b];
           handleUncertainty[expr_, f_, {a_, b_}] := handleUncertainty[expr, {a, b}];
           handleUncertainty[expr_ : Except[_Ask], list_ ?listMayPassQ] := Which[
               MemberQ[list, _RuleStub], mergeStubs[Select[list, RuleStubQ]],
               MemberQ[list, _Uncertain], mergeUncertains[Select[list, UncertainQ]],
               True, expr]
           SetAttributes[handleUncertainty, HoldFirst];
```

Helper function: A list should be trapped (not evaluated further) if it contains `Ask` and not (`RuleStub` or
`Uncertain`). In other words, if it has `RuleStub` or `Uncertain`, it can be evaluated; if it has `Ask` it
cannot; otherwise it can.

```
In[31]:=   listMayPassQ[list_List] := Which[
               MemberQ[list, _RuleStub] || MemberQ[list, _Uncertain], True,
               MemberQ[list, _Ask], False,
               True, True];
```

Time Series Operations

Overview

Introduction

As explained elsewhere in great detail, modeling time is a particular challenge in building rule-based systems. The following functions create time series objects and operations that are used extensively in legal rules. A time series is a list of date-value pairs (not necessarily regularly spaced), and time series can be added, subtracted, etc., just like scalar values. So as to avoid conflicts with the `TimeSeries` object as defined in the Wolfram Language, we'll create a new object called `TimeLine` and define a variety of operations on them. The core data structure within a `TimeLine` will be compatible with that of a `TimeSeries`, so we can take advantage of the Wolfram Language's existing `TimeSeries` functions when necessary.

Beginning and End of Time

There's a need for values that represent the outer limits of a time series. These are not represented as `DateObjects`, even though they are dates, because complex time series operations perform faster this way.

```
In[32]:=   DawnOfTime = {2000, 1, 1};
           EndOfTime = {2050, 12, 31};
```

The dawn and end of time expressed in absolute time . This is used for internal `TimeLine` processing.

```
In[34]:=   absDawnOfTime = AbsoluteTime[DawnOfTime];
           absEndOfTime = AbsoluteTime[EndOfTime];
```

TimeLine

TimeLine

A TimeLine is a list of date-value pairs. Here's an example of a Boolean `TimeLine`, and its internal representation using `AbsoluteTime` (the number of seconds since 1900-01-01):

```
MakeTimeLine[{{{2000, 1, 1}, False}, {{2010, 1, 1}, True}}]

TimeLine[{{3 155 673 600, False}, {3 471 292 800, True}}]
```

```
MakeTimeLine[{{ 📅 Sat 1 Jan 2000 , False}, { 📅 Fri 1 Jan 2010 , True}}]
```

```
TimeLine[{{3 155 673 600, False}, {3 471 292 800, True}}]
```

```
ShowTimeLine[TimeLine[{{3 155 673 600, False}, {3 471 292 800, True}}]]
{{{2000, 1, 1}, False}, {{2010, 1, 1}, True}}
```

This function constructs a `TimeLine` object.

In[36]:=
```
MakeTimeLine[pairs_] := TimeLine[Map[{AbsoluteTime[#[[1]]], #[[2]]} &, pairs]]
```

A shorthand way of constructing a new `TimeLine`:

In[37]:=
```
T[ts_] := MakeTimeLine[ts];
```

Convert a `TimeLine` to a human-readable `T` object:

In[38]:=
```
ShowTimeLine[ts_TimeLine] :=
   Map[{DateList[#[[1]]][[1 ;; 3]], #[[2]]} &, TimeLineUnbox[ts]];
ShowTimeLine[scalar_] := scalar;
```

Another possibility is to display `DateObjects` in the output:

```
ShowTimeLine[ts_TimeLine] :=
   Map[{DateObject[DateList[#[[1]]][[1 ;; 3]]], #[[2]]} &, TimeLineUnbox[ts]];
ShowTimeLine[scalar_] := scalar;
```

```
ShowTimeLine[TimeLine[{{3 155 673 600, False}, {3 471 292 800, True}}]]
{{ 📅 Sat 1 Jan 2000 , False}, { 📅 Fri 1 Jan 2010 , True}}
```

Internal Machinery

An internal operation to get data out of a `TimeLine` object:

In[40]:=
```
TimeLineUnbox[t_TimeLine] := t /. TimeLine[innards_] -> innards;
```

Convert a scalar to a `TimeLine` (internal):

In[41]:=
```
ToTimeLine[v_TimeLine] := v;
ToTimeLine[v_] := TimeLine[{{absDawnOfTime, v}}];
```

Extract the dates from one or more time series:

In[43]:=
```
TimeLineDates[ts_TimeLine] := TimeLineUnbox[ts][[All, 1]];
TimeLineDates[ts1_TimeLine, ts2_TimeLine] :=
   Union[TimeLineDates[ts1], TimeLineDates[ts2]];
```

Extract the values from a time series:

```
In[45]:=  TimeLineValues[ts_TimeLine] := TimeLineUnbox[ts][[All, 2]];
```

Delete redundant time intervals from a time series. If there's only one interval remains, it returns a scalar. Despite the name, the input is assumed to be a `List`, not a `TimeLine`. (Avg. execution time = 0.00023s.)

```
In[46]:=  TimeLineTrim[t_List] := Block[{trim},
              trim = Map[#[[1]] &, Split[t, #1[[2]] === #2[[2]] &]];
              If[Length[trim] === 1, trim[[1, 2]], TimeLine[trim]]
          ];
```

Determine whether something is a `TimeLine`:

```
In[47]:=  TimeLineQ[x_] := Head[x] === TimeLine;
```

Retrieves the value of the first time-value pair in the time series.

```
In[48]:=  TimeLineFirstValue[ts_] := handleUncertainty[TimeLineUnbox[ts][[1]][[2]], {ts}];
```

Applies a function to the list of all values in a `TimeLine` (treating them all as a single `List` and then putting the transformed list back onto the dates of the timeline).

```
In[49]:=  TimeLineValuesApply[f_, ts_] :=
            zipDatesValues[TimeLineDates[ts], f[TimeLineValues[ts]]]
```

AsOf

Get the value of a `TimeLine` at a particular point in time. `AsOf` accepts either `{y,m,d}` or absolute times.

```
In[50]:=  AsOf[date_, ts_TimeLine] := handleUncertainty[QuickAsOf[date, ts], {date, ts}];
          AsOf[date_, ts_stub] := handleUncertainty[ts, {date, ts}];
          AsOf[date_, scalar_] := scalar;
```

It also accepts temporal inputs:

```
In[53]:=  AsOf[date_TimeLine, val_TimeLine] := TimeLineMap[AsOf[#, val] &, date];
```

An internal method that actually does the lookup:

In[54]:=
```
QuickAsOf[date_, ts_TimeLine] :=
    Block[{i, t = TimeLineUnbox[ts], len, abTime = AbsoluteTime[date]},
     len = Length[t];
     For[i = 1, i <= len, i++,
         (* If the date is before the index date,
      return the value of the prior interval *)
         If[abTime < t[[i, 1]], Return[t[[i - 1]][[2]]] ]];
      (* Else, return the value of the last interval *)
      Return[t[[len]][[2]]]];
 ];
QuickAsOf[date_, scalar_] := scalar;
```

TimeLineMap

This function maps a scalar function (or functions) onto a time series. For performance reasons, the merging/mapping algorithm varies depending on the nature of the arguments. The order of the following definitions may affect the function's behavior.

In[56]:=
```
TimeLineMap[f_, ts_TimeLine] :=

  TimeLineTrim[Map[{#[[1]], handleUncertainty[f[#[[2]]], toList[#[[2]]]] } &,
    TimeLineUnbox[ts]]];

TimeLineMap[f_, scalar_ : Except[_Ask]] :=
  handleUncertainty[f[scalar], {scalar}];

(* Merges two time series like a zipper and
 applies a function to the values in each interval. *)
TimeLineMap[f_, ts1_TimeLine, ts2_TimeLine] :=
  TimeLineMapZip[handleUncertainty[f[#1, #2], f, {#1, #2}] &, ts1, ts2];

(* If the time series doesn't have any stub intervals,
return the scalar stub. *)
TimeLineMap[f_, ts_TimeLine, s_stub] :=
    If[TimeLineContainsStubInterval[ts],
        TimeLineTrim[
         Map[{#[[1]], handleUncertainty[f[#[[2]]], s], f, {#[[2]], s}]} &,
       TimeLineUnbox[ts]]
         ],
      s];
TimeLineMap[f_, s_stub, ts_TimeLine] :=
    If[TimeLineContainsStubInterval[ts],
        TimeLineTrim[
         Map[{#[[1]], handleUncertainty[f[s, #[[2]]], f, {s, #[[2]]}]} &,
```

```
        TimeLineUnbox[ts]]
            ],
          s];


(* Map the scalar to the time series and apply the function. *)
TimeLineMap[f_, ts_TimeLine, scalar_ : Except[_ask]] := TimeLineTrim[
 Map[{#[[1]],
   handleUncertainty[f[#[[2]], scalar], f, {#[[2]], scalar}]
   } &, TimeLineUnbox[ts]]
 ];
TimeLineMap[f_, scalar_ : Except[_Ask], ts_TimeLine] := TimeLineTrim[
 Map[{#[[1]],
   handleUncertainty[f[scalar, #[[2]]], f, {scalar, #[[2]]}]
   } &, TimeLineUnbox[ts]]
 ];


(* TODO: Handle stub arguments *)
TimeLineMap[f_, scalar1_ : Except[_Ask], scalar2_ : Except[_ask]] :=
   handleUncertainty[f[scalar1, scalar2], f, {scalar1, scalar2}];


(* Indicates whether any interval in the time series is a stub *)
TimeLineContainsStubInterval[ts_TimeLine] :=
 MemberQ[TimeLineUnbox[ts], {_, _stub}]
```

Utility function

In[65]:=
```
toList[val_List] := val;
toList[val_] := {val};
```


TimeLineMapZip

Combines two time series like a zipper, which is more efficient that using `Union[TimeLineDates[]]`
and then applying `f` to each interval. This function is the same as the core `TimeLineMap`, but doesn't
handle uncertainty when applying the function `f` at each interval. This is needed for when the default
value in an `IfThen` statement is `Uncertain`.

In[67]:=
```
TimeLineMapZip[f_, ts1_TimeLine, ts2_TimeLine] :=
 Block[{result, t1 = TimeLineUnbox[ts1],
    t2 = TimeLineUnbox[ts2], idx1 = 1, idx2 = 1, val1,
     val2, t1Count, t2Count, nextIdx1, nextIdx2,
    nextDate1, nextDate2, pair, lastPair},

   result = Reap[

     val1 = t1[[1, 2]];
```

```
val2 = t2[[1, 2]];
t1Count = Length[t1];
t2Count = Length[t2];

(* Add first time-value pair.  Assumes all time series start at dawn! *)
lastPair = f[val1, val2];
(* Sow[{DawnOfTime, lastPair}]; *)
 (* Time series starts at earlier of input time series *)
Sow[{Min[{t1[[1, 1]], t2[[1, 1]]}], lastPair}];

       (* Walk along the two time series,
 index by index, until reaching the end of both. *)
While[idx1 < t1Count || idx2 < t2Count,

 (* Don't exceed the length of either list *)
 nextIdx1 = Min[idx1 + 1, t1Count];
 nextIdx2 = Min[idx2 + 1, t2Count];

 (* Get the next change date of each time series *)
 nextDate1 = t1[[nextIdx1, 1]];
 nextDate2 = t2[[nextIdx2, 1]];

 Which[
  (* Case 1: If the next dates on each series are the same,
     advance along both *)
  nextDate1 === nextDate2,
  idx1 = nextIdx1;
  val1 = t1[[idx1, 2]];
  idx2 = nextIdx2;
  val2 = t2[[idx2, 2]];
  pair = f[val1, val2];
  (* Only add a value if it differs from the prior value *)
  If[pair =!= lastPair, Sow[{nextDate1, pair}]; lastPair = pair;];,

  (* Otherwise, advance along the series that's farther behind,
     except when the one that's behind is at its end *)
  (* Case 2: Advance time series 1 *)
    idx2 === t2Count || (idx1 =!= t1Count && nextDate2 > nextDate1),
  idx1 = nextIdx1;
  val1 = t1[[idx1, 2]];
  pair = f[val1, val2];

    If[pair =!= lastPair, Sow[{nextDate1, pair}]; lastPair = pair;];,
```

```
     (* Case3: Advance time series 2 *)
     True,
     idx2 = nextIdx2;
     val2 = t2[[idx2, 2]];
     pair = f[val1, val2];

       If[pair =!= lastPair, Sow[{nextDate2, pair}]; lastPair = pair;];
     ]; (* End Which *)
   ]; (* End While loop *)

 ][[2, 1]]; (* End Reap *)

  Return[If[Length[result] === 1, result[[1, 2]], TimeLine[result]]];
 ];
```

This version is necessary in order to ensure that the `IfThen` function doesn't return a time series that starts at the `DawnOfTime`:

In[68]:=
```
TimeLineMapZip[f_, ts1_TimeLine, scalar_] :=
 TimeLineMapZip[f, ts1, TimeLine[{{TimeLineUnbox[ts1][[1, 1]], scalar}}]]
```

Visualizing TimeLines

The following functions visually display TimeLines. Note that `TimeLinePlot`, defined here, is different from `TimelinePlot`, defined in the core Wolfram Language.

In[69]:=

```
TimeLinePlot[ts_TimeLine] :=
  TimelinePlot[plotData[ts], PlotLayout → "Overlapped"];
TimeLinePlot[list_List] := TimelinePlot[
   plotData[#] & /@ list, PlotLayout → "Overlapped"];

plotData[ts_TimeLine] := intervalStyling[#[[1]], #[[3]], #[[2]]] & /@
  Partition[Flatten[TimeLineUnbox[ts], 1], 3, 2, 1, x]

intervalStyling[start_, x, value_] :=
  intervalStyling[start, DatePlus[start, {10, "Day"}], value];
intervalStyling[start_, end_, True] := Style[Labeled[
    Interval[{DateObject[start], DateObject[end]}], True], Darker[Green]];
intervalStyling[start_, end_, False] := Style[
   Labeled[Interval[{DateObject[start], DateObject[end]}], False], Darker[Red]];
intervalStyling[start_, end_, val_Uncertain] :=
  Style[Labeled[Interval[{DateObject[start], DateObject[end]}], val], Gray];
intervalStyling[start_, end_, val_RuleStub] :=
  Style[Labeled[Interval[{DateObject[start], DateObject[end]}], val], Purple];
intervalStyling[start_, end_, val_] :=
  Labeled[Interval[{DateObject[start], DateObject[end]}], val];
```
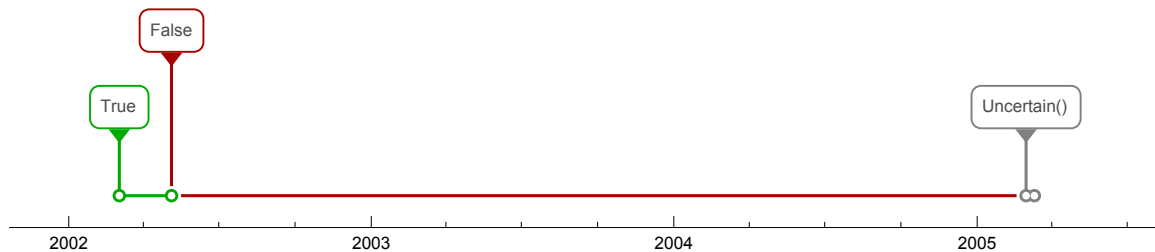
```
TimeLinePlot[
 TimeLine[{{{2002, 3, 3}, True}, {{2002, 5, 5}, False}, {{2005, 3, 1}, Uncertain[]}}]]
```
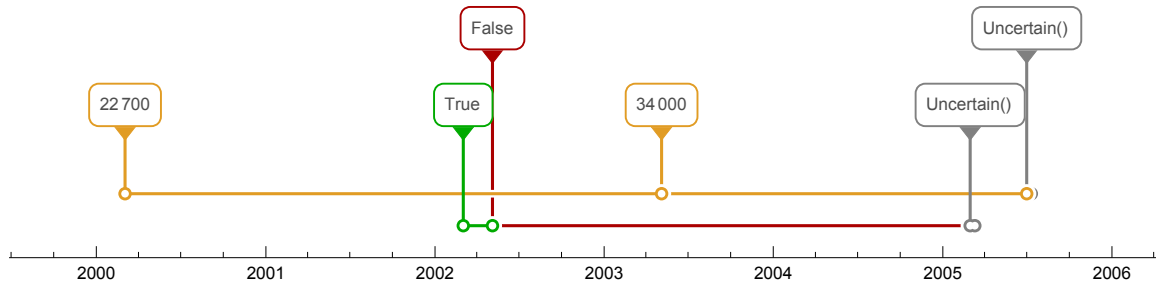
```
TimeLinePlot[
 {TimeLine[{{{2002, 3, 3}, True}, {{2002, 5, 5}, False}, {{2005, 3, 1}, Uncertain[]}}],
  TimeLine[{{{2000, 3, 3}, 22 700},
    {{2003, 5, 5}, 34 000}, {{2005, 7, 1}, Uncertain[]}}]}]
```


TimeLineWindow

Extracts a subset of a TimeLine. The input dates can be in the `{y,m,f}` format or in absolute times.

In[78]:=
```
TimeLineWindow[t_, start_List, end_List] :=
   TimeLineWindow[t, AbsoluteTime[start], AbsoluteTime[end]];
TimeLineWindow[t_, start_, end_] := TimeLine[Union[
     {{start, AsOf[start, t]}},
      Select[TimeLineUnbox[t], start < #[[1]] < end &]
    ]];
```

TimeLineGenerator

Using the date values of an existing `TimeLine`, this function applies a generating function to establish the new values for those dates.

In[80]:=
```
TimeLineGenerator[timeLine_, fcn_] := Block[{dates},
    dates = TimeLineDates[timeLine];
    zipDatesValues[dates, Array[fcn, Length[dates]]]
];
SetAttributes[TimeLineGenerator, HoldAll];
```

```
TimeLineGenerator[theYear, #^2 &]
```

Helper Functions

Helper function to keep dates in a format that maximizes performance:

In[82]:=
```
toDateList[date_DateObject] := DateList[date][[1 ;; 3]]
```

Zip up a list of dates and a list of values to form a new timeline:

```
In[83]:=    zipDatesValues[dates_, vals_] := TimeLine[Transpose[{dates, vals}]]
```

Determines whether the first interval in a time series represents the dawn of time:

```
In[84]:=    timeLineStartsAtDawn[ts_] :=
              handleUncertainty[TimeLineUnbox[ts][[1]][[1]] == absDawnOfTime, {ts}];
```

AnnualTimeLine

Keep?:

```
(* Creates a time series starting at the beginning of a calendar year,
with values that change annually *)
AnnualTimeLine[startYear_, list_List] := TimeLine[
 Insert[Transpose[{Map[{#, 1, 1} &,
   Range[startYear, startYear + Length[list] - 1]], list}],
     {DawnOfTime, RuleStub["Law"]}, {1}]
  ];
```

Boolean TimeLines

Boolean Operators

Ordinary logical operators, but they apply to time series objects rather than Boolean objects.

```
In[85]:=   and[p_, q_] := TimeLineMap[And, p, q];
           Unprotect[And];
           And[False, a_] = False;
           And[a_, False] = False;
           And[a_, b_TimeLine] := and[a, b];
           And[a_, b_RuleStub] := and[a, b];
           And[a_, b_Uncertain] := and[a, b];
           Protect[And];

           or[p_, q_] := TimeLineMap[Or, p, q];
           Unprotect[Or];
           Or[True, a_] = True;
           Or[a_, True] = True;
           Or[a_, b_TimeLine] := or[a, b];
           Or[a_, b_RuleStub] := or[a, b];
           Or[a_, b_Uncertain] := or[a, b];
           Protect[Or];

           not[p_] := TimeLineMap[! # &, p];
           Unprotect[Not];
           Not[a_TimeLine] := not[a];
           Not[a_RuleStub] := a;
           Not[a_Uncertain] := a;
           Protect[Not];
```

Constructing Boolean TimeLines

An easy way to construct time series whose truth value changes on a particular date (or dates).

Creates a Boolean time series that's false before a given date, and true thereafter.

```
In[107]:=   TrueOnOrAfter[date_] := handleUncertainty[
               If[date === DawnOfTime, True,
                 MakeTimeLine[{{DawnOfTime, False}, {date, True}}]],
               {date}];
```

Creates a Boolean time series that's true before a given date, and false thereafter.

```
In[108]:=   TrueBefore[date_] := handleUncertainty[
               If[date === DawnOfTime, False,
                 MakeTimeLine[{{DawnOfTime, True}, {date, False}}]],
               {date}];
```

Creates a Boolean time series that's true between two dates, and otherwise false.

In[109]:=
```
TrueBetween[date1_, date2_] := and[TrueOnOrAfter[date1], TrueBefore[date2]];
```

Creates a Boolean time series that's true on a given date, and otherwise false.

In[110]:=
```
TrueOn[date_] := TrueBetween[date, AddDays[date, 1]];
```

Ever or Always True

Does a time series ever have a particular value? Does it always? (TODO: Deal with scalars and temporal uncertainty.)

In[111]:=
```
EverQ[ts_, val_] := MemberQ[TimeLineValues[ts], val];
EverQ[ts_] := EverQ[ts, True];

AlwaysQ[ts_, val_] := Block[{vals = TimeLineValues[ts]},
    and[Length[vals] === 1, MemberQ[vals, val]]]; (* TODO: rewrite *)
AlwaysQ[ts_] := AlwaysQ[ts, True];
```

When Next or Last True

At any point in time, when will a Boolean time series next be true? If, at a given point in time, the `TimeLine` is true, the value for that interval is `theDate`. TODO: handle scalars, temporal uncertainty, test, performance, and prevent `TimeLines` as arguments.

In[114]:=
```
DateNextTrue[timeLine_] := Block[{currentlyTrue, vals, newVals},
  currentlyTrue = IfThen[timeLine, theDate, x];
   (* Assign theDate to True intervals.  Slow b/c it uses theDate. *)
  vals = TimeLineValues[currentlyTrue];
  If[Last[vals] == x, vals[[-1]] = EndOfTime]; (* Deal with last interval *)
  newVals = Map[If[#[[1]] === x, #[[2]], #[[1]]] &, Partition[vals, 2, 1, 1, x]];
   (* Get date of next True interval *)
  zipDatesValues[TimeLineDates[currentlyTrue], newVals]
  ]
```

```
testval = TrueOnOrAfter[{2000, 1, 5}] && TrueBefore[{2000, 1, 10}];
TimeLinePlot[{testval, DateNextTrue[testval]}]
```
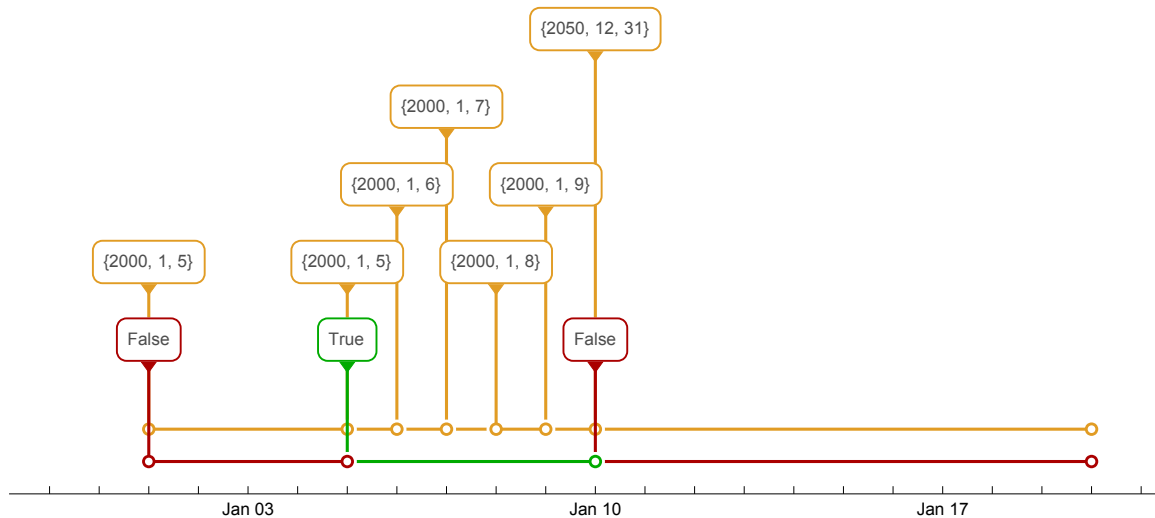

At any point in time, when was a Boolean time series last true?

In[115]:=
```
DateLastTrue[timeLine_] := RuleStub[];
```

Conditionals

Usage Note

The following conditional functions implement time series versions of `If`, `Which`, and `Switch`. Due to the difficulty of filtering function definitions so as to cleanly separate the time series version from the core Wolfram Language version, the conditional functions have names that diverge from the Wolfram Language. (Conditionals are delicate since, if implemented carelessly, they can easily spin out into infinite loops.)

InternalIf

The if-then-else function for time series, used only within this package. This evaluates lazily to permit temporal recursion.

```
In[116]:=   InternalIf[True, val1_, val2_] := val1;
            InternalIf[False, val1_, val2_] := val2;
            InternalIf[test_, val1_, val2_] :=
              Block[{first = TimeLineMap[ifTrueMap, test, val1]},
                If[! EverQ[first, False], first, TimeLineMapZip[ifFalseMap, first, val2]]
              ];
            SetAttributes[InternalIf, HoldRest]

            (* Broken out to make if[] slightly easier to read. *)
            ifTrueMap[val1_, val2_] := If[val1, val2, val1];
            ifFalseMap[val1_, val2_] := If[val1 === False, val2, val1];
```

IfThen

This is the externally exposed function that implements the time series version of `If` and `Which`. Note that, unlike `Which`, the last argument is the default value.

```
In[122]:=   IfThen[test1_, val1_, args___, def_] :=
              InternalIf[test1, val1, IfThen[args, def]];
            IfThen[def_] := def;
            SetAttributes[IfThen, HoldRest];
```

SwitchThen

This is the time series version of `Switch`. Note that it's different than `Switch` because here the last argument is the default value.

```
In[125]:=   SwitchThen[test_List, t1_, v1_, args___, def_] :=
              InternalIf[listEqual[t1, test], v1, SwitchThen[test, args, def]];
            SwitchThen[test_, t1_, v1_, args___, def_] :=
              InternalIf[t1 == test, v1, SwitchThen[test, args, def]];
            SwitchThen[irrelevanTest_, def_] := def;
            SetAttributes[SwitchThen, HoldRest];
```

Test for the equality of two lists:

```
In[129]:=   listEqual[{a1_, a2_}, {b1_, b2_}] :=
              handleUncertainty[a1 == b1 && a2 == b2, {a1, a2, b1, b2}];
            listEqual[a_List, b_List] := handleUncertainty[a == b, Join[a, b]];
```

Arithmetic

Implementation Details

The repetitive declaration structures below are necessary because using signatures like `f[a_ ?DSLTypeQ, b_?DSLTypeQ]` somehow causes interference with the `Times` operator. This exhibited itself when evaluating the expression `DateDifference[{2000, 1, 1}, {2017, 1, 2}]` immediately after initializing this notebook. Overloading `Plus` and `Times` is not recommended. See http://stackoverflow.-com/questions/5252179/how-to-overload-times-and-plus-for-matrix-multiplication-in-mathematica. An alternative, if problems persist, would be to use `CircleTimes`, etc.:

```
In[258]:= CircleTimes[a_ ? DSLTypeQ, b_?DSLTypeQ] := TimeLineMap[Times, a, b];
          CircleTimes[a_ ? DSLTypeQ, b_ ] := TimeLineMap[Times, a, b];
          CircleTimes[a_ , b_?DSLTypeQ ] := TimeLineMap[Times, a, b];
          CircleTimes[a_, b_] := a * b;
```

In[266]:= 7 ⊗ 8

Out[266]= 56

In[265]:= 8 ⊗ MakeTimeLine[{{DawnOfTime, 5}, {{2015, 2, 2}, 9}}]

Out[265]= TimeLine[{{3 155 673 600, 40}, {3 631 824 000, 72}}]

Addition & Subtraction

Note: The order of these overloaded definitions seems to affect performance (or did in a previous implementation from which this was adapted).

Addition & subtraction:

```
In[131]:=  Unprotect[Plus];
           Plus[a_TimeLine, b_TimeLine] := TimeLineMap[Plus, a, b];
           Plus[a_TimeLine, b_] := TimeLineMap[Plus, a, b];
           Plus[a_Uncertain, b_] := TimeLineMap[Plus, a, b];
           Plus[a_RuleStub, b_] := TimeLineMap[Plus, a, b];
           Plus[a_ , b_TimeLine] := TimeLineMap[Plus, a, b];
           Plus[a_ , b_Uncertain] := TimeLineMap[Plus, a, b];
           Plus[a_ , b_RuleStub] := TimeLineMap[Plus, a, b];
           Protect[Plus];
```

From older implementation: Possibly add the code below to the definition of `Plus`. Without this, inter-view question order sometimes gets rearranged. However, `Orderless` only remains cleared in Akkadi-an.nb upon first initialization. Upon the second evaluation of `Attributes[Plus]`, `Orderless` is mysteri-ously back.

```
ClearAttributes[Plus, Orderless];
```

Multiplication

Multiplication.

```
In[140]:=   Unprotect[Times];
            Times[a_TimeLine, b_TimeLine] := TimeLineMap[Times, a, b];
            Times[a_TimeLine, b_] := TimeLineMap[Times, a, b];
            Times[a_Uncertain, b_] := TimeLineMap[Times, a, b];
            Times[a_RuleStub, b_] := TimeLineMap[Times, a, b];
            Times[a_ , b_TimeLine] := TimeLineMap[Times, a, b];
            Times[a_ , b_Uncertain] := TimeLineMap[Times, a, b];
            Times[a_ , b_RuleStub] := TimeLineMap[Times, a, b];
            Protect[Times];
```

Division

Division. Because the Wolfram Language represents `a/b` as `Times[a,Power[b,-1]]`, the `Power` function has to be overloaded as well.

```
In[149]:=   Unprotect[Power];
            Power[t_ ? DSLTypeQ, -1] := TimeLineMap[1 / # &, t];
            Protect[Power];
```

Numeric

Numerical form. Like `N[]`, this converts fractions to decimal form.

```
In[152]:=   Numeric[ts_] := TimeLineMap[N, ts];
```

Modulo

Gives the remainder on division of m by n:

```
In[153]:=   Modulo[m_, n_] := TimeLineMap[Mod, m, n];
```

Rounding

Round to the nearest multiple (ties broken by rounding toward the even alternative):

```
In[154]:=   Unprotect[Round];
            Round[a_TimeLine, b_TimeLine] := TimeLineMap[Round, a, b];
            Round[a_TimeLine, b_] := TimeLineMap[Round, a, b];
            Round[a_Uncertain, b_] := TimeLineMap[Round, a, b];
            Round[a_RuleStub, b_] := TimeLineMap[Round, a, b];
            Round[a_ , b_TimeLine] := TimeLineMap[Round, a, b];
            Round[a_ , b_Uncertain] := TimeLineMap[Round, a, b];
            Round[a_ , b_RuleStub] := TimeLineMap[Round, a, b];
            Protect[Round];
```

Ceiling (round up to the nearest multiple):

In[163]:=
```
Unprotect[Ceiling];
Ceiling[a_TimeLine, b_TimeLine] := TimeLineMap[Ceiling, a, b];
Ceiling[a_TimeLine, b_] := TimeLineMap[Ceiling, a, b];
Ceiling[a_Uncertain, b_] := TimeLineMap[Ceiling, a, b];
Ceiling[a_RuleStub, b_] := TimeLineMap[Ceiling, a, b];
Ceiling[a_ , b_TimeLine] := TimeLineMap[Ceiling, a, b];
Ceiling[a_ , b_Uncertain] := TimeLineMap[Ceiling, a, b];
Ceiling[a_ , b_RuleStub] := TimeLineMap[Ceiling, a, b];
Protect[Ceiling];
```

Floor (round down to the nearest multiple):

In[172]:=
```
Unprotect[Floor];
Floor[a_TimeLine, b_TimeLine] := TimeLineMap[Floor, a, b];
Floor[a_TimeLine, b_] := TimeLineMap[Floor, a, b];
Floor[a_Uncertain, b_] := TimeLineMap[Floor, a, b];
Floor[a_RuleStub, b_] := TimeLineMap[Floor, a, b];
Floor[a_ , b_TimeLine] := TimeLineMap[Floor, a, b];
Floor[a_ , b_Uncertain] := TimeLineMap[Floor, a, b];
Floor[a_ , b_RuleStub] := TimeLineMap[Floor, a, b];
Protect[Floor];
```

Comparison

Comparison operators. These also perform date comparison on `{y,m,d}` objects.

Greater than.

In[181]:=
```
Unprotect[Greater];
Greater[a_TimeLine, b_TimeLine] := TimeLineMap[Greater, a, b];
Greater[a_TimeLine, b_] := TimeLineMap[Greater, a, b];
Greater[a_Uncertain, b_] := TimeLineMap[Greater, a, b];
Greater[a_RuleStub, b_] := TimeLineMap[Greater, a, b];
Greater[a_ , b_TimeLine] := TimeLineMap[Greater, a, b];
Greater[a_ , b_Uncertain] := TimeLineMap[Greater, a, b];
Greater[a_ , b_RuleStub] := TimeLineMap[Greater, a, b];
Greater[{ay_, am_, ad_}, {by_, bm_, bd_}] :=
   AbsoluteTime[{ay, am, ad}] > AbsoluteTime[{by, bm, bd}];
Protect[Greater];
```

Greater than or equal to.

```
In[191]:=   Unprotect[GreaterEqual];
            GreaterEqual[a_TimeLine, b_TimeLine] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_TimeLine, b_] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_Uncertain, b_] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_RuleStub, b_] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_ , b_TimeLine] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_ , b_Uncertain] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[a_ , b_RuleStub] := TimeLineMap[GreaterEqual, a, b];
            GreaterEqual[{ay_, am_, ad_}, {by_, bm_, bd_}] :=
               AbsoluteTime[{ay, am, ad}] ≥ AbsoluteTime[{by, bm, bd}];
            Protect[GreaterEqual];
```

Less than.

```
In[201]:=   Unprotect[Less];
            Less[a_TimeLine, b_TimeLine] := TimeLineMap[Less, a, b];
            Less[a_TimeLine, b_] := TimeLineMap[Less, a, b];
            Less[a_Uncertain, b_] := TimeLineMap[Less, a, b];
            Less[a_RuleStub, b_] := TimeLineMap[Less, a, b];
            Less[a_ , b_TimeLine] := TimeLineMap[Less, a, b];
            Less[a_ , b_Uncertain] := TimeLineMap[Less, a, b];
            Less[a_ , b_RuleStub] := TimeLineMap[Less, a, b];
            Less[{ay_, am_, ad_}, {by_, bm_, bd_}] :=
               AbsoluteTime[{ay, am, ad}] < AbsoluteTime[{by, bm, bd}];
            Protect[Less];
```

Less than or equal to.

```
In[211]:=   Unprotect[LessEqual];
            LessEqual[a_TimeLine, b_TimeLine] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_TimeLine, b_] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_Uncertain, b_] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_RuleStub, b_] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_ , b_TimeLine] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_ , b_Uncertain] := TimeLineMap[LessEqual, a, b];
            LessEqual[a_ , b_RuleStub] := TimeLineMap[LessEqual, a, b];
            LessEqual[{ay_, am_, ad_}, {by_, bm_, bd_}] :=
               AbsoluteTime[{ay, am, ad}] ≤ AbsoluteTime[{by, bm, bd}];
            Protect[LessEqual];
```

Equal to.

```
In[221]:=   Unprotect[Equal];
            Equal[a_TimeLine, b_TimeLine] := TimeLineMap[Equal, a, b];
            Equal[a_TimeLine, b_] := TimeLineMap[Equal, a, b];
            Equal[a_Uncertain, b_] := TimeLineMap[Equal, a, b];
            Equal[a_RuleStub, b_] := TimeLineMap[Equal, a, b];
            Equal[a_ , b_TimeLine] := TimeLineMap[Equal, a, b];
            Equal[a_ , b_Uncertain] := TimeLineMap[Equal, a, b];
            Equal[a_ , b_RuleStub] := TimeLineMap[Equal, a, b];
            Equal[{ay_, am_, ad_}, {by_, bm_, bd_} ] :=
              AbsoluteTime[{ay, am, ad}] == AbsoluteTime[{by, bm, bd}];
            Protect[Equal];
```

Not equal to.

```
In[231]:=   Unprotect[Unequal];
            Unequal[a_TimeLine, b_TimeLine] := TimeLineMap[Unequal, a, b];
            Unequal[a_TimeLine, b_] := TimeLineMap[Unequal, a, b];
            Unequal[a_Uncertain, b_] := TimeLineMap[Unequal, a, b];
            Unequal[a_RuleStub, b_] := TimeLineMap[Unequal, a, b];
            Unequal[a_ , b_TimeLine] := TimeLineMap[Unequal, a, b];
            Unequal[a_ , b_Uncertain] := TimeLineMap[Unequal, a, b];
            Unequal[a_ , b_RuleStub] := TimeLineMap[Unequal, a, b];
            Unequal[{ay_, am_, ad_}, {by_, bm_, bd_} ] :=
              AbsoluteTime[{ay, am, ad}] != AbsoluteTime[{by, bm, bd}];
            Protect[Unequal];
```

Date Operations

Composition

At least one of the inputs must be a scalar. (Need `TimeLineMap` to handle three inputs in order to implement this fully.)

```
In[242]:=   date[y_? DSLTypeQ, m_ , d_] := TimeLineMap[{#, m, d} &, y];
            date[y_? DSLTypeQ, m_?DSLTypeQ, d_] := TimeLineMap[{#1, #2, d} &, y, m];
            date[y_? DSLTypeQ, m_, d_?DSLTypeQ] := TimeLineMap[{#1, m, #2} &, y, d];
            date[y_, m_? DSLTypeQ, d_] := TimeLineMap[{y, #, d} &, m];
            date[y_, m_? DSLTypeQ, d_?DSLTypeQ] := TimeLineMap[{y, #1, #2} &, m, d];
            date[y_, m_, d_? DSLTypeQ] := TimeLineMap[{y, m, #} &, d];
            date[y_, m_, d_] := {y, m, d};
```

Decomposition

Extract the components of a (possibly temporal) date:

```
In[248]:= GetYear[date_] := TimeLineMap[#[[1]] &, date];
         GetMonth[date_] := TimeLineMap[#[[2]] &, date];
         GetDay[date_] := TimeLineMap[#[[3]] &, date];
```

Differences Between Dates

These functions do not follow the naming pattern of their counterparts in the Wolfram Language.

Gives the number of days between two dates (without units of measure):

```
In[251]:= DayDiff[a_, b_] :=
            TimeLineMap[QuantityMagnitude[DateDifference[#1, #2]] &, a, b];
```

Gives the number of weeks between two dates (without units of measure):

```
In[252]:= WeekDiff[a_, b_] :=
            TimeLineMap[QuantityMagnitude[DateDifference[#1, #2, "Week"]] &, a, b];
```

Gives the number of months between two dates (without units of measure):

```
In[253]:= MonthDiff[a_, b_] :=
            TimeLineMap[QuantityMagnitude[DateDifference[#1, #2, "Month"]] &, a, b];
```

Gives the number of years between two dates (without units of measure):

```
In[254]:= YearDiff[a_, b_] :=
            TimeLineMap[QuantityMagnitude[DateDifference[#1, #2, "Year"]] &, a, b];
```

A Date Plus Some Interval

These functions do not follow the naming pattern of their counterparts in the Wolfram Language.

```
In[255]:= AddDays[date_, n_] := TimeLineMap[DatePlus[#1, #2] &, date, n];
```

```
In[256]:= AddWeeks[date_, n_] := TimeLineMap[DatePlus[#1, {#2, "Week"}] &, date, n];
```

```
In[257]:= AddMonths[date_, n_] := TimeLineMap[DatePlus[#1, {#2, "Month"}] &, date, n];
```

```
In[258]:= AddYears[date_, n_] := TimeLineMap[DatePlus[#1, {#2, "Year"}] &, date, n];
```

List Operations

These are named differently than their counterparts in the Wolfram Language to avoid conflicts.

Length

Number of items in a (temporal) list:

In[259]:=
```
Len[ts_] := TimeLineMap[Length, ts];
```

Minimum & Maximum

Minimum value in a (temporal) list:

In[260]:=
```
Minimum[ts_] := TimeLineMap[Min, ts];
```

Maximum value in a (temporal) list:

In[261]:=
```
Maximum[ts_] := TimeLineMap[Max, ts];
```

Total

Total of values in a (temporal) list:

In[262]:=
```
Tot[ts_] := TimeLineMap[Total, ts];
```

Other

TODO:

```
Map
Union
Intersection
MemberQ
ContainsAny
ContainsAll
```

Interval Count Relative to a Point in Time

YearsSince

Creates a timeline that counts years until/from a given date. Essentially, this returns a number line that has the interval of a year, with the origin located at
the input date. Date input is assumed not to be a time series. Avg. execution time = 0.0002s when time range is 70 years.

```
In[263]:=  YearsSince[date_] := handleUncertainty[
             Block[{ts = TimeLine[Table[{{i, date[[2]], date[[3]]}, i - date[[1]]},
                     {i, DawnOfTime[[1]], EndOfTime[[1]]}]]},
              If[timeLineStartsAtDawn[ts], ts,
                TimeLine[Insert[TimeLineUnbox[ts],
                    {absDawnOfTime, TimeLineFirstValue[ts] - 1}, {1}]]]
             ],
             {date}];
```

DaysSince

Creates a timeline that counts days until/from a given date. Date input is assumed not to be a time series. Avg. execution time = 0.007s when time range is 70 years.

```
In[264]:=  DaysSince[date_] := handleUncertainty[
             Block[{start = QuantityMagnitude[DateDifference[DawnOfTime, date]] * -1,
               diff = Length[absoluteTimeDates] - 1},
              zipDatesValues[absoluteTimeDates, Range[start, start + diff]]
             ],
             {date}];
```

MonthsSince

WeeksSince

Counts weeks until/from a given date:

```
In[265]:=  WeeksSince[date_] := Floor[DaysSince[date] / 7];
```

IntervalsSince

IN PROGRESS. This creates a number line with the origin at a particular point in time:

```
IntervalsSince[origin_, interval_] := TimeLineGenerator[interval, #^2 &];
```

```
IntervalsSince[{2017, 1, 1}, theYear]
```

```
Array[# - 20 &, 50]
```

```
{-19, -18, -17, -16, -15, -14, -13, -12, -11, -10, -9, -8,
 -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12,
 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30}
```

Absolute Time

Internal Machinery

List of dates from the dawn of time to the end of time. This exists for performance reasons, as an internal representation of absolute time; it is not expected to be referenced externally.

```
In[266]:=   allDates = DateRange[DawnOfTime, EndOfTime];
            absoluteTimeDates = Map[AbsoluteTime, allDates];
```

Because the following variables are set using = instead of :=, they must be ordered in the notebook so dependencies are evaluated first (i.e. be further up the page).

Calendar-Based TimeLines

A time series in which each day has the value of the date itself. For example, on July 11, 2034, the time series value is {2034,7,11}.

```
In[268]:=   theDate = TimeLine[Transpose[{absoluteTimeDates, allDates}]];
```

```
TimeLinePlot[TimeLineWindow[theDate, {2017, 1, 1}, {2017, 1, 19}]]
```
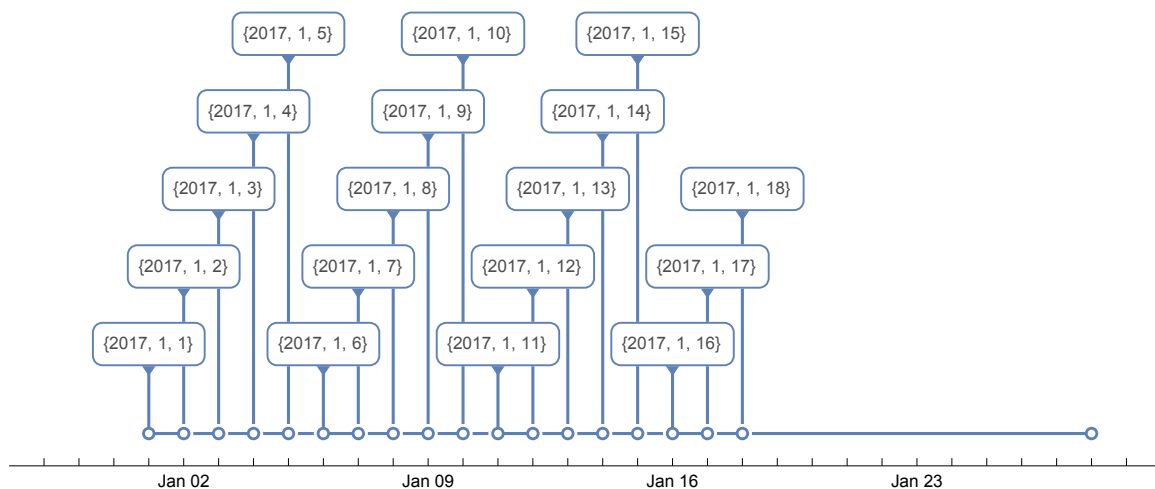


```
In[269]:=   theMonth = GetMonth[theDate];
```
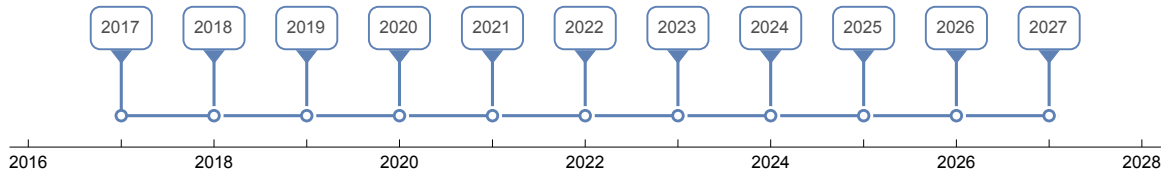
```
In[270]:=   theDayOfTheMonth = GetDay[theDate];
```

```
In[271]:=   theCalendarQuarter = TimeLineMap[Which[
              # < 4, 1,
              # < 7, 2,
              # < 10, 3,
              True, 4] &,
              theMonth];
```

A time series representing the calendar year.

```
In[272]:=   theYear = GetYear[theDate];

            TimeLinePlot[TimeLineWindow[theYear, {2017, 1, 1}, {2027, 1, 19}]]
```



```
In[273]:=   leapYearQ = TimeLineMap[LeapYearQ[{#}] &, theYear];
```

```
In[274]:=   theCalendarWeek = RuleStub[];
```

First/Last Day of Interval

Time series representing the first and last day of every month. It may be the case in practice that a function like `firstDayOfMonth[date]` does the trick and that these are unnecessary.

```
In[275]:=   firstDayOfMonth = date[theYear, theMonth, 1];
```

```
In[276]:=   lastDayOfMonth = AddDays[AddMonths[firstDayOfMonth, 1], -1];
```

Interval Ratios

```
In[277]:=   daysPerYear = TimeLineMap[If[LeapYearQ[{#}], 366, 365] &, theYear];
```

```
In[278]:=   daysPerMonth = GetDay[lastDayOfMonth];
```

```
In[279]:=   daysPerCalendarQuarter = RuleStub[];
```

```
In[280]:=   weeksPerMonth = Numeric[daysPerMonth / 7];
```

Weekdays

This is an internal helper function. Even though ISO 8601 considers Monday as the first day of the week, the U.S. follows a different convention:

```
In[281]:=   dayNameToNumber = <|Sunday → 1, Monday → 2,
                Tuesday → 3, Wednesday → 4, Thursday → 5, Friday → 6, Saturday → 7|>;
```

Day of the week (as a temporal number):

```
In[282]:= dayOfWeek = zipDatesValues[TimeLineDates[theDate],
            Array[Mod[#, 7] + 1 &, Length[absoluteTimeDates],
              dayNameToNumber[DateValue[DawnOfTime, "DayName"]] - 1]];
```

Is the day a weekday?

```
In[283]:= weekdayQ = ! (dayOfWeek == 1 || dayOfWeek == 7);
```

Is the day a U.S. Federal holiday? Note: The legal authority for this is 5 U.S.C. 6103, but we're relying on the Wolfram Language `HolidayCalendar` implementation. This implementation currently (Sept. 2016) has a bug that fails to recognize Veterans Days that fall on a Saturday but that are observed on the preceding Friday. But has been reported and assuming it will eventually get fixed.

```
In[284]:= usFederalHolidayQ = Block[{holidays, firstVal},
          holidays = DayRange[DawnOfTime, EndOfTime, "Holiday"];
          firstVal = {{AbsoluteTime[DatePlus[DawnOfTime, -1]], False}};
          TimeLine[Union[firstVal, Map[{AbsoluteTime[#], True} &, holidays],
              Map[{AbsoluteTime[#], False} &, DatePlus[holidays, 1]]]]
         ];
```

```
TimeLinePlot[TimeLineWindow[usFederalHolidayQ, {2017, 1, 1}, {2017, 6, 1}]]
```
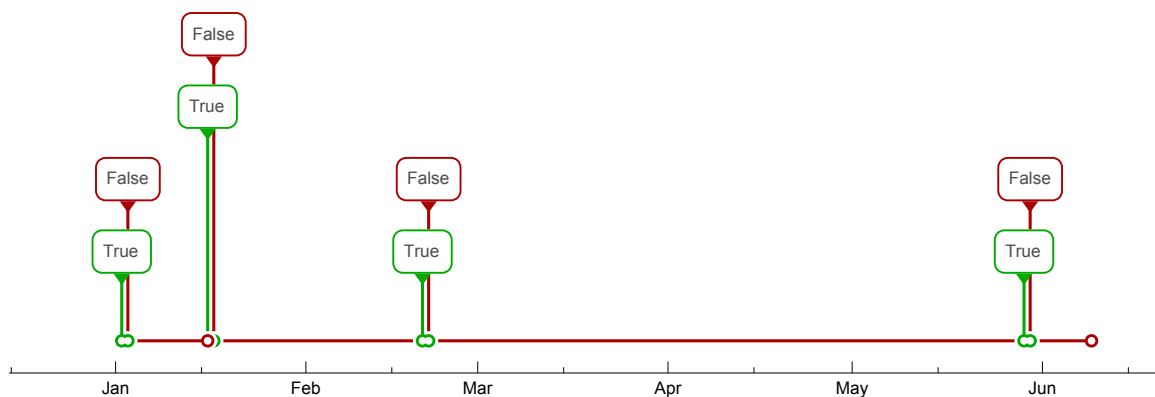


```
In[285]:= businessDayQ = weekdayQ && ! usFederalHolidayQ;
```

```
In[286]:= nextBusinessDay = DateNextTrue[businessDayQ];
```

Per Interval

Machinery

For internal use: For each interval in a `TimeLine`, returns the beginning and end date (in absolute time). Result is a `List`.

```
In[287]:=    TimeLineDateSpans[ts_] :=
               Partition[TimeLineDates[ts], 2, 1, 1, x] /. x → absEndOfTime;
```

Apply a function to a TimeLine per some other interval:

```
In[288]:=    ApplyPerInterval[f_, ts_, interval_] :=
               TimeLineTrim[Map[{#[[1]], f[TimeLineWindow[ts, #[[1]], #[[2]]]]} &,
                 TimeLineDateSpans[interval]]];
```

All Values in a Subinterval

For each interval in a larger time period, gather all of the time series values of a `TimeLine` with smaller intervals. This is pretty slow.

```
In[289]:=    GatherValuesPer[ts_, interval_] := ApplyPerInterval[TimeLineValues, ts, interval]
```

EverPer / AlwaysPer

Is a Boolean `TimeLine` (ts) ever true in a time interval?

```
In[290]:=    EverPer[ts_, interval_] := ApplyPerInterval[EverQ, ts, interval]
```

Is a Boolean `TimeLine` (ts) always true in a time interval?

```
In[291]:=    AlwaysPer[ts_, interval_] := ApplyPerInterval[AlwaysQ, ts, interval]
```

Is a Given Date in an Interval?

In which interval (of a given type) does a given date fall?

```
In[292]:=    DateInPeriodQ[date_, interval_] := EverPer[TrueOn[date], interval];
```

Number of Subintervals in a Larger Interval

Count how many subintervals there are in each larger interval:

```
In[293]:=    SubintervalsPer[smaller_, larger_] := Len[GatherValuesPer[smaller, larger]];
```

Date of Next Interval

For each interval in a `TimeLine`, returns the date that that the next interval begins.

```
In[294]:=    DateOfNextInterval[ts_] := TimeLineTrim[
               Map[{#[[1]], toDateList[DateObject[#[[2]]]]} &, TimeLineDateSpans[ts]]];
```

Value at End of Interval

What is the value of a `TimeLine` at the end of each reference interval? (For example, how old is a person at the end of each calendar quarter?) The end is taken to be one second before the start of the next interval.

```
In[295]:=  IntervalEndValue[ts_, interval_] :=
             TimeLineTrim[Map[{#[[1]], AsOf[#[[2]] - 1, ts]} &, TimeLineDateSpans[interval]]];
```

Other

```
SubintervalCountPer
RunningCountPer
```

Elapsed Time

Miscellaneous

```
Regularize[T, interval]
```

Shift the values in a time series to the right or left:

```
Shift[T, n]
```

Maybe more general than Shift (applies fcn to all times):

```
TimeSeriesDatesMap[f, T]
```

Proof Trees

Proof Trees

A proof tree is a hierarchical report of the reasons for a particular determination. This needs work.

```
ProofTree[{expr_, steps___}] :=
 OpenerView[{Tooltip[expr, ReleaseHold[expr]], Column[ProofTree /@ {steps}]}]
ProofTree[x_] := x
```

```
Trace[standardDeduction["Pat"], _["Pat"]] // ProofTree
```

▼ standardDeduction[Pat]

   ▼ ineligibleForStandardDeductionQ[Pat]

      ▶ {mfsQ[Pat], {marriedQ[Pat], {maritalStatus[Pat]}}}

      ▼ shortTaxYearQ[Pat]

         ▶ taxYearType[Pat]

      ▶ nonresidentAlienQ[Pat]

      ▶ dualStatusAlienQ[Pat]

   ▶ table20Dash3Applies[Pat]

   ▶ table20Dash2Applies[Pat]

   ▶ standardDeductionMostPeople[Pat]

EndPackage

```
End[];
EndPackage[];
```